

FE590. Assignment #2.

2017-03-03

Instructions

In this assignment, you should use R markdown to answer the questions below. Simply type your R code into embedded chunks as shown above. When you have completed the assignment, knit the document into a PDF file, and upload both the .pdf and .Rmd files to Canvas.

Question 1 (based on JWHT Chapter 2, Problem 9)

Use the Auto data set from the textbook's website. When reading the data, use the options `as.is = TRUE` and `na.strings = "?"`. Remove the unavailable data using the `na.omit()` function.

```
library(ISLR)
setwd("/Users/apple/Desktop/590")
auto <- read.csv("Auto.csv", as.is = T, na.strings = "?")
auto <- na.omit(auto)
```

1. List the names of the variables in the data set.

```
colnames(auto)

## [1] "mpg"          "cylinders"    "displacement" "horsepower"
## [5] "weight"       "acceleration" "year"         "origin"
## [9] "name"
```

2. The columns `origin` and `name` are unimportant variables. Create a new data frame called `cars` that contains none of these unimportant variables

```
cars <- subset(auto, select = -c(origin, name))
```

3. What is the range of each quantitative variable? Answer this question using the `range()` function with the `sapply()` function (e.g., `sapply(cars, range)`). Print a simple table of the ranges of the variables. The rows should correspond to the variables. The first column should be the lowest value of the corresponding variable, and the second column should be the maximum value of the variable. The columns should be suitably labeled.

```
car.range <- sapply(cars, range)
car.range <- t(car.range)
colnames(car.range) <- c("min", "max")

knitr::kable(car.range, caption = "The variable ranges of Cars")
```

Table 1: The variable ranges of Cars

	min	max
mpg	9	46.6
cylinders	3	8.0
displacement	68	455.0
horsepower	46	230.0
weight	1613	5140.0
acceleration	8	24.8
year	70	82.0

4. What is the mean and standard deviation of each variable? Create a simple table of the means and standard deviations.

```
vector.m <- sapply(cars, mean)
vector.sd <- sapply(cars, sd)
md <- rbind(vector.m, vector.sd)
md <- t(md)
colnames(md) <- c("mean", "standard_deviation")

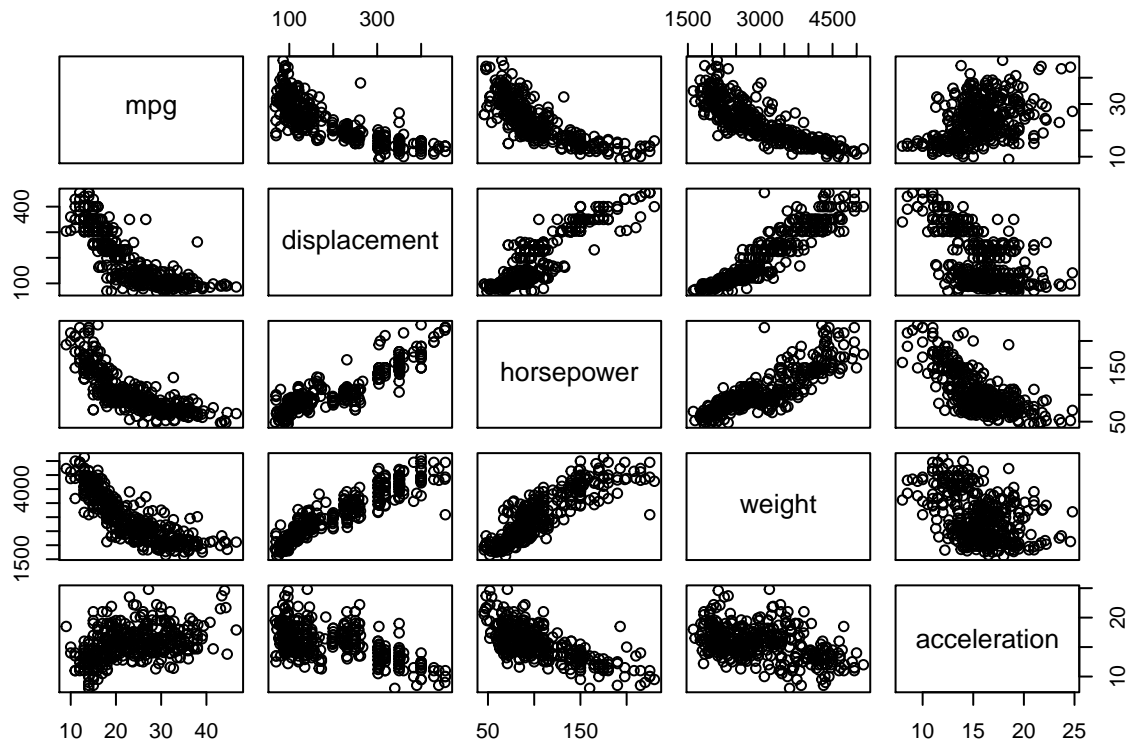
knitr::kable(md, caption = "Means and SD of Cars")
```

Table 2: Means and SD of Cars

	mean	standard_deviation
mpg	23.445918	7.805008
cylinders	5.471939	1.705783
displacement	194.411990	104.644004
horsepower	104.469388	38.491160
weight	2977.584184	849.402560
acceleration	15.541327	2.758864
year	75.979592	3.683737

5. Create a scatterplot matrix that includes the variables mpg, displacement, horsepower, weight, and acceleration using the pairs() function.

```
newdf <- subset(cars, select = c(mpg, displacement, horsepower, weight, acceleration))
pairs(newdf)
```



6. From the scatterplot, it should be clear that mpg has an almost linear relationship to predictors, and higher-order relationships to other variables. Using the `regsubsets` function in the `leaps` library, regress mpg onto

- displacement
- displacement squared
- horsepower
- horsepower squared
- weight
- weight squared
- acceleration

```
library(leaps)
attach(newdf)
newdf$displacement_squared <- displacement^2
newdf$horsepower_squared <- horsepower^2
newdf$weight_squared <- weight^2
detach(newdf)

m <- regsubsets(mpg~., data = newdf)
regs <- t(summary(m)$which)
```

Print a table showing what variables would be selected using best subset selection for all model orders.

```
knitr::kable(regs, caption = "Selections of variables")
```

Table 3: Selections of variables

	1	2	3	4	5	6	7
(Intercept)	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE	TRUE
displacement	FALSE	FALSE	FALSE	TRUE	TRUE	TRUE	TRUE
horsepower	FALSE	FALSE	TRUE	TRUE	TRUE	TRUE	TRUE
weight	TRUE	TRUE	TRUE	FALSE	FALSE	TRUE	TRUE
acceleration	FALSE	FALSE	FALSE	TRUE	TRUE	TRUE	TRUE
displacement_squared	FALSE	FALSE	FALSE	FALSE	TRUE	TRUE	TRUE
horsepower_squared	FALSE	FALSE	TRUE	TRUE	TRUE	TRUE	TRUE
weight_squared	FALSE	TRUE	FALSE	FALSE	FALSE	FALSE	TRUE

What is the most important variable affecting fuel consumption?

```
rownames(as.data.frame(coef(m, 1)))[2]
```

```
## [1] "weight"
```

What is the second most important variable affecting fuel consumption?

```
rownames(as.data.frame(coef(m, 2)))[3]
```

```
## [1] "weight_squared"
```

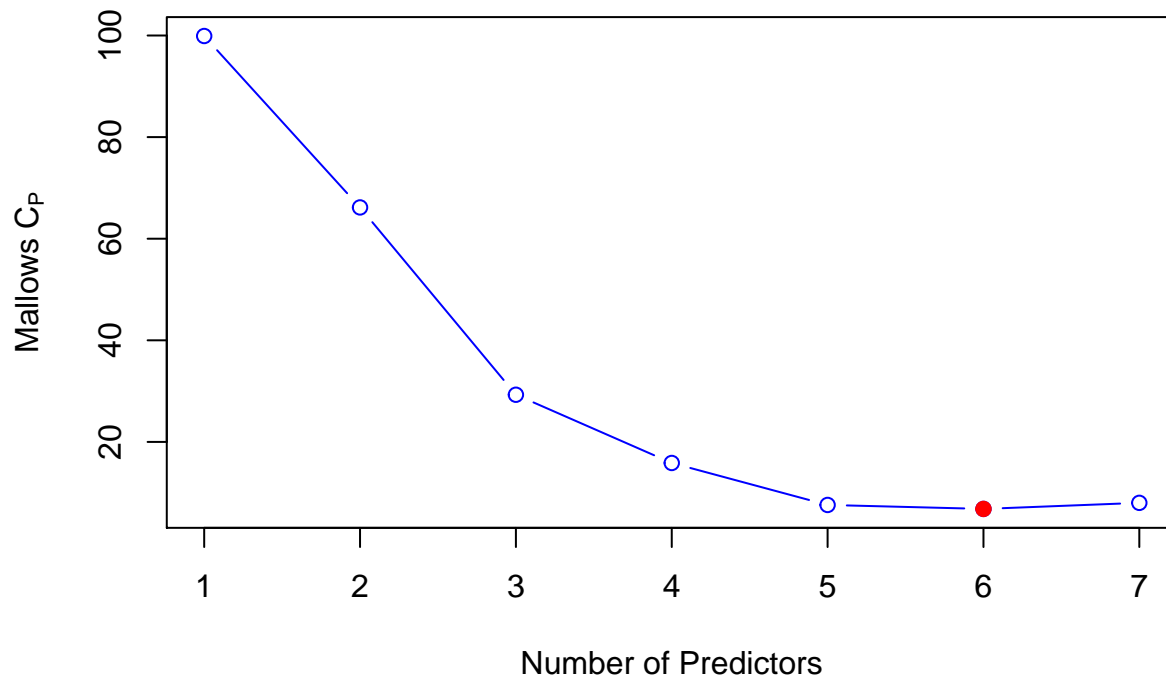
What is the third most important variable affecting fuel consumption?

```
rownames(as.data.frame(coef(m, 3)))[4]
```

```
## [1] "horsepower_squared"
```

7. Plot a graph showing Mallows's C_p as a function of the order of the model. Which model is the best?

```
cp=summary(m)$cp
i=which.min(cp)
plot(cp,type='b',col="blue",xlab="Number of Predictors",ylab=expression("Mallows C"[P]))
points(i,cp[i],pch=19,col="red")
```



The Mallows's C_p takes its minimum when the number of predictors is 6.

```
best_model <- summary(regsubsets(mpg~., data = newdf, nvmax = 6))$which
t(best_model[6,])
```

```
##      (Intercept) displacement horsepower weight acceleration
## [1,]      TRUE      TRUE      TRUE      TRUE      TRUE
##      displacement_squared horsepower_squared weight_squared
## [1,]      TRUE      TRUE      FALSE
```

The best model

Question 2 (based on JWHT Chapter 3, Problem 10)

This exercise involves the Boston housing data set.

1. Load in the Boston data set, which is part of the MASS library in R. The data set is contained in the object Boston. Read about the data set using the command `?Boston`. How many rows are in this data set? How many columns? What do the rows and columns represent?

```
library(MASS)
?Boston
```

There are 506 rows and 14 columns in the object Boston. Each row is an observation. For columns:

crim: per capita crime rate by town.

zn: proportion of residential land zoned for lots over 25,000 sq.ft.

indus: proportion of non-retail business acres per town.

chas: Charles River dummy variable (= 1 if tract bounds river; 0 otherwise).

nox: nitrogen oxides concentration (parts per 10 million).

rm: average number of rooms per dwelling.

age: proportion of owner-occupied units built prior to 1940.

dis: weighted mean of distances to five Boston employment centres.

rad: index of accessibility to radial highways.

tax: full-value property-tax rate per \$10,000.

ptratio: pupil-teacher ratio by town.

black: $1000(\text{Bk} - 0.63)^2$ where Bk is the proportion of blacks by town.

lstat: lower status of the population (percent).

medv: median value of owner-occupied homes in \$1000s.

2. Do any of the suburbs of Boston appear to have particularly high crime rates?

```
summary(Boston)
```

```
##          crim              zn          indus          chas
## Min.      : 0.00632    Min.      : 0.00    Min.      : 0.46    Min.      :0.00000
## 1st Qu.: 0.08204    1st Qu.: 0.00    1st Qu.: 5.19    1st Qu.:0.00000
## Median : 0.25651    Median : 0.00    Median : 9.69    Median :0.00000
## Mean      : 3.61352    Mean      : 11.36    Mean      :11.14    Mean      :0.06917
## 3rd Qu.: 3.67708    3rd Qu.: 12.50    3rd Qu.:18.10    3rd Qu.:0.00000
## Max.      :88.97620    Max.      :100.00    Max.      :27.74    Max.      :1.00000
##          nox          rm          age          dis
## Min.      :0.3850    Min.      :3.561    Min.      : 2.90    Min.      : 1.130
## 1st Qu.:0.4490    1st Qu.:5.886    1st Qu.: 45.02    1st Qu.: 2.100
## Median :0.5380    Median :6.208    Median : 77.50    Median : 3.207
## Mean      :0.5547    Mean      :6.285    Mean      : 68.57    Mean      : 3.795
## 3rd Qu.:0.6240    3rd Qu.:6.623    3rd Qu.: 94.08    3rd Qu.: 5.188
## Max.      :0.8710    Max.      :8.780    Max.      :100.00    Max.      :12.127
##          rad          tax          ptratio          black
## Min.      : 1.000    Min.      :187.0    Min.      :12.60    Min.      : 0.32
## 1st Qu.: 4.000    1st Qu.:279.0    1st Qu.:17.40    1st Qu.:375.38
## Median : 5.000    Median :330.0    Median :19.05    Median :391.44
## Mean      : 9.549    Mean      :408.2    Mean      :18.46    Mean      :356.67
## 3rd Qu.:24.000    3rd Qu.:666.0    3rd Qu.:20.20    3rd Qu.:396.23
## Max.      :24.000    Max.      :711.0    Max.      :22.00    Max.      :396.90
##          lstat          medv
## Min.      : 1.73    Min.      : 5.00
## 1st Qu.: 6.95    1st Qu.:17.02
## Median :11.36    Median :21.20
## Mean      :12.65    Mean      :22.53
## 3rd Qu.:16.95    3rd Qu.:25.00
## Max.      :37.97    Max.      :50.00
```

From the summary, we can see a wide range of crim rate (0.00632% - 88.97620%). However the mean and 3rd quantile is relatively low which indicate most parts of suburbs are safe and other parts are very dangerous.

Tax rates?

The range of tax rate is 187% to 711% which is also quite large.

Pupil-teacher ratios?

Pupil-teacher ranges from 12.6% to 22% which is relatively low compared to former two indicators.

Comment on the range of each predictor.

3. How many of the suburbs in this data set bound the Charles river?

```
sum(Boston$chas)
```

```
## [1] 35
```

4. What is the median pupil-teacher ratio among the towns in this data set?

```
median(Boston$ptratio)
```

```
## [1] 19.05
```

5. In this data set, how many of the suburbs average more than seven rooms per dwelling?

```
sum(Boston$rm > 7)
```

```
## [1] 64
```

More than eight rooms per dwelling?

```
sum(Boston$rm > 8)
```

```
## [1] 13
```

Comment on the suburbs that average more than eight rooms per dwelling.

```
summary(subset(Boston, rm > 8))
```

```
##      crim      zn      indus      chas
##  Min.   :0.02009  Min.   : 0.00  Min.   : 2.680  Min.   :0.0000
## 1st Qu.:0.33147  1st Qu.: 0.00  1st Qu.: 3.970  1st Qu.:0.0000
## Median :0.52014  Median : 0.00  Median : 6.200  Median :0.0000
## Mean   :0.71879  Mean   :13.62  Mean   : 7.078  Mean   :0.1538
## 3rd Qu.:0.57834  3rd Qu.:20.00  3rd Qu.: 6.200  3rd Qu.:0.0000
## Max.   :3.47428  Max.   :95.00  Max.   :19.580  Max.   :1.0000
##      nox      rm      age      dis
##  Min.   :0.4161  Min.   :8.034  Min.   : 8.40  Min.   :1.801
## 1st Qu.:0.5040  1st Qu.:8.247  1st Qu.:70.40  1st Qu.:2.288
## Median :0.5070  Median :8.297  Median :78.30  Median :2.894
## Mean   :0.5392  Mean   :8.349  Mean   :71.54  Mean   :3.430
## 3rd Qu.:0.6050  3rd Qu.:8.398  3rd Qu.:86.50  3rd Qu.:3.652
## Max.   :0.7180  Max.   :8.780  Max.   :93.90  Max.   :8.907
##      rad      tax      ptratio      black
##  Min.   : 2.000  Min.   :224.0  Min.   :13.00  Min.   :354.6
## 1st Qu.: 5.000  1st Qu.:264.0  1st Qu.:14.70  1st Qu.:384.5
## Median : 7.000  Median :307.0  Median :17.40  Median :386.9
```

```
## Mean      : 7.462      Mean      :325.1      Mean      :16.36      Mean      :385.2
## 3rd Qu.: 8.000      3rd Qu.:307.0      3rd Qu.:17.40      3rd Qu.:389.7
## Max.      :24.000      Max.      :666.0      Max.      :20.20      Max.      :396.9
##      lstat      medv
## Min.      :2.47      Min.      :21.9
## 1st Qu.:3.32      1st Qu.:41.7
## Median :4.14      Median :48.3
## Mean      :4.31      Mean      :44.2
## 3rd Qu.:5.12      3rd Qu.:50.0
## Max.      :7.44      Max.      :50.0
```

Compared to other suburbs, these suburbs that average more than eight rooms per dwelling have more lower status of the population (lstat).

Question 3 (based on JWHT Chapter 4, Problem 10)

This question should be answered using the Weekly data set, which is part of the ISLR package. This data contains 1,089 weekly returns for 21 years, from the beginning of 1990 to the end of 2010.

1. What does the data represent?

```
library(ISLR)
?Weekly
```

The data represents weekly percentage returns for the S&P 500 stock index between 1990 and 2010.

Year: The year that the observation was recorded

Lag1: Percentage return for previous week

Lag2: Percentage return for 2 weeks previous

Lag3: Percentage return for 3 weeks previous

Lag4: Percentage return for 4 weeks previous

Lag5: Percentage return for 5 weeks previous

Volume: Volume of shares traded (average number of daily shares traded in billions)

Today: Percentage return for this week

Direction: A factor with levels Down and Up indicating whether the market had a positive or negative return on a given week

2. Use the full data set to perform a logistic regression with Direction as the response and the five lag variables plus Volume as predictors. Use the summary function to print the results. Do any of the predictors appear to be statistically significant? If so, which ones?

```
attach(Weekly)
glm.fit <- glm(Direction ~ Lag1 + Lag2 + Lag3 + Lag4 + Lag5 + Volume, family=binomial)
summary(glm.fit)
```



```
##
## Call:
## glm(formula = Direction ~ Lag1 + Lag2 + Lag3 + Lag4 + Lag5 +
##       Volume, family = binomial)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -1.6949  -1.2565   0.9913   1.0849   1.4579
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept)  0.26686    0.08593   3.106  0.0019 **
## Lag1        -0.04127    0.02641  -1.563  0.1181
## Lag2         0.05844    0.02686   2.175  0.0296 *
## Lag3        -0.01606    0.02666  -0.602  0.5469
## Lag4        -0.02779    0.02646  -1.050  0.2937
## Lag5        -0.01447    0.02638  -0.549  0.5833
## Volume      -0.02274    0.03690  -0.616  0.5377
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 1496.2  on 1088  degrees of freedom
## Residual deviance: 1486.4  on 1082  degrees of freedom
## AIC: 1500.4
##
## Number of Fisher Scoring iterations: 4
detach(Weekly)
```

The predictor “Lag2” is statistically significant.

3. Fit a logistic regression model using a training data period from 1990 to 2008, with Lag2 as the only predictor. Compute the confusion matrix and the overall fraction of correct predictions for the held out data (that is, the data from 2009 and 2010).

```
Weekly.train <- subset(Weekly, Year <= 2008)
Weekly.test  <- subset(Weekly, Year > 2008)
fit <- glm(Direction ~ Lag2, data = Weekly.train, family = binomial)
glm.probs <- predict(fit, Weekly.test, type = "response")

glm.pred <- rep("Down", nrow(Weekly.test))
glm.pred[glm.probs > .5] <- "Up"

table(glm.pred, Weekly.test$Direction)

##
## glm.pred Down Up
##      Down    9  5
##      Up    34 56
```

```
glm.ratio <- mean(glm.pred == Weekly.test$Direction)
glm.ratio
```

```
## [1] 0.625
```

The fraction of correct predictions is 0.625.

4. Repeat Part 3 using LDA.

```
lda.fit <- lda(Direction ~ Lag2, data = Weekly.train)
lda.pred <- predict(lda.fit, Weekly.test)
lda.class <- lda.pred$class
```

```
table(lda.class, Weekly.test$Direction)
```

```
##
## lda.class Down Up
##      Down    9  5
##      Up     34 56
```

```
lda.ratio <- mean(lda.class == Weekly.test$Direction)
lda.ratio
```

```
## [1] 0.625
```

The fraction of correct predictions is 0.625.

5. Repeat Part 3 using QDA.

```
qda.fit <- qda(Direction ~ Lag2, data = Weekly.train)
qda.pred <- predict(qda.fit, Weekly.test)
qda.class <- qda.pred$class
```

```
table(qda.class, Weekly.test$Direction)
```

```
##
## qda.class Down Up
##      Down    0  0
##      Up     43 61
```

```
qda.ratio <- mean(qda.class == Weekly.test$Direction)
qda.ratio
```

```
## [1] 0.5865385
```

The fraction of correct predictions is 0.587.

6. Repeat Part 3 using KNN with $K = 1, 2, 3$.

```
library(class)
direction <- Weekly.train$Direction
Train.knn <- as.matrix(Weekly.train[, 3])
```

```

Test.knn <- as.matrix(Weekly.test[, 3])

knn.pred1 <- knn(Train.knn, Test.knn, direction, k = 1)
table(knn.pred1, Weekly.test$Direction)

##
## knn.pred1 Down Up
##      Down   21 29
##      Up     22 32

knn1.ratio <- mean(knn.pred1 == Weekly.test$Direction)
knn1.ratio

## [1] 0.5096154

knn.pred2 <- knn(Train.knn, Test.knn, direction, k = 2)
table(knn.pred2, Weekly.test$Direction)

##
## knn.pred2 Down Up
##      Down   21 29
##      Up     22 32

knn2.ratio <- mean(knn.pred2 == Weekly.test$Direction)
knn2.ratio

## [1] 0.5096154

knn.pred3 <- knn(Train.knn, Test.knn, direction, k = 3)
table(knn.pred3, Weekly.test$Direction)

##
## knn.pred3 Down Up
##      Down   16 19
##      Up     27 42

knn3.ratio <- mean(knn.pred3 == Weekly.test$Direction)
knn3.ratio

## [1] 0.5576923

```

7. Which of these methods in Parts 3, 4, 5, and 6 appears to provide the best results on this data?

```

method <- data.frame(glm.ratio, lda.ratio, qda.ratio, knn1.ratio, knn2.ratio, knn3.ratio)
knitr::kable(method)

```

glm.ratio	lda.ratio	qda.ratio	knn1.ratio	knn2.ratio	knn3.ratio
0.625	0.625	0.5865385	0.5096154	0.5096154	0.5576923

The logistic regression model and LDA model provide the best results on this data.

Question 4

Write a function that works in R to gives you the parameters from a linear regression on a data set between two sets of values (in other words you only have to do the 2-D case). Include in the output the standard error of your variables. You cannot use the `lm` command in this function or any of the other built in regression models. For example your output could be a 2x2 matrix with the parameters in the first column and the standard errors in the second column. For up to 5 bonus points, format your output so that it displays and operates similar in function to the output of the `lm` command.(i.e. in a data frame that includes all potentially useful outputs)

```
linear.regression <- function(data1, data2) {
  m1 <- mean(data1) # means of data
  m2 <- mean(data2)
  n <- length(data1)
  b <- (sum(data1*data2) - n*m1*m2)/(sum(data1^2) - n*m1^2)
  a <- m2 - b*m1
  data2.hat <- a + b*data1
  epsilon <- data2.hat - data2
  se.b <- sqrt(n*sum(epsilon^2)/(n-2)/(n*sum(data1^2)-(sum(data1))^2))
  se.a <- se.b*sqrt(sum(data1^2)/n)
  t.b <- b/se.b
  t.a <- a/se.a
  pr.b <- dt(t.b, n-2)
  pr.a <- dt(t.a, n-2)

  Estimate <- c(a, b)
  Std.Error <- c(se.a, se.b)
  t_value <- c(t.a, t.b)
  Pr <- c(pr.a, pr.b)
  df <- data.frame(Estimate, Std.Error, t_value, Pr)
  rownames(df) <- c("(Intercept)", "slope")
  return(df)
}
linear.regression(Weekly$Lag1, Weekly$Lag2)
```

```
##              Estimate Std.Error   t_value      Pr
## (Intercept)  0.16235187 0.07140973  2.273526 0.03020116
## slope       -0.07486073 0.03024891 -2.474824 0.01876503
```

Compare the output of your function to that of the `lm` command in R.

```
LG <- lm(Lag1 ~ Lag2, data = Weekly)
summary(LG)

##
## Call:
## lm(formula = Lag1 ~ Lag2, data = Weekly)
##
## Residuals:
```

```

##      Min      1Q   Median      3Q      Max
## -19.0604 -1.2715  0.1134   1.2796 11.2362
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  0.16189    0.07140   2.267  0.0236 *
## Lag2        -0.07485    0.03024  -2.475  0.0135 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.351 on 1087 degrees of freedom
## Multiple R-squared:  0.005603,    Adjusted R-squared:  0.004688
## F-statistic: 6.125 on 1 and 1087 DF,  p-value: 0.01348

```