

Theory

Language as a set of strings

Regular operation on language A, B

Union $A \cup B = \{x \mid x \in A \text{ or } x \in B\}$

Concatenation $A \circ B = \{XY \mid X \in A \text{ and } Y \in B\}$

Star $A^* = \{X_1, X_2, \dots, X_k \mid k \geq 0, X_i \in A\}$

Theorem:

There exist a language that is not regular

Type of proof

If A and only if B

Prove A leads to B and B leads to A

Proof by counter example (prove false)

Proof by construction

Proof by induction

Prove $n^2 \geq 2N$ given $n \geq 2$

Base case $2^2 \geq 2 \times 2$

Induction case: also true for $n=m$, prove that $n = m+1$

$(M+1)^2 \geq 2(M+1)$

$M^2 + 2M + 1 \geq 2M + 2$

$M^2 \geq 1$