CS 3110 Fall 2016 Sample problems for Prelim 1 based on Spring 2015

Please note that the actual Spring 2015 Prelim 1 was longer than this selection of problems. We have attempted to remove any problems that were about topics not covered this semester, but it's possible we missed some.

1. True–False	[20]	pts
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Label the following statements with either "true" (T) or "false" (F). Correct answers receive two points, blank or omitted answers receive 1 point, and incorrect answers receive zero points.

- a. ____ List.fold_left f acc l and List.fold_right f l acc always return the same value, but the former is tail recursive and the latter is not.
- b. ____ map can be implemented with fold_left but not with fold_right.
- c. ____ "The pair (n,d) represents the rational number n/d" is a representation invariant for rational numbers.
- d. ____ Anonymous functions are expressions in OCaml.
- e. ____ The following expression is well-typed: 3110 + failwith "ZARDOZ"

2. Types and values [15 pts] For each of the following expressions, write the type of the expression and the value to which it evaluates. Or, if the expression would not compile, indicate this by writing "would not compile" and give a brief explanation of why. If it evaluates to a function, use the substitution model to provide your answer.

```
(a) [3 pts] let (x,y) = (3,5) in (float_of_int x) *. (float_of_int y)
```

- (b) [3 pts] List.fold_left (fun a x -> a::x) (see Appendix for type of List.fold_left)
- (c) [3 pts]
 let u f (x,y) = f x y in
 let f x y = 3 in
 u f
- (e) [3 pts] Assume the following definitions:

```
module type T = sig val x : int end
module X : T = struct
  let x = 7
  let y = 3
end
```

Now answer the question above for this expression:

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3. Functions on lists [20 pts]

(a) [14 pts] Consider writing a function count: int -> int list -> int, such that count n lst is the number of elements of lst that are strictly greater than n. For example, count 5 [4;5;6] should return 1.

Implement this function in four ways:

- i. count_rec: recursively, without using any List module functions;
- ii. count_fold: using List.fold_left or List.fold_right, but no other List module functions nor the rec keyword;
- iii. count_lib: using any combination of List module functions, but excluding any fold functions and the rec keyword; and
- iv. count_tr: tail recursively, using any functions or keywords you wish, including any of the previous three implementations.

The Appendix provides the names and types of many List module functions.

(b) [6 pts] Write a function cart: 'a list -> 'b list -> ('a * 'b) list that computes the Cartesian product of two lists. That is, cart 11 12 should return a list 13, which contains the pair (x,y) iff x is an element of 11 and y is an element of 12. For example, cart [3110;7] [2;13] could return [(3110,2); (3110,13); (7,2); (7;13)]. The order of pairs in 13 is unspecified. You may assume that 11 does not contain any duplicate elements, and likewise for 12. For full credit, your solution should be tail recursive and run in $O(|11| \cdot |12|)$ time, where $|\ell|$ denotes the length of list ℓ .

4. Datatypes and Folding [30 pts]

HTML (HyperText Markup Language) is used to create web pages. Here is a grammar for a simple subset of HTML text, in which string represents an OCaml string:

A URL, for example, could be http://3110.com/zardoz.html. The scheme is http, the host is 3110.com, and the path is zardoz.html. Here is an example of some HTML text according to this grammar:

3110 is fun

(a) [5 pts] Define two OCaml types to represent url and text.

```
type url =
```

type text =

(b) [2 pts] Write an expression, using the types you defined, that represents the following HTML:

```
<br/><a href="http://3110.com/zardoz.html">3110 is fun</a>
<br/><br/>
```

(c) [4 pts] Write a function count_breaks : text -> int that counts the number of breaks in HTML text.

- 5. Modular programming [25 pts] Define a type 'a t to be *list-like* if the following conditions hold:
 - There is a value empty of type 'a t.
 - There is a cons operation that takes an element of type 'a and a list-like value of type 'a t and returns a list-like value of type 'a t.
 - There is a decons operation that takes a list-like value of type 'a t and
 - returns None if the list-like value is empty, or
 - returns Some (x,xs) if the list-like value is the cons of an element x and a list-like value xs.

You may use any function from the OCaml List module. The Appendix contains a list of function names and their types.

(a) [6 pts] Write a module type ListLike that encodes the above specification. You do not need to write any specification comments.

(b) [6 pts] Write a module ListImpl that uses list to implement the ListLike interface.

(c) [5 pts] Write a functor that takes a ListLike module and produces a module containing a function map. That function should behave like List.map but generalized from list to ListLike values.

- (d) [8 pts] An 'a list of length k can be encoded as a function f of type int -> 'a option, where f n returns one of the following values:
 - Some x if x is the value at position n of the list. The first element of the list is at position 0.
 - None if n is not a valid position in the list.

Use this encoding to write a module FunImpl that implements the ListLike interface with the type 'a t = int -> 'a option.