JEE

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I. Section-A JEE Advanced/ IIT-JEE

1) $f(x) = \begin{vmatrix} \sec(x) & \cos(x) & \sec^2(x) + \cot(x)\csc(x) \\ \cos^2(x) & \cos^2(x) & \csc^2(x) \\ 1 & \cos^2(x) & \cos^2(x) \end{vmatrix}$

   Then $\int_0^{\frac{\pi}{2}} f(x)\,dx = \ldots$ (1987 - 2 Marks)

2) The integral $\int_0^{1.5} \left(x^2\right) dx$,   (1988 - 2 Marks)
   Where $[d]$enotes the greatest integer finction, equals $\ldots$

3) The value of $\int_{-2}^{2} |1 - x^2| dx$ is $\ldots$ (1989 - 2 Marks)

4) The value of $\int_{\frac{\pi}{4}}^{\frac{3\pi}{4}} \frac{\phi}{1+\sin\phi} d\phi$ (1993 - 2 Marks)

5) The value of $\int_2^3 \frac{\sqrt{x}}{\sqrt{5-x}+\sqrt{x}} dx$ (1994 - 2 Marks)

6) If for nonzero x, $af(x) + bf\left(\frac{1}{x}\right) = \frac{1}{x} - 5$ where $a \neq b$, then $\int_1^2 f(x) dx = \ldots$ (1996 - 1 Mark)

7) If $n > 0$, $\int_1^{2\pi} \frac{x\sin^{2n}x}{\sin^{2n}x+\cos^{2n}x} dx$ (1996 -1 Mark)

8) The value of $\int_1^{e^{37}} \frac{\pi\sin(\pi lnx)}{x} dx$ is $\ldots$ (1997 - 2 Marks)

9) Let $\frac{d}{dx}F(x) = \frac{e^{\sin(x)}}{x}, x > 0$. If $\int_1^4 \frac{2e^{\sin(x^2)}}{x} = F(k) - F(1)$ then one of the possible valued of k is $\ldots$ (1997 - 2 Marks)

II. Section B True/False

1) The value of the intrgral $\int_0^{2a} \frac{f(x)}{(f(x)+f(2a-x))} dx$ is equal to a (1988 - 1 Mark)

III. Section C MCQs with One Correct Answer

1) The value of the definite integral $\int_0^{2a} (1+e^{-x^2}) dx$ is

   a) -1

   b) 2

   c) $1+e^{-1}$

   d) none of these   (1981 - 2 Marks)

2) Let a, b, c be non-zero real numbers such that $\int_0^1 \left(1 + \cos^8(x)\right)\left(ax^2 + bx + c\right) dx = \int_0^2 \left(1 + \cos^8(x)\right)\left(ax^2 + bx + c\right) dx$.
   Then the quadratic equation $ax^2 + bx + c = 0$ has

   a) no roots in$(0, 2)$
   b) at least one root in$(0, 2)$
   c) double root in$(0, 2)$
   d) two imagenary roots   (1981 - 2 Marks)

3) The area bounded by the curves $y = f(x)$, the x-axis and the ordinate $x = 1$ and $x = b$ is $(b - 1)\sin(3b + 4)$. Then $f(x)$ is

   a) $(x - 1)\cos(3x + 4)$
   b) $\sin(3x + 4)$
   c) $\sin(3x + 4) + 3(x - 1)\cos(3x + 4)$
   d) none of the above   (1982 - 2 Marks)

4) the value of the integral $\int_0^{\frac{\pi}{2}} \frac{\sqrt{\cot(x)}}{\sqrt{\cot(x)}+\sqrt{\tan(x)}} dx$ is

   a) $\frac{\pi}{4}$
   b) $\frac{\pi}{2}$
   c) π
   d) none of the above   (1983 - 1 Marks)

5) For any integer n the integral- $\int_0^{\pi} e^{\cos^2(x)} \cos^3(2n + 1)xdx$ has the value

   a) π
   b) 1
   c) 0
   d) none of these   (1985 - 2 Marks)