

Differentiate:

$$\sec(ax) \rightarrow a \sec(ax) \tan(ax) \quad \left[\sec(x) \equiv \frac{1}{\cos(x)} \right]$$

$$\tan(ax) \rightarrow a \sec^2(ax) \quad \left[\tan(x) \equiv \frac{\sin(x)}{\cos(x)} \right]$$

$$\csc(ax) \rightarrow -a \csc(ax) \cot(ax) \quad \left[\csc(x) \equiv \frac{1}{\sin(x)} \right]$$

$$\cot(ax) \rightarrow -a \operatorname{cosec}^2(ax) \quad \left[\cot(x) \equiv \frac{\cos(x)}{\sin(x)} \right]$$

$$\arcsin\left(\frac{x}{a}\right) \rightarrow \frac{1}{\sqrt{a^2 - x^2}}$$

$$\operatorname{arsinh}\left(\frac{x}{a}\right) \rightarrow \frac{1}{\sqrt{x^2 + a^2}}$$

$$\arccos\left(\frac{x}{a}\right) \rightarrow \frac{-1}{\sqrt{a^2 - x^2}}$$

$$\operatorname{arcosh}\left(\frac{x}{a}\right) \rightarrow \frac{1}{\sqrt{x^2 - a^2}}$$

$$\arctan\left(\frac{x}{a}\right) \rightarrow \frac{a}{a^2 + x^2}$$

$$\operatorname{arctanh}\left(\frac{x}{a}\right) \rightarrow \frac{a}{a^2 - x^2}$$

Integrate: (AU + C)

$$a^x \rightarrow \frac{a^x}{\ln(a)}$$

$$\tan(x) \rightarrow -\ln|\cos(x)|$$

$$\cos\theta \sin^n\theta \rightarrow \frac{\sin^{n+1}\theta}{n+1} \quad (\text{same for } \sin\theta \cos^n\theta, \text{ just switched})$$

$$\sinh(x) \rightarrow \cosh(x)$$

$$\cosh(x) \rightarrow \sinh(x)$$

$$\tanh(x) \rightarrow \ln|\cosh(x)|$$