



Quantum
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Hardware

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Quantum
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Simulation
Qubits

Hardware
devices

Simplifying
circuits

Designing
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circuits

Measuring and
characterizing

Quantum Computing Hardware

Ed Kuijpers¹

HBO-ICT Technical Computing

May 16, 2024

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Qubit hardware overview

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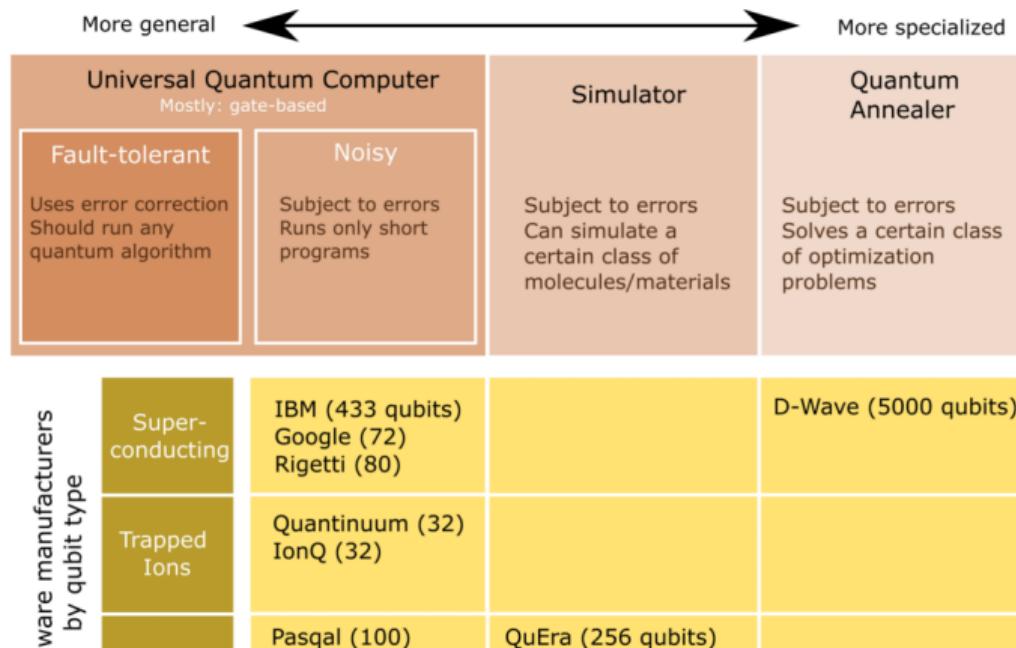
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- The professional's guide to Quantum Technology
- The hardware part guide





Quantum theory and simulation

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- Scientific Python examples
- 1D-tutorial equation solution
- Solving Schrödinger equations numerically
- Elektromagnetism
- QuTiP.org, QuTIP github
- QuTIP github



Classic damped oscillator

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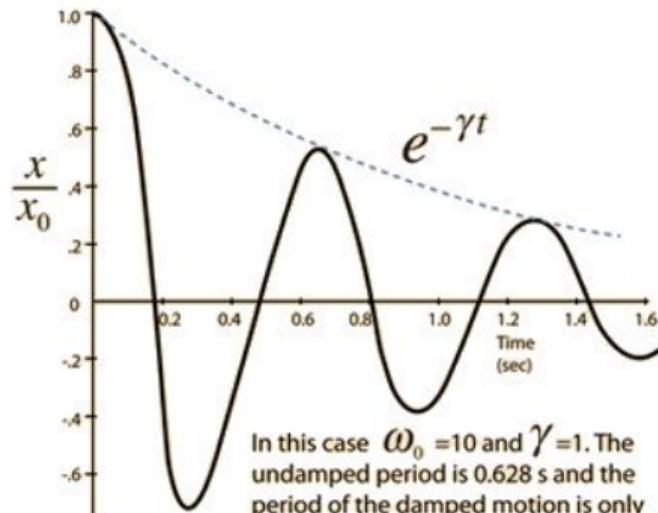
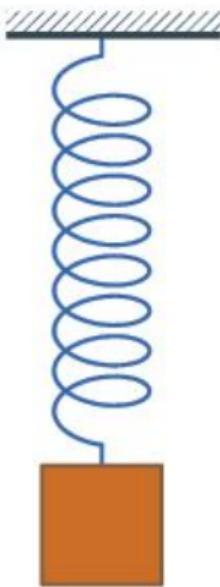
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Classic damped oscillator



In this case $\omega_0 = 10$ and $\gamma = 1$. The undamped period is 0.628 s and the period of the damped motion is only marginally longer, 0.632 s.



Quantum Mechanics basics

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the wave function conclusively describes the chance to detect the particle according to a probability distribution:

$$P(\mathbf{x}) = \psi^*(\mathbf{x}) \cdot \psi(\mathbf{x}) = \|\mathbf{x}\|^2$$

where the * denotes a complex conjugate, or negating the imaginary part of the number, and the whole operation is equivalent to getting the magnitude squared of the complex numbers. This probabilistic interpretation requires that the following be true:

$$\int \|\psi(\mathbf{x})\|^2 d\mathbf{x} = 1$$

meaning the meaning the total magnitude of the complex field is 1, conserving p



Time evolution Schrödinger equation

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The purpose of quantum mechanics is to describe how wave functions change as a function of time, i.e. $\psi(\mathbf{x}, t)$. This is captured by the Schrödinger equation in its most general form:

$$i\hbar \frac{\partial \psi(\mathbf{x}, t)}{\partial t} = \mathcal{H}(\psi(\mathbf{x}, t))$$

Here, \mathcal{H} is called the Hamiltonian operator and essentially measures, or specifies, the energy of a wave function. Namely, the energy of a wave function is the expectation value of the Hamiltonian, which physicists write as

$$E = \mathbb{E}(\mathcal{H}) = \int \psi^*(\mathbf{x}) \mathcal{H} \psi(\mathbf{x}) d\mathbf{x}$$

which can be thought of as a weighted average of the Hamiltonian applied to the wave function everywhere.



Solving Schrödinger equation

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The Schrödinger equation says that the rate of change of the wave function is related to the energy of $\phi(x)$. Eigenstates satisfy the following relationship:

$$\mathcal{H}\phi = E\phi$$

meaning the result of the Hamiltonian operating on ϕ is the same wave function ϕ scaled by a fixed energy E constraints on what ϕ can be, which depends on exactly what the Hamiltonian is. Eigenstates of the Hamiltonian will satisfy

$$\frac{d\phi}{dt} = -iE\phi$$

The solution to this is any function proportional e^{iEt} , which shows that

$$\phi(x, t) = e^{iEt} \phi(x)$$

meaning only the complex phase of the eigenstates change with time, which is the



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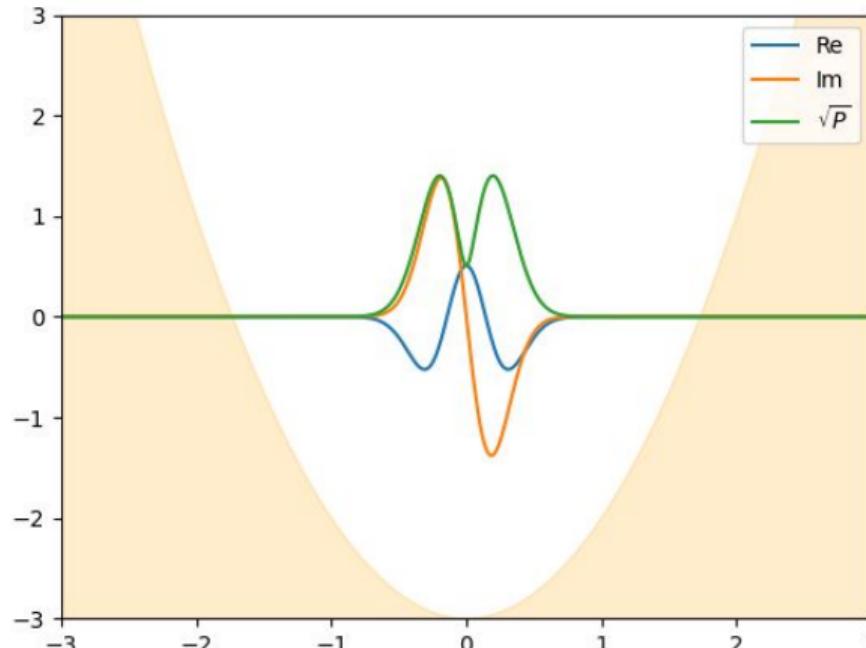
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See notebook extracted from: [Quantum Mechanics simulation](#)





Quantum Harmonic Oscillator

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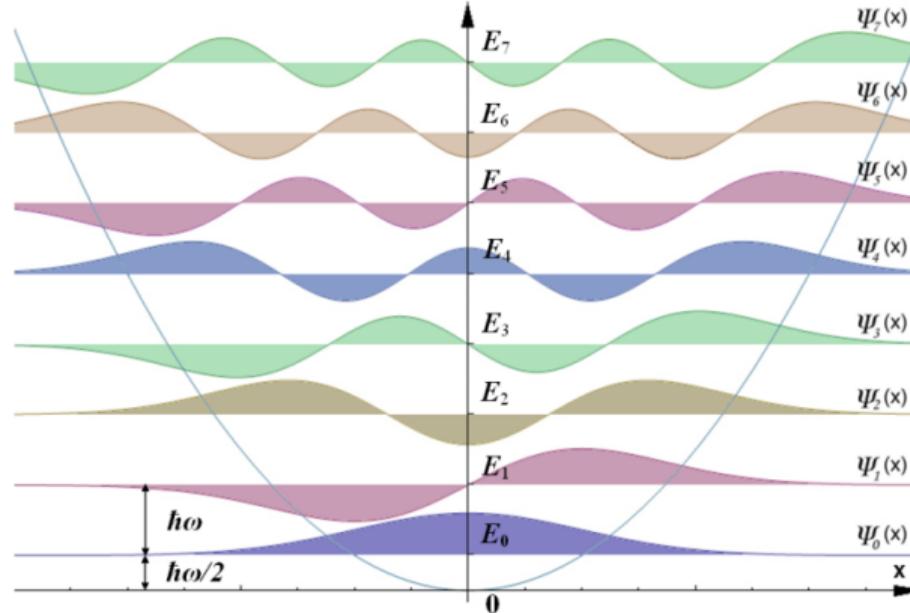
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$$H = \sum_k E_k |\psi_k\rangle \langle \psi_k|, \langle \psi_k| |\psi_k\rangle = \delta_j, k, |\psi_k\rangle \mapsto |k\rangle$$





Quantum Machine Learning and stack

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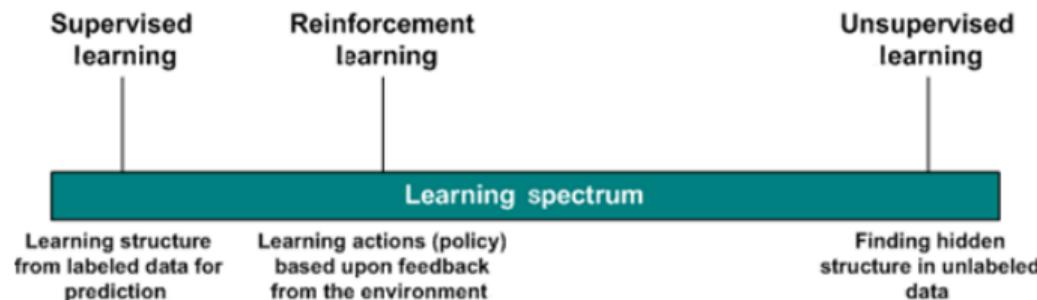
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- ML Tutorials Qiskit)
- Pennylane.ai
- Recent package sklearn [1]
- Qiskit and AI [2]
- Optimizatioin and Learnning ofview[3]
- Overviews: [4], [5], [6]





News messages May 2024

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- Teleoperation Breakthrough
- Breakthrough high temperature superconductors
- Rydberg quantum simulation
- QuEra
- NVida CUDA-Q
- new groundbreaking device
- Million Qubits?
- Fault-tolerant quantum memory
- Alternatives?
- Promising?



Investigating electronics

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- IBM Quantum learning
- Example in Transmon physics
- pennylane.ai



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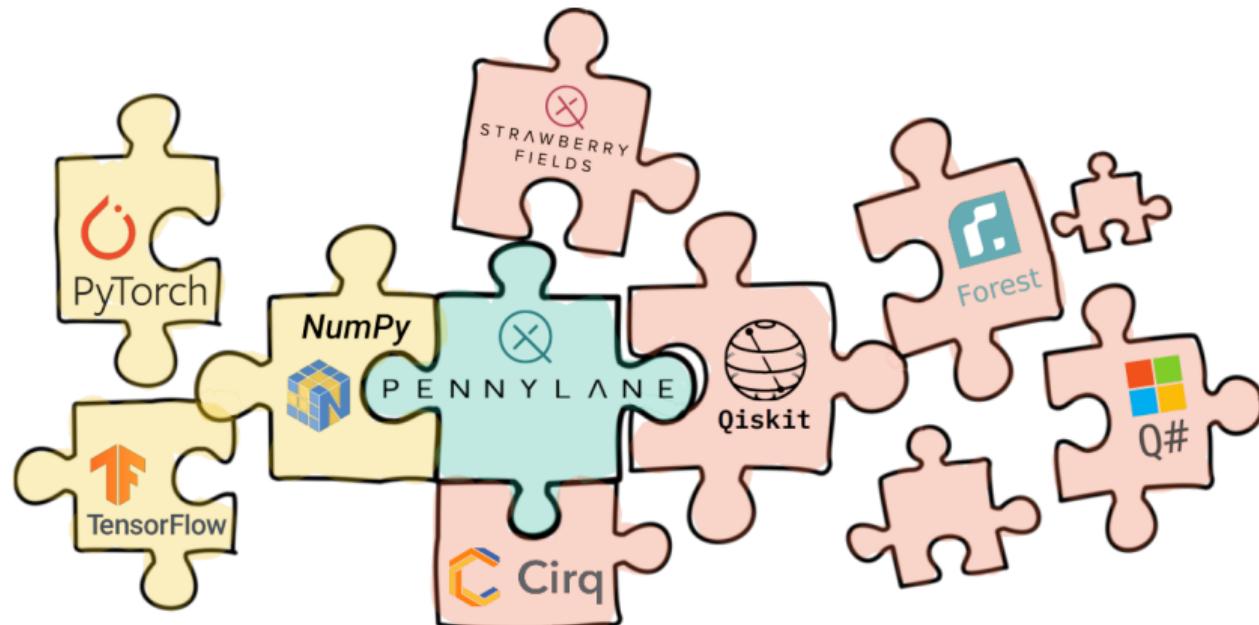
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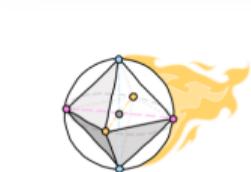
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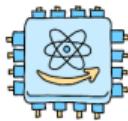
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▀ Demo

Efficient Simulation of
Clifford Circuits



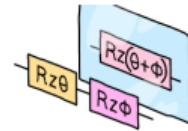
▀ Demo

Getting started with the
Amazon Braket Hybrid Jobs



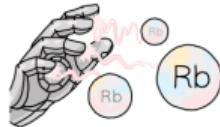
▀ Demo

Using PennyLane with IBM's
quantum devices and Qiskit



▀ Demo

Compilation of quantum
circuits



▀ Demo

Pulse programming on
Rydberg atom hardware



▀ Demo

Using PennyLane with PySCF
and OpenFermion



▀ Demo

Using JAX with PennyLane



▀ Demo

Computing gradients in
parallel with Amazon Braket



Pennylane demos HW 2

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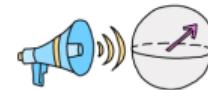
Demo

Turning quantum nodes into
Torch Layers



Demo

Turning quantum nodes into
Keras Layers



Demo

Optimizing noisy circuits with
Cirq



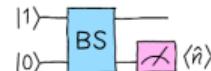
Demo

PyTorch and noisy devices



Demo

Training a quantum circuit
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Demo

Plugins and hybrid
computation





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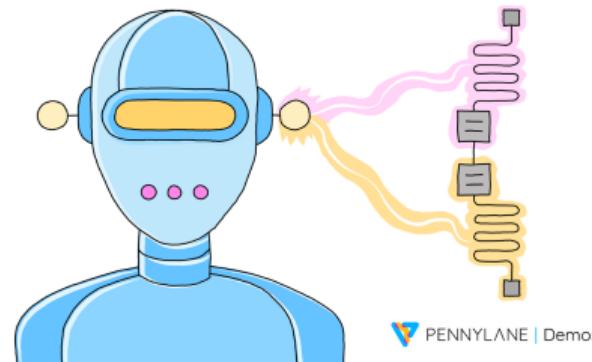
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Gate calibration reinforcement Learning



Other approach [7]



Quantum, Reinforcement learning and robotic navigation

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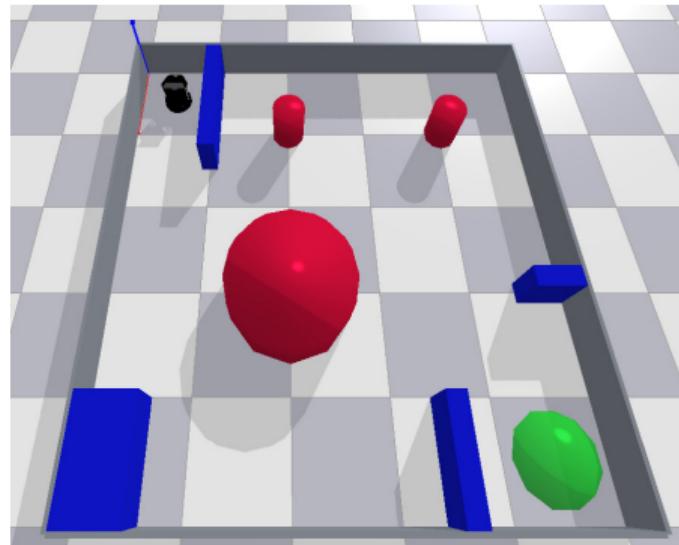
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- Quantum Deep Reinforcement Learning for Robot Navigation Tasks [8]





Pennylane hardware notebook tutorial

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quantum_volume.ipynb tutorial_mbqc.ipynb tutorial_neutral_atoms.ipynb
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- Overview ([9], [10])
- Different qubits overview
- Google ([11])
- QC_CMU
- Course: the Hardware of a Quantum Computer
- Qubit dashboard Factbased Insight



Superconducting Quantum Computer example

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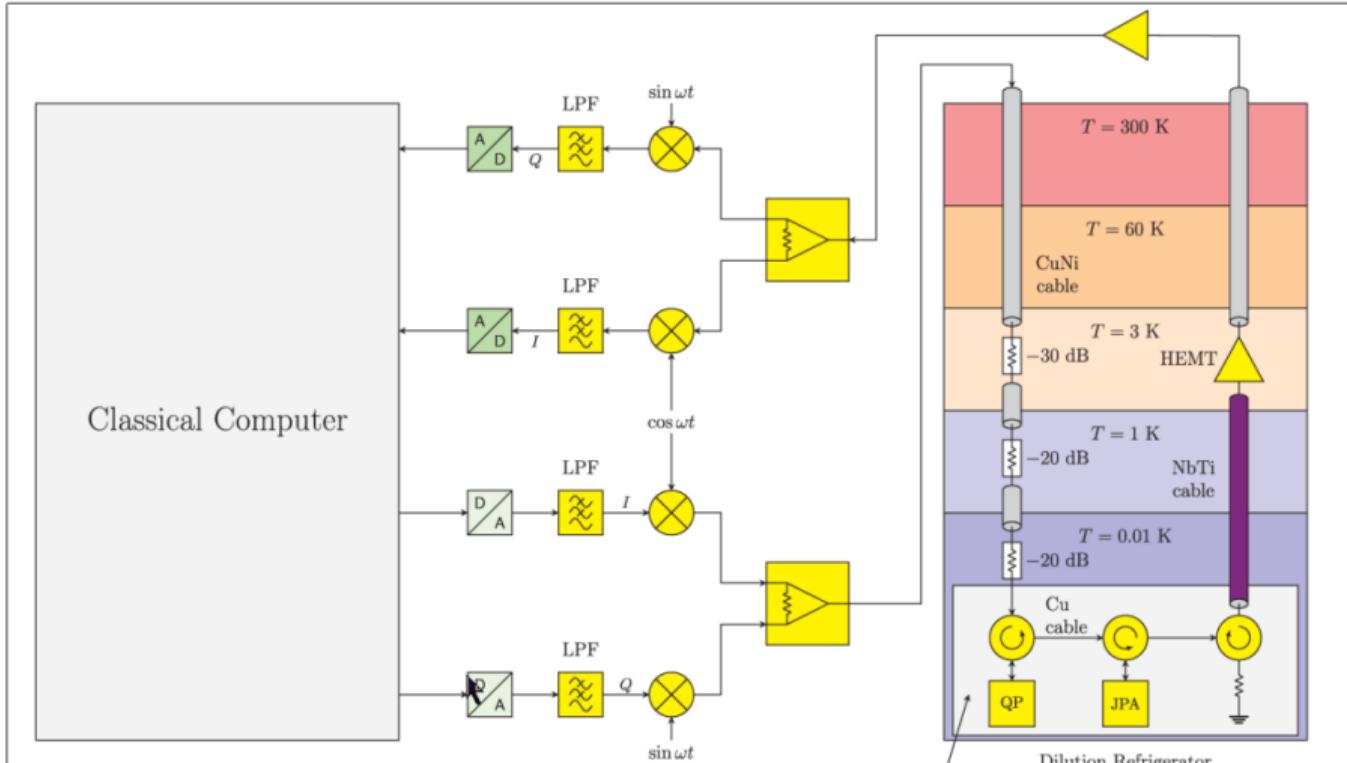
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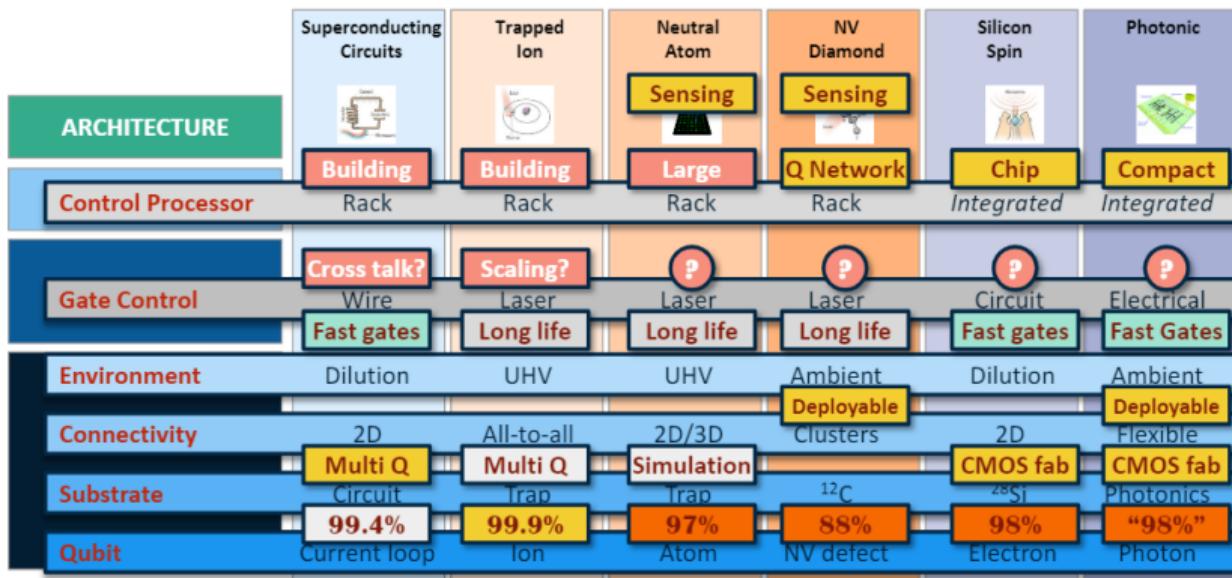
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Old high level comparison of qubit technologies





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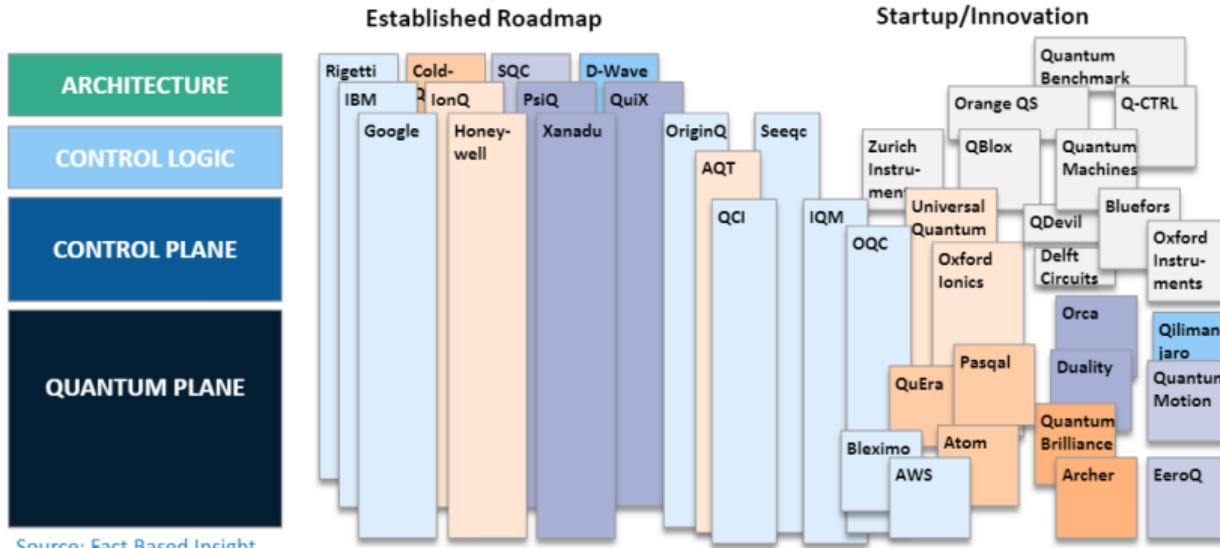
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Established players plus thriving startups and innovation





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	Superconducting Circuits	Trapped Ions	Neutral Atoms	NV Diamond	Silicon Spin	Photonic
Important Variants	Tunable, Fixed Freq., Parametric	Hyperfine, Optical, NF Microwave, GF Microwave	Hyperfine, Optical	Nitrogen Vacancy, Silicon Vacancy	Quantum Dots, Imp. Donor, STM-Fab. Door	MBQC, CVQC
Qubit T2 Lifetimes	Short 15-120µs	Long 0.2-50s	Long 0.2-50s	Long 10s	Mixed 1µs-0.5s	Short 150µs
2Q. Gate Fidelity	High 99%-99.85%	High 99%-99.9%	Promising 97%	Interesting 99% (88%)	Promising 98%	Promising 98%
Gate Speeds	Fast 12-200ns	Mixed 1µs-3ms	Intermediate 1µs	Slow 100µs	Fast 0.8-80ns	Very Fast 1ns
Lifetime/ Speed	1250-100	1000000-500	1000000-100000	c.100000	10-50	c.150000
Environment	20mK	Ultra High Vacuum	Ultra High Vacuum	Ambient	20mK - 1K	1K - 10K (detectors)
Current Devices	65Q	20Q	51Q	10Q	2Q	12Q
Announced Devices for 2021	100Q 128Q	32Q 50Q	100Q	10Q	6Q	24Q 40Q-80Q
FTQC Footprint	Building	Building	Large	Network	Chip	Compact

Source: Fact Based Insight

1s = 1000ms = 1000,000µs = 1000,000,000ns





Optical quantum computer progress

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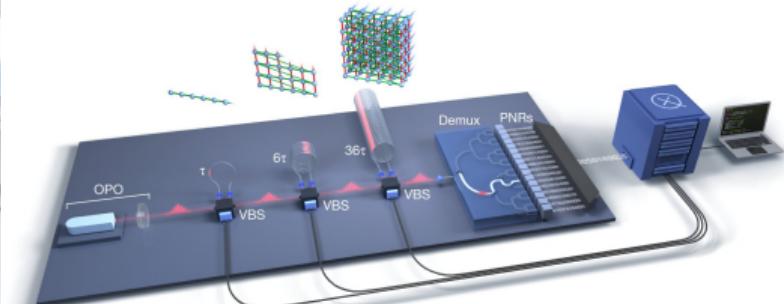
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- New Scientist announcement 1 June 2022: Advanced quantum computer made available to the public for first time (219 photons)
- Quantum computational advantage with a programmable photonic processor
- Jiuzhang 3.0 255 photons detected





Quantum stack

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A simplified quantum stack





Quantum HW roadmap

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Quantum hardware roadmaps are hard to directly compare

Platform	Player	2020	2021	2022	2023	2024	2025 to 2030	
Superconducting	Google	53Q	100Q		10^3 Q		10^4 Q -	10^4 Q - 1MQ
Superconducting	IBM	65Q	127Q	433Q	1121Q		path to 1MQ	
Superconducting	Rigetti	32Q	4x32Q					
Trapped Ion	Honeywell	H1		H2		H3	H4	H5
Trapped Ion	IonQ	22AQ		29AQ		256AQ		1024AQ
Neutral Atom	ColdQuanta		100Q	300Q		1000Q		
Silicon	CEA Leti		6Q		100Q			
Silicon	SQC			10Q				100Q
Photonic	QuiX		12Qm	50Qm				
Photonic	PsiQ						1MQ	
Photonic	Xanadu	X24	X40	X80	XD80			1MQ

Source: Fact Based Insight



Atoms and spectra

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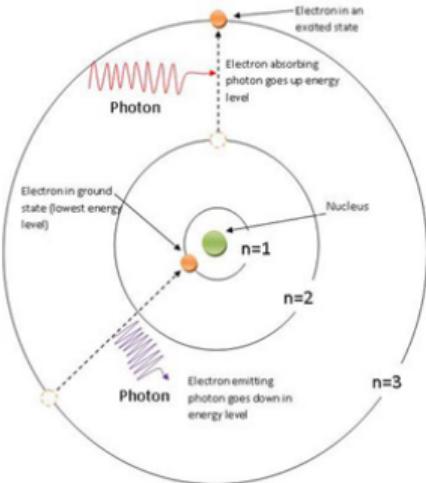


Figure 3

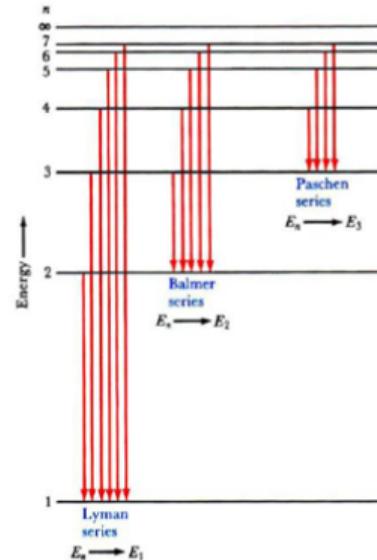


Figure 4



Quantum qubits

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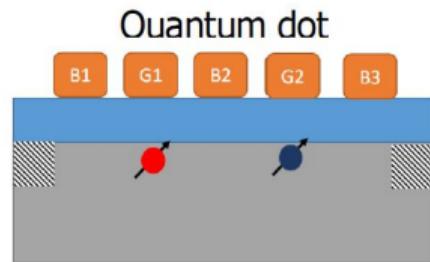
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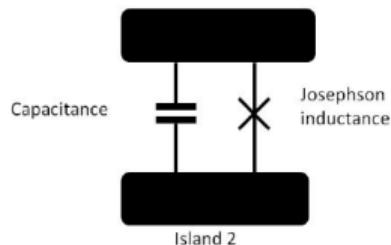
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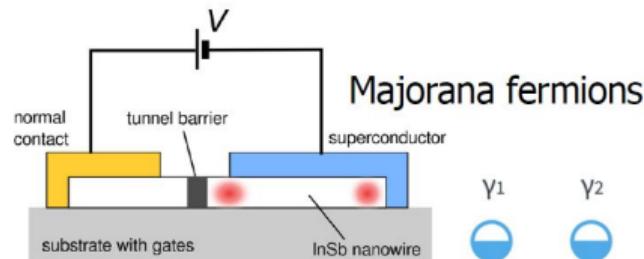
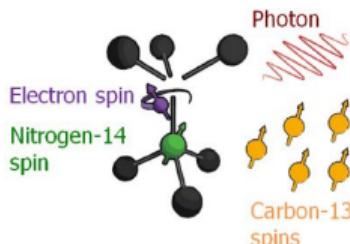
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Superconducting transmon



The NV center in diamond





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	Qubit(s)	Measured quantity(ies)	Typical frequency
Neutral atoms	Atomic vapor	Atomic spin	Magnetic field, Rotation, Time/Frequency
	Cold clouds	Atomic spin	Magnetic field, Acceleration, Time/Frequency
Trapped ion(s)		Long-lived electronic state Vibrational mode	Time/Frequency Rotation Electric field, Force
Rydberg atoms		Rydberg states	Electric field
Solid state spins (ensembles)	NMR sensors NV center ensembles	Nuclear spins Electron spins	Magnetic field Magnetic field, Electric field, Temperature, Pressure, Rotation
Solid state spins (single spins)	P donor in Si Semiconductor quantum dots Single NV center	Electron spin Electron spin Electron spin	Magnetic field Magnetic field, Electric field Magnetic field, Electric field, Temperature, Pressure, Rotation



Quantum sensing 2

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Superconducting circuits				
SQUID	Supercurrent	Magnetic field	DC–10 GHz	
Flux qubit	Circulating currents	Magnetic field	DC–10 GHz	
Charge qubit	Charge eigenstates	Electric field	DC–10 GHz	
Elementary particles				
Muon	Muonic spin	Magnetic field	DC	
Neutron	Nuclear spin	Magnetic field, Phonon density, Gravity	DC	
Other sensors				
SET	Charge eigenstates	Electric field	DC–100 MHz	
Optomechanics	Phonons	Force, Acceleration, Mass, Magnetic field, Voltage	kHz–GHz	
Interferometer	Photons, (Atoms, Molecules)	Displacement, Refractive Index	–	

Table: Experimental implementations of quantum sensors. SET: single electron transistor, NV: nitrogen-vacancy, status 2017 ([12])



Quantum technology hardware for distributed operations

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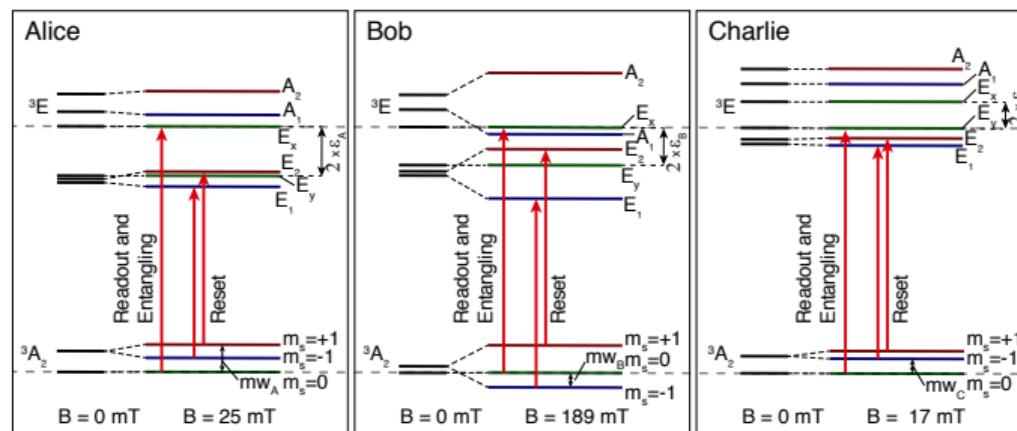
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- Technology of quantum clocks to synchronize **integrated quantum clock consortium**. Prof. Florian Schleck from the University of Amsterdam is involved.
- In the quantum internet experiments in Delft spectra used ([13]) with a demo ([14])





Quantum technologies for space applications

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Cooperation between ESA and EU (see e.g. Policy papers)

- Secure Quantum Communication (QKD via satellite)
- Quantum technology for accurate time and Frequency Transfer (e.g. Navigation)
- Earth Sensing and Observation(e.g. measuring gravity field Earth)
- Fundamental Physics (e.g. Bose-Einstein Condensates)



QuTech Quantum computer visit

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Webreference of related projects in vandersypenlab





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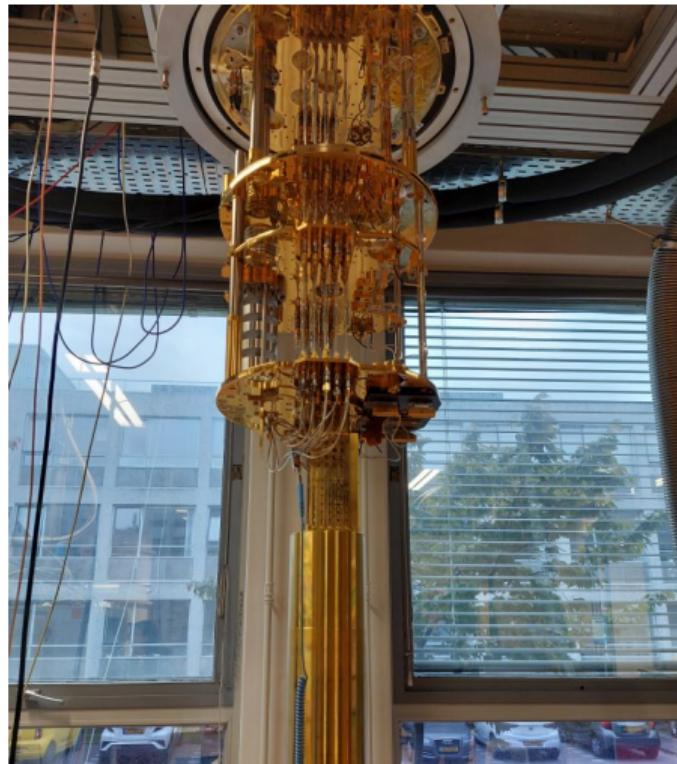
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Neutral atoms

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Four laser beams around atom ensemble to realise Magnetic-Optical-Trap

FACT BASED / INSIGHT

Trapped ions – very different approaches

Notable variations	USP	Key Challenge	Notable Players	Leading device 2020	Announced For 2021
Hyperfine qubits with laser gates	99.9% Highest fidelity	Scaling-up laser control system	IonQ, Honeywell	10Q (QV 128)	QV
Optical qubits with laser gates	99.6% Easier optical integration	Mitigating shorter qubit lifetime	AQT, NextGenQ	20Q	50Q
Hyperfine qubits with near-field microwave gates	99.7% High fidelity without lasers	Demonstrate multi-qubit device	Oxford Ionics	2Q	
Dressed states with global-field microwave gates	Very modular and scalable	2Q gate fidelities	Universal, NextGenQ	2Q	



Trapped Ions

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Source: Fact Based Insight



Superconducting circuits

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FACT BASED INSIGHT

Superconducting circuits – a challenge of fidelity and scaling

Notable variations	USP	Key Challenge	Notable Players	Leading device 2020	Announced For 2021
Tunable qubits	Fast gates 99.7%	Scaling-up	Google, OriginQ, QuTech, IQM, Seeqc,	53Q	100Q
Fixed-frequency	Longer qubit lifetime 99.85%	Integrating tunable couplers	IBM, OQC	27Q (QV 128)	128Q
Parametric gates	Hybrid benefits 99%	2Q gate fidelities	Rigetti, Bleximo,	32Q	4x32Q
Flux qubits	Rapid scale-up for quantum annealing	Demonstrating quantum advantage	D-Wave, Qilimanjaro	5000Q	

Source: Fact Based Insight



Example NOT-gate

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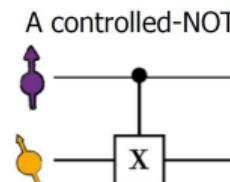
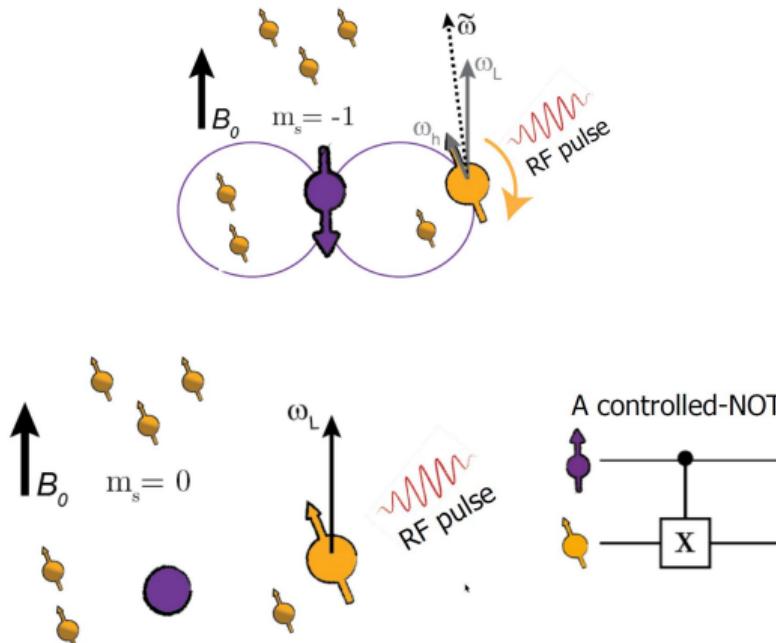
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Different Superconducting Qubit types

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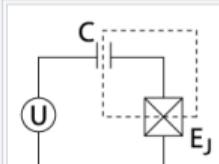
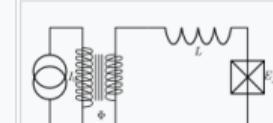
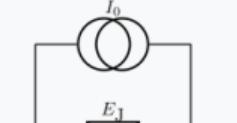
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Type Aspect	Charge qubit	RF-SQUID qubit (prototype of the Flux Qubit)	Phase qubit
Circuit	 <p>Charge qubit circuit. A superconducting island (encircled with a dashed line) is defined between the leads of a capacitor with capacitance C and a Josephson junction with energy E_J biased by voltage U.</p>	 <p>Flux qubit circuit. A superconducting loop with inductance L is interrupted by a junction with Josephson energy E_J. Bias flux Φ is induced by a flux line with current I_0.</p>	 <p>Phase qubit circuit. A Josephson junction with energy parameter E_J is biased by current I_0.</p>
Hamiltonian	$H = E_C(N - N_g)^2 - E_J \cos \phi$ <p>In this case N is the number of Cooper pairs to tunnel through the junction, $N_g = CV_0/2e$ is the charge on the capacitor in units of Cooper pairs number, $E_C = (2e)^2/2(C_J + C)$ is the charging energy associated with both capacitance C and Josephson</p>	$H = \frac{q^2}{2C_J} + \left(\frac{\Phi_0}{2\pi}\right)^2 \frac{\phi^2}{2L} - E_J \cos\left[\phi - \Phi \frac{2\pi}{\Phi_0}\right]$ <p>Note that ϕ is only allowed to take values greater than 2π and is alternatively defined as the time integral of voltage along inductance L.</p>	$H = \frac{(2e)^2}{2C_J} q^2 - I_0 \frac{\Phi_0}{2\pi} \phi - E_J \cos \phi$ <p>Here Φ_0 is magnetic flux quantum.</p>



Different potentials Qubit

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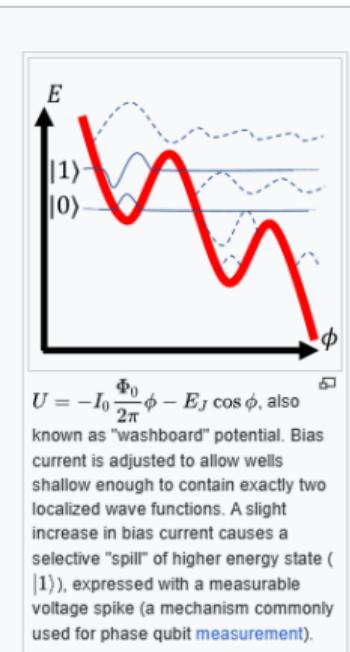
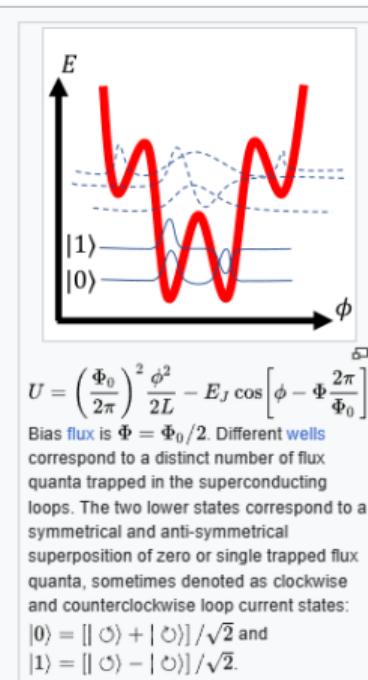
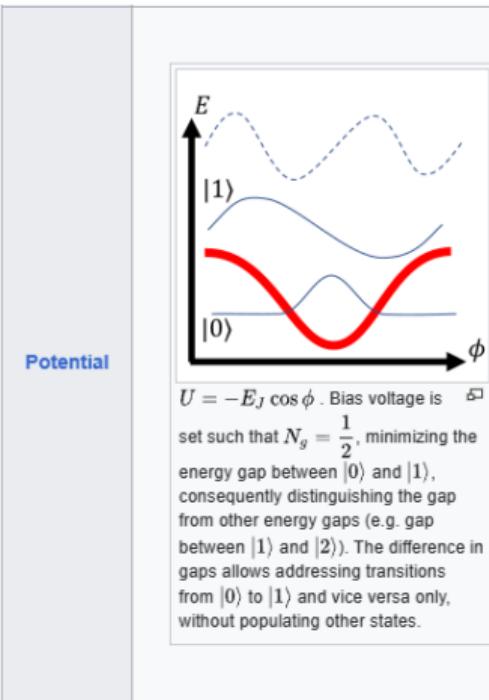
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D-wave SQUID

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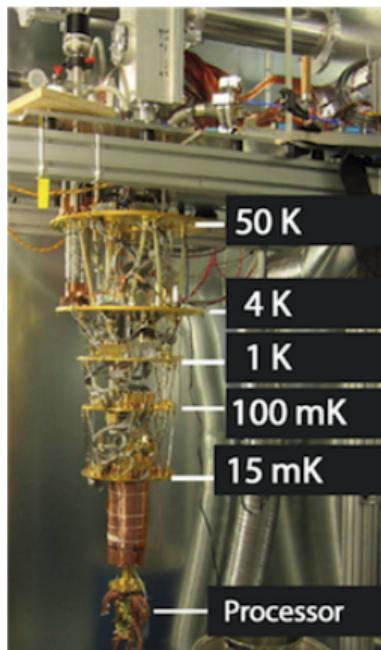
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How annealing Works in D-Wave QPUs D-wave hardware references, D-Wave Quantum hardware





D-Wave hardware cross-section

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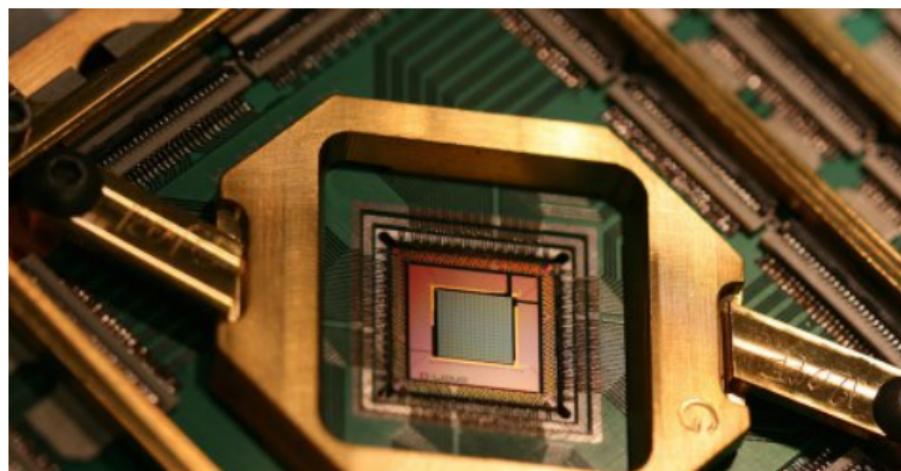
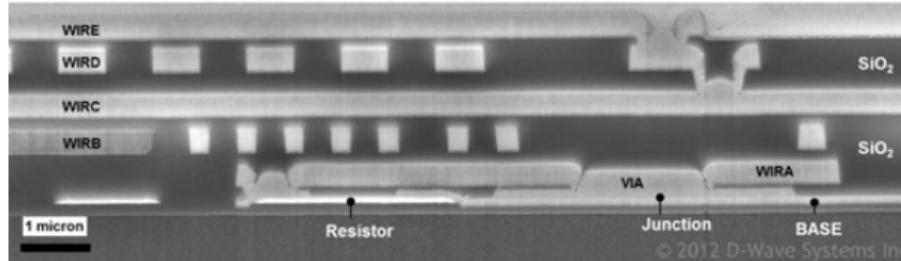
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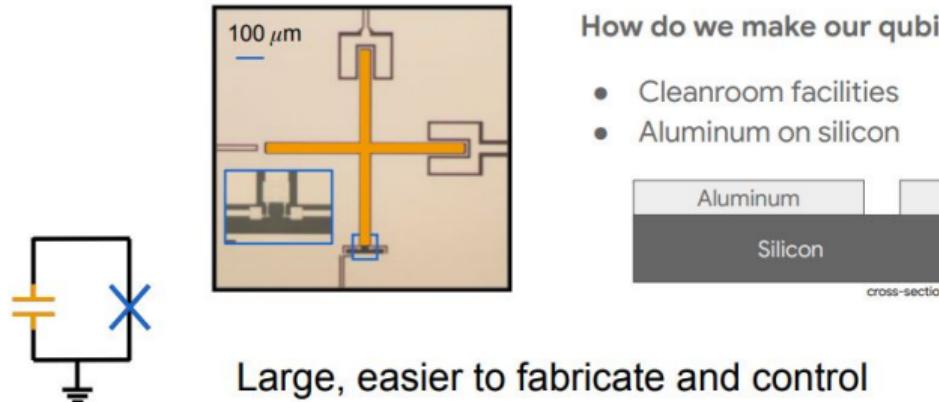
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GHz microwave oscillator



How do we make our qubits?

- Cleanroom facilities
- Aluminum on silicon

Aluminum

Silicon

cross-section



Harmonic Oscillator

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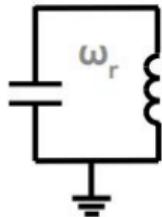
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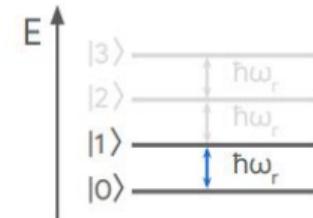
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Quantum mechanics: **energy is quantized**,
oscillator stores n photons (of energy $\hbar\omega_r$)



Quantum state is encoded in the energy level of an (electric circuit) oscillator

Details computation: [Qiskit intro Transmon Physics](#)



9 Qubits

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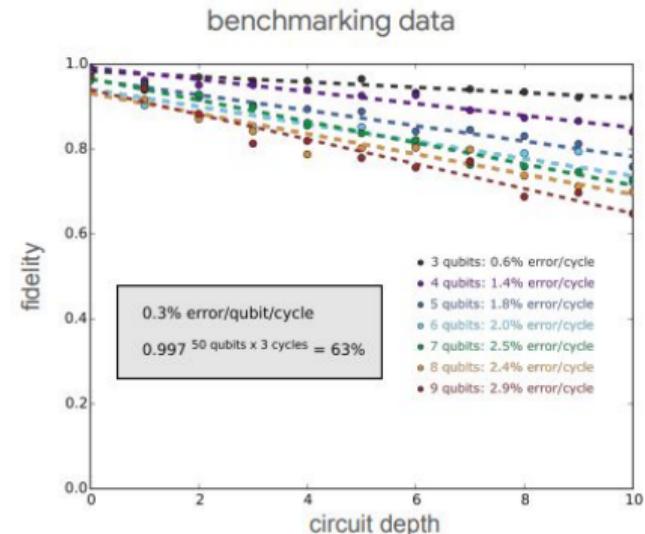
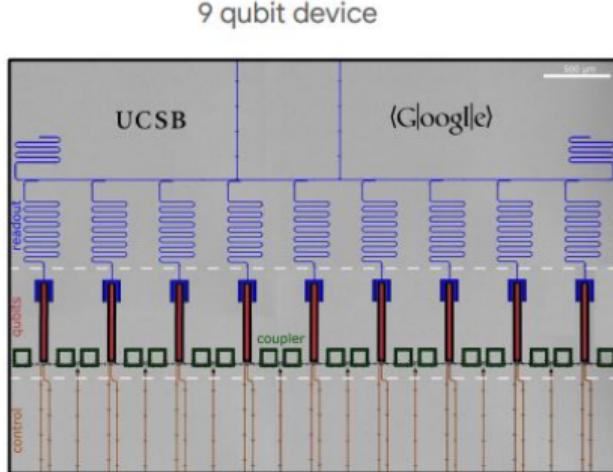
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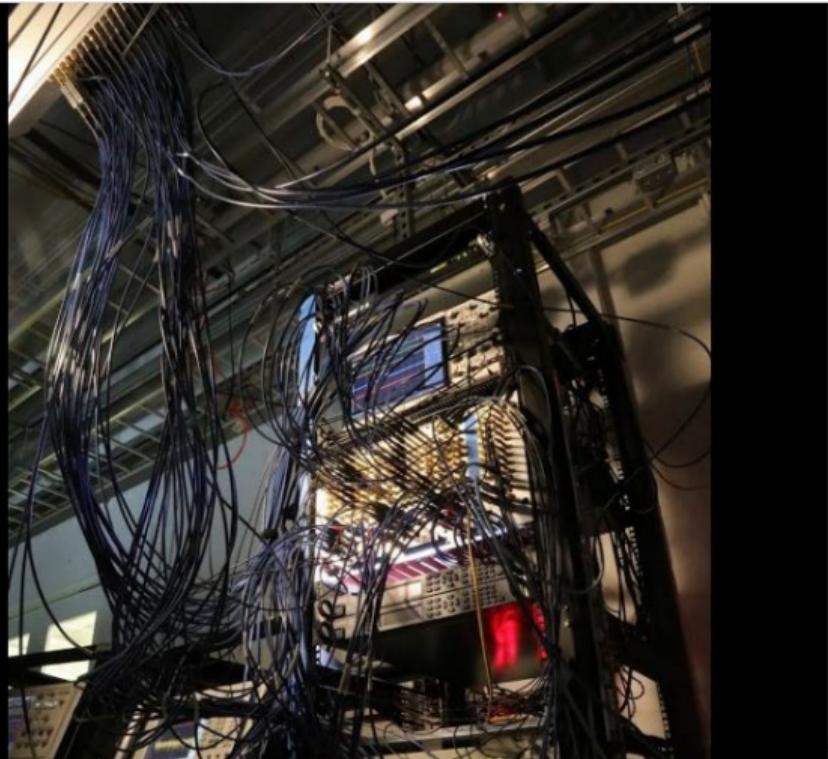
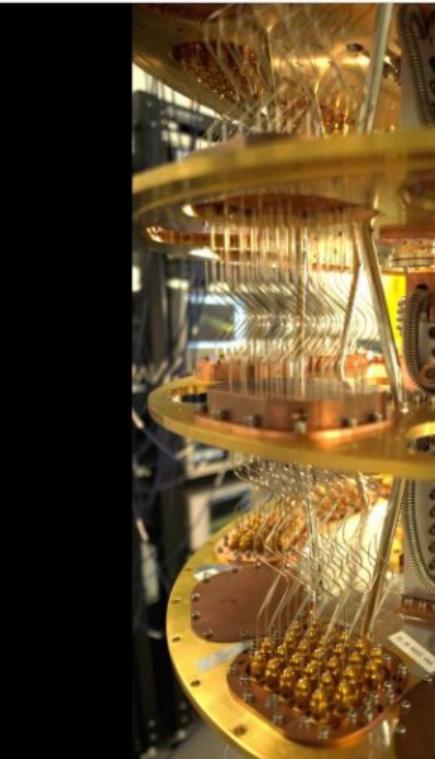
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Gate implementation

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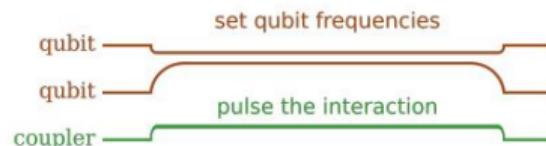
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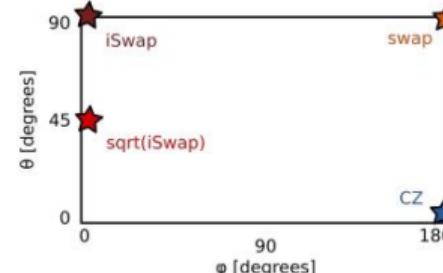
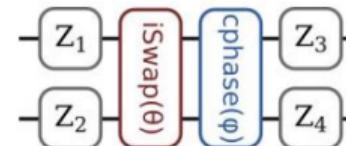
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$$\begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & e^{i\alpha} \cos \theta & e^{i\beta} \sin \theta & 0 \\ 0 & e^{i\gamma} \sin \theta & e^{i\delta} \cos \theta & 0 \\ 0 & 0 & 0 & e^{i\phi} \end{pmatrix}$$

00 01 10 11

Model for arbitrary photon-conserving gate





Transmon-5 factsheet

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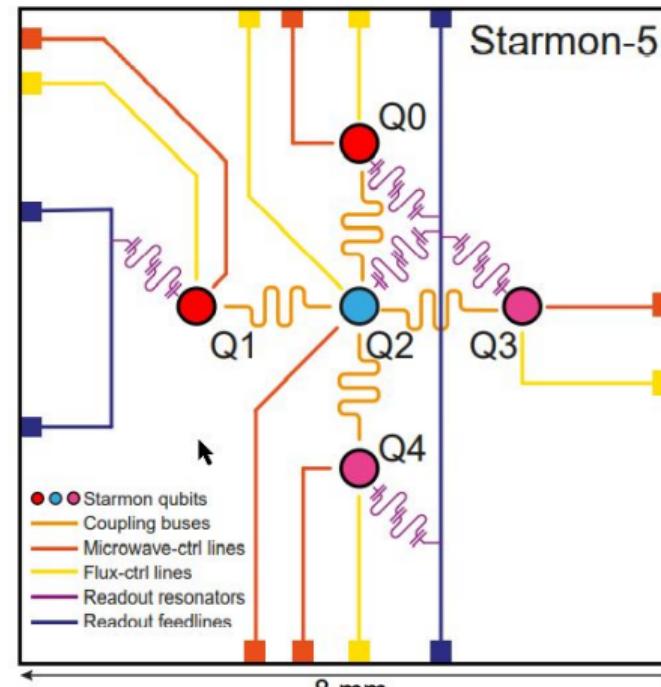
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Reference to factsheet





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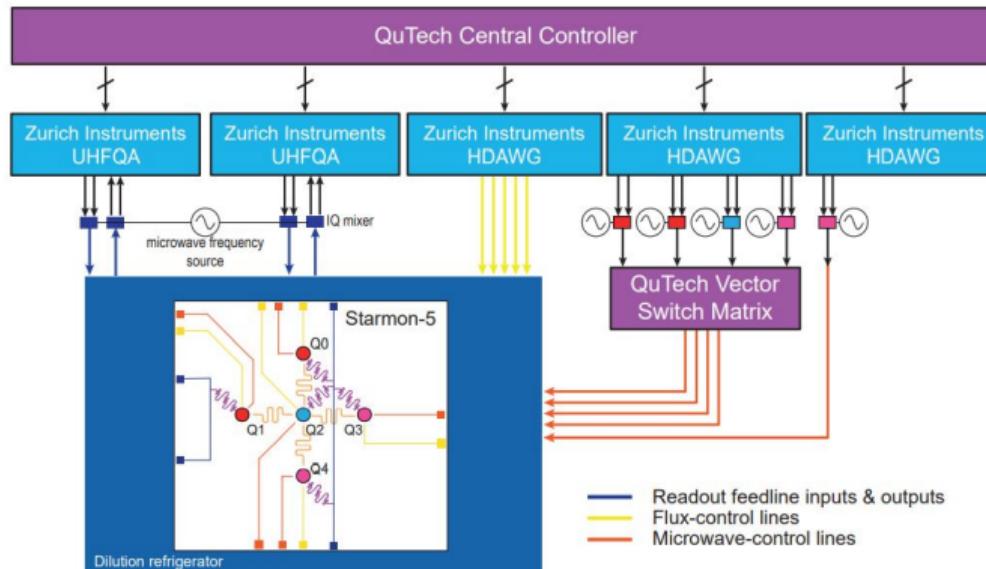
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Chinese computer with 62 qubits based on optical principles([15])





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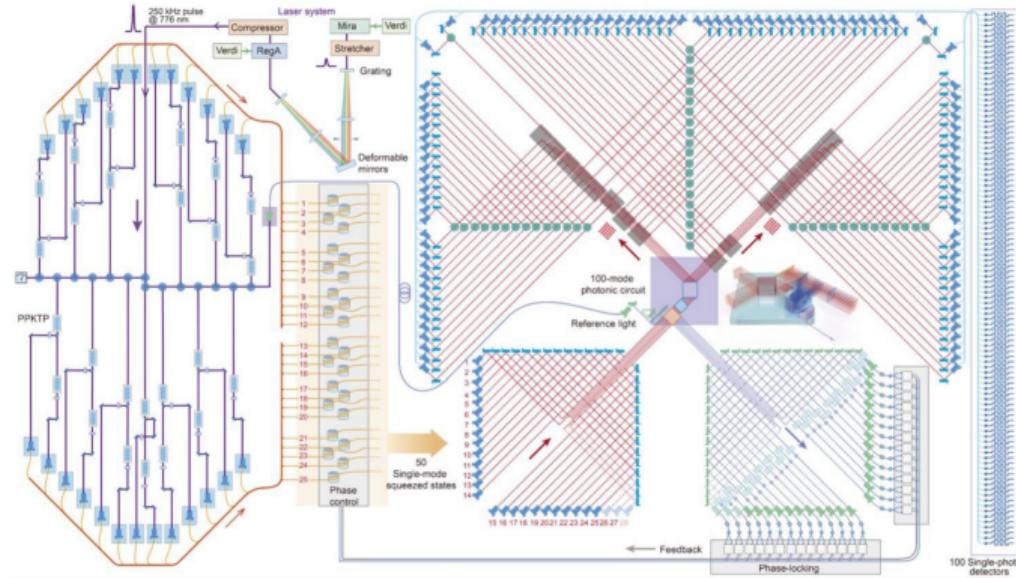
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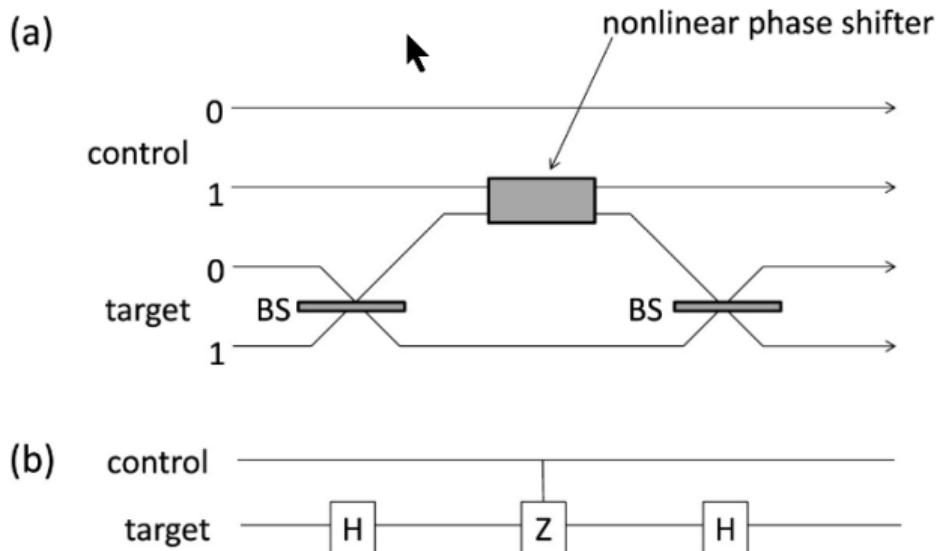
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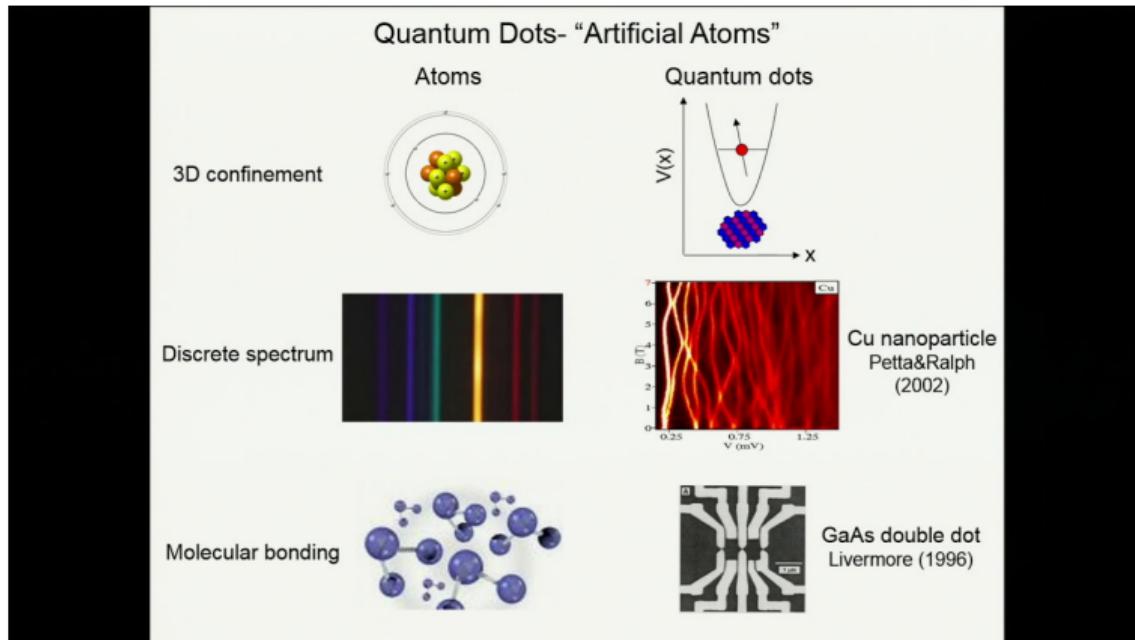
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FACT BASED INSIGHT

Increasingly, variations of qubit technology are important

	Superconducting Circuits	Trapped Ion	Neutral Atom	NV Diamond	Silicon Spin	Photonic
Error Correction	Surface code Colour code	Bacon-Shor code Surface code	Surface code		Surface code	Beyond foliation GKP code
Control Processor	CryoCMOS SFQ	Rack	Rack	Mounted	Monolithic	Flipchip
Gate Control	Freq. tuning M Tunable couplers	Laser NF Microwave GF Microwave	Laser	Laser	CMOS fab STM fab	Electrical
Environment	20mK	UHV	UHV	Ambient	200mK?	2K (detector)
Connectivity	Square grid Hex grid	All-to-all Shuttling	2D+	Clusters	2D	Flexible
Substrate	Circuit	RF trap	MOT trap	1000Q?	99%	¹² C ²⁸ Si
Qubit	Tunable Freq. Fixed Freq.	Hyperfine Optical	Hyperfine Optical	NV SIV	Qdot Donor	Single Photon Squeezed Light

Sources: [arXiv:2309.07053](https://arxiv.org/abs/2309.07053), [arXiv:2309.07053](https://arxiv.org/abs/2309.07053)





Simplyfing circuits

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- Use of Transpiler
- Manual simplification
- Use of dedicated libraries
- Classical for Boolean algebra, e.g. Karnaugh Maps, simplification rules



Example PyZX library

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PyZX (pronounce as Pisics) is a Python tool implementing the theory of ZX-calculus for the creation, visualisation, and automated rewriting of large-scale quantum circuits ([Github library](#), [16])

- `Circuit` - The name of the circuit
- `qubits` - Amount of qubits in the circuit
- `G-count` - Gate count of original circuit
- `2-count` - Amount of 2-qubit gates in original circuit
- `G/2-NRSCM` - Total amount and 2-qubit gate amount from optimized circuit of [1]
- `G/2-Tpar` - Total amount and 2-qubit gate amount from optimized circuit of [2]
- `G/2-PyZX` - Total amount and 2-qubit gate amount from optimized circuit made by PyZX
- `Time-Simp` - The time taken for running the simplification routine on the circuit
- `Time-Extract` - The time taken for extracting the circuit after the simplification



Examples PyZX library

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```
In [4]: print("Circuit".ljust(20), "qubits", "G-count", "2-count", "G-NRSCM", "2-NRSCM", "G-Tpar", "2-Tpar", ' '
for c in fast_circuits:
    print(c.get_output())
```

Circuit	qubits	G-count	2-count	G-NRSCM	2-NRSCM	G-Tpar	2-Tpar	G-PyZX	2-PyZX	Time-Simp	Ti
me-Opt											
Adder8 0.13	23	637	243	190	94	-	-	362	199	1.06	
adder_8 0.21	24	900	409	606	291	1280	885	677	337	2.03	
barenco_tof_10 ^**	19	450	192	264	130	517	328	365	176	0.62	
hw8.qc 13.42	12	14856	7129	-	-	-	-	12491	6234	174.24	
mod_adder_1024 1.80	28	4285	1720	2736	1278	5183	3540	3136	1430	12.82	
nth_prime8.tfc 18.58	12	16968	8235	-	-	-	-	14511	7229	136.90	
QFT32 0.34	32	1562	612	1012	612	-	-	1012	612	1.71	
QFTAdd16 0.51	32	1822	716	1168	716	-	-	1186	716	2.90	
QFTAdd32 1.44	64	4814	1900	3040	1900	-	-	3077	1900	10.31	



Designing with Qiskit metal

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- [Qiskit Metal](#)
- [Qiskit metal documentation](#)
- Quantum Device Design (QDesign): QDesign
- Quantum Device Components (QComponent): Core Classes
- Quantum Renderer (QRenderer): Renderer Base
- Quantum Analysis (QAnalysis): Analysis Core



Qiskit metal interfaces

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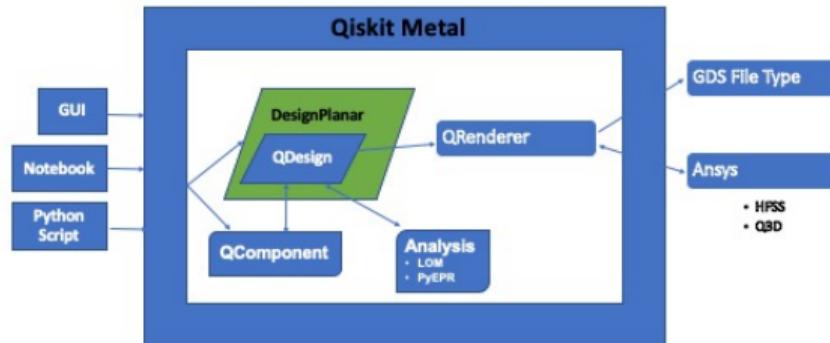
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Example: QDesign Connections





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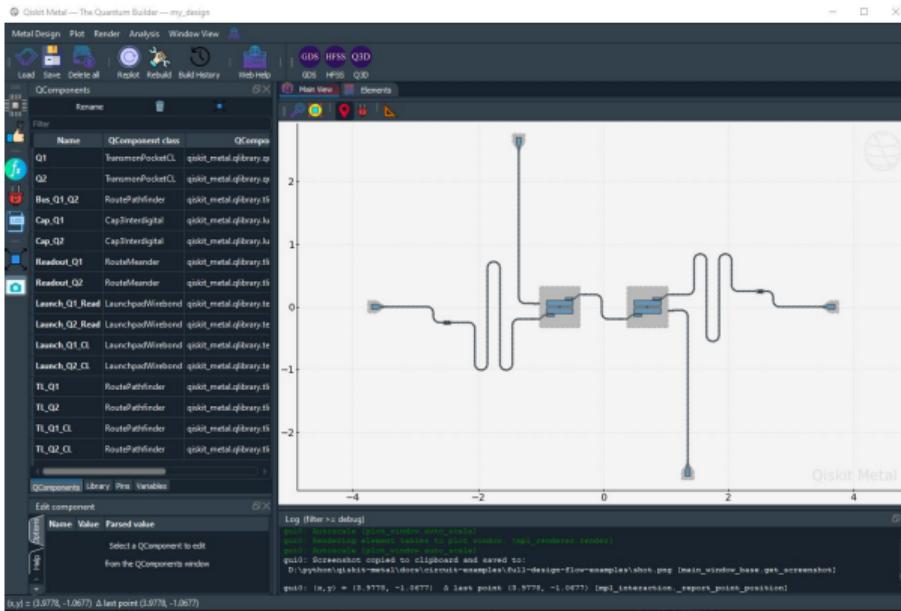
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Qiskit-metal including tutorials





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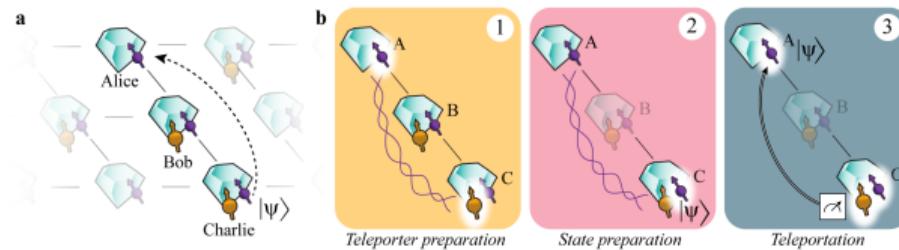
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- Science daily news quantum computers
- Overview tools
- Qubit teleportation between non-neighbouring nodes in a quantum network, (arxiv) [14]





Quantum repeater protocol using quantum memory

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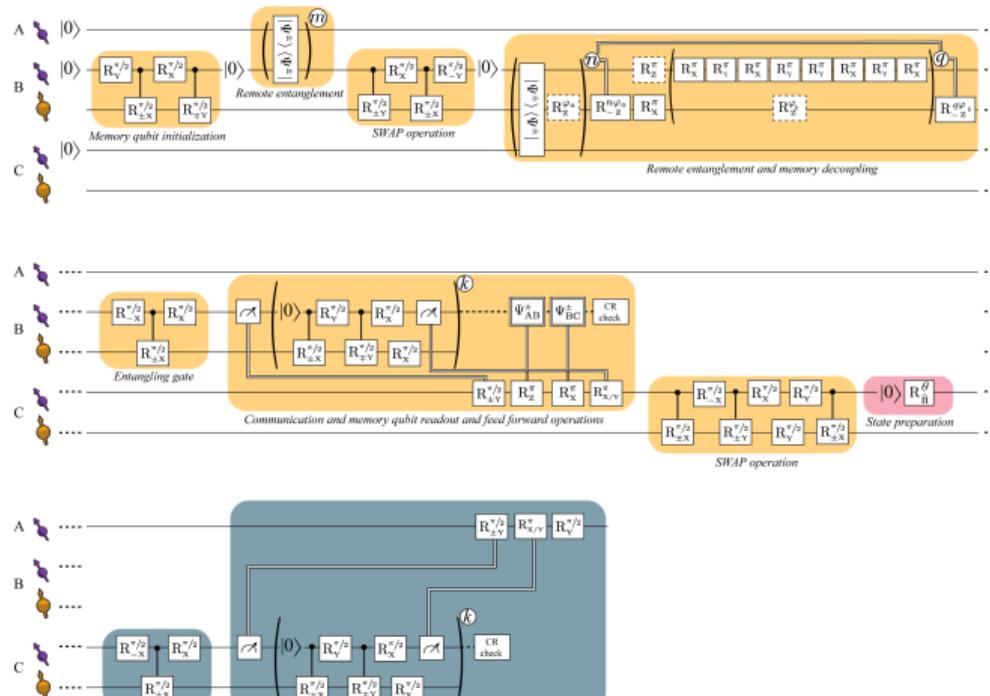
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- number of Qubits
- error rates
- error mitigation
- noise
- decoherence
- topology



Quantum Volume protocol

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Ref: [Qiskit Measuring Quantum Volume](#)

- Generate QV sequences
- Simulate the ideal QV circuits
- Calculate the heavy outputs
- Define the noise model
- Calculate the average gate fidelity
- Calculate the achievable depth
- Calculate the Quantum Volume



Quantum Volume

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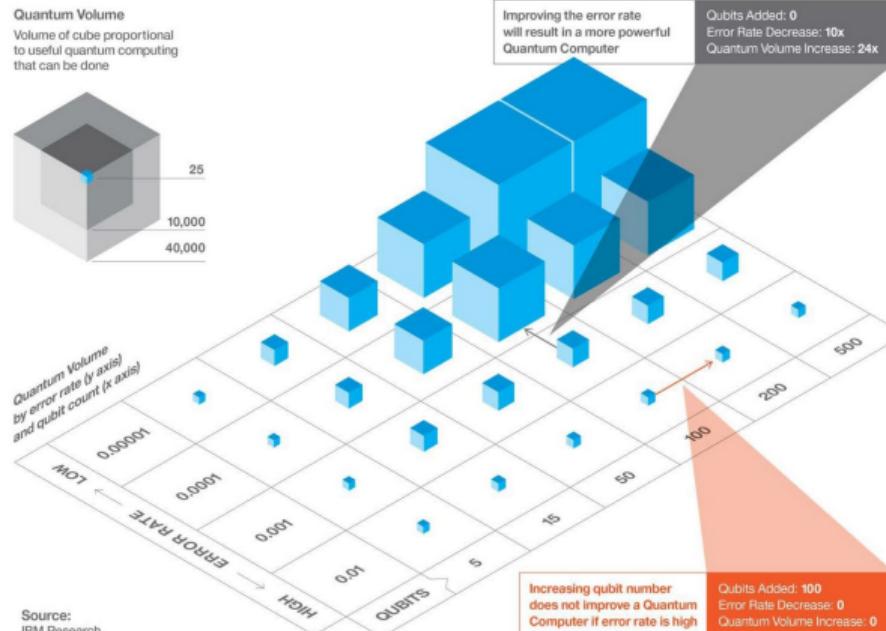
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Investigating Quantum Hardware in Qiskit, Quantum measurement lab Qiskit

- Quantum Error Correction using Repetition Codes
- Measurement Error Mitigation
- Randomized Benchmarking ([17])
- Measuring Quantum Volume
- The Density Matrix & Mixed States



Calibration and measurements

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- During initialization a quantum computer needs to be calibrated before using quantum computer for calculations
- Quantum measurement lab Qiskit
- Calibrating Qubits with Qiskit Pulse



Conclusion

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Measuring and
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- Different hardware technologies are competing
- Hardware underlying software design quite complicated
- Hardware design tools are being developed
- interface to hardware requires interfacing to electronics
- Quantum computing requires time consuming calibration
- Criteria needed to evaluate quantum hardware



Exercises: and ideas for Quantum Stack

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Measuring and
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- Exercise fundamental Schrödinger equation solution examples and links with Quantum hardware
- [Report on Quantum Hardware in Qiskit or Pennylane](#)
- Explore design options in Qiskit metal: [Qiskit Metal tutorial examples](#)
- [Qiskit notebook on quantum volume](#)



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