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1)	If the characteristic	equation	of a 3x3	matrix	is λ^3 -	$-\lambda^2$ +	$\lambda - 1$	= 0,	then	the	matrix
	should be										

- a) Hermitian
- b) unitary
- c) skew symmetric d) identity

- 2) $2 \lim_{(x,y)\to(0,0)} \frac{x^4 + xy}{x^3 y^3}$ is
 - a) 0

b) 1

- c) -1
- d) does not exist

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3) If f(z) = u + iv is an analytic function and $u - v = (x - y)^3 + kxy(x - y)$, then k is

- a) 2
- b) -4
- c) 6
- d) -8

4) The directional derivative at the point P(1,2,3) to the surface $x^2 + \frac{y^2}{4} + \frac{z^2}{9} = 3$ in the direction of the vector \overrightarrow{OP} , where O denotes the origin, is

- a) 0
- b) $\frac{2}{\sqrt{14}}$
- c) $\frac{3}{\sqrt{14}}$
- d) $\frac{6}{\sqrt{14}}$

5) If the solution of the differential equation

$$\frac{dy}{dx} + P(x)y = xy^3$$

is $y^2(1+ce^{x^2})=1$, c being an arbitrary constant, then P(x) is

- a) -x
- b) $\frac{x}{2}$

c) x

d) 2x

6) The system of equations

$$ax + by + a^2 = 0$$

$$bx + ay - b^2 = 0$$

$$x + y + a - b = 0$$

- a) admits unique solution if $a = b \neq 0$
- b) admits unique solution if $a = -b \neq 0$
- c) admits unique solution if a = b = 0
- d) does not admit unique solution

7) The matrix

$$\begin{pmatrix} l & 0 & \sin \theta \\ 0 & 1 & m \\ n & 0 & \cos \theta \end{pmatrix}$$

is orthogonal, if

- a) $l = -\sin\theta, m = -\cos\theta, n = 0$
- b) $l = -\sin\theta, m = 0, n = \cos\theta$
- c) $l = \cos \theta, m = \sin \theta, n = 0$
- d) $l = -\cos\theta, m = 0, n = \sin\theta$
- 8) The radius of convergence of the real power series

$$\sum_{m=0}^{\infty} \frac{(m!)^2}{(2m+1)!} x^m$$

is

- a) 4
- b) 3
- c) 2
- d) 1
- 9) The value of

$$\left(\int_0^{\frac{\pi}{2}} (\sin \theta)^{3/4} d\theta\right) x \left(\int_0^{\frac{\pi}{2}} (\sin \theta)^{-3/4} d\theta\right)$$

is

a)
$$\frac{2\pi}{3}(\sqrt{2}+1)$$

c)
$$\frac{\pi}{2} \sqrt{3}$$

a)
$$\frac{2\pi}{3}(\sqrt{2}+1)$$

b) $\frac{2\pi}{3}(\sqrt{2}-1)$

c)
$$\frac{\pi}{2} \sqrt{3}$$

d) $-\frac{\pi}{2} \sqrt{3}$

10) If
$$f(z) = y(1+x^2) + x^2 + i(y^2 + 2y)x$$
 is differentiable at a point $z = z_0$, then $f'(z_0)$ is

- a) 0
- b) 1
- c) i
- d) -i
- 11) The value of the integral

$$\oint_{|z|=2} \frac{e^{1/z}}{(z-1)^2} dz$$

is

- a) 0
- b) $(2e\pi)i$
- c) $(4e\pi)i$
- d) $(4\pi)i$

12) The absolute value of the integral

$$\oint_c (-zdx + xdy + ydz),$$

where c is the curve obtained by the intersection of $x^2 + y^2 = a^2$, a > 0 and y = z, is

- a) $\frac{\pi a^2}{\sqrt{2}}$ b) $\frac{\pi a^2}{\sqrt{3}}$
- c) $\pi a^2 \sqrt{2}$
- d) $2\pi a^2$
- 13) One of the values of

$$\frac{1}{(4x^2D^2 + 8xD + 1)}(\ln x) \text{ where } D \equiv \frac{d}{dx},$$

is

- a) $\ln x + 4$
- b) $\ln x 4$
- c) $4 \ln x 4$
- d) $4 \ln x + 4$
- 14) A particular integral of the differential equation

$$\frac{d^2y}{dx^2} - y = \sec hx$$

is

- a) $-(\cosh x)(\ln \cosh x) + x \sinh x$
- b) $-(\sinh x)(\ln \cosh x) + x \cosh x$
- c) $(\cosh x)(\ln \sinh x) + x \sinh x$
- d) $(\sinh x)(\ln \cosh x) x \cosh x$
- 15) If u = u(x, t) is such that

$$\frac{\partial^2 u}{\partial t^2} = 4 \frac{\partial^2 u}{\partial x^2}, 0 \le x \le \pi, t \ge 0,$$

$$u(0,t) = u(\pi,t) = 0, u(x,0) = 0, \frac{\partial u}{\partial t}(x,0) = \sin x,$$

then $u\left(\frac{\pi}{3}, \frac{\pi}{6}\right)$ is

- 16) The two lines of regression of the variables x and y are 4x+2.4y = 20 and 1.6x+4y = 2012. The coefficient of correlation between x and y is

- a) 0.49
- b) -0.49
- c) 0.35
- d) -0.35
- 17) While solving the initial value problem $\frac{dy}{dx} + ky = 0$, y(0) = 1 at x = h by fourth order Runge-Kutta method, the expression for k_3 is
 - a) $-kh + \frac{(kh)^2}{2!} \frac{(kh)^3}{3!}$ b) $-kh + \frac{(kh)^2}{2!} \frac{(kh)^3}{3!}$ c) $-kh + \frac{(kh)^2}{2} \frac{(kh)^3}{4}$ d) $-k\left(1 + \frac{h}{2} \frac{h^2}{3}\right)$