

# ECE 3140 / CS 3420

# EMBEDDED SYSTEMS

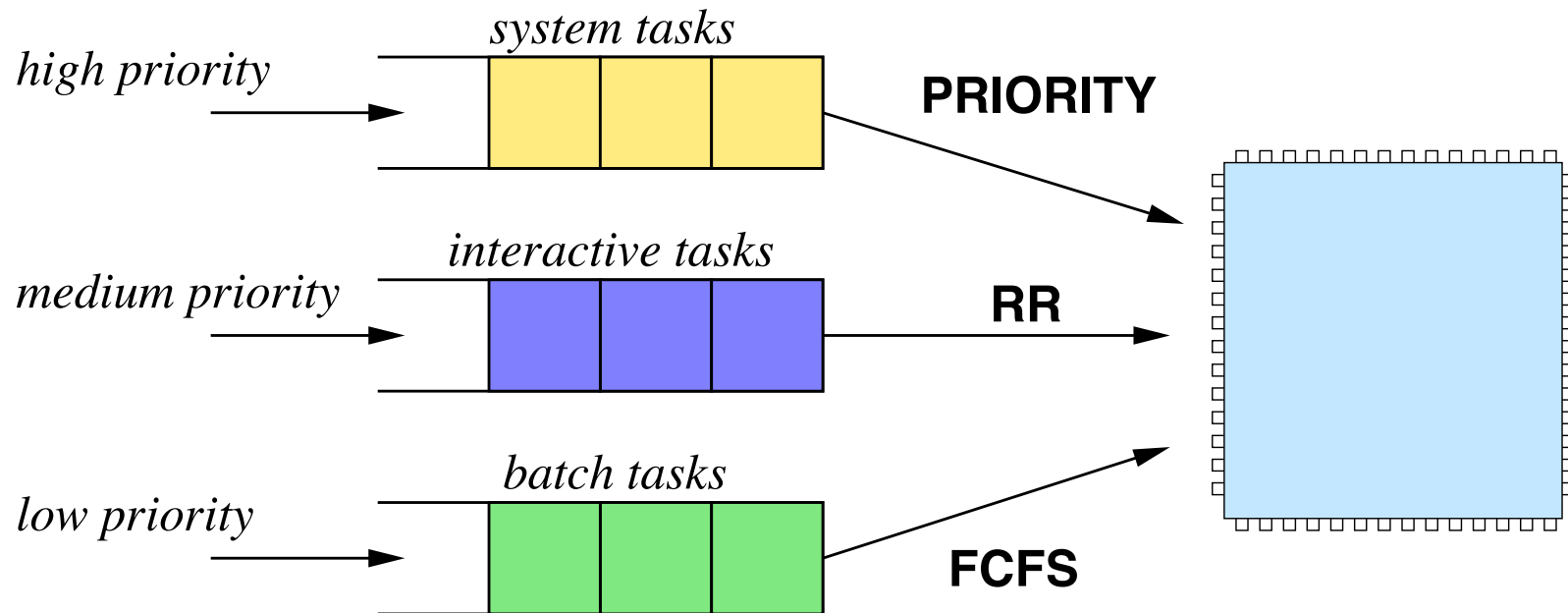
## LECTURE 16

**Prof. José F. Martínez**  
TR 1:25-2:40pm in 150 Olin



# MULTI-LEVEL SCHEDULING

Mix and match different scheduling algorithms

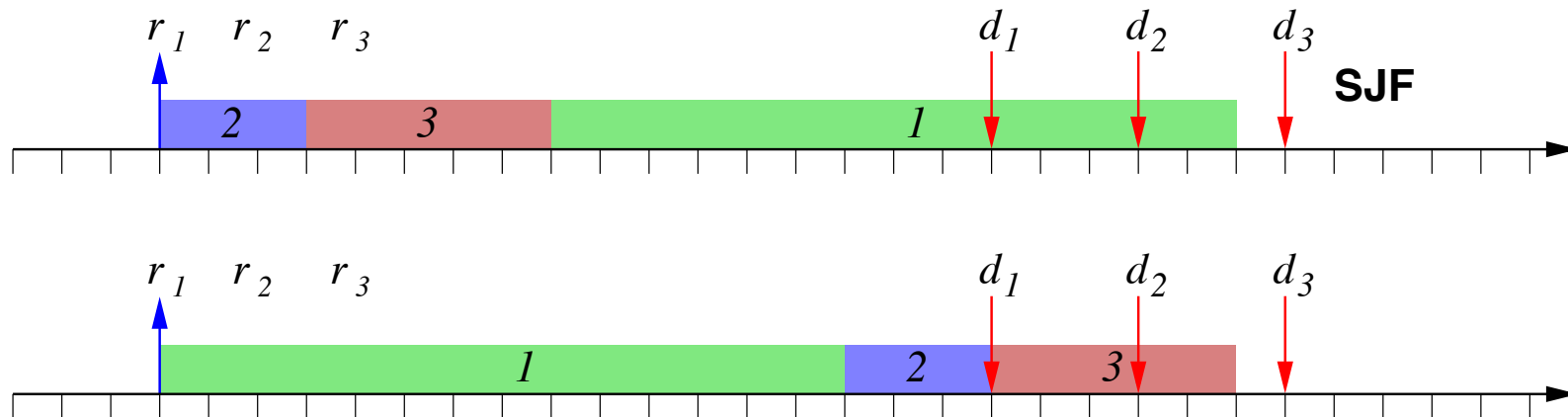


# REAL-TIME ALGORITHMS

Tasks can be scheduled by:

- relative deadlines  $D_i$ —static
- absolute deadlines  $d_i$ —dynamic

Since the goal is to meet deadlines, we should be using knowledge of deadlines to determine the schedule.



# EARLIEST DUE DATE

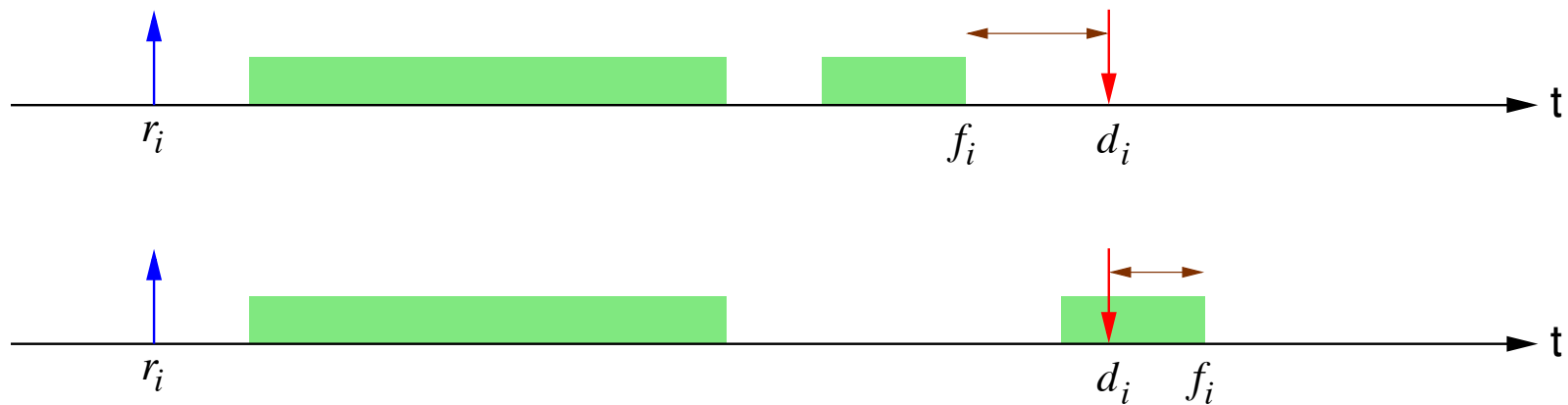
**Earliest Due Date (EDD):** select the task with the earliest *relative* deadline.

- All tasks arrive simultaneously
- Fixed priority ( $D_i$  is known)
- Preemption is not an issue
- *It minimizes the maximum lateness  $L_{max}$*



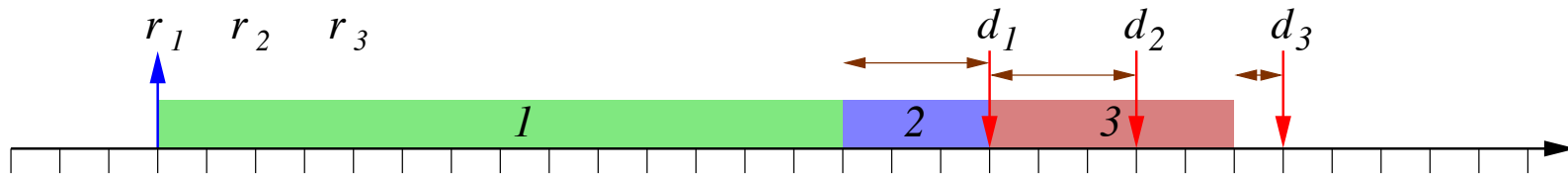
# EARLIEST DUE DATE

$$L_i = f_i - d_i$$



# MAXIMUM LATENESS

$$L_{max} = \max_i(L_i)$$



- $L_{max} < 0 \Rightarrow$  no task misses its deadline



# EARLIEST DUE DATE

**Jackson's Rule:** *Given a set of  $n$  independent tasks, any algorithm that executes the tasks in order of nondecreasing deadlines is optimal with respect to maximum lateness.*

Why does it minimize the maximum lateness? Proof?

- In particular, if  $L_{max}(\sigma)$  is the maximum lateness of a schedule, then:

$$\forall \sigma : \quad L_{max}(\sigma_{EDD}) \leq L_{max}(\sigma)$$



# EARLIEST DUE DATE

How can we guarantee that a task set  $\Gamma$  is feasible?

- We can compute  $L_{max}$ !

A task set is feasible iff  $\forall i : f_i \leq d_i$

If we sort the tasks using EDD and all tasks arrive simultaneously, then

$$f_i = \sum_{k=1}^i C_k$$





# EARLIEST DEADLINE FIRST

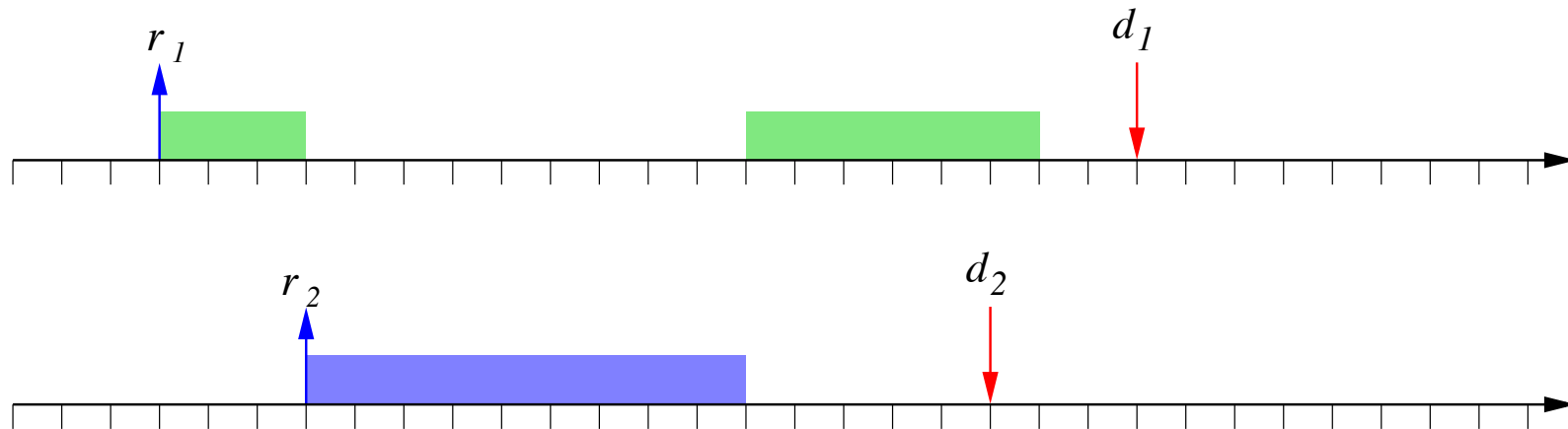
**Earliest Deadline First (EDF):** select the task with the earliest *absolute* deadline.

- Tasks may arrive at any time
- Dynamic priority ( $d_i$  depends on when the tasks arrive)
- Preemptive tasks
- *It minimizes the maximum lateness  $L_{max}$*

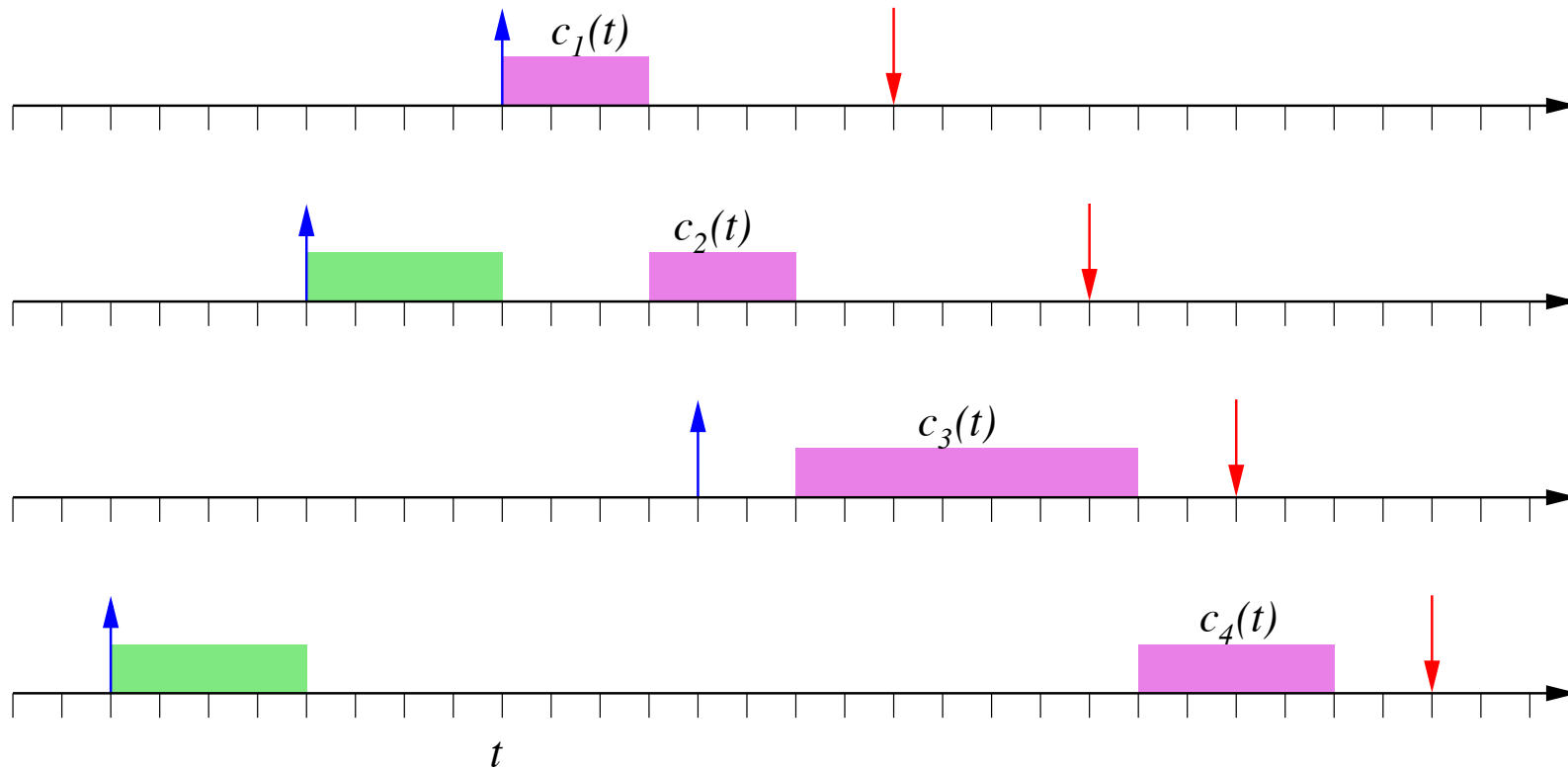


# EARLIEST DEADLINE FIRST

Tasks that arrive with earlier deadlines pre-empt tasks with later deadlines.



# EARLIEST DEADLINE FIRST: FEASIBILITY

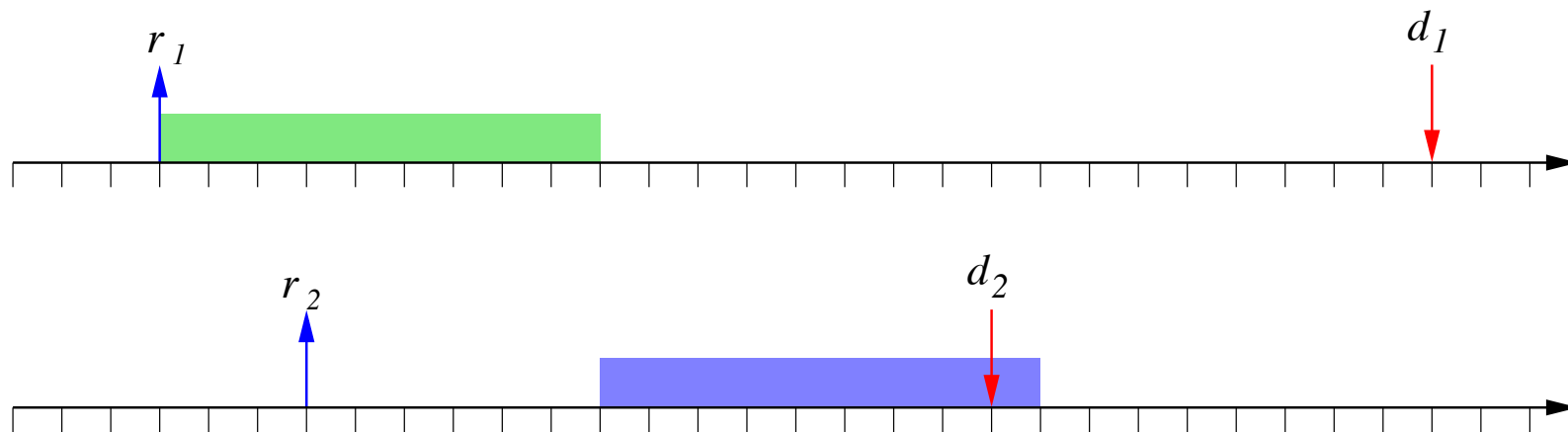


$$\forall i : \sum_{k=1}^i c_k(t) \leq d_i - t$$



# EARLIEST DEADLINE FIRST

Under non-preemptive scheduling, EDF is not optimal



# EARLIEST DEADLINE FIRST

... unless the algorithm has knowledge of the future!

