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# Can EWC overcome task saturation?

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## Abstract

1 Elastic Weight Consolidation (EWC) showed promising results to mitigate catas-  
2 trophic forgetting in neural networks. However, the memory constraint becomes  
3 ill-defined as the number of tasks increases, and experiments in the original paper  
4 only train up to 10 tasks. This is important because we expect that a trade-off  
5 between task saturation and catastrophic forgetting will compromise model perfor-  
6 mance once the task number is sufficiently large. In this work, we define a novel  
7 task sampling procedure on the CIFAR100 dataset, which allows to obtain a very  
8 large number of tasks. Using this paradigm, we trained EWC and some baseline  
9 models on a total of 100 tasks. Our experiments show EWC enters a task saturation  
10 regime during the second half of training.

## 11 1 Introduction

12 When trained on a sequence of task, neural networks typically suffer from catastrophic forgetting  
13 [1, 2]. This is because important weights from previous tasks are updated to meet the objectives of  
14 the new task. However, the mammalian brain can avoid catastrophic forgetting thanks to synaptic  
15 consolidation, a process which reduces the plasticity of important synapses [3, 4].

16 Analogous to synaptic consolidation, [5] proposes the Elastic Weight Consolidation (EWC) algorithm,  
17 which slows down learning on weights that were important for previous tasks. This work became a  
18 pioneering approach in the continual learning literature. The key idea of EWC [5] is to remember  
19 old tasks by selectively penalizing gradients on the weights that were important for those tasks.  
20 More formally, given a previous task  $A$  with optimal parameters  $\theta_A^*$ , and a new task  $B$  with optimal  
21 parameters  $\theta_B^*$ , EWC protects the weights learned on task  $A$  by constraining the parameters  $\theta_B^*$  to be  
22 similar to  $\theta_A^*$ . Importantly, this penalty should be greater for parameters that were more important for  
23 task  $A$ . This is implemented using the diagonal of the Fischer information matrix,  $F$ :

$$L(\theta) = L_B(\theta) + \sum_i \frac{\lambda}{2} F_i (\theta_i - \theta_{A,i}^*)^2 \quad (1)$$

24 Where  $L_B(\theta)$  is simply the loss on the new task, and the penalty term  $\sum_i \frac{\lambda}{2} F_i (\theta_i - \theta_{A,i}^*)^2$  can  
25 be thought of as a prior-based constraint, which defines which directions of parameter variation  
26 are expected to cause severe performance degradation on the previous task. However, this penalty  
27 becomes ill-defined as the number of tasks increases. This is because we would need a separate  
28 penalty to embed the sub-components of the network which are deemed important for every single  
29 task. For example, suppose that we don't have 2 tasks, but 100 tasks,  $T \in \{T_1, T_2, \dots, T_{100}\}$ . The  
30 combined loss function when training on the 100th task in a continual learning setting would then

31 become:

$$\begin{aligned}
L(\theta) = L^{(T_{100})}(\theta) &+ \sum_i \frac{\lambda}{2} F_i^{(T_1)}(\theta_i - \theta_{T_1,i}^*)^2 \\
&+ \sum_i \frac{\lambda}{2} F_i^{(T_2)}(\theta_i - \theta_{T_2,i}^*)^2 + \dots \\
&+ \sum_i \frac{\lambda}{2} F_i^{(T_{99})}(\theta_i - \theta_{T_{99},i}^*)^2
\end{aligned} \tag{2}$$

32 We hypothesize that, if one were required to train a model on a large number of tasks, this penalty  
33 formulation would be prone to task saturation. This is because the additive nature of single-task  
34 penalties, which is required to memorize each previous task, will overshadow the loss of the new  
35 task if the regularization coefficient  $\lambda$  is sufficient big. Thus, the optimization path will favor small  
36 gradients in most directions, and, assuming a constraint of fixed parameter capacity, the model will  
37 be unable to learn a suitable representation of the new task. On the other hand, if  $\lambda$  is too small, the  
38 model might degrade to a catastrophic forgetting regime. It is unfortunately impossible to observe  
39 any evidence or refutation of this task saturation hypothesis in the original EWC paper, since they  
40 stopped training after 10 tasks of the permuted MNIST benchmark.

41 In this work, we investigated this trade-off between task saturation and forgetting. In order to do  
42 so, we designed a task sampling procedure on the CIFAR100 dataset which allows to train on  
43 several thousands of tasks. This method allows to really test EWC to its limits, and observe how the  
44 performance across tasks might change as the algorithm progresses through this extensive training.  
45 Our main objective is to conduct a robustness experiment on EWC, with the trade-off between task  
46 saturation and catastrophic forgetting in mind.

## 47 2 Related work

48 In the continual learning literature, EWC is often classified as a prior-based method. Other methods  
49 of this same family include SI [6], MAS [7], and, Riemannian Walk [8]. A common theme with  
50 prior-based methods is that, since they require a memory trace of every previously encountered task,  
51 it becomes increasingly hard with a larger number of tasks to make this memory trace sufficiently  
52 constraining in order to preserve critical information from each of these tasks, but not as constraining  
53 as to impede learning new tasks. Thus, other prior-based methods are likely to suffer from a similar  
54 trade-off than EWC, between task saturation and forgetting.

55 Riemannian Walk [8] is interesting because it also provides an algorithmic definition of intransigence,  
56 or the inability of a model to update its knowledge, which is closely related to task saturation. For  
57 this reason, [8] might be more robust to task saturation, but it is unclear whether a proper balance  
58 between intransigence and forgetting can be achieved in practice, especially when the number of  
59 tasks is sufficiently large.

60 In a similar line of thought than our EWC critique, [9] identified some frequent shortcomings of  
61 continual learning papers, in terms of the robustness of performance evaluation. They pointed out  
62 that popular benchmarks such as Permuted MNIST [10] and Split MNIST [6] tend to make continual  
63 learning easier for prior-based methods, since the distribution shift between tasks is fairly small.  
64 Thus, memory traces from previous tasks are more likely to be already well-aligned with an efficient  
65 representation of future tasks, even though the model has never seen any sample from the future tasks  
66 beforehand. Evaluating EWC on tasks derived from CIFAR100 instead of Permuted MNIST will  
67 also allow to test the algorithm in a more natural training environment.

## 68 3 Methods

69 In order to have a very large number of tasks, we define a task sampling procedure on the CIFAR100  
70 dataset, which can be summarized as follows:

- 71 1. Define the list  $T$  of all possible binary classification tasks.
- 72 2. Randomly select without replacement 50 class pairs, without replacement of the individual
- 73 CIFAR100 classes. Remove these class pairs from  $T$ .

74 3. Repeat until exhaustion of all the tasks in  $T$ .

75 We note that approach allows a total of 4950 tasks. Nevertheless, we decided to use only 100 tasks for  
76 our experiments, because we observed that the training behaviour of our models was already stable  
77 at this number of task. Also, we decided to use CIFAR100 as opposed to a larger dataset that also  
78 contains many classes, such as ImageNet, because we wanted to evaluate the robustness of EWC  
79 within a reasonable computational budget.

80 In addition to EWC, we implemented two baseline models to compare performance: the naive model  
81 and the foolish model. When it reaches a new task, the naive model keeps training on the parameters  
82 from the previous task, without any form of regularization. On the other hand, the foolish approach  
83 re-initializes the parameters randomly after each task. Because of this, the foolish model has no  
84 memory of previous tasks. We note that the foolish also doesn't have any form of regularization.

85 Finally, in terms of the model architecture, we used a convolutional neural network (CNN) with the  
86 following signature:

```
87 class Net(nn.Module):
88     def __init__(self):
89         super(Net, self).__init__()
90         self.conv1 = nn.Conv2d(1, 10, kernel_size=5)
91         self.conv2 = nn.Conv2d(10, 20, kernel_size=5)
92         self.conv2_drop = nn.Dropout2d()
93         self.fc1 = nn.Linear(500, 50)
94         self.fc2 = nn.Linear(50, 10)
95
96     def forward(self, x):
97         x = F.relu(F.max_pool2d(self.conv1(x), 2))
98         x = self.conv2_drop(self.conv2(x))
99         x = F.relu(F.max_pool2d(x, 2))
100        x = x.view(-1, 320)
101        x = F.relu(self.fc1(x))
102        x = F.dropout(x, training=self.training)
103        x = self.fc2(x)
104        return x
```

105 The models were trained using a stochastic gradient with a learning rate of 0.01 and a momentum  
106 coefficient of 0.9. In all cases, we used the accuracy metric to measure model performance.

## 107 4 Results

108 First, we measured the average accuracy of each model across all tasks, after training for some  
109 number of tasks (Figure 1). Contrary to our expectations, we do not observe any memory overhead  
110 with EWC. Indeed, the average accuracy already degrades to random performance after 10 tasks.  
111 We think that this could be due to the relatively small sample size in each of our tasks. Indeed, the  
112 size of the training partition of CIFAR100 is 50,000 samples, of which 500 samples belong to each  
113 class. Thus, each of our tasks, which exactly contains the samples from 2 of the CIFAR100 classes,  
114 only has 1000 samples. Given this small sample size, we think that the Fischer Information Matrix  
115 estimate from EWC might not be precise enough to effectively enforce a memory constraint on the  
116 previous tasks.

117 Another reason which might cause this rapid performance degradation of EWC is the distribution shift  
118 between different tasks. Indeed, in the original paper, EWC was evaluated on the Permuted MNIST  
119 benchmark, which always has small distribution shift as mentioned in [9]. However, CIFAR100 does  
120 not provide EWC with such a controlled environment, and the classification problem might vary from  
121 discriminating cars and airplanes to discriminating cats and dogs. It is possible that EWC just isn't  
122 robust to large distribution shifts between tasks.

123 We then measured the accuracy of the last task only, in order to investigate model saturation (Figure  
124 2). We observed that, even though there can be huge systematic performance variations between  
125 different tasks, the foolish model gets the best accuracy most of the time. This makes a lot of sense

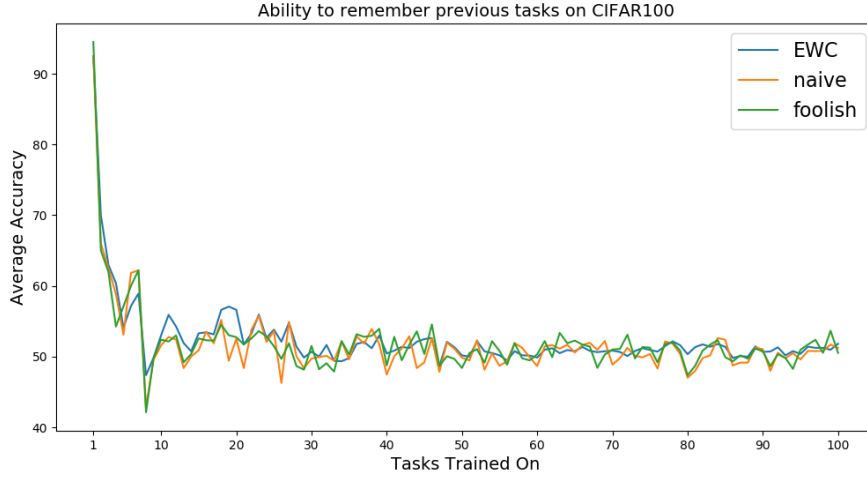


Figure 1: Ability to remember previous tasks on the CIFAR100 dataset. The average accuracy across all encountered tasks is measured against the number of tasks that the models have been trained on so far. EWC: Elastic Weight Consolidation.



Figure 2: Ability to learn a new task on the CIFAR100 dataset. The accuracy on the last task the models were trained on is plotted against the total number of training tasks so far. EWC: Elastic Weight Consolidation.

126 because, since the foolish doesn't have any memory of the previous tasks, it should not exhibit any  
 127 task saturation behaviour. We note that the naive model tends to have slightly worse accuracy than  
 128 the foolish model. Since the naive model also doesn't have any mechanism that could introduce task  
 129 saturation, this might just mean that, on average, random initialization is a better prior for model  
 130 learning than the optimal weights of a previous tasks.

131 In the case of EWC, we find that during the first 30 tasks of training, the accuracy on the last task  
 132 seems quite similar to the naive model. However, once we get beyond that point, we start to observe  
 133 much lower accuracy, and the accuracy is often not much better than random for EWC during the  
 134 second half of training. This suggests that task saturation is indeed happening, but several dozens  
 135 of tasks are required before it becomes a major issue. It would be interesting to investigate how the  
 136 dataset size or the distribution shift between tasks might affect the number of tasks required before  
 137 EWC enters a task saturation regime.

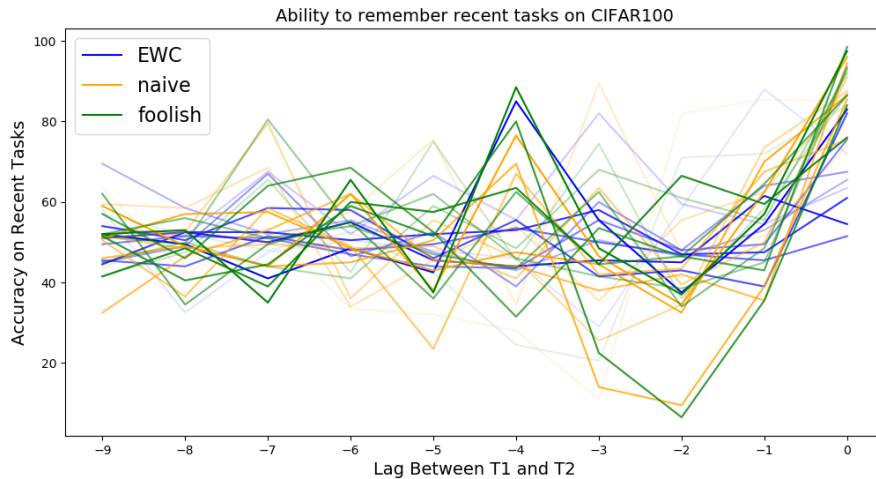


Figure 3: Ability to remember recent tasks on the CIFAR100 dataset. The accuracies up to a lag of 9 tasks are shown for each multiple of 10 tasks trained on. The most recent tasks are shown with opaque lines, and the first encountered tasks are shown with the more transparent lines. EWC: Elastic Weight Consolidation.

138 Finally, because the accuracy on previous tasks observed in Figure 1 was extremely low, even after  
 139 only a few tasks, we decided to investigate the short-term memory of EWC. The accuracies on the  
 140 previous 10 tasks after training for some number of tasks are shown in Figure 3. What we see is  
 141 that, even when looking only 2 or 3 tasks in the past, the performance is already almost random.  
 142 This reinforces our belief that, with the current experimental setting, the Fischer Information Matrix  
 143 estimate might not be precise enough to effectively enforce a memory constraint.

## 144 5 Conclusion

145 To conclude, we performed a robustness experiment on EWC using a novel task sampling procedure  
 146 on the CIFAR100 dataset. By randomly selecting pairs of CIFAR100 classes, we were able to train  
 147 the model on 100 distinct tasks. We observed that, after about 30 tasks of training, EWC starts to  
 148 exhibit task saturation, and it becomes very severe in the second half of training. This suggests that  
 149 a proper balance between task saturation and forgetting fails to be achieved when the number of  
 150 tasks is too large. We also observed, to our greatest surprise, that EWC didn't seem to remember  
 151 previous tasks any better than the naive model or the foolish model, and we identified two possible  
 152 reasons for this: first, the sample size could be too small to have a good Fischer Information Matrix  
 153 estimate; second, EWC might simply not robust to large distribution shifts. To investigate this first  
 154 hypothesis, one could replace CIFAR100 with the ImageNet dataset, and implement a similar task  
 155 sampling procedure to get a large number of task. However, using such a large dataset as ImageNet  
 156 would significantly increase the computational resources required to perform these experiments.

157 Additionally, we mentioned that prior-based methods in general are at risk of suffering from task  
 158 saturation when the number of tasks is large. An interesting future experiment would be to test  
 159 some of these other methods using a similar task paradigm. In particular, since Riemannian Walk  
 160 introduces an algorithmic definition of intransigence, it might fare a little bit better than competing  
 161 algorithms in that regard. Finally, we propose that our task sampling procedure can be replicated for  
 162 any continual learning approach, possibly with a larger dataset such as ImageNet, in order to properly  
 163 evaluate its robustness to task saturation, as well as other issues that may arise from a large number of  
 164 tasks. In the long-term agenda of continual learning, it will be necessary to develop artificial systems  
 165 that can not only prevent catastrophic forgetting, but also enable knowledge transfer from a large  
 166 body of previous tasks to learn new tasks more efficiently.

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