全连接神经网络

在前面的作业中,你在CIFAR-10上实现了一个两层的全连接神经网络。那个实现很简单,但不是很模块化,因为损失和梯度计算在一个函数内。对于一个简单的两层网络来说,还可以人为处理,但是当我们使用更大的模型时,人工处理损失和梯度就变得不切实际了。理想情况下,我们希望使用更加模块化的设计来构建网络,这样我们就可以独立地实现不同类型的层,然后将它们整合到不同架构的模型中。

在本练习中,我们将使用更模块化的方法实现全连接网络。对于每一层,我们将实现一个 forward 和一个 backward 的函数。 forward 函数将接收输入、权重和其他参数,并返回一个 输出和一个 cache 对象,存储反向传播所需的数据,如下所示:

```
def layer_forward(x, w):
  """ Receive inputs x and weights w """
  # Do some computations ...
  z = # ... some intermediate value
  # Do some more computations ...
  out = # the output
  cache = (x, w, z, out) # Values we need to compute gradients
  return out, cache
反向传播将接收上游的梯度和 cache 对象,并返回相对于输入和权重的梯度:
def layer backward(dout, cache):
  Receive dout (derivative of loss with respect to outputs) and cache,
  and compute derivative with respect to inputs.
  # Unpack cache values
  x, w, z, out = cache
  # Use values in cache to compute derivatives
  dx = \# Derivative of loss with respect to x
  dw = # Derivative of loss with respect to w
  return dx, dw
```

以这种方式实现了一些层之后,我们能够轻松地将它们组合起来,以构建不同架构的分类器。

除了实现任意深度的全连接网络外,我们还将探索不同的优化更新规则,并引入Dropout作为正则化器和Batch/Layer归一化工具来更有效地优化网络。

```
In [3]: # As usual, a bit of setup
from __future__ import print_function
import time
import numpy as np
import matplotlib.pyplot as plt
from daseCV.classifiers.fc_net import *
from daseCV.data_utils import get_CIFAR10_data
from daseCV.gradient_check import eval_numerical_gradient, eval_numerical_gradient_an
from daseCV.solver import Solver

%matplotlib inline
```

```
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'

# for auto-reloading external modules
# see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
%load_ext autoreload
%autoreload 2

def rel_error(x, y):
    """ returns relative error """
    return np. max(np. abs(x - y) / (np. maximum(1e-8, np. abs(x) + np. abs(y))))
```

The autoreload extension is already loaded. To reload it, use: %reload ext autoreload

```
In [4]: # Load the (preprocessed) CIFAR10 data.

data = get_CIFAR10_data()
    for k, v in list(data.items()):
        print(('%s: ' % k, v.shape))

('X_train: ', (49000, 3, 32, 32))
    ('y_train: ', (49000,))
    ('X_val: ', (1000, 3, 32, 32))
    ('y_val: ', (1000,))
    ('X_test: ', (1000, 3, 32, 32))
    ('y_test: ', (1000,))
```

仿射层: 前向传播

打开 daseCV/layers.py 并实现 affine_forward 函数。

当你完成上述函数后, 你可以用下面的代码测试你的实现正确与否

```
# Test the affine forward function
num inputs = 2
input\_shape = (4, 5, 6)
output_dim = 3
input size = num inputs * np. prod(input shape)
weight size = output dim * np. prod(input shape)
x = np. 1inspace(-0.1, 0.5, num=input size). reshape(num inputs, *input shape)
w = np. linspace(-0.2, 0.3, num=weight_size).reshape(np.prod(input_shape), output_dim)
b = np. 1inspace(-0.3, 0.1, num=output dim)
out, _ = affine_forward(x, w, b)
correct_out = np. array([[ 1.49834967, 1.70660132, 1.91485297].
                        3. 25553199, 3. 5141327,
                                                    3.77273342]])
# Compare your output with ours. The error should be around e-9 or less.
print('Testing affine forward function:')
print('difference: ', rel_error(out, correct_out))
```

Testing affine_forward function: difference: 9.769849468192957e-10

仿射层: 反向传播

实现 affine_backwards 函数,并使用数值梯度检查测试你的实现。

```
# Test the affine backward function
np. random. seed (231)
x = np. random. randn(10, 2, 3)
w = np. random. randn(6, 5)
b = np. random. randn(5)
dout = np. random. randn(10, 5)
dx_num = eval_numerical_gradient_array(lambda x: affine_forward(x, w, b)[0], x, dout)
dw num = eval\_numerical\_gradient\_array(lambda w: affine\_forward(x, w, b)[0], w, dout)
db_num = eval_numerical_gradient_array(lambda b: affine_forward(x, w, b)[0], b, dout)
 _, cache = affine_forward(x, w, b)
dx, dw, db = affine_backward(dout, cache)
\# The error should be around e-10 or less
print('Testing affine backward function:')
print('dx error: ', rel_error(dx_num, dx))
print('dw error: ', rel_error(dw_num, dw))
print('db error: ', rel_error(db_num, db))
Testing affine backward function:
dx error: 5.399100368651805e-11
dw error: 9.904211865398145e-11
db error: 2.4122867568119087e-11
```

ReLU 激活函数: 前向传播

在 relu_forward 函数中实现ReLU激活函数的前向传播,并使用以下代码测试您的实现:

Testing relu_forward function: difference: 4.99999798022158e-08

ReLU 激活函数:反向传播

在 relu_back 函数中为ReLU激活函数实现反向传播,并使用数值梯度检查来测试你的实现

```
dx_num = eval_numerical_gradient_array(lambda x: relu_forward(x)[0], x, dout)

_, cache = relu_forward(x)
dx = relu_backward(dout, cache)

# The error should be on the order of e-12
print('Testing relu_backward function:')
print('dx error: ', rel_error(dx_num, dx))
```

Testing relu_backward function: dx error: 3.2756349136310288e-12

Inline Question 1:

作业中只要求你实现ReLU,但是神经网络可以使用很多不同的激活函数,每个都有它的优点和缺点。但是,激活函数的一个常见问题是在反向传播时出现零(或接近零)梯度流。下列哪个激活函数会有这个问题?如果在一维情况下考虑这些函数,什么样的输入将会发生这种现象?

- 1. Sigmoid
- 2. ReLU
- 3. Leaky ReLU

Answer:

Sigmoid, ReLU激活函数会有这个问题

由于Sigmoid定义: f(x) = 1/(1 + exp(-x)), 所以当输入趋向于0或1时,用Sigmoid进行反向传播就会导致梯度消失;

由于ReLU定义: f(x) = max(0,x),所以当输入小于0的时候,用ReLU反向传导就会造成梯度消失。

ReLU 会在x 是负数的时候出现0 梯度流,而Leaky ReLU 则避免了这样死亡RELU 的问题

"三明治"层

在神经网络中有一些常用的层模式。例如,仿射层后面经常跟一个ReLU层。为了简化这些常见模式,我们在文件 daseCV/layer utils.py 中定义了几个常用的层

请查看 affine_relu_forward 和 affine_relu_backward 函数, 并且运行下列代码进行数值 梯度检查:

```
In [9]:
    from daseCV.layer_utils import affine_relu_forward, affine_relu_backward
    np. random. seed(231)
    x = np. random. randn(2, 3, 4)
    w = np. random. randn(12, 10)
    b = np. random. randn(10)
    dout = np. random. randn(2, 10)

out, cache = affine_relu_forward(x, w, b)
    dx, dw, db = affine_relu_backward(dout, cache)

dx_num = eval_numerical_gradient_array(lambda x: affine_relu_forward(x, w, b)[0], x,
```

```
dw_num = eval_numerical_gradient_array(lambda w: affine_relu_forward(x, w, b)[0], w,
db_num = eval_numerical_gradient_array(lambda b: affine_relu_forward(x, w, b)[0], b,

# Relative error should be around e-10 or less
print('Testing affine_relu_forward and affine_relu_backward:')
print('dx error: ', rel_error(dx_num, dx))
print('dw error: ', rel_error(dw_num, dw))
print('db error: ', rel_error(db_num, db))
```

Testing affine relu forward and affine relu backward:

dx error: 2.299579177309368e-11
dw error: 8.162011105764925e-11
db error: 7.826724021458994e-12

损失层: Softmax and SVM

在上次作业中你已经实现了这些损失函数,所以这次作业就不用做了,免费送你了。当然,你仍然应该通过查看 daseCV/layers.py 其中的实现来确保理解它们是如何工作的。

你可以通过运行以下程序来确保实现是正确的:

```
np. random. seed (231)
num_classes, num_inputs = 10, 50
x = 0.001 * np. random. randn (num inputs, num classes)
y = np. random. randint(num_classes, size=num_inputs)
dx num = eval numerical gradient(lambda x: svm loss(x, y)[0], x, verbose=False)
loss, dx = svm_loss(x, y)
# Test sym loss function. Loss should be around 9 and dx error should be around the or
print('Testing svm_loss:')
print('loss: ', loss)
print('dx error: ', rel_error(dx_num, dx))
dx num = eval numerical gradient(lambda x: softmax loss(x, y)[0], x, verbose=False)
loss, dx = softmax loss(x, y)
# Test softmax loss function. Loss should be close to 2.3 and dx error should be aroun
print('\nTesting softmax loss:')
print('loss: ', loss)
print('dx error: ', rel error(dx num, dx))
Testing svm loss:
loss: 8.999602749096233
```

dx error: 1.4021566006651672e-09

Testing softmax_loss: loss: 2.302545844500738

dx error: 9.384673161989355e-09

两层网络

在之前的作业中,你已经实现了一个简单的两层神经网络。现在你已经模块化地实现了一些层,你将使用这些模块重新实现两层网络。

打开文件 daseCV/classifiers/fc_net 。并完成 TwoLayerNet 类的实现。这个类将作为这个作业中其他网络的模块,所以请通读它以确保你理解了这个API。 你可以运行下面的单元来测试您的实现。

```
np. random. seed (231)
N, D, H, C = 3, 5, 50, 7
X = np. random. randn(N, D)
y = np. random. randint(C, size=N)
std = 1e-3
model = TwoLayerNet(input_dim=D, hidden_dim=H, num_classes=C, weight_scale=std)
print('Testing initialization ...')
W1_std = abs(model.params['W1'].std() - std)
b1 = model.params['b1']
W2 std = abs(model.params['W2'].std() - std)
b2 = model. params ['b2']
assert Wl_std < std / 10, 'First layer weights do not seem right'
assert np. all(b1 == 0), 'First layer biases do not seem right'
assert W2_std < std / 10, 'Second layer weights do not seem right'
assert np. all(b2 == 0), 'Second layer biases do not seem right'
print('Testing test-time forward pass ...')
model. params ['W1'] = np. linspace (-0.7, 0.3, num=D*H). reshape (D, H)
model.params['bl'] = np.linspace(-0.1, 0.9, num=H)
model.params['W2'] = np. linspace(-0.3, 0.4, num=H*C).reshape(H, C)
model. params['b2'] = np. linspace(-0.9, 0.1, num=C)
X = \text{np. linspace}(-5.5, 4.5, \text{num}=N*D). \text{reshape}(D, N). T
scores = model. loss(X)
correct_scores = np. asarray(
   [[11.53165108, 12.2917344,
                                  13. 05181771, 13. 81190102, 14. 57198434, 15. 33206765,
    [12.\ 05769098, \quad 12.\ 74614105, \quad 13.\ 43459113, \quad 14.\ 1230412, \quad 14.\ 81149128, \quad 15.\ 49994135,
    [12.\ 58373087, \quad 13.\ 20054771, \quad 13.\ 81736455, \quad 14.\ 43418138, \quad 15.\ 05099822, \quad 15.\ 66781506,
scores diff = np. abs(scores - correct scores). sum()
assert scores_diff < 1e-6, 'Problem with test-time forward pass'
print('Testing training loss (no regularization)')
y = np. asarray([0, 5, 1])
loss, grads = model.loss(X, y)
correct loss = 3.4702243556
assert abs(loss - correct_loss) < 1e-10, 'Problem with training-time loss'
model.reg = 1.0
loss, grads = model.loss(X, y)
correct loss = 26.5948426952
assert abs(loss - correct loss) < 1e-10, 'Problem with regularization loss'
# Errors should be around e-7 or less
for reg in [0.0, 0.7]:
   print('Running numeric gradient check with reg = ', reg)
   model.reg = reg
   loss, grads = model.loss(X, y)
   for name in sorted(grads):
     f = 1 \text{ ambda} _: model. loss(X, y)[0]
     grad_num = eval_numerical_gradient(f, model.params[name], verbose=False)
     print('%s relative error: %.2e' % (name, rel error(grad num, grads[name])))
Testing initialization ...
Testing test-time forward pass ...
```

```
Testing initialization ...
Testing test-time forward pass ...
Testing training loss (no regularization)
Running numeric gradient check with reg = 0.0
W1 relative error: 1.52e-08
W2 relative error: 3.21e-10
b1 relative error: 8.37e-09
b2 relative error: 4.33e-10
Running numeric gradient check with reg = 0.7
```

```
W1 relative error: 3.12e-07
W2 relative error: 2.85e-08
b1 relative error: 1.56e-08
b2 relative error: 7.76e-10
```

Solver

在之前的作业中,模型的训练逻辑与模型本身是耦合的。在这次作业中,按照更加模块化的设计,我们将模型的训练逻辑划分为单独的类。

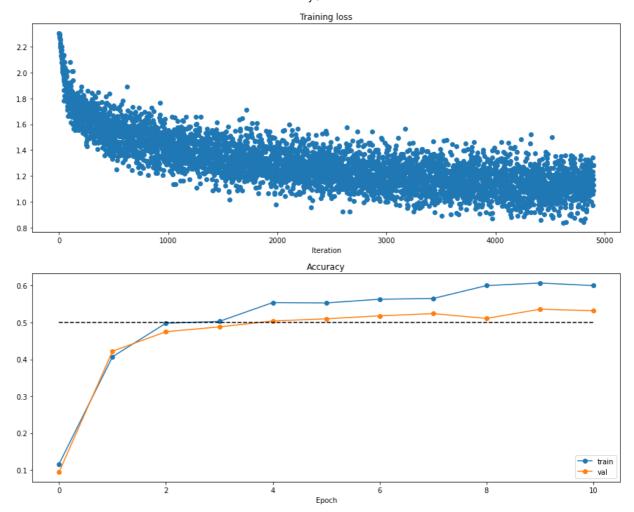
打开文件 daseCV/solver ,通读一遍以熟悉API。然后使用一个 Sovler 实例来训练一个 TwoLayerNet ,它可以在验证集上达到至少 50% 的精度。

```
model = TwoLayerNet()
solver = None
# TODO: Use a Solver instance to train a TwoLayerNet that achieves at least #
# 50% accuracy on the validation set.
# *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
solver = Solver(model, data, update_rule='sgd',
       optim config={'learning rate':1e-3,},1r decay=0.80,
       num epochs=10, batch size=100, print every=100)
solver. train()
scores = solver. model. loss(data['X test'])
acc = np. mean(data['y test'] == np. argmax(scores, axis=1))
print("test acc:", acc)
# ****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
END OF YOUR CODE
(Iteration 1 / 4900) loss: 2.304060
(Epoch 0 / 10) train acc: 0.116000; val_acc: 0.094000
(Iteration 101 / 4900) loss: 1.829613
(Iteration 201 / 4900) loss: 1.857390
(Iteration 301 / 4900) loss: 1.744448
(Iteration 401 / 4900) loss: 1.420187
(Epoch 1 / 10) train acc: 0.407000; val acc: 0.422000
(Iteration 501 / 4900) loss: 1.542427
(Iteration 601 / 4900) loss: 1.649871
(Iteration 701 / 4900) loss: 1.695672
(Iteration 801 / 4900) loss: 1.659121
(Iteration 901 / 4900) loss: 1.428991
(Epoch 2 / 10) train acc: 0.498000; val_acc: 0.475000
(Iteration 1001 / 4900) loss: 1.376289
(Iteration 1101 / 4900) loss: 1.275565
(Iteration 1201 / 4900) loss: 1.584220
(Iteration 1301 / 4900) loss: 1.392124
(Iteration 1401 / 4900) loss: 1.173616
(Epoch 3 / 10) train acc: 0.503000; val acc: 0.488000
(Iteration 1501 / 4900) loss: 1.334806
(Iteration 1601 / 4900) loss: 1.266435
(Iteration 1701 / 4900) loss: 1.270974
(Iteration 1801 / 4900) loss: 1.375694
(Iteration 1901 / 4900) loss: 1.306264
(Epoch 4 / 10) train acc: 0.554000; val acc: 0.504000
(Iteration 2001 / 4900) loss: 1.331799
```

(Iteration 2101 / 4900) loss: 1.324633

```
FullyConnectedNets
             (Iteration 2201 / 4900) loss: 1.310493
             (Iteration 2301 / 4900) loss: 1.268084
             (Iteration 2401 / 4900) loss: 1.311096
             (Epoch 5 / 10) train acc: 0.553000; val acc: 0.510000
             (Iteration 2501 / 4900) loss: 1.361757
(Iteration 2601 / 4900) loss: 1.221786
             (Iteration 2701 / 4900) loss: 1.058463
             (Iteration 2801 / 4900) loss: 1.223126
             (Iteration 2901 / 4900) loss: 1.248591
             (Epoch 6 / 10) train acc: 0.563000; val acc: 0.518000
             (Iteration 3001 / 4900) loss: 1.230829
(Iteration 3101 / 4900) loss: 1.320762
             (Iteration 3201 / 4900) loss: 1.227759
             (Iteration 3301 / 4900) loss: 1.284588
             (Iteration 3401 / 4900) loss: 1.330825
             (Epoch 7 / 10) train acc: 0.565000; val acc: 0.524000
             (Iteration 3501 / 4900) loss: 1.237669
(Iteration 3601 / 4900) loss: 1.062200
(Iteration 3701 / 4900) loss: 1.150153
             (Iteration 3801 / 4900) loss: 1.076288
(Iteration 3901 / 4900) loss: 1.087968
             (Epoch 8 / 10) train acc: 0.600000; val acc: 0.511000
             (Iteration 4001 / 4900) loss: 1.211316
(Iteration 4101 / 4900) loss: 1.297307
(Iteration 4201 / 4900) loss: 1.178958
(Iteration 4301 / 4900) loss: 1.064057
             (Iteration 4401 / 4900) loss: 1.318329
             (Epoch 9 / 10) train acc: 0.607000; val acc: 0.536000
             (Iteration 4501 / 4900) loss: 0.977584
             (Iteration 4601 / 4900) loss: 1.351527
(Iteration 4701 / 4900) loss: 1.018171
             (Iteration 4801 / 4900) loss: 1.078572
             (Epoch 10 / 10) train acc: 0.600000; val acc: 0.532000
             test acc: 0.523
In [13]:
             # Run this cell to visualize training loss and train / val accuracy
             plt. subplot (2, 1, 1)
             plt. title('Training loss')
             plt. plot (solver. loss history, 'o')
             plt. xlabel('Iteration')
             plt. subplot (2, 1, 2)
             plt. title('Accuracy')
             plt.plot(solver.train_acc_history, '-o', label='train')
             plt. plot(solver. val_acc_history, '-o', label='val')
             plt. plot([0.5] * len(solver. val acc history), 'k--')
             plt. xlabel ('Epoch')
             plt. legend (loc='lower right')
             plt. gcf(). set size inches(15, 12)
```

plt. show()



多层网络

接下来,请实现一个带有任意数量的隐层的全连接网络。

阅读 daseCV/classifiers/fc net.py 中的 FullyConnectedNet 类。

实现初始化、前向传播和反向传播的函数,暂时不要考虑实现dropout或batch/layer normalization,我们将在后面添加上去。

初始化loss和梯度检查

刚开始要做完整性检查,运行以下代码来检查初始loss,并对有正则化和无正则化的网络进行梯度检查。请问初始的loss合理吗?

在梯度检查中,你应该期望得到1e-7或更少的errors。

```
print('Initial loss: ', loss)

# Most of the errors should be on the order of e-7 or smaller.
# NOTE: It is fine however to see an error for W2 on the order of e-5
# for the check when reg = 0.0
for name in sorted(grads):
    f = lambda _: model.loss(X, y)[0]
    grad_num = eval_numerical_gradient(f, model.params[name], verbose=False, h=1e-5)
    print('%s relative error: %.2e' % (name, rel_error(grad_num, grads[name])))
```

```
Running check with reg = 0
Initial loss: 2.3004790897684924
W1 relative error: 1.48e-07
W2 relative error: 2.21e-05
W3 relative error: 3.53e-07
bl relative error: 5.38e-09
b2 relative error: 2.09e-09
b3 relative error: 5.80e-11
Running check with reg = 3.14
Initial loss: 7.052114776533016
W1 relative error: 6.86e-09
W2 relative error: 3.52e-08
W3 relative error: 1.32e-08
bl relative error: 1.48e-08
b2 relative error: 1.72e-09
b3 relative error: 1.80e-10
```

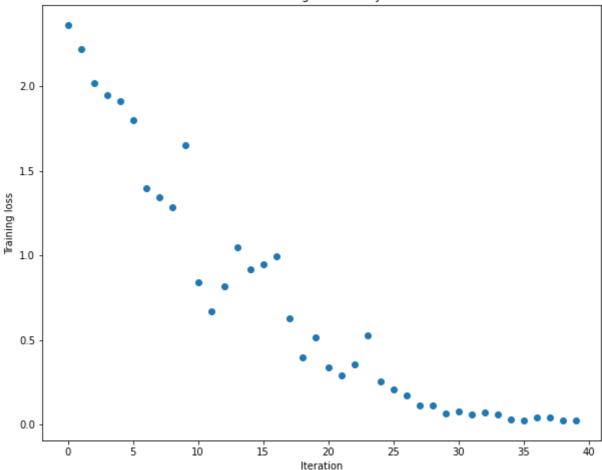
实现另一个完整性检查,请确保你可以过拟合50个图像的小数据集。首先,我们将尝试一个三层网络,每个隐藏层有100个单元。在接下来的代码中,调整learning rate和weight initialization scale以达到过拟合,在20 epoch内达到100%的训练精度。

```
# TODO: Use a three-layer Net to overfit 50 training examples by
# tweaking just the learning rate and initialization scale.
num train = 50
small data = {
  'X_train': data['X_train'][:num_train],
  'y_train': data['y_train'][:num_train],
  'X_val': data['X_val'],
  'y val': data['y val'],
weight scale = 1e-2  # Experiment with this!
learning rate = 1e-2 # Experiment with this!
model = FullyConnectedNet([100, 100],
              weight scale=weight scale, dtype=np. float64)
solver = Solver(model, small_data,
                 print every=10, num epochs=20, batch size=25,
                 update_rule='sgd',
                 optim config={
                   'learning rate': learning rate,
solver. train()
plt. plot (solver. loss history, 'o')
plt. title('Training loss history')
plt. xlabel('Iteration')
plt. ylabel('Training loss')
plt. show()
(Iteration 1 / 40) loss: 2.363364
(Epoch 0 / 20) train acc: 0.180000; val acc: 0.108000
```

(Epoch 1 / 20) train acc: 0.320000; val_acc: 0.127000

```
(Epoch 2 / 20) train acc: 0.440000; val acc: 0.172000
(Epoch 3 / 20) train acc: 0.500000; val acc: 0.184000
(Epoch 4 / 20) train acc: 0.540000; val acc: 0.181000
(Epoch 5 / 20) train acc: 0.740000; val acc: 0.190000
(Iteration 11 / 40) loss: 0.839976
(Epoch 6 / 20) train acc: 0.740000; val_acc: 0.187000
(Epoch 7 / 20) train acc: 0.740000; val_acc: 0.183000
(Epoch 8 / 20) train acc: 0.820000; val_acc: 0.177000
(Epoch 9 / 20) train acc: 0.860000; val_acc: 0.200000
(Epoch 10 / 20) train acc: 0.920000; val_acc: 0.191000
(Iteration 21 / 40) loss: 0.337174
(Epoch 11 / 20) train acc: 0.960000; val_acc: 0.189000
(Epoch 12 / 20) train acc: 0.940000; val_acc: 0.180000
(Epoch 13 / 20) train acc: 1.000000; val_acc: 0.199000
(Epoch 14 / 20) train acc: 1.000000; val_acc: 0.199000
(Epoch 15 / 20) train acc: 1.000000; val_acc: 0.195000
(Iteration 31 / 40) loss: 0.075911
(Epoch 16 / 20) train acc: 1.000000; val_acc: 0.182000
(Epoch 17 / 20) train acc: 1.000000; val acc: 0.201000
(Epoch 18 / 20) train acc: 1.000000; val acc: 0.207000
(Epoch 19 / 20) train acc: 1.000000; val acc: 0.185000
(Epoch 20 / 20) train acc: 1.000000; val acc: 0.192000
```

Training loss history



现在尝试使用一个五层的网络,每层100个单元,对50张图片进行训练。同样,你将调整learning rate和weight initialization scale比例,你应该能够在20个epoch内实现100%的训练精度。

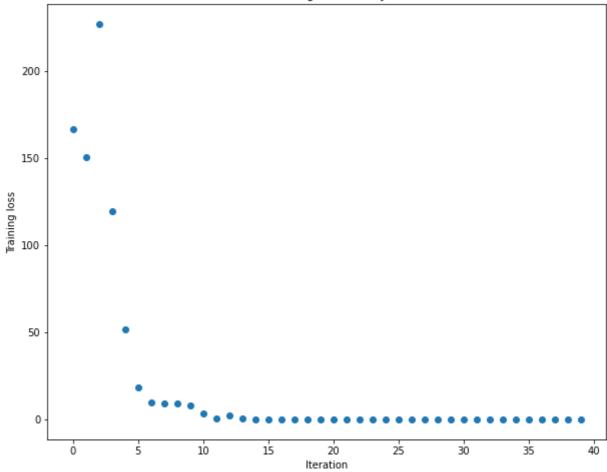
```
In [16]: # TODO: Use a five-layer Net to overfit 50 training examples by
# tweaking just the learning rate and initialization scale.

num_train = 50
small_data = {
    'X_train': data['X_train'][:num_train],
    'y_train': data['y_train'][:num_train],
    'X_val': data['X_val'],
```

```
'y_val': data['y_val'],
weight scale = 1e-1 # Experiment with this!
learning_rate = 2e-3 # Experiment with this!
model = FullyConnectedNet([100, 100, 100, 100],
                weight scale=weight scale, dtype=np. float64)
solver = Solver(model, small_data,
                print every=10, num epochs=20, batch size=25,
                update rule='sgd',
                optim_config={
                  'learning_rate': learning_rate,
solver. train()
plt. plot (solver. loss history, 'o')
plt. title('Training loss history')
plt. xlabel('Iteration')
plt. ylabel('Training loss')
plt. show()
```

```
(Iteration 1 / 40) loss: 166.501707
(Epoch 0 / 20) train acc: 0.100000; val_acc: 0.107000
(Epoch 1 / 20) train acc: 0.320000; val_acc: 0.101000
(Epoch 2 / 20) train acc: 0.160000; val_acc: 0.122000
(Epoch 3 / 20) train acc: 0.380000; val_acc: 0.106000
(Epoch 4 / 20) train acc: 0.520000; val_acc: 0.111000
(Epoch 5 / 20) train acc: 0.760000; val_acc: 0.113000
(Iteration 11 / 40) loss: 3.343141
(Epoch 6 / 20) train acc: 0.840000; val_acc: 0.122000
(Epoch 7 / 20) train acc: 0.920000; val_acc: 0.113000
(Epoch 8 / 20) train acc: 0.940000; val_acc: 0.125000
(Epoch 9 / 20) train acc: 0.960000; val_acc: 0.125000
(Epoch 10 / 20) train acc: 0.980000; val_acc: 0.121000
(Iteration 21 / 40) loss: 0.039138
(Epoch 11 / 20) train acc: 0.980000; val_acc: 0.123000
(Epoch 12 / 20) train acc: 1.000000; val_acc: 0.121000
(Epoch 13 / 20) train acc: 1.000000; val_acc: 0.121000
(Epoch 14 / 20) train acc: 1.000000; val_acc: 0.121000
(Epoch 15 / 20) train acc: 1.000000; val_acc: 0.121000
(Iteration 31 / 40) loss: 0.000644
(Epoch 16 / 20) train acc: 1.000000; val_acc: 0.121000
(Epoch 17 / 20) train acc: 1.000000; val_acc: 0.121000
(Epoch 18 / 20) train acc: 1.000000; val_acc: 0.121000
(Epoch 19 / 20) train acc: 1.000000; val_acc: 0.121000
(Epoch 20 / 20) train acc: 1.000000; val_acc: 0.121000
```

Training loss history



Inline Question 2:

你注意到训练三层网和训练五层网难度的区别了吗?根据你的经验,哪个网络对initalization scale 更敏感?为什么会这样呢?

Answer:

5层更难训练,5层对initalization scale更加敏感,因为网络越深,每个神经元受到其他神经元的影响就越大,也更容易发生"梯度消失"或者"梯度爆炸"。五层网络的损失函数要更复杂,一旦层数更多,就需要更多的超参数,那么初始化的权重和偏置值也会更加敏感,条件更加苛刻,如果权重值设置过大,容易造成梯度爆炸,如果权重值设置过小,层数增多,容易造成梯度消失。并且,随着层数的增多,在更深层要想得到较好的分布也会变得更难。

更新规则

到目前为止,我们使用了普通的随机梯度下降法(SGD)作为我们的更新规则。更复杂的更新规则可以更容易地训练深度网络。我们将实现一些最常用的更新规则,并将它们与普通的SGD进行比较。

SGD+Momentum

带动量的随机梯度下降法是一种广泛使用的更新规则,它使深度网络的收敛速度快于普通的随机梯度下降法。更多信息参见http://cs231n.github.io/neural-networks-3/#sqd 动量更新部分。

打开文件 daseCV/optim , 并阅读该文件顶部的文档,以确保你理解了该API。在函数 sgd_momentum 中实现SGD+动量更新规则,并运行以下代码检查你的实现。你会看到errors小于 e-8。

```
In [17]:
          from daseCV.optim import sgd momentum
          N, D = 4, 5
          w = np. 1inspace(-0.4, 0.6, num=N*D).reshape(N, D)
           dw = np. linspace(-0.6, 0.4, num=N*D). reshape(N, D)
           v = np. linspace(0.6, 0.9, num=N*D). reshape(N, D)
           config = {'learning rate': le-3, 'velocity': v}
           next w, = sgd momentum(w, dw, config=config)
           expected next w = np. asarray([
             [ 0.1406, \qquad 0.20738947, \quad 0.27417895, \quad 0.34096842, \quad 0.40775789 ],
             [0.47454737, 0.54133684, 0.60812632, 0.67491579, 0.74170526],
             [0.80849474, 0.87528421, 0.94207368, 1.00886316, 1.07565263],
             [ 1.14244211, 1.20923158, 1.27602105, 1.34281053, 1.4096
                                                                          11)
           expected velocity = np. asarray([
             [0.5406, 0.55475789, 0.56891579, 0.58307368, 0.59723158],
             [0.61138947, 0.62554737, 0.63970526, 0.65386316, 0.66802105],
             [0.68217895, 0.69633684, 0.71049474, 0.72465263, 0.73881053],
             [0.75296842, 0.76712632, 0.78128421, 0.79544211, 0.8096]
          # Should see relative errors around e-8 or less
           print('next_w error: ', rel_error(next_w, expected_next_w))
           print('velocity error: ', rel_error(expected_velocity, config['velocity']))
```

next_w error: 8.882347033505819e-09
velocity error: 4.269287743278663e-09

当你完成了上面的步骤,运行以下代码来训练一个具有SGD和SGD+momentum的六层网络。你应该看到SGD+momentum更新规则收敛得更快。

```
In [18]:
           num train = 4000
           small data = {
             'X_train': data['X_train'][:num_train],
             'y train': data['y train'][:num train],
             'X_val': data['X_val'],
              y val': data['y val'],
           solvers = \{\}
           for update_rule in ['sgd', 'sgd_momentum']:
             print('running with ', update rule)
             model = FullyConnectedNet([100, 100, 100, 100, 100], weight scale=5e-2)
             solver = Solver (model, small data,
                              num epochs=5, batch size=100,
                              update rule=update rule,
                              optim config={
                                'learning rate': 5e-3,
                              },
                              verbose=True)
             solvers[update rule] = solver
             solver. train()
             print()
           plt. subplot (3, 1, 1)
```

```
plt. title ('Training loss')
plt. xlabel ('Iteration')
plt. subplot (3, 1, 2)
plt. title('Training accuracy')
plt. xlabel('Epoch')
plt. subplot (3, 1, 3)
plt. title ('Validation accuracy')
plt. xlabel ('Epoch')
for update_rule, solver in solvers.items():
  plt. subplot (3, 1, 1)
  plt.plot(solver.loss_history, 'o', label="loss_%s" % update_rule)
  plt. subplot (3, 1, 2)
  plt.plot(solver.train_acc_history, '-o', label="train_acc_%s" % update_rule)
  plt. subplot (3, 1, 3)
  plt.plot(solver.val_acc_history, '-o', label="val_acc_%s" % update_rule)
for i in [1, 2, 3]:
  plt. subplot(3, 1, i)
  plt. legend (loc='upper center', ncol=4)
plt. gcf(). set size inches(15, 15)
plt. show()
```

```
running with sgd
(Iteration 1 / 200) loss: 2.559978
(Epoch 0 / 5) train acc: 0.104000; val acc: 0.107000
(Iteration 11 / 200) loss: 2.356070
(Iteration 21 / 200) loss: 2.214091
(Iteration 31 / 200) loss: 2.205928
(Epoch 1 / 5) train acc: 0.225000; val acc: 0.193000
(Iteration 41 / 200) loss: 2.132095
(Iteration 51 / 200) loss: 2.118950
(Iteration 61 / 200) loss: 2.116443
(Iteration 71 / 200) loss: 2.132549
(Epoch 2 / 5) train acc: 0.298000; val acc: 0.260000
(Iteration 81 / 200) loss: 1.977227
(Iteration 91 / 200) loss: 2.007528
(Iteration 101 / 200) loss: 2.004762
(Iteration 111 / 200) loss: 1.885342
(Epoch 3 / 5) train acc: 0.343000; val_acc: 0.287000
(Iteration 121 / 200) loss: 1.891517
(Iteration 131 / 200) loss: 1.923677
(Iteration 141 / 200) loss: 1.957743
(Iteration 151 / 200) loss: 1.966736
(Epoch 4 / 5) train acc: 0.322000; val_acc: 0.305000
(Iteration 161 / 200) loss: 1.801483
(Iteration 171 / 200) loss: 1.973780
(Iteration 181 / 200) loss: 1.666572
(Iteration 191 / 200) loss: 1.909494
(Epoch 5 / 5) train acc: 0.373000; val acc: 0.319000
running\ with\ sgd\_momentum
(Iteration 1 / 200) loss: 3.153778
(Epoch 0 / 5) train acc: 0.099000; val acc: 0.088000
(Iteration 11 / 200) loss: 2.227203
(Iteration 21 / 200) loss: 2.125706
(Iteration 31 / 200) loss: 1.932695
(Epoch 1 / 5) train acc: 0.307000; val_acc: 0.260000
(Iteration 41 / 200) loss: 1.946488
(Iteration 51 / 200) loss: 1.778584
(Iteration 61 / 200) loss: 1.758119
(Iteration 71 / 200) loss: 1.849137
(Epoch 2 / 5) train acc: 0.382000; val acc: 0.322000
```

```
(Iteration 81 / 200) loss: 2.048671

(Iteration 91 / 200) loss: 1.693223

(Iteration 101 / 200) loss: 1.511693

(Iteration 111 / 200) loss: 1.390754

(Epoch 3 / 5) train acc: 0.458000; val_acc: 0.338000

(Iteration 121 / 200) loss: 1.670614

(Iteration 131 / 200) loss: 1.540272

(Iteration 141 / 200) loss: 1.597365

(Iteration 151 / 200) loss: 1.609851

(Epoch 4 / 5) train acc: 0.490000; val_acc: 0.327000

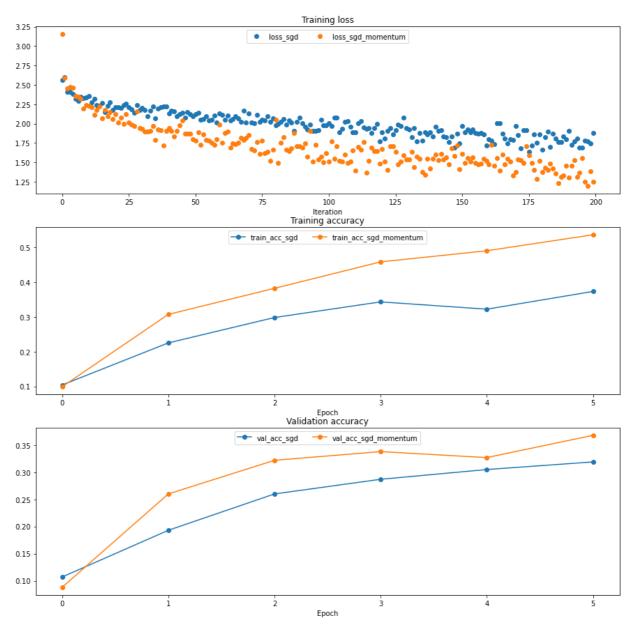
(Iteration 161 / 200) loss: 1.472687

(Iteration 171 / 200) loss: 1.378620

(Iteration 181 / 200) loss: 1.378174

(Iteration 191 / 200) loss: 1.305935

(Epoch 5 / 5) train acc: 0.536000; val_acc: 0.368000
```



RMSProp and Adam

RMSProp [1] 和Adam [2] 是另外两个更新规则,它们通过使用梯度的二阶矩平均值来设置每个参数的学习速率。

在文件 daseCV/optim 中实现 RMSProp 函数和 Adam 函数,并使用下面的代码来检查您的实现。

- [1] Tijmen Tieleman and Geoffrey Hinton. "Lecture 6.5-rmsprop: Divide the gradient by a running average of its recent magnitude." COURSERA: Neural Networks for Machine Learning 4 (2012).
- [2] Diederik Kingma and Jimmy Ba, "Adam: A Method for Stochastic Optimization", ICLR 2015.

```
# Test RMSProp implementation
from daseCV.optim import rmsprop
N, D = 4, 5
w = np. linspace(-0.4, 0.6, num=N*D). reshape(N, D)
dw = np. linspace(-0.6, 0.4, num=N*D). reshape(N, D)
cache = np. linspace (0.6, 0.9, num=N*D). reshape (N, D)
config = {'learning rate': 1e-2, 'cache': cache}
next_w, _ = rmsprop(w, dw, config=config)
expected next w = np. asarray([
  [-0.39223849, -0.34037513, -0.28849239, -0.23659121, -0.18467247],
  [-0.132737, -0.08078555, -0.02881884, 0.02316247, 0.07515774],
  [0.12716641, 0.17918792, 0.23122175, 0.28326742, 0.33532447],
  [0.38739248, 0.43947102, 0.49155973, 0.54365823, 0.59576619]])
expected cache = np. asarray([
  [ 0.5976,
                0.6126277, 0.6277108, 0.64284931, 0.65804321],
  [0.67329252, 0.68859723, 0.70395734, 0.71937285, 0.73484377],
  [0.75037008, 0.7659518, 0.78158892, 0.79728144, 0.81302936],
  [ 0.82883269, 0.84469141, 0.86060554, 0.87657507, 0.8926
                                                                  ]])
# You should see relative errors around e-7 or less
print('next_w error: ', rel_error(expected_next_w, next_w))
print('cache error: ', rel_error(expected_cache, config['cache']))
next_w error: 9.524687511038133e-08
cache error: 2.6477955807156126e-09
# Test Adam implementation
from daseCV.optim import adam
N, D = 4, 5
w = np. 1inspace(-0.4, 0.6, num=N*D). reshape(N, D)
dw = np. linspace(-0.6, 0.4, num=N*D). reshape(N, D)
```

m = np. linspace(0.6, 0.9, num=N*D). reshape(N, D)v = np. linspace(0.7, 0.5, num=N*D). reshape(N, D)config = {'learning rate': 1e-2, 'm': m, 'v': v, 't': 5} next_w, _ = adam(w, dw, config=config) expected next w = np. asarray([[-0.40094747, -0.34836187, -0.29577703, -0.24319299, -0.19060977],[-0.1380274, -0.08544591, -0.03286534, 0.01971428, 0.0722929],0. 17744702, 0. 23002243, 0.28259667, 0.33516969], 0.1248705, [0.38774145, 0.44031188, 0.49288093, 0.54544852, 0.59801459]])expected v = np. asarray([[0.69966, 0.68908382, 0.67851319, 0.66794809, 0.65738853,],0.64683452, 0.63628604, 0.6257431, 0.61520571, 0.60467385,], [0.59414753, 0.58362676, 0.57311152, 0.56260183, 0.55209767,], $\begin{bmatrix} 0.54159906, 0.53110598, 0.52061845, 0.51013645, 0.49966, \end{bmatrix}$ expected m = np. asarray([0.49947368, 0.51894737, 0.53842105, 0.55789474], [0.48,[0.57736842, 0.59684211, 0.61631579, 0.63578947, 0.65526316],[0.67473684, 0.69421053, 0.71368421,0.73315789, 0.75263158, [0.77210526, 0.79157895, 0.81105263, 0.83052632, 0.85]])

```
# You should see relative errors around e-7 or less
print('next_w error: ', rel_error(expected_next_w, next_w))
print('v error: ', rel_error(expected_v, config['v']))
print('m error: ', rel_error(expected_m, config['m']))
```

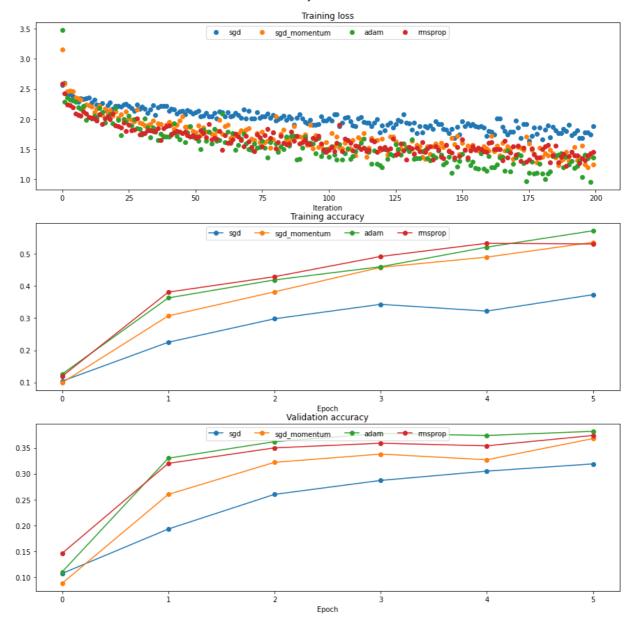
next_w error: 1.1395691798535431e-07 v error: 4.208314038113071e-09 m error: 4.214963193114416e-09

当你完成了上面RMSProp和Adam函数后,运行下面的代码训练一对网络,其中分别使用了上述两个方法

```
learning rates = {'rmsprop': le-4, 'adam': le-3}
for update rule in ['adam', 'rmsprop']:
  print('running with ', update rule)
  model = FullyConnectedNet([100, 100, 100, 100, 100], weight scale=5e-2)
  solver = Solver(model, small_data,
                   num epochs=5, batch size=100,
                   update_rule=update_rule,
                   optim_config={
                     'learning rate': learning rates[update rule]
                   },
                   verbose=True)
  solvers[update rule] = solver
  solver. train()
  print()
plt. subplot (3, 1, 1)
plt. title('Training loss')
plt. xlabel ('Iteration')
plt. subplot (3, 1, 2)
plt. title ('Training accuracy')
plt. xlabel ('Epoch')
plt. subplot (3, 1, 3)
plt. title('Validation accuracy')
plt. xlabel ('Epoch')
for update rule, solver in list(solvers.items()):
  plt. subplot (3, 1, 1)
  plt. plot (solver. loss_history, 'o', label=update_rule)
  plt. subplot (3, 1, 2)
  plt.plot(solver.train_acc_history, '-o', label=update_rule)
  plt. subplot (3, 1, 3)
  plt. plot (solver. val acc history, '-o', label=update rule)
for i in [1, 2, 3]:
  plt. subplot(3, 1, i)
  plt. legend (loc='upper center', ncol=4)
plt. gcf(). set size inches(15, 15)
plt. show()
running with adam
```

```
running with adam
(Iteration 1 / 200) loss: 3.476928
(Epoch 0 / 5) train acc: 0.126000; val_acc: 0.110000
(Iteration 11 / 200) loss: 2.027712
(Iteration 21 / 200) loss: 2.183358
(Iteration 31 / 200) loss: 1.744257
(Epoch 1 / 5) train acc: 0.363000; val_acc: 0.330000
(Iteration 41 / 200) loss: 1.707951
```

```
(Iteration 51 / 200) loss: 1.703835
(Iteration 61 / 200) loss: 2.094758
(Iteration 71 / 200) loss: 1.505558
(Epoch 2 / 5) train acc: 0.419000; val acc: 0.362000
(Iteration 81 / 200) loss: 1.594429
(Iteration 91 / 200) loss: 1.519017
(Iteration 101 / 200) loss: 1.368522
(Iteration 111 / 200) loss: 1.470400
(Epoch 3 / 5) train acc: 0.460000; val acc: 0.378000
(Iteration 121 / 200) loss: 1.199064
(Iteration 131 / 200) loss: 1.464705
(Iteration 141 / 200) loss: 1.359863
(Iteration 151 / 200) loss: 1.415068
(Epoch 4 / 5) train acc: 0.521000; val acc: 0.374000
(Iteration 161 / 200) loss: 1.382818
(Iteration 171 / 200) loss: 1.359900
(Iteration 181 / 200) loss: 1.095947
(Iteration 191 / 200) loss: 1.243087
(Epoch 5 / 5) train acc: 0.572000; val acc: 0.382000
running with rmsprop
(Iteration 1 / 200) loss: 2.589166
(Epoch 0 / 5) train acc: 0.119000; val acc: 0.146000
(Iteration 11 / 200) loss: 2.032921
(Iteration 21 / 200) loss: 1.897278
(Iteration 31 / 200) loss: 1.770793
(Epoch 1 / 5) train acc: 0.381000; val acc: 0.320000
(Iteration 41 / 200) loss: 1.895732
(Iteration 51 / 200) loss: 1.681091
(Iteration 61 / 200) loss: 1.487204
(Iteration 71 / 200) loss: 1.629973
(Epoch 2 / 5) train acc: 0.429000; val acc: 0.350000
(Iteration 81 / 200) loss: 1.506686
(Iteration 91 / 200) loss: 1.610742
(Iteration 101 / 200) loss: 1.486124
(Iteration 111 / 200) loss: 1.559454
(Epoch 3 / 5) train acc: 0.492000; val_acc: 0.359000
(Iteration 121 / 200) loss: 1.496859
(Iteration 131 / 200) loss: 1.531552
(Iteration 141 / 200) loss: 1.550195
(Iteration 151 / 200) loss: 1.657838
(Epoch 4 / 5) train acc: 0.533000; val_acc: 0.354000
(Iteration 161 / 200) loss: 1.603105
(Iteration 171 / 200) loss: 1.405372
(Iteration 181 / 200) loss: 1.503740
(Iteration 191 / 200) loss: 1.385278
(Epoch 5 / 5) train acc: 0.531000; val_acc: 0.374000
```



Inline Question 3:

AdaGrad, 类似于Adam, 是一个per-parameter优化方法, 它使用以下更新规则:

```
cache += dw**2
w += - learning_rate * dw / (np.sqrt(cache) + eps)
```

当使用AdaGrad训练一个网络时,更新的值会变得非常小,而且他的网络学习的非常慢。利用你对AdaGrad更新规则的了解,解释为什么更新的值会变得非常小? Adam会有同样的问题吗?

Answer:

在每次迭代中,我们都将平方梯度相加。因此,如果迭代次数很大,那么cache将非常大,因为我们正在累积正值(cache+=dw**2)。因此,当梯度(dw)除以缓存值的平方根(np.sqrt(cache))时,所以更新的值将变得非常小。

Adam没有这个问题,因为它使用了平方梯度的指数加权平均(EWA)。也就是说,它以指数方式累积过去的梯度,为最近的梯度分配大权重,为旧梯度分配小权重(类似于计算机网络和操作系统

中的老化算法)。除此之外,Adam使用动量的EWA而不是默认梯度(dw),从而导致由平方梯度的EWA控制的大量更新。

根据上面的公式,adagrad 每步更新会越除越小。adam 结合了adagrad 和动量的方法,避免了这个问题。

训练一个效果足够好的模型!

在CIFAR-10上尽可能训练最好的全连接模型,将最好的模型存储在 best_model 变量中。我们要求你在验证集上获得至少50%的准确性。

如果你细心的话,应该是有可能得到55%以上精度的,但我们不苛求你达到这么高的精度。在后面的作业上,我们会要求你们在CIFAR-10上训练最好的卷积神经网络,我们希望你们把精力放在卷积网络上,而不是全连接网络上。

在做这部分之前完成 BatchNormalization.ipynb 和 Dropout.ipynb 可能会对你有帮助,因为这些技术可以帮助你训练强大的模型。

```
In [22]:
          best model = None
          best val acc = 0
          best_model = None
          best val acc = 0
          # TODO: Train the best FullyConnectedNet that you can on CIFAR-10. You might
          # find batch/layer normalization and dropout useful. Store your best model in #
          # the best model variable.
          # ****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
          learning rates = \begin{bmatrix} 5 * 10 ** i \text{ for i in range}(-5, -2) \end{bmatrix}
          weight scales = [i * 10 ** -2 \text{ for } i \text{ in range}(1, 6)]
          for learning rate in learning rates:
            for weight_scale in weight_scales:
              model = FullyConnectedNet([300, 200, 150, 80, 50], weight scale=weight scale)
              solver = Solver(model, data,
                       num epochs=5, batch size=100,
                       update rule='adam',
                       optim config={
                         'learning rate': learning rate,
                       verbose=False)
              print('learning_rate: ', learning_rate, 'weight_scale: ', weight_scale)
              solver. train()
              print('val acc: ', solver.best val acc)
              if solver.best val acc > best val acc:
               best model = model
               best_val_acc = solver.best_val_acc
               print('updated model with new val acc: ', best val acc)
              print()
          print('best_val_acc: ', best_val_acc)
          # ****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
```

```
learning rate: 5e-05 weight scale: 0.01
val acc: 0.386
updated model with new val acc: 0.386
learning rate: 5e-05 weight scale: 0.02
val acc: 0.513
updated model with new val_acc: 0.513
learning rate: 5e-05 weight scale: 0.03
val acc: 0.5
learning_rate: 5e-05 weight_scale: 0.04
val acc: 0.49
learning_rate: 5e-05 weight_scale: 0.05
val acc: 0.472
learning_rate: 0.0005 weight_scale: 0.01
val acc: 0.509
learning_rate: 0.0005 weight_scale: 0.02
val_acc: 0.548
updated model with new val_acc: 0.548
learning_rate: 0.0005 weight_scale: 0.03
val_acc: 0.529
learning_rate: 0.0005 weight_scale: 0.04
val_acc: 0.494
learning_rate: 0.0005 weight_scale: 0.05
val acc: 0.509
learning_rate: 0.005 weight_scale: 0.01
val_acc: 0.312
learning rate: 0.005 weight scale: 0.02
val acc: 0.363
learning rate: 0.005 weight scale: 0.03
val acc: 0.399
learning rate: 0.005 weight scale: 0.04
val acc: 0.408
learning rate: 0.005 weight scale: 0.05
val acc: 0.462
best val acc: 0.548
```

测试你的模型!

在验证和测试集上运行您的最佳模型。验证集的准确率应达到50%以上。

```
y_test_pred = np. argmax(best_model. loss(data['X_test']), axis=1)
y_val_pred = np. argmax(best_model. loss(data['X_val']), axis=1)
print('Validation set accuracy: ', (y_val_pred == data['y_val']). mean())
print('Test set accuracy: ', (y_test_pred == data['y_test']). mean())

Validation set accuracy: 0.548
Test set accuracy: 0.526
```

Data for leaderboard

这里额外提供了一组未给标签的测试集X,用于leaderborad上的竞赛。

提示: 该题的目的是鼓励同学们探索能够提升模型性能的方法。

提醒:运行完下面代码之后,点击下面的submit,然后去leaderboard上查看你的成绩。本模型对应的成绩在phase1的leaderboard中。

```
import os
#输出格式
def output file(preds, phase id=1):
    path=os.getcwd()
    if not os.path.exists(path + '/output/phase {}'.format(phase id)):
        os. mkdir(path + '/output/phase_{}'. format(phase_id))
    path=path + '/output/phase_{}/prediction.npy'. format(phase_id)
    np. save (path, preds)
def zip_fun(phase_id=1):
    path=os.getcwd()
    output path = path + '/output'
    files = os. listdir(output path)
    for file in files:
        if _file.find('zip') != -1:
            os. remove (output path + '/' + file)
    newpath=path+'/output/phase_{}'. format(phase_id)
    os. chdir (newpath)
    cmd = 'zip ../prediction_phase_{{}}.zip prediction.npy'.format(phase_id)
    os. system(cmd)
    os. chdir (path)
output file(preds)
zip fun()
```

```
In [ ]:
```