PHAS1102 – Physics of the Universe

21st October 2009

Assignment 1 – Model answers

[marks]

1.

$$E = hv = h\frac{c}{\lambda} = 6.63 \times 10^{-34} \frac{3.0 \times 10^8}{663 \times 10^{-9}} J = 3.0 \times 10^{-19} J$$
$$= \frac{3.0 \times 10^{-19}}{1.6 \times 10^{-19}} eV = 1.9 \ eV$$

[2 marks total]

2. The star distance is d = 1/0.02" = 50 pc.

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The distance modulus will be $m - M = 5\log_{10}d - 5 = 8.5 - 5 = 3.5$ The absolute magnitude is M = m - 3.5 = 2.5 mag

[3 marks total]

3. If λ and λ_0 are the observed and emitted wavelengths respectively:

$$\frac{\lambda - \lambda_0}{\lambda_0} = \frac{v}{c}$$
 and $\lambda = \lambda_0 \left(1 + \frac{v}{c} \right)$

Thus the observed wavelength will be

(i) $\lambda = 660.0 \text{ x} (1-150/3.0 \text{x} 10^5) \text{ nm} = 659.7 \text{ nm}$ (because the star is travelling towards us)

(ii)
$$\lambda = 4340 \text{ x} (1+350/3.0\text{x}10^5) \text{ Å} = 4345 \text{ Å}$$

[2 marks total]

4. In the lectures the formula to compute the H energy levels was given:

 $E(n) = -13.6 \frac{1}{n^2}$ eV, thus for n = 2 (the first excited level above the ground

level with
$$n=1$$
) we have $E(1) = -3.4$ eV.

Thus the photon must have an energy,

$$E = 3.4 \text{ eV} = 3.4 \text{ x } 1.6 \text{ x } 10^{-19} \text{ J} = 5.44 \text{ x } 10^{-19} \text{ J}$$

This corresponds to a frequency,

$$v = \frac{E}{h} = \frac{5.44 \times 10^{-19}}{6.63 \times 10^{-34}} \text{Hz} = 8.2 \times 10^{14} \text{Hz}$$

and a wavelength

$$\lambda = \frac{ch}{E} = \frac{3 \times 10^8 \times 6.63 \times 10^{-34}}{5.44 \times 10^{-19}} \text{m} = 3.7 \times 10^{-7} \text{m} = 370 \text{ nm}$$

[4 marks total]

5. Let's set: $T_A = 18,000 \text{ K}$, $T_B = 6,000 \text{ K}$, $R_A = 2 R_B$

Applying the Stefan-Boltzmann law, the luminosity of star A will be

$$L_{\rm A} \propto T_{\rm A}^{4} R_{\rm A}^{2}$$

and that of star B
$$L_{\rm B} \propto T_{\rm B}^4 R_{\rm B}^2$$

Thus
$$\frac{L_A}{L_B} = \frac{T_A^4 R_A^2}{T_B^4 R_B^2} = \left(\frac{18000}{6000}\right)^4 \times (2)^2 = 324$$

[2 marks total]

6. (i) $(B-V) = 0.92$
(ii) $E(B-V) = (B-V) - (B-V)_0$
We can use the Sun's $(B-V)_0 = 0.62$ in the equation, since the star is of the same spectral type. Therefore, $E(B-V) = 0.3$.

(iii) $AV=3.1 E(B-V) = 0.93$
(iv) To derive the distance we use the distance modulus equation, using the absolute magnitude of the Sun for $M_V=4.82$ (assuming that all G2 stars have the same properties):

 $m_V=M_V=5 \log_{10} d - 5 + AV$
 $9.55-4.82=5 \log_{10} d - 5 + AV$
 $9.55-4.82=5 \log_{10} d - 5 + 0.93$
 $5 \log_{10} d = 8.8$
 $d = 57.5 \text{ pc}$

1 Thus the combination of the two stars will produce a flux Fsum= $(1+10) \times F_2$
Hence, $m_{\text{sum}} - m_2 = -2.5 \log_{10}(F_{\text{sum}}/F_2) = -2.5 \log_{10}(11 F_2/F_2)$ and $m_{\text{sum}} = -2.5 \log_{10}(11) + 8.5 = 5.9$

[3 marks total]

8. $V_1 = V_2 = 7.5$ and $B_1 = 8.0$, $B_2 = 8.9$
Thus $(B-V)_1 = 0.5$ and $(B-V)_2 = 1.4$
Star 1 is bluer, because its blue magnitude is smaller than for star 2.