Relevant Ambiguity vs Irrelevant Ambiguity

February 22, 2018

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They're trying to work backwards, and map from the sentences to the grammar.

$$\{S_1S_2S_3\ldots\}\to G$$

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▶ a set of competing grammars, as in Clark's Genetic Algorithm:

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▶ a vector of per-parameter confidence levels, as in Katherine's learner:

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Sentences

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- ▶ Each sentence the learner receives from L(G) is a potential piece of evidence they can use to update their hypothesis.
- ▶ If we characterize the learner as forming a hypothesis for each parameter value separately, we can classify a sentence s as evidence for the setting of parameter P_i in the following three ways.

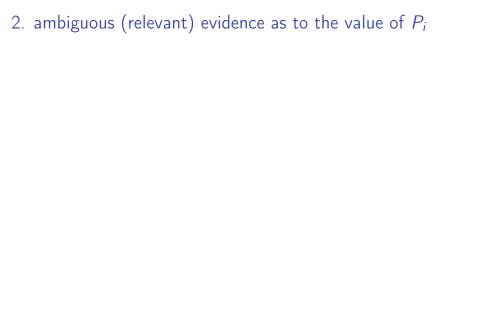
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- ▶ The only grammars in the domain that ever license sentence s are those that have have $P_5 = 1$, for example.
- ▶ Observing s in the input data is a globally valid trigger for $P_5 = 1$. We would never observe s in a language with $P_5 = 0$.



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2. ambiguous (relevant) evidence as to the value of P_i

- ▶ s exists in languages where $P_5 = 0$ and in languages where $P_5 = 1$.
- ▶ The fact that we've observed *s* is not useful information on its own, it's not a global trigger.
- ▶ But maybe we can still learn something relevant to the setting of *P*₅ by inspecting the contents of *s*.

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- ▶ G and G' are minimal pairs on P₅.
- Like the ambiguous case, the fact that we've observed s is not useful information on its own,
- ▶ But we can also conclude that because it never matters what P_5 is set to, we should not try to learn about P_5 from s.

Whatever syntactic phenomena P₅ describes is simply not expressed at all in s (can we actually draw this strong conclusion from the domain-level data?).

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 - ▶ then s is a globally valid trigger for $P_3 = 0$ or $P_3 = 1$, respectively. Emit a 0 or 1.

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 - ▶ look for the minimal pair 2 of g on P_3 . We can do this by toggling bit P_3 in g, and checking if $toggled(g) \in G^s$.

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An Algorithm for generating irrelevance strings

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 - else if it doesn't exist, but that's because it's not one of the legal 3072 colag languages, we can't make a claim (?)

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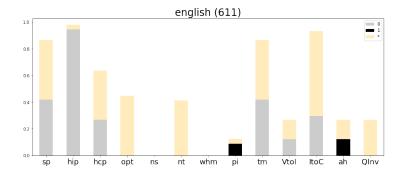
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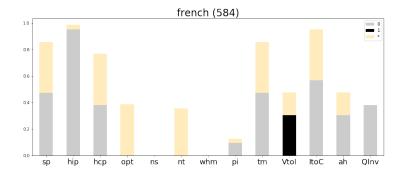
- 1. G^s = all grammars that license s.
- 2. P_3^s = the set of all values of P_3 in G^s
- 3. If P₃^s = {0} or P₃^s = {1} (only one value showed up),
 then s is a globally valid trigger for P₃ = 0 or P₃ = 1, respectively. Emit a 0 or 1.
- 4. Otherwise we can now assume s is either ambiguously relevant * or irrelevant ~. Assume s irrelevant, unless step 5 finds finds otherwise.
 - 5. For each g in G^s
 - ▶ look for the minimal pair 2 of g on P_3 . We can do this by toggling bit P_3 in g, and checking if $toggled(g) \in G^s$.
 - if one exists, then toggling P_3 changed nothing wrt s.
 - ▶ else if it doesn't exist, but that's because it's not one of the legal 3072 colag languages, we can't make a claim (?)
 - else if it doesn't exist, we've found an example where P₃ actually has some effect on the appearance of s in a language. It's not irrelevant, just ambiguous. Emit a *.

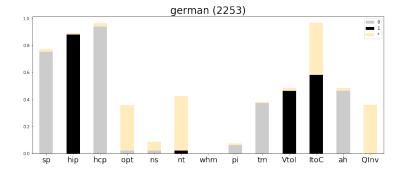
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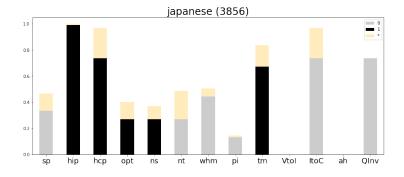
Question

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if (minimal_pair not in generators and
   minimal_pair not in disallowed):
   relstr[param] = '*'
   break
```





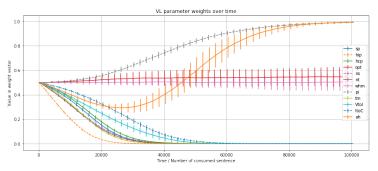


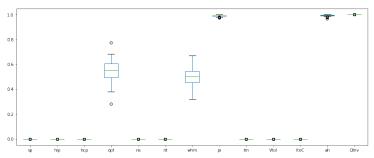


Discarding useless data

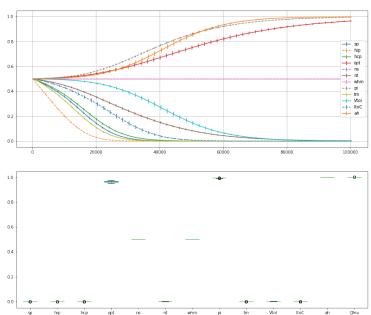
► What happens if a learner uses information about irrelevance to discard sentences?

Yang's Reward-only VL Learning English (611)





Reward-relevant-only VL Learning English (611)

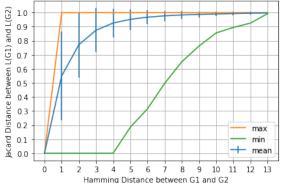


Reward-relevant-only VL Learning English (611)

- Optional Topic converges
- Null Subject fails to converge
- Affix-hopping moves in a single direction
- Vtol, ItoC and Null Topic take longer to learn

Smoothness: Parameters vs Sentences

Hamming Distance between G1, G2 vs Jacard Distance between L(G1) and L(G2)



 hamming distance – number of bits that differ between two bit-strings

$$jaccard(L(G1),L(G2)) = \frac{L(G1) \cap L(G2)}{L(G1) \cup L(G2)} = \frac{\# \text{ sentences in common}}{\# \text{ sentences in total}}$$

Smoothness: Parameters vs Trigger-types

