

机器学习理论作业3

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正: $x_1 = (1, 2)^T$, $x_2 = (2, 3)^T$, $x_3 = (3, 3)^T$

负: $x_4 = (2, 1)^T$, $x_5 = (3, 2)^T$

$$\min_{w, b} \frac{1}{2} \|w\|^2$$

s.t.

$$w_1 + 2w_2 + b \geq 1 \quad ①$$

$$2w_1 + 3w_2 + b \geq 1 \quad ②$$

$$3w_1 + 3w_2 + b \geq 1 \quad ③$$

$$2w_1 + w_2 + b \leq -1 \quad ④ \Leftrightarrow -2w_1 - w_2 - b \geq 1 \quad ⑥$$

$$3w_1 + 2w_2 + b \leq -1 \quad ⑤ \Leftrightarrow -3w_1 - 2w_2 - b \geq 1 \quad ⑦$$

① ⑦

$$-2w_1 \geq 2 \Leftrightarrow 2w_1 \leq -2 \quad w_1 \leq -1$$

② ⑥

$$2w_2 \geq 2 \Leftrightarrow w_2 \geq 1$$

⑦ ③

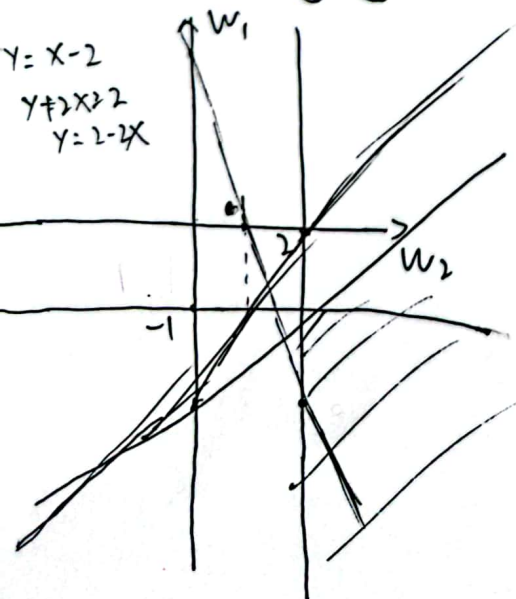
$$w_2 \geq 2$$

⑥ ①

$$-w_1 + w_2 \geq 2 \Rightarrow w_1 - w_2 \leq -2$$

⑥ ③

$$w_1 + 2w_2 \geq 2$$



$$\therefore \min_{w, b} \frac{1}{2} \|w\|^2 \text{ 时 } w_1 = -1 \quad w_2 = 2$$

代入①⑤

$$① \quad -1 + 4 + b \geq 1 \Rightarrow b \geq -2$$

$$⑤ \quad -3 + 4 + b \leq -1 \Rightarrow b \leq -2 \Rightarrow b = -2$$

分离超平面 $-x_1 + 2x_2 - 2 = 0$

分类决策函数 $f(x) = \text{sign}(-x_1 + 2x_2 - 2)$

$$-x_1 + 2x_2 - 2 = 1$$

$x_1 \checkmark$

~~x_2~~

$x_3 \checkmark$

$$-x_1 + 2x_2 - 2 = -1$$

~~x_4~~

$x_5 \checkmark$

$\therefore x_1, x_3, x_5$ 是支持向量