

博士論文

Doctoral Dissertation

Time Dependent Charge-Parity Violation in  $B^0 \rightarrow K_s^0 K_s^0 K_s^0$  in Belle

II early operation

(Belle II 初期データを使った  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  崩壊の時間に依存する  
荷電・パリティ非保存の研究)

令和2年12月博士(理学)申請

A Dissertation Submitted for the Degree of Doctor of Philosophy

December 22nd, 2020

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**Time Dependent Charge-Parity Violation in  $B^0 \rightarrow K_s^0 K_s^0 K_s^0$  in  
Belle II early operation**

by

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Submitted to the Department of Physics  
on December 22nd, 2020, in partial fulfillment of the  
requirements for the degree of  
Doctor of Philosophy

**Abstract**

The Belle II experiment is a next-generation super  $B$ -factory experiment. The targeted instantaneous luminosity is  $8 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$  and the expected integrated luminosity is  $50 \text{ ab}^{-1}$  by 2030 with the majority of data collected at the  $\Upsilon(4S)$  resonance using SuperKEKB accelerator.

The thesis is based on the time-dependent  $CP$  violation study of  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  decay to precisely measure the  $CP$  parameters  $\mathcal{S}$  and  $\mathcal{A}$  in penguin-dominated  $b \rightarrow s$  transition, which is sensitive to New Physics effects. Such a precise measurement mainly depends on determination of the distance between two vertices of two neutral  $B$  mesons. The blind analysis and fit by a unbinned maximum likelihood method are performed using about  $62.8 \text{ fb}^{-1}$  recorded experiment data from Belle II detector 2019 and 2020 (spring and summer) operation. The measurement results:  $\mathcal{S} = -\sin(2\phi_1) = -0.82 \pm 0.85 \text{ (stat)} \pm 0.07 \text{ (syst)}$  and  $\mathcal{A} = -0.21 \pm 0.28 \text{ (stat)} \pm 0.06 \text{ (syst)}$  are obtained.

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# Chapter 1

## Introduction

### 1.1 The Standard Model

The Standard Model (SM) was built in the late 70th of 20th century to describe the matter compositions and interactions using a group of fundamental particles - fermions and bosons. In the Standard Model, there are three generations of quarks and leptons, along with their anti-particles, which are all fermions. On the other hand, the bosons in the Standard Model consist of gluons, photons,  $W^\pm$  and  $Z^0$  bosons that are all gauge bosons and one Higgs boson that is a scalar boson. This group of particles are summarized in Figure 1-1. The Standard Model depicts the interactions between elementary particles as the exchange of the bosons. The strong interaction requires the exchange of gluons. Photons,  $W^\pm$  and  $Z^0$  bosons carry the electromagnetic force and weak force, which are unified as electroweak interaction in the Standard Model. Higgs boson is responsible for the generation of masses for the gauge bosons through electroweak symmetry breaking[1]. The Standard Model has been proved to be an excellent theoretical model that can be used to explain many experimental observations, but sadly not all of them. For instance, neutrino mass is expected to be zero in the Standard Model but the flavor oscillation indicates non-zero mass of neutrinos. The observation of Charge-Parity ( $CP$ ) asymmetry in universe presented by the absence of antimatter can not be fully explained by the  $CP$  violation sources within the Standard Model. These experimental observations

require further researches beyond the Standard Model, which is called New Physics (NP) studies.

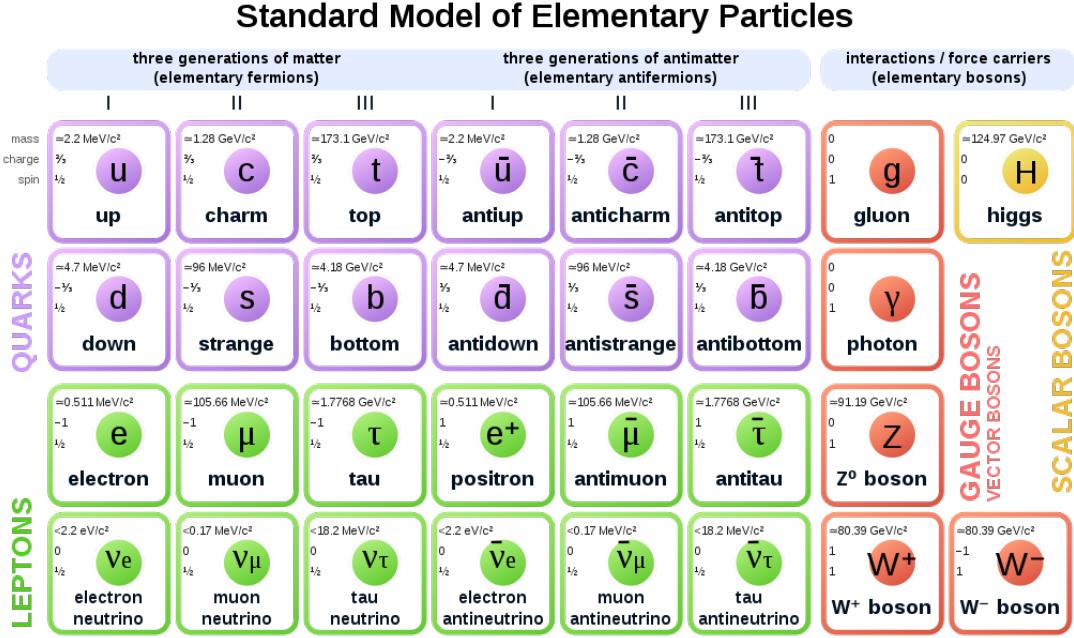


Figure 1-1: Elementary particles in the Standard Model.[2]

## 1.2 Symmetry Violation

Symmetry violation has been one of the focuses in NP studies due to the internal link between symmetries and conservation laws, which makes it a good probe for possible NP theories beyond the SM. When a known symmetry is found to be broken, it usually leads to the discovery of a new theory.

There are three types of discrete symmetric operations which play important roles in particle physics. Charge-conjugation  $C$  is the operation that turns particle to its anti-particle. Parity transformation  $P$  is the one that puts a negative sign before all the spatial related vector such as  $\vec{r} \rightarrow -\vec{r}$ . The time-reversing operation  $T$  is to reversely proceed a physical process backward time. Physicists were convinced that each of these three symmetric operations makes no change to any physics system. However, in 1950s, Lee and Yang [3] first questioned that parity symmetry might be

broken in weak interactions. They offered a few possible ways to test it and then by Wu [4], an observation on the  $\beta$  decay of  $^{60}\text{Co}$  was presented that the electrons emitted from  $^{60}\text{Co}$  decay prefers the direction of nuclear spin that can be controlled by the external magnetic field. The violation of  $P$  symmetry was discovered by this clear evidence.

The first evidence of  $CP$  violation was discovered in neutral  $K^0$  system by Cronin and Fitch's experiment[5]. The neutral  $K^0$  mesons can be observed as two states that have significantly different lifetime (called as " $K_S^0$ " and " $K_L^0$ " for short and long lifetime particles) with opposite  $CP$  eigenvalue. The experiment measured the decay products at 57 foot of a neutral  $K^0$  beamline assuming all the particle at the end of the beam should be long lifetime  $K_L^0$ , nearly no  $K_S^0$ . But 0.002% of  $K_L^0$  were found to decay into  $\pi^+\pi^-$  which is the main decay process of  $K_S^0$ . ( $CP$  eigenvalue = 1 in  $\pi^+\pi^-$  final states, while  $K_L$  has  $CP$  eigenvalue = -1). Given that the expected distance to have 0.002% of  $K_S^0$  at about speed of light is no more than 1 meter in the beamline, such a deviation at 57 foot is an obvious evidence that  $K_L^0 \rightarrow \pi^+\pi^-$  exists and therefore  $CP$  symmetry is violated in the neutral  $K^0$  system.

In 1973, Kobayashi and Maskawa introduced a quark mixing matrix called CKM matrix for three or more generations of quarks before the discovery of the third generation of the quark family[6]. The theory naturally explained an irreducible complex phase in CKM matrix and it accounts for the origin of  $CP$  asymmetries of weak interactions in the Standard Model. The experimental evidence of  $CP$  violation in  $B$  meson system was observed in 2001 by Belle and BaBar experiments[7][8]. They measured the time-dependent decay time difference of  $B$  and  $\bar{B}$  in the decay of  $B \rightarrow J/\psi K_S^0$ . This channel provided a good clearness in theoretical prediction and has relatively large branching fraction, thus it's called the "golden mode"[9]. In 2008, Kobayashi and Maskawa were rewarded the Nobel Prize to highly value their contribution to  $CP$  violation mechanism in the SM, to which Belle experiment contributes greatly. Later in 2010, the upgrade of Belle, Belle II and the upgrade of KEK accelerator, SuperKEKB, were approved to further push the understanding of  $CP$  violation along with other topics in New Physics researches.

### 1.3 CKM mechanism

$$\Phi = \begin{pmatrix} \phi^+ \\ \nu + \frac{H+i\chi}{\sqrt{2}} \end{pmatrix} \quad (1.1)$$

Equation 1.1 is the Higgs potential doublets in the SM, where the value of  $H$  is 174 GeV as the expected Higgs potential for vacuum[10]. The  $\phi$  and  $\chi$  are the psuedo-Goldstone fields which are appearing when introducing Higgs field  $\phi$  without breaking the gauge symmetry. The Lagrangian for Yukawa interaction of the quark fields[11] can be presented by Equation 1.2.

$$\mathcal{L}_{Yuk}^q = -Q^\dagger Y^d \Phi d'_R - Q^\dagger Y^u \epsilon \Phi^* u'_R + h.c. \quad (1.2)$$

where the primed fields stand for the weak eigenstates of quarks. The  $\epsilon$  is a  $2 \times 2$  matrix and  $Q^\dagger$  is the left-handed doublets that stand for weak eigenstates of up and down types quarks, see Equation 1.3 and 1.4.

$$\epsilon = \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix} \quad (1.3)$$

$$Q = \begin{pmatrix} u' & d' \\ c' & s' \\ t' & b' \end{pmatrix}_L \quad (1.4)$$

Yukawa matrix is an arbitrary  $3 \times 3$  complex matrix  $Y^{u,d}$  which gives the rise of up and down type massive quark field  $M^{u,d} = Y^{u,d} \nu$  according to Equation 1.2. The representation of the quark fields using weak eigenstates can be transformed to mass eigenstates by Equation 1.5 and 1.6.

$$S_{L,R}^u \begin{pmatrix} u' \\ c' \\ t' \end{pmatrix}_{L,R} = \begin{pmatrix} u \\ c \\ t \end{pmatrix}_{L,R} \quad (1.5)$$

$$S_{L,R}^d \begin{pmatrix} d' \\ s' \\ b' \end{pmatrix}_{L,R} = \begin{pmatrix} d \\ s \\ b \end{pmatrix}_{L,R} \quad (1.6)$$

In Equation 1.5 and 1.6,  $S_{L,R}^{u,d}$  are all unitary matrices since they are generated by the normalized eigenstate states of Yukawa matrix. The mass item in the Lagrangian can be presented as Equation 1.7

$$\mathcal{L}_m = - \sum_{q=u,c,t,d,s,b} M_q q^\dagger q \quad (1.7)$$

where the  $q = (q_L + q_R)$  is four-component Dirac field, and  $q_L^\dagger q_L = q_R^\dagger q_R = 0$ . As a result of diagonalizing  $Y^{u,d}$ , the charged current  $W^\pm$  interactions couple to the physical quarks and the Lagrangian is written as Equation 1.8, where  $V_{CKM} \equiv S_L^u S_L^{d\dagger}$ .

$$\mathcal{L}_W^q = \frac{g}{\sqrt{2}} \left[ \begin{pmatrix} \bar{u} & \bar{c} & \bar{t} \end{pmatrix}_L \gamma^\mu W_\mu^+ V_{CKM} \begin{pmatrix} d \\ s \\ b \end{pmatrix}_L + \begin{pmatrix} \bar{d} & \bar{s} & \bar{b} \end{pmatrix}_L \gamma^\mu W_\mu^- V_{CKM}^\dagger \begin{pmatrix} u \\ c \\ t \end{pmatrix}_L \right] \quad (1.8)$$

The Lagrangian hereby clearly declares the transition of different charged quarks through the coupling of charged current  $W^\pm$ , where such a coupling only applies for the left-handed quarks. For example, a left-handed charm quark only transits to left-handed strange quark by a  $W$  boson. By only applying  $C$  or  $P$  conjugation, the Lagrangian is not invariant, indicating the non-conservation of  $C$  or  $P$  individually. However, if the  $CP$  conjugation is applied, the Equation 1.8 transits as Equation 1.9 shows.

$$\begin{pmatrix} \bar{u} & \bar{c} & \bar{t} \end{pmatrix}_L \gamma^\mu W_\mu^+ V_{CKM} \begin{pmatrix} d \\ s \\ b \end{pmatrix}_L \Leftrightarrow \begin{pmatrix} u & c & t \end{pmatrix}_L \gamma^\mu W_\mu^- V_{CKM} \begin{pmatrix} \bar{d} \\ \bar{s} \\ \bar{b} \end{pmatrix}_L \quad (1.9)$$

Comparing Equation 1.9 and 1.8, the  $CP$  symmetry requires the invariance before and after  $CP$  conjugation, meaning that Equation 1.10 is expected.

$$u_L^i V_{ij} \bar{d}_L^j \gamma^\mu W_\mu^- = u_L^n V_{nm}^* \bar{d}_L^m \gamma^\mu W_\mu^- \quad (1.10)$$

The same indices  $ij$  and  $nm$  are summed over on both side. This is equivalent to Equation 1.11:

$$V_{ij} = V_{ij}^* \quad (1.11)$$

On the one hand, if the CKM matrix is real,  $CP$  will be conserved in the weak interaction in the SM due to the natural hold of Equation 1.11. On the other hand, from Equation 1.10, it's still possible to make Lagrangian invariant even if  $V_{CKM}$  is not real, which can be achieved by introducing non-physical phases for each quark field  $u_L^k e^{(i\phi_{uk})}$  and  $d_L^j e^{(i\phi_{dj})}$ , the Equation 1.11 becomes Equation 1.12.

$$V_{kj} e^{i(\phi_{dj} - \phi_{uk})} = V_{kj}^* e^{i(\phi_{uk} - \phi_{dj})} \quad (1.12)$$

Assuming the complex phase of the  $kj$ -th element in CKM matrix is  $\theta_{kj}$ , it's obviously required Equation 1.13 to hold.

$$\theta_{kj} = \phi_{uk} - \phi_{dj} \quad (1.13)$$

If the number of generations in quark family is 3 or more, the non-physical phases can not render proper values to ensure the hold of Equation 1.13, and there will always be one irreducible complex phase parameter in the CKM matrix in the existence of three generations of quarks, which means  $CP$  symmetry is no longer conserved in the weak interactions.

The  $3 \times 3$  unitary CKM matrix can be written as Equation 1.14 based on the

quark fields it connects using Equation 1.5 and 1.6.

$$V_{CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \quad (1.14)$$

It can be parameterized into the form of Equation 1.15.

$$V_{CKM} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{-i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{-i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}s_{23}s_{13}e^{-i\delta} & -c_{12}c_{23} - s_{12}s_{23}s_{13}e^{-i\delta} & c_{23}c_{13} \end{pmatrix} \quad (1.15)$$

where the  $c_{jk} = \cos(\theta_{jk})$  and  $s_{jk} = \sin(\theta_{jk})$ , and  $\delta$  is the irreducible complex phase. By measuring the relative branching ratio of  $b \rightarrow c$ ,  $s \rightarrow u$  and  $b \rightarrow u$  in tree level transitions as shown in Equation 1.16.

$$|V_{ub}| \ll |V_{cb}| \ll |V_{us}| \quad (1.16)$$

The relations in Equation 1.17 are often used to simplify CKM matrix presentation.

$$s_{13} = \lambda, s_{23} = A\lambda^2, s_{13}e^{i\delta} = A\lambda^3(\rho - i\eta) \quad (1.17)$$

By using Equation 1.17, CKM matrix is parameterized as Equation 1.18.

$$V_{CKM} = \begin{pmatrix} 1 - 1/2\lambda^2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - 1/2\lambda^2 & A\lambda^2 \\ A\lambda^3(\rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4) \quad (1.18)$$

Using the unitary condition, the Equation 1.19 is obtained.

$$1 + \frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} + \frac{V_{td}V_{tb}^*}{V_{cd}V_{cb}^*} = 0 \quad (1.19)$$

Using Equation 1.19, 1.20 and 1.21, the shape of CKM triangle can be defined on the

complex plane in Figure 1-2.

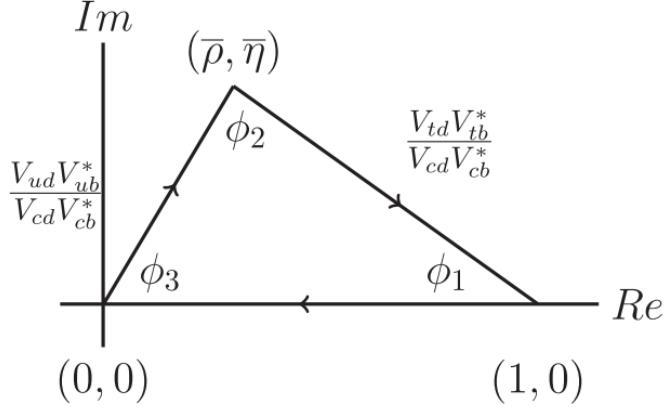


Figure 1-2: The unitary triangles of CKM[12].

$$\bar{\rho} + i\bar{\eta} = -\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} \quad (1.20)$$

$$1 - (\bar{\rho} + i\bar{\eta}) = -\frac{V_{td}V_{tb}^*}{V_{cd}V_{cb}^*} \quad (1.21)$$

These angles are obtained by drawing the  $(\bar{\rho}, \bar{\eta})$  on the complex coordinates, and they are also well-known in the names as:  $\phi_1 = \beta, \phi_2 = \alpha, \phi_3 = \gamma$ . The results presenting the measurement of CKM angles or  $(\bar{\rho}, \bar{\eta})$  in 2019 are shown in Figure 1-3.

The measurement of  $\phi_1$  and  $\phi_2$  are mainly obtained from the time-dependent  $CP$  violations (TDCPV) measurement. The  $\phi_1$  in the tree-level dominated decays has been precisely measured due to the small hadronic uncertainties. Flavor-Changing-Neutral-Current (FCNC) processes can rise through the  $B_d^0 - \bar{B}_d^0$  mixing in box diagram, and it's believed that potential NP processes might contribute to the difference in between results of CKM angles measured from experiments, such as  $\phi_1$  value in tree-dominated processes and penguin-dominated processes, where both involve  $b \rightarrow s$  transition. It requires the precise measurements on multiple decay channels to search for the potential NP effects. The prospective large Belle II data and improved detector performance will be much useful to help the discovery of NP in future.

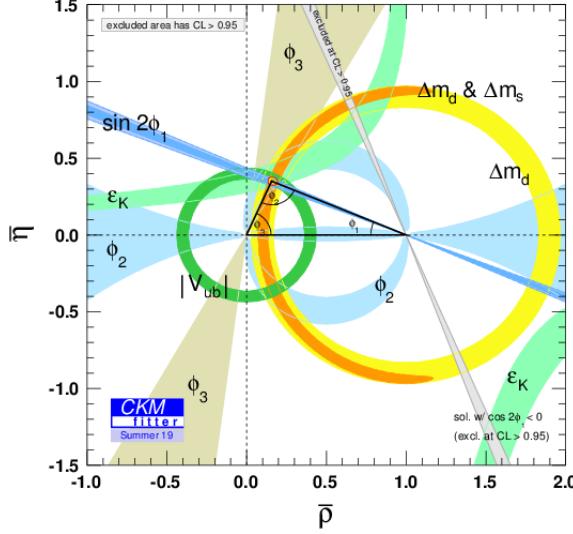


Figure 1-3: The CKM triangle fit in the complex plane of  $\bar{\rho} - \bar{\eta}$ .[12]

## 1.4 Time Dependent $CP$ violation

### 1.4.1 $CP$ violation in neutral $B$ system

The  $\phi_1$ ,  $\phi_2$  and  $\phi_3$  are essentially measuring the CKM  $CP$  violating phase since there's only one complex phase in the CKM matrix and it can be determined by these three angles. For determining the value of  $\phi_1$ , TDCPV measurements provide a good experimental environment. From Figure 1-2, one can obtain  $\phi_1$  and  $\phi_2$  by Equation 1.22 and 1.23.

$$\phi_1 = \text{Arg}\left(-\frac{V_{td}V_{tb}^*}{V_{cd}V_{cb}^*}\right) \quad (1.22)$$

$$\phi_2 = \text{Arg}\left(-\frac{V_{td}V_{tb}^*}{V_{ud}V_{ub}^*}\right) \quad (1.23)$$

The time-dependent  $CP$  violation comes from the interference of neutral  $B$  mixing phase and the weak phase in the decay amplitude. The mass eigenstates which are driving the propagation of neutral  $B$  meson states with mixing are:  $|B\rangle_{H,L} = p|B\rangle \pm q|\bar{B}\rangle$ , where  $H$  and  $L$  stand for the heavier and lighter mass eigenvalues. The  $|B\rangle$  and  $|\bar{B}\rangle$  present the flavor eigenstates of neutral  $B$  mesons. The Hamiltonian

matrix can be written using flavor eigenstates as shown in Equation 1.24.

$$M_\Gamma = \begin{bmatrix} m - i/2\Gamma & M_{12} - i/2\Gamma_{12} \\ M_{12}^* - i/2\Gamma_{12}^* & m - i/2\Gamma \end{bmatrix} \quad (1.24)$$

Considering the time evolution of mass eigenstates, the time-dependent states can be shown as Equation 1.25 and 1.26 by using the notation of  $B_{H,L}$  as physical states at  $t = 0$ .

$$B_H(t) = e^{-im_H t} e^{-\Gamma_H t/2} B_H \quad (1.25)$$

$$B_L(t) = e^{-im_L t} e^{-\Gamma_L t/2} B_L \quad (1.26)$$

where  $M_{H,L}$  and  $\Gamma_{H,L}$  are the masses and decay widths of two mass eigenstates. By expanding the mass eigenstates using flavor eigenstates, which are shown in Equation 1.27 and 1.28.

$$B(t) = (1/2p)e^{-im_H t} e^{-\Gamma_H t/2}(pB + q\bar{B}) + (1/2p)e^{-im_L t} e^{-\Gamma_L t/2}(pB - q\bar{B}) \quad (1.27)$$

$$\bar{B}(t) = (1/2q)e^{-im_H t} e^{-\Gamma_H t/2}(pB + q\bar{B}) - (1/2q)e^{-im_L t} e^{-\Gamma_L t/2}(pB - q\bar{B}) \quad (1.28)$$

Replacing  $g_\pm(t) = \frac{1}{2}(e^{-im_H t - \Gamma_H/2t} \pm e^{-im_L t - \Gamma_L/2t})$ , Equation 1.27 and 1.28 become Equation 1.29 and 1.30.

$$B(t) = g_+(t)B + \frac{q}{p}g_-(t)\bar{B} \quad (1.29)$$

$$\bar{B}(t) = g_+(t)\bar{B} + \frac{p}{q}g_-(t)B \quad (1.30)$$

Considering all the phase-spaces of the decay from flavor eigenstates to final states  $f(\bar{f})$  are included in the amplitudes  $\mathcal{A}_f(\bar{\mathcal{A}}_{\bar{f}})$ , one needs to expand the flavor eigenstates using the final states amplitudes to have the differential decay rate  $\Gamma(B \rightarrow f, t)$ . From  $B(t) \propto \mathcal{A}_f \psi_f + h.c$  and  $(\bar{B}(t) \propto \bar{\mathcal{A}}_{\bar{f}} \psi_{\bar{f}} + h.c)$ , combined with Equation 1.29 and

1.30, the decay rate can be shown in Equation 1.31 and 1.32.

$$\Gamma(B \rightarrow f, t) = |\mathcal{A}_f|(|g_+(t)|^2 + |\lambda_f|^2 |g_-(t)|^2 + 2\text{Re}(\lambda_f g_+^*(t) g_-(t))) \quad (1.31)$$

$$\Gamma(\bar{B} \rightarrow \bar{f}, t) = |\bar{\mathcal{A}}_f|(|g_+(t)|^2 + |\bar{\lambda}_{\bar{f}}|^2 |g_-(t)|^2 + 2\text{Re}(\bar{\lambda}_{\bar{f}} g_+^*(t) g_-(t))) \quad (1.32)$$

where the parameter  $\lambda_f$  and  $\bar{\lambda}_{\bar{f}}$  can be defined as Equation 1.33 and 1.34.

$$\lambda_f \equiv (q/p)(\bar{\mathcal{A}}_f / \mathcal{A}_f) \quad (1.33)$$

$$\bar{\lambda}_{\bar{f}} \equiv (q/p)(\mathcal{A}_{\bar{f}} / \bar{\mathcal{A}}_{\bar{f}}) \quad (1.34)$$

The  $q/p$  is introduced by the coefficient of mass eigenstates from weak eigenstates. Using the Hamiltonian matrix,  $q/p$  can be presented using Equation 1.35

$$q/p = \frac{\Delta M - i/2\Delta\Gamma}{2(M_{12} - i/2\Gamma_{12})} \quad (1.35)$$

where the  $M_{12}$  and  $\Gamma_{12}$  stands for the contribution of non-diagnosed term in the Hamiltonian matirx.  $\Delta M = M_H - M_L$  and  $\Delta\Gamma = \Gamma_H - \Gamma_L$  are the difference of mass and decay width for two mass eigenstates, respectively. It's obvious that if  $|\mathcal{A}_f| \neq |\bar{\mathcal{A}}_{\bar{f}}|$ , direct  $CP$  violation will occur. The time-dependent decay rate difference is defined as Equation 1.36.

$$\begin{aligned} A_{CP}(t) &\equiv \frac{\Gamma(B \rightarrow f, t) - \Gamma(\bar{B} \rightarrow \bar{f}, t)}{\Gamma(B \rightarrow f, t) + \Gamma(\bar{B} \rightarrow \bar{f}, t)} \\ &= \frac{\mathcal{S}\sin(\Delta Mt) - \mathcal{A}\cos(\Delta Mt)}{\cosh(\Delta\Gamma t/2) + A_{\Delta\Gamma}^f \sinh(\Delta\Gamma t/2)} \end{aligned} \quad (1.36)$$

where

$$\mathcal{S} = \frac{2\text{Im}(\lambda_f)}{1 + |\lambda_f|^2} \quad (1.37)$$

$$\mathcal{A} = \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2} \quad (1.38)$$

$$A_{\Delta\Gamma}^f = -\frac{2\text{Re}(\lambda_f)}{1 + |\lambda_f|^2} \quad (1.39)$$

From Equation 1.37 and 1.38, the time-dependent CP violation parameters  $\mathcal{S}$  and  $\mathcal{A}$  are dependent on the parameter  $\lambda_f$ .

### 1.4.2 $\phi_1$ from $B^0 \rightarrow J/\psi K_S^0$

If final states are  $CP$  eigenstates, the amplitudes are obtained by  $\mathcal{A}_f \equiv \langle f | H | B \rangle$  and  $\bar{\mathcal{A}}_f \equiv \langle f | H | \bar{B} \rangle$ . In  $B_d^0 - \bar{B}_d^0$  mixing system, the  $q/p$  can be treated as  $e^{i\phi_d}$  as a pure phase term. This relative phase accounts the transition from  $b$  to up-type quarks to strange quark  $s$  in mixing, so it can be presented as  $\phi_d = \text{Arg}(V_{td}^* V_{tb}) / (V_{tb}^* V_{td}) \approx 2\phi_1$  based on negligible correction to the SM. In mode  $B^0 \rightarrow J/\psi K_S^0$ , considering  $\Delta\Gamma$  can be treated as zero in the SM in this case[13], Equation 1.36 can be reduced to Equation 1.40.

$$A_{CP}(t) = \mathcal{S}\sin(\Delta M t) - \mathcal{A}\cos(\Delta M t) \quad (1.40)$$

which receives contributions from tree-level and loop-level processes shown in Figure 1-4 ,

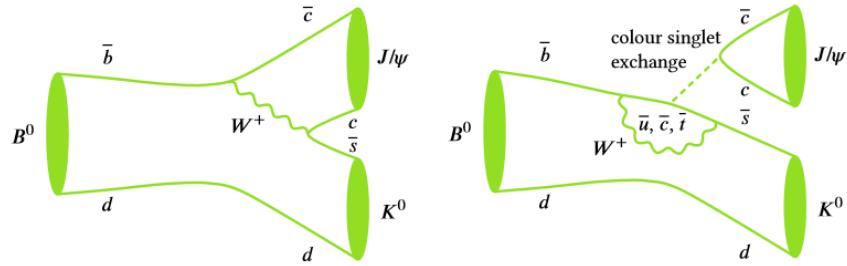


Figure 1-4: The dominated tree-level (left) and the suppressed loop-level (right) of  $B \rightarrow J/\psi K^0$ , in which  $K^0$  particles are detected  $K_S^0$ [14].

Using the relation  $|V_{ub}| \ll |V_{cb}| \ll |V_{us}| < |V_{cs}|$ , it's obvious that  $V_{ub}^* V_{us} \ll V_{cb}^* V_{cs}$ , so the penguin-mode is suppressed in the Standard Model. The  $\eta_f$  is defined as the  $CP$  eigenvalue. Given  $\eta_f = 1$  and  $|\lambda_f| = 1$  in  $B^0 \rightarrow J/\psi K_S^0$ , from 1.37,  $CP$  violation parameters can be presented as shown in Equation 1.41.

$$\mathcal{S} = \text{Im}(\lambda_f) = -\sin(\phi_d)\eta_f = \sin(2\phi_1); \mathcal{A} = 0 \quad (1.41)$$

From Equation 1.41 ,  $\phi_1$  can be obtained precisely in the measurement of time-dependent  $CP$  violation in  $B^0 \rightarrow J/\psi K_S^0$ .

### 1.4.3 $\phi_1$ from penguin-dominated mode $b \rightarrow q\bar{q}s$

Compared to  $B^0 \rightarrow J/\psi K_S^0$  channel, the measurement of  $\mathcal{S}$  and  $\mathcal{A}$  from penguin-dominated channels through  $b \rightarrow q\bar{q}s$  where  $q$  is  $u, d, s$  can be different due to the varied tree-to-penguin amplitude ratio. Furthermore, they are quite sensitive to NP effects for the following reasons[15]. First, they can probe  $B^0 - \bar{B}^0$  mixing through different short-distance vertices compared to the tree-level dominated decays. Second, the tree-level decay amplitude is suppressed and penguin-level amplitude is dominated, while the overall non-NP amplitude is relatively small so NP effects may show up easier. Last but not least, they comprise a large number of different final states, which can help disentangling non-perturbation long-distance physics from short-distance information, such as  $\phi_1$  or NP contributions to the weak Hamiltonian.

Considering possible New Physics contribution besides the tree-level and penguin-level processes as  $A_f^{NP}$ , the decay amplitude can be rendered as Equation 1.42

$$\mathcal{A}_f = \lambda_u^s T_f + \lambda_c^s P_f + A_f^{NP} \quad (1.42)$$

where  $T_f$  and  $P_f$  are tree-level and penguin-level amplitudes. The coefficients  $\lambda_u^s$  and  $\lambda_c^s$  are determined from CKM matrix elements by  $\lambda_i^q \equiv V_{ib}^* V_{iq}$ . Note that compared to the  $B^0 \rightarrow J/\psi K_S^0$ , the tree level amplitude  $T_f$  is suppressed and penguin amplitude  $P_f$  is dominated in  $b \rightarrow q\bar{q}s$ . It is also worth noting that  $T_f$  contains tree-level  $W^\pm$  exchange, QCD and electroweak penguin contributions. These carry the combination of CKM matrix elements  $\lambda_t^s = V_{ts} V_{tb}^* = -(1 + \epsilon_{uc}) \lambda_c^s$  where  $\epsilon_{uc} \equiv \lambda_u^s / \lambda_c^s = \mathcal{O}(\lambda^2)$ . In the SM with neglected  $\epsilon$ ,  $b \rightarrow q\bar{q}s$  modes are pure penguin with the same weak phase as  $B^0 \rightarrow J/\psi K_S^0$  has. Thus, direct  $CP$  violation vanishes and time-dependent  $CP$  violation reflects  $\mathcal{S}$  in the same way as  $B^0 \rightarrow J/\psi K_S^0$  does.

Departures from this limit, non-neglected tree amplitude  $T_f$  (often called “tree pollution”), as well as possible NP effects, could give different results on  $\phi_1$ . The  $\phi_1$

differences can be reflected by the  $\mathcal{S}$  difference, hence  $\Delta S$  is defined as Equation 1.43.

$$\Delta S = \mathcal{S}_f - \mathcal{S}_{J/\psi K_s^0} \quad (1.43)$$

Introducing the tree-penguin ratio  $r_f^T = T_f/P_f$ , NP-to-SM ratio  $r_f^{NP} = \mathcal{A}_f^{NP}/(\lambda_c^s P_f)$ , the following statements are usually used[15]:

- Branching ratios are affected at  $\mathcal{O}(|\epsilon_{uc} r_f^T|, |r_f^{NP}|)$
- Direct CP violation in the SM are of  $\mathcal{O}(\epsilon_{uc} \text{Im}(r_f^T))$
- $-n_f^{CP} \mathcal{S} = \sin(2\phi_1) + \Delta S$ , where  $\Delta S = 2\cos 2\phi_1 \sin \phi_3 |\epsilon_{uc}| \text{Re}(r_f^t) + \Delta S^{NP}$ . This suggests that non-zero  $\Delta S$  without the NP effect is still allowed in a small scale within the SM. Therefore, in the precised measurement using the future Belle II data, it's important to understand  $\Delta S$  within the SM correction to properly explain the experiment results. The  $\Delta S$  should be larger than the SM allowed value by  $5\sigma$  to be called as the evidence of the NP, where  $\sigma$  is the total uncertainty of  $\Delta S$ .

#### 1.4.4 $\phi_1$ from $B^0 \rightarrow K_S^0 K_S^0 K_S^0$

Since the Belle experiment reported the time-dependent  $CP$  analysis on various  $b \rightarrow q\bar{q}s$  which experimentally showed that the difference on  $\phi_1$  has a margin for NP effects[16], the improved measurements with a larger data collection is popularly discussed in order to reduce the impact of uncertainties and clear the tension between results. The decay channel  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  is one of the most promising modes for this purpose. The  $CP$  eigenvalue of  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  is positive ( $CP$  eigenvalue = +1). There's no up-quark shown in the final states, the potential contribution of  $b \rightarrow u\bar{u}s$  re-scattered into  $b \rightarrow s\bar{s}s$  is almost of absence, which makes  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  a much cleaner channel compared to  $B^0 \rightarrow K^+ K^- K_S^0$ [17]. In all final states with three  $K_S^0$  from a neutral  $B$  decay, the phase-space based decay process and the resonant decay process such as  $B^0 \rightarrow f_0(980) K_S^0 (f_0(980) \rightarrow K_S^0 K_S^0)$  are shown in the left and middle of Figure 1-5, which all yield  $CP$ -even states treated as signal events. In the meanwhile,  $b \rightarrow c \rightarrow s$  can also produce the final states with three  $K_S^0$  through a tree-level process like  $B^0 \rightarrow \chi_{c0} K_S^0 (\chi_{c0} \rightarrow K_S^0 K_S^0)$  with a different weak phase

and  $CP$ -odd states, as shown in the right of Figure 1-5. Such a tree-level process is treated as background and can be rejected by applying veto on two  $K_S^0$  invariant mass within  $\chi_{c0}$  mass window, which is considered as a minor background at the current luminosity. Due to the same weak phase in the decay amplitudes, any potential NP effects expected in the  $B^0 \rightarrow \phi K_S^0$  and  $B^0 \rightarrow \eta' K_S^0$  should also affect  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  and the absence of NP effects will lead the close  $CP$  violation as  $J/\psi K_S^0$ [17]. To be noted, as discussed in the previous section that the SM correction due to the different tree-penguin ratio,  $B^0 \rightarrow \eta' K_S^0$ ,  $B^0 \rightarrow \phi K_S^0$  and  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  modes could create non-zero  $\Delta\mathcal{S}$  in a slightly different level. There were attempted theoretical calculation based on the QCD model for the  $\Delta\mathcal{S}$  in these modes. For  $B^0 \rightarrow \eta' K_S^0$  and  $B^0 \rightarrow \phi K_S^0$ , the details about such a calculation on  $\Delta\mathcal{S}$  within the SM can be find in Ref.~[18]. As for  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$ , the calculation of  $\Delta\mathcal{S}$  within the SM can be find in Ref.~[19]. In general, the expected SM-allowed  $\Delta\mathcal{S}$  from QCD model suggests the upper limit at  $\sim 0.05$  for  $B^0 \rightarrow \phi K_S^0$ ,  $0.03$  for  $B^0 \rightarrow \eta' K_S^0$ , and  $0.06$  for  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$ . For  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$ , the theoretical uncertainty is expected to be small compared with the experimental uncertainties. Thus, in the comparison of SM-allowed  $\Delta S$  and the experimental results, we current only focus on the statistical and systematic uncertainties from the experiment and ignore the QCD model uncertainty. The theoretical calculation suggests the positive sign of  $\Delta\mathcal{S}_{3K_S^0}$ . We take  $\Delta\mathcal{S} \sim 0.05$  as the SM-allowed upper limit predicted by the QCD model.

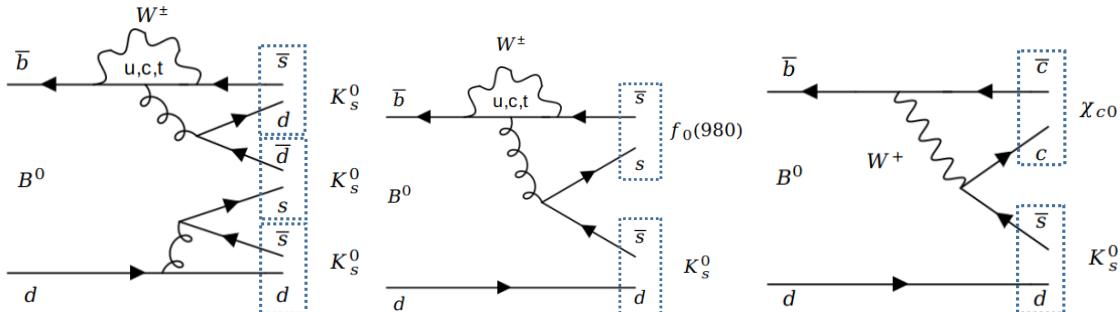


Figure 1-5

The current result of  $B^0 \rightarrow J/\psi K_S^0$  using the full Belle data is presented as  $\mathcal{S}_{J/\psi K_S^0} = +0.670 \pm 0.029(\text{stat}) \pm 0.013(\text{syst})$ [15]. In the meantime, the latest result

from  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  using the full Belle data[20] is presented as:  $\mathcal{S}_{3K_S^0} = -0.71 \pm 0.23(\text{stat}) \pm 0.05(\text{syst})$ , and the result from BaBar [21] is:  $\mathcal{S}_{3K_S^0} = -0.94^{+0.21}_{-0.24}(\text{stat}) \pm 0.06(\text{syst})$ . Both results have shown a small deviation from the result in  $B^0 \rightarrow J/\psi K_S^0$  while the statistical uncertainties are much dominated which prevents the claim about whether NP effects are existed. For  $\Delta\mathcal{S}$  from  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$ , the experimental sensitivity of  $\Delta\mathcal{S}$  will be dominated by  $\mathcal{S}_{3K_S^0}$  uncertainty because the total uncertainty from  $J/\psi K_S^0$  will be reduced to  $\sim 0.005$  at  $50\text{ab}^{-1}$  Belle II data[15], which is negligible. The Figure 1-6 shows the expected  $\Delta\mathcal{S}$  uncertainty from the Belle II technical design report with respect to the luminosity in future Belle II[22], which requires that the Belle II results should be prepared for  $\Delta\mathcal{S} < 0.2$  caused by the NP effects. The curves are extrapolated based on the Belle results from  $492\text{ fb}^{-1}$  data and take into account the reducible systematic and statistical uncertainties[23]. The Table 1.1 shows the corresponding total uncertainties of  $\Delta\mathcal{S}$  in Figure 1-6 at  $0.5\text{ ab}^{-1}$ ,  $5\text{ ab}^{-1}$  and  $50\text{ ab}^{-1}$  luminosity. For  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  at  $50\text{ ab}^{-1}$ , if  $\Delta\mathcal{S}_{3K_S^0} \sim 0.25$ , the total uncertainty should be less than  $0.04$  to claim a  $5\sigma$  deviation from the SM upper limit  $0.05$  for the appearance of the NP effects, which is close to the expected total uncertainty in Table 1.1.

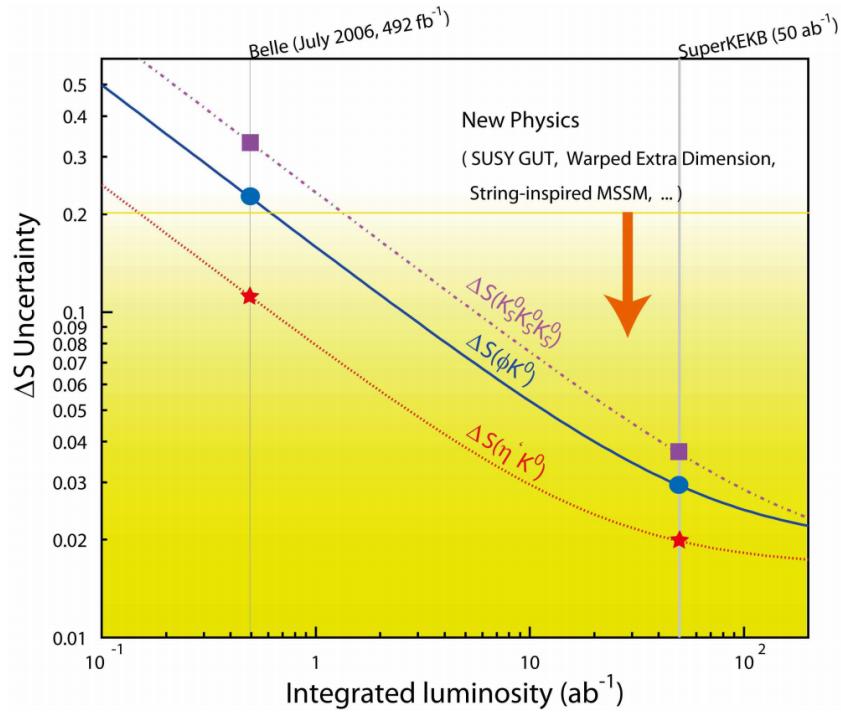


Figure 1-6: Expected sensitivity of  $\Delta\mathcal{S}$  with respect to the integrated luminosity of the Belle II future data from the Belle II technical design report[22].

Table 1.1:  $\Delta\mathcal{S}$  estimated total uncertainties with respect to the integral luminosities in the Belle II technical design report[22]. Three decay modes receive the same potential NP effects due to the same weak phases involved in the decay processes[17].

Observable	Belle (0.5 ab <sup>-1</sup> )	Belle II (5 ab <sup>-1</sup> )	Belle II (50 ab <sup>-1</sup> )
$\Delta\mathcal{S}_{\phi K_S^0}$	0.22	0.073	0.029
$\Delta\mathcal{S}_{\eta' K_S^0}$	0.11	0.038	0.020
$\Delta\mathcal{S}_{K_S^0 K_S^0 K_S^0}$	0.33	0.105	0.037



# Chapter 2

## Belle II experiment

### 2.1 Belle II and SuperKEKB overview

The goal of the Belle II experiment is to search for evidence of New Physics, and the expected operation period is from 2019 to the end of 2030. The facilities are located in KEK, Tsukuba City, around 70 km in the north of Tokyo, Japan. The SuperKEKB accelerator enables electron-positron collision at the center-of-mass energy on the region of  $\Upsilon(4S)$  resonances which is just above the mass of two  $B$  mesons. The electron and positron beams are designed at 7 GeV and 4 GeV, respectively, with boost factor of 0.28, providing an environment for measuring time-dependent  $CP$  violation by displacing the decay vertices of a  $B$  meson pair in a measurable distance along the boosted direction. The SuperKEKB has a targeted luminosity of  $8 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$ , a factor of 40 times higher than its predecessor, the KEKB. Some key parameters of the SuperKEKB are listed in Table 2.1. The schematic view of SuperKEKB and Belle II are shown in Figure 2-1.

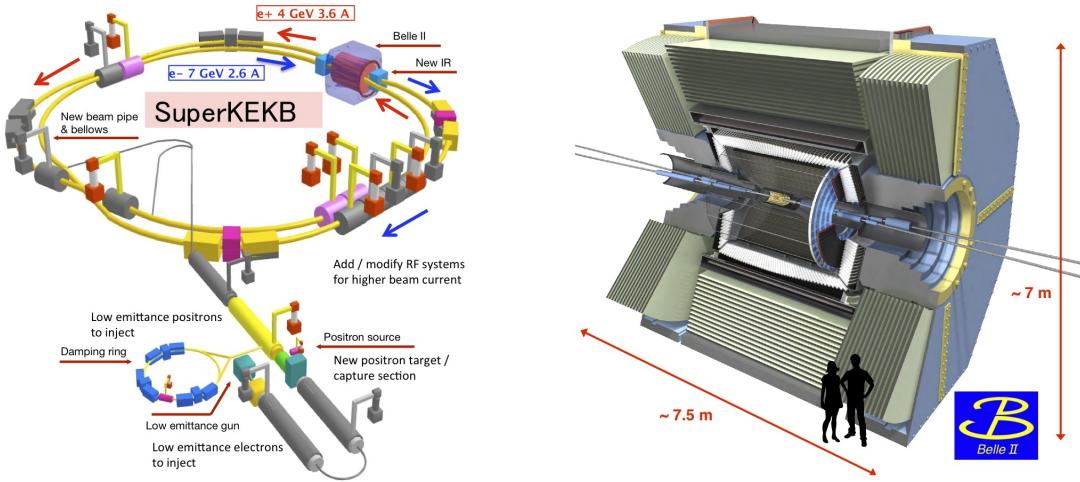


Figure 2-1: The schematic view of SuperKEKB and Belle II detector [22].

Table 2.1: SuperKEKB parameters for low energy (LER) and high energy (HER) rings [15].

Parameters	LER ( $e^+$ )	HER ( $e^-$ )	Unit
Energy	4.0	7.0	GeV
Half crossing angle		41.5	mrad
Horizontal emittance	3.2	4.6	nm
Emittance ratio	0.27	0.25	%
Beta functions at IP ( $x/y$ )	32/0.27	25/0.30	mm
Beam currents	3.6	2.6	A
Beam-beam parameter	0.0881	0.0807	
Luminosity		$8 \times 10^{35}$	$\text{cm}^{-2}\text{s}^{-1}$
Perimeter of ring		3	km

The Belle II detector has a close size as the Belle detector so that it is placed in the same shell, but all sub-detectors and electronic systems have been either newly built or considerably upgraded. The advantage of the SuperKEKB requires that the

Belle II has to be able to stably operate at a 40 times higher event rates as well as 10 to 20 times higher beam background compared to Belle. The mitigation of the effects caused by such high beam background is essential to the success of the Belle II. Higher background level leads to higher occupancy and radiation damage to the detectors, along with more fake hits in the vertex detectors and central drift chamber, pile-up backgrounds in electromagnetic calorimeter and neutron-induced hits in muon detector. Data-acquisition system (DAQ) and trigger are also upgraded not only to adapt to higher luminosity but also for a better low-multiplicity event sensitivity. The Belle II detector in the top view is shown in Figure 2-2.

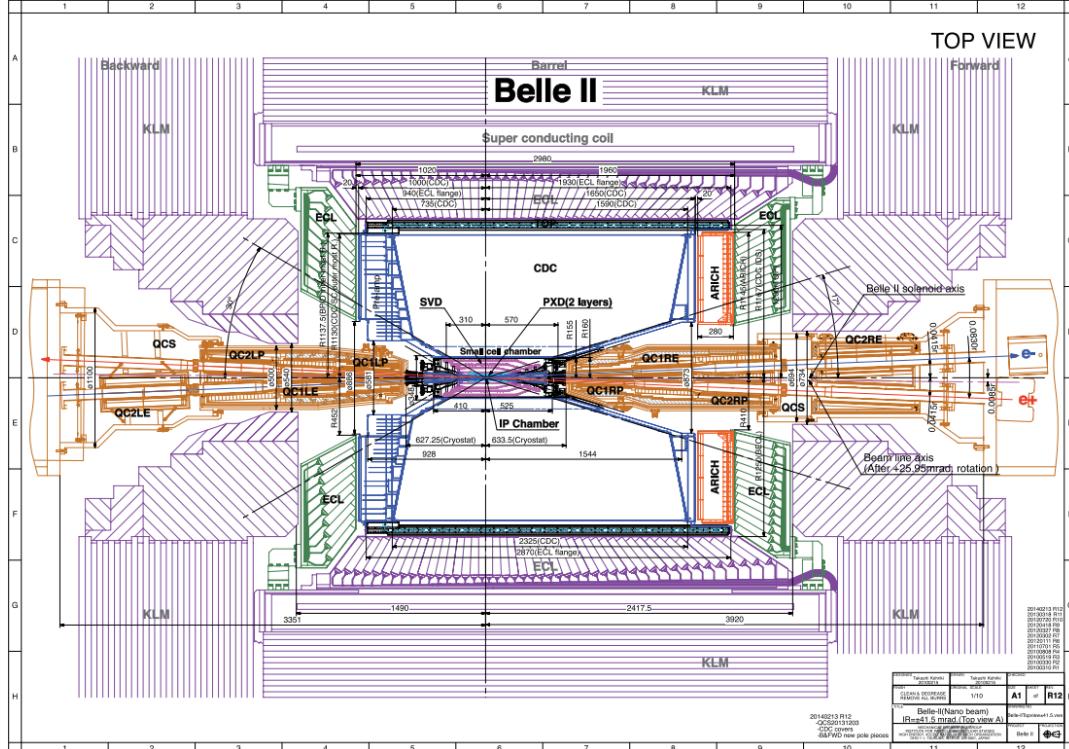


Figure 2-2: The Belle II detector top view [15].

The success of the Belle II detector depends on the complex of sub-detectors where each of them is design for specific purposes. The critical components and features are explained in the following sections.

## 2.2 Vertex detector (VXD)

The vertex detector is composed of two detectors, the silicon based pixel detector (PXD) and silicon based vertex detector (SVD), where total 6 layers are placed in the inner-most region from interaction point (IP). The geometry of VXD is shown in Figure 2-3. The PXD is placed at a radii of  $r = 14$  mm and  $r = 22$  mm with DEPFET [22] type pixel sensors, which is designed to provide two dimensional hit position information. The inner layer leaves a sufficient space for possible variations of the beampipe layout. The size of two layers are determined by the required acceptance angle, which is 17 degrees (forward) to 150 degrees (backward). The pixel sensor is a monolithic structure with current-digitizing electronics at the end of the sensor which makes a very thin layer at about 50 microns. The schematic view of sensors on PXD is shown in Figure 2-4. As the very close range the PXD is, the sensors are exposed to

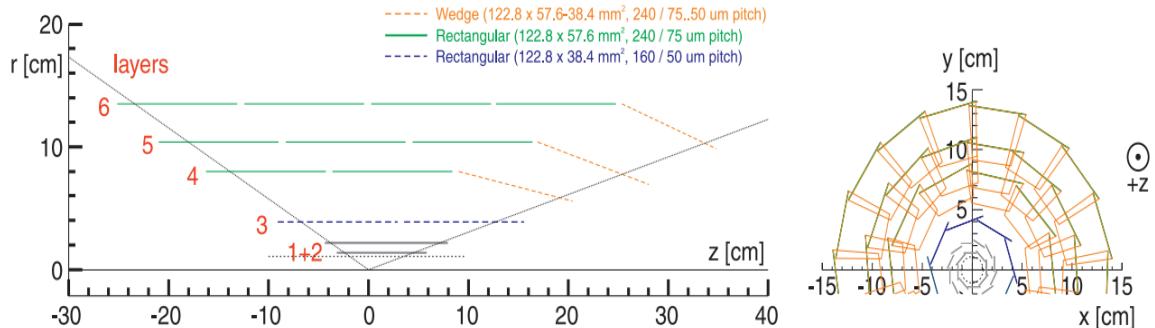


Figure 2-3: A schematic view of the VXD detector. Two PXD layers are in grey, SVD layer 3 is in blue and layers 4, 5, 6 are in green [22].

a very high event rate and very high beam background environment. The large data flow from PXD without any data reduction scheme is problematic for data acquisition system. In order to reduce the data that is not interested by physics analysis such as beam backgrounds, a fast online tracking system is built up for searching a “region of interest” (ROI) on the PXD sensors. To be specific, the data from PXD will be first readout to a system called “ONSEN” which can store large size temporary data up to 5 seconds. In this timing window, a fast online tracking system will perform a track fitting using vertex detector and central drift chamber to extrapolate the fitted

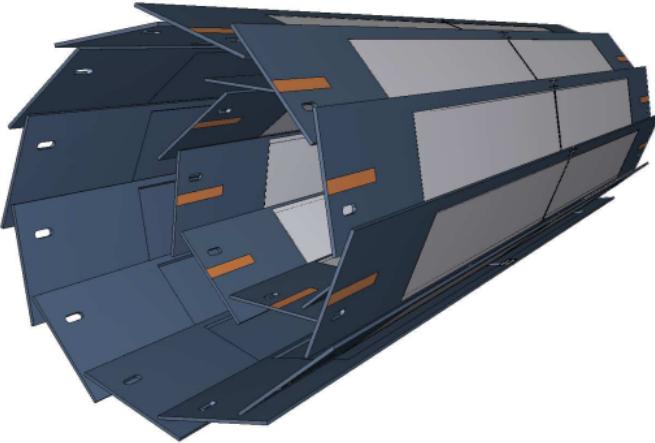


Figure 2-4: The geometry of sensors on PXD where the light grey surfaces are DEPFET sensors with a thinness of 50 microns. The full length including the out modules is 174 mm [22].

tracks backward to PXD plane so the ROI on the PXD sensors can be defined. The data from PXD outside of the ROI is not read out to external tapes where offline data is written.

SVD detector consists of 4 layers of detectors called “double-sided silicon strip detectors” (DSSDs) at 39 mm, 80 mm, 104 mm, and 135 mm away from IP, respectively. The two sides of the sensors are called *p*-side and *n*-side, where the former is for strips on  $r - \phi$  direction (transverse direction) and the latter is for strips on the  $z$  direction (beamline direction). To suppress the background hits, a readout chip with a fast shaping time of  $\mathcal{O}(50\text{ ns})$  is indispensable. The APV25 chip [24] is chosen as the readout chip that was originally developed for CMS silicon tracker, with total 128 identical channels of low-noise preamplifiers followed by a 50 ns peaking time shaper stage. The polar angular acceptance ranges from 17 degrees to 150 degrees, which is asymmetric to account for the forward boost of the center-of-mass frame. The combination between sensors, electronics and the supporting structure uses so-called “Origami” concept which stands for a chip-on-sensor design, as shown in Figure 2-5. In the Origami scheme, the readout chips APV25 are placed on a single flexible circuit mounted on the *n*-side of the sensors. The channels of *p*-side are attached by small flexible fan-outs wrapped around the edge of the sensors. All connections between

flex pieces, sensor, and APV25 chips are made by wire bonds.

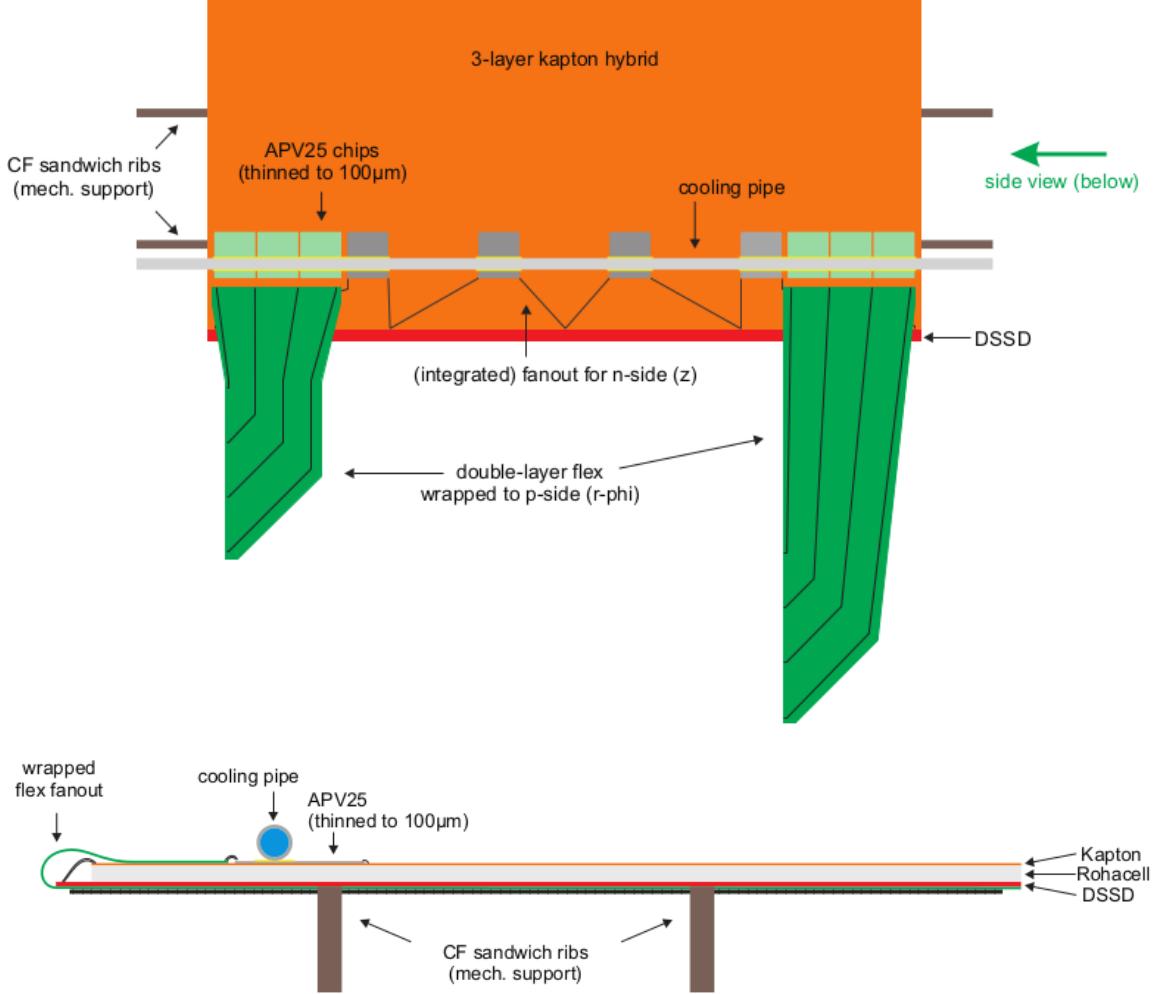


Figure 2-5: The top and side views of Origami chip-on-sensor design for DSSDs of SVD. Top: the APV25 chips in grey read out the same side sensors channel while chips in green read out the sensors on the opposite side using wrapped-around flex pieces. Bottom: side view of the Origami design shows the location of wrapped flex which connects the strips of the bottom sides which are placed at the left edge [22].

## 2.3 Central drift chamber (CDC)

The central drift chamber (CDC) is the core component of spectrometer in the Belle II, which consists of a fairly big drift chamber made of many small drift cells filled with gas. The chamber gas is comprised of a He–C<sub>2</sub>H<sub>6</sub> 50%:50% mixture with an average drift velocity of 3.3 cm  $\mu\text{s}^{-1}$  and a maximum drift time of about 350 ns for a 17 mm

cell size. The out radius of CDC has been extended to 1130 mm from 880 mm of Belle, owed to a new thinner particle identification detector which will be introduced in the next section. The whole CDC contains 14336 sense wires in 56 layers, placed in the axial direction and the stereo direction [15][22]. Such a design can utilize the information from axial and stereo wires to construct a full 3 dimensional hits which reflects helix tracks in CDC volume. Thus, CDC is one of the key components for measuring the helix parameters for tracking, providing precise information on the charged tracks momentum. Also, it provides particle identification information using measurements of energy loss within its gas volume. Low-momentum tracks, which do not reach the particle identification device, can be identified using the CDC alone. Finally, it provides efficient and reliable trigger signals for charged particles.

The Belle II CDC is expected to handle higher trigger rates with less dead time. The front-end electronics are located near the backward end-plate and send digital signals to the electronics hut through optical fibers. Due to the higher radiation and higher beam background in the Belle II, also to create more space for SVD volume, the inner radius of CDC in Belle II is 160 mm. CDC can also create three dimensional trigger information from a dedicated trigger type called  $z$  trigger [22] based on the 3D tracking achieved by an FPGA using axial and stereo wires.

The structure of CDC consists of three main components which are a thin carbon-fiber reinforced plastic (CFRP) inner cylinder, two aluminum endplates, and a CFRP outer cylinder, as shown in Figure 2-6. The outer cylinder is a thickness of 5 mm structure supporting most of the wire tension of 4 tonnes. The inner cylinder is as thin as 0.5 mm to minimize the material and support small cell chamber such as the layers in the inner most region.

## 2.4 TOP and ARICH detectors

The particle identification (PID) system of the Belle II mainly consists of two parts, time-of-propagation counter (TOP) and aerogel based Cherenkov radiation imaging ring (ARICH).

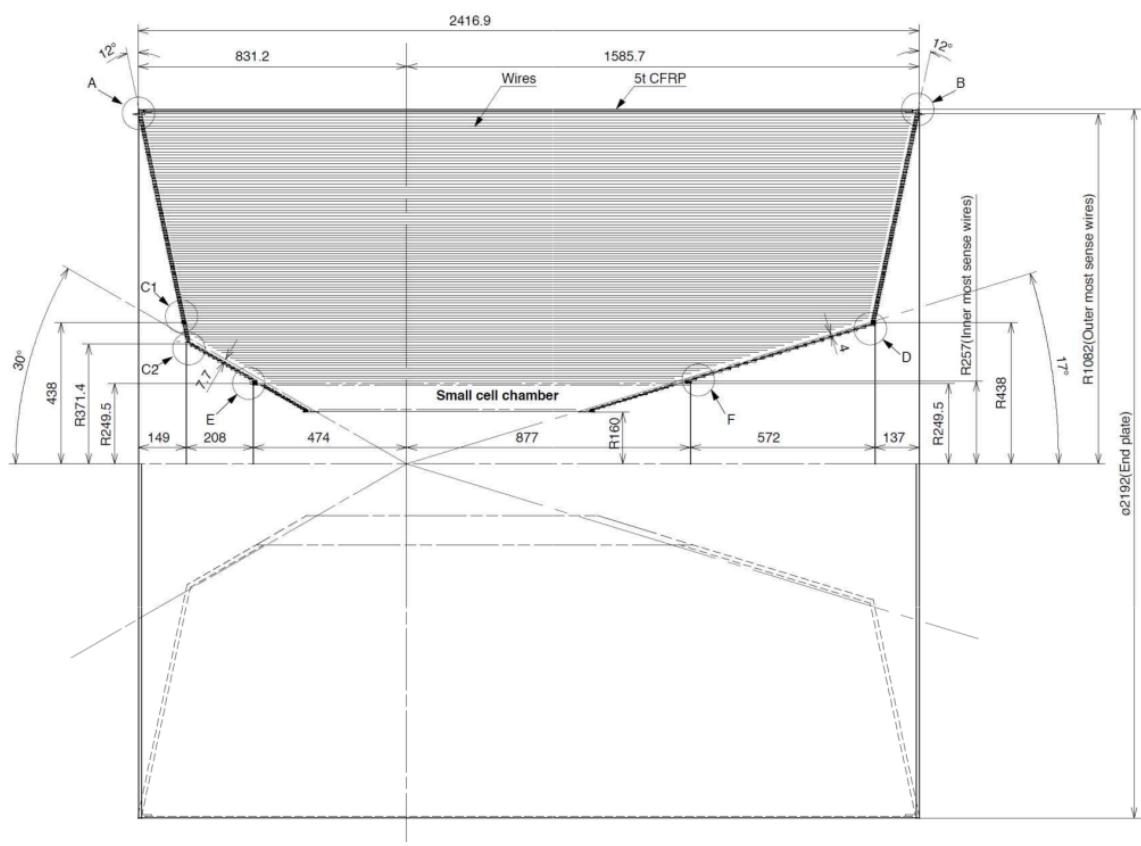


Figure 2-6: CDC structure schematic view [22].

TOP is the specialized detector that can reconstruct Cherenkov radiation's time of arrival and generated position by a photon detector placed at the end of a 2.6 cm quartz bar. The TOP is placed at the barrel region of the spectrometer, as shown in Figure 2-2. The conceptional view and the working principle of TOP counter are shown in Figure 2-7. In this counter, the time of propagation of the Cherenkov photons that are internally reflected inside a quartz radiator is measured. The quartz radiator is composed of three components. The first is a long bar for radiating Cherenkov photons. The photons then propagate via total internal reflection towards the bar end, where the MCP-PMTs are mounted. The second is a spherical mirror installed on the forward end of the bar for focusing the photons. The third is a prism that attaches to the backward end of the bar which allows the Cherenkov ring image to expand before the photons are recorded by the PMTs. By this structure, a 3-dimentional information with  $x - y$  position and a timing information are obtained by micro-channel plate (MCP) PMTs at the end surfaces of the quartz bar. The resolution of starting time is achieved about 50 ps [22]. As the key component of the photon detector, the squared shape MCP PMTs, donated as SL-10 [25], have been developed with a  $4 \times 4$  anode array, a multi-alkali photocathode, two MCP plates with  $10 \mu\text{m}$  pore size, and an aluminum layer on the second MCP to protect against ion feedback. The image of a SL-10 MCP PMT and an anode schematic view are shown in Figure 2-8.

Aerogel Ring-Imaging Cherenkov detector (ARICH) is located at the forward endcap in Figure 2-2 to separate charged particles in a momentum range from 0.5 GeV/c to 4 GeV/c, which requires single-photon-sensitive high-granularity sensor to reconstruct the Cherenkov angle with small photon yield. Hamamatsu company and the hardware experts from the Belle II collaboration have developed a hybrid avalanche photon detector (HAPD) to meet the requirements. Each sensor is  $73 \times 73 \text{ mm}^2$  embedded with 144 channels to accelerate emitted electrons in a 8 kV field. Avalanche photo-diodes (APD) are used for the detection of electrons at the end of electron acceleration, see Figure 2-9. The ARICH detector outlook and the ring image of cosmic muon on the HAPD sensors are shown in Figure 2-10.

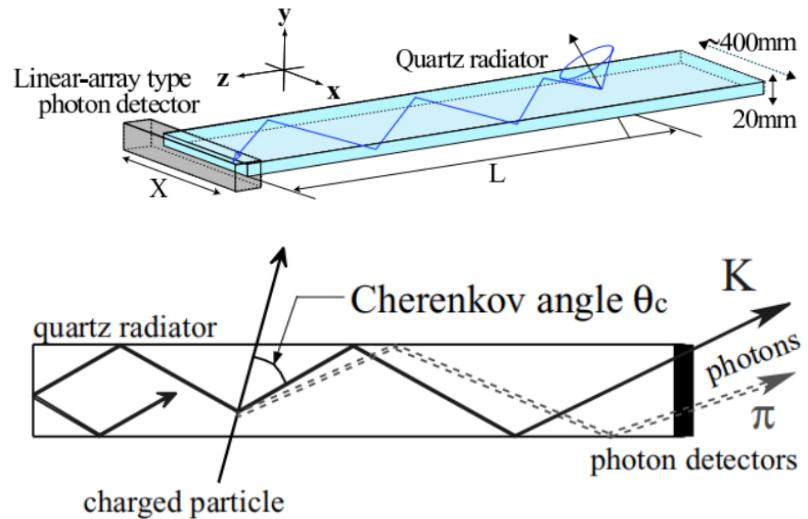


Figure 2-7: Conceptional view of TOP counter (up) and its imaging process of  $K^\pm$  and  $\pi^\pm$  (down) for PID purpose. [22]

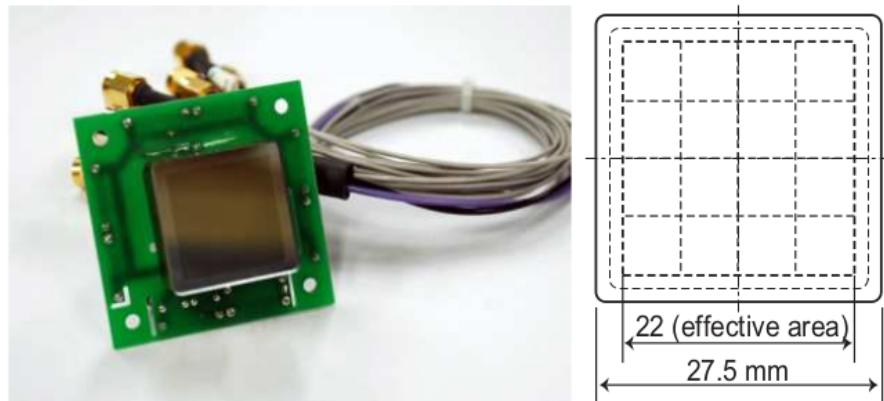


Figure 2-8: SL-10 MCP PMT (left) and the schematic view of  $4 \times 4$  anode (right) [22]

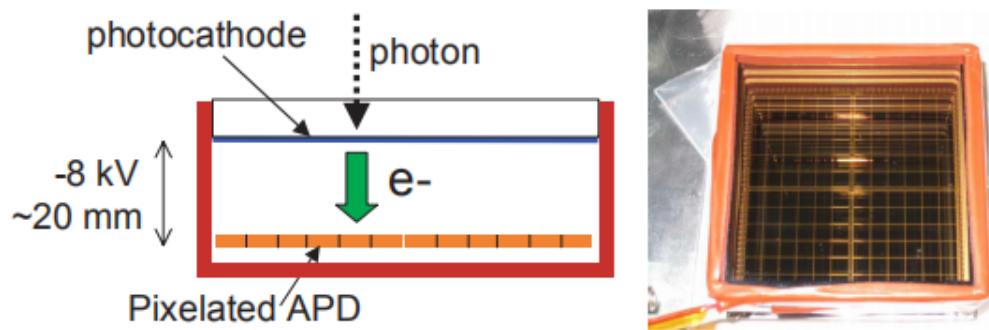


Figure 2-9: Photon-electrons acceleration (left) and pixelated APD (right) at the end [22].

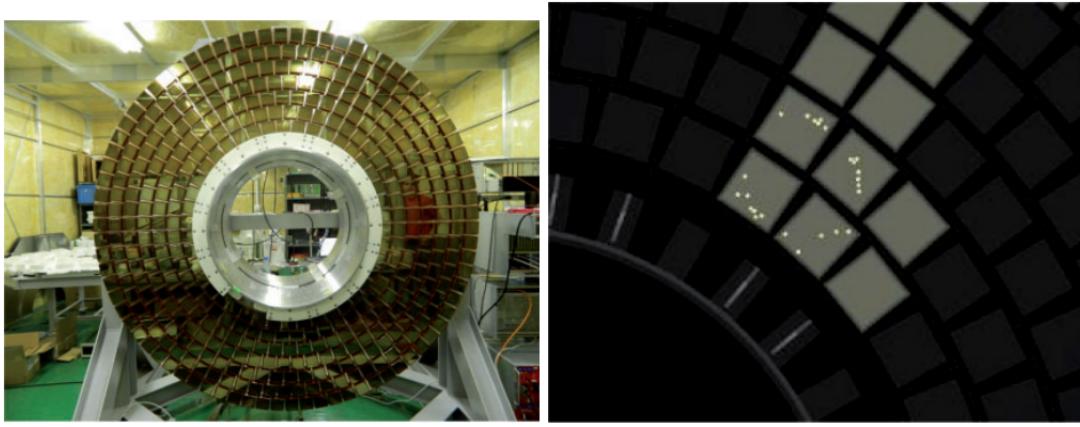


Figure 2-10: ARICH detector (left) and the ring image of cosmic muon on the HAPD sensors[15].

## 2.5 Electromagnetic calorimeter (ECL)

The electromagnetic calorimeter (ECL) in the Belle II is mainly responsible for the detection of  $\gamma$  radiation and electrons, providing energy deposition information for trigger, particle reconstruction and PID. ECL consists of three sections as shown in Figure 2-2: a 3 m long barrel section with an inner radius 1.25 m, and two annular endcaps at  $z = 1.96$  m (forward) and  $z = -1.02$  m (backward) from the IP. The barrel section contains 6624 CsI(Tl) crystals of 29 distinct shapes and each crystal is a pyramid shape with about  $6 \times 6$  in cross section and 30 cm in length. The endcaps section contains 2112 CsI crystals of 69 shapes and the total number of crystals is 8736, with a total mass of about 43 tons [22].

As the basic component of ECL, the thallium doped caesium iodide CsI(Tl) crystals are assembled tightly in end-caps and barrel sections. Compared to the previous ECL in Belle, the pre-amplifiers and the structures remain unchanged, while the read-out electronics have been upgraded. The estimated background level in Belle II ECL will cause the much longer decay time in the scintillation of CsI(Tl). This will lead to the pile-up effect of readout noise. To compensate this effect, wave-form sampling electronics are embedded with the photon detectors (PMT).

## 2.6 $K_L^0$ muon detector (KLM)

The  $K_L^0$  and muon detector (KLM) system of the Belle II consists of a sandwich stacked iron plates at outside of the superconducting solenoid and it acts as a return york of the magnet. The iron plates serve as the interaction materials with  $> 3.9$  times the interacting length of material ( $\sim 132.1$  g/cm $^2$ ) compared to the ECL, allowing  $K_L^0$  particles to shower through. The octagonal barrel covers the polar angle range from 45 degrees to 125 degrees, while the endcaps extend this coverage from 20 degrees to 155 degrees. There are 15 detector layers and 14 iron plates in the barrel and 14 detector layers and 14 iron plates in each endcap. The side view of KLM is shown in Figure 2-11. The Belle KLM material uses the glass-electrode resistivity plate chambers (RPC) which is not suitable for the Belle II due to high background level. Neutrons dose is significantly larger due to the much more electromagnetic radiation reaction on detector materials. The long dead time of RPC under such dose rate will reduce the efficiency of KLM. To mitigate this problem, the RPCs are replaced by the layers of scintillator strips with wavelength-shifting fibers, read out by silicon photomultipliers (called “SiPMs”, Geiger mode operated APDs) as light sensors, which is proven to be able to reliably operate by setting up the discrimination threshold [15].

## 2.7 Trigger and DAQ system

The interesting topics in Belle II physics analysis highly depend on the trigger system. The Belle II trigger system is composed of two levels: a hardware-based, low-level trigger called “L1” trigger, and a software-based high-level trigger (HLT). The L1 trigger has a latency of  $\sim 5\mu s$  and the maximum trigger output rate is 30 kHz, which is limited by the read-in rate of data acquisition system (DAQ). Considered the high event rate and background level from future Belle II luminosity, a series of upgrades have been implemented for L1 trigger. The key improvements of L1 come from the firmware-based reconstruction algorithm and trigger logic.

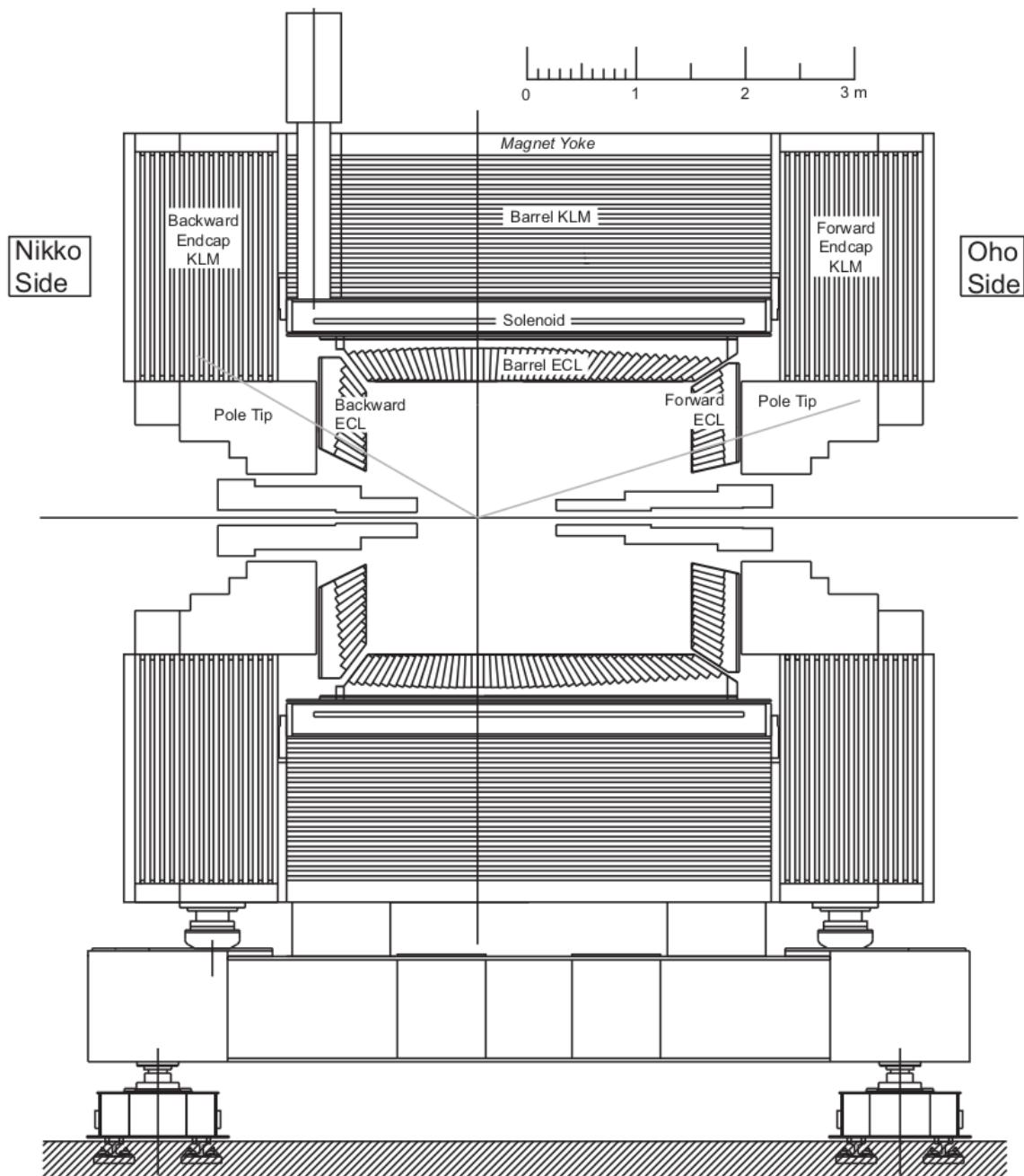


Figure 2-11: The side view of KLM in between the ECL and the solenoid, which the grey lines presents the nominal acceptance angle of the Belle II [22].

The HLT, as the second level of Belle II trigger system, plays an important role in DAQ. As discussed in the section of PXD, the data size in PXD is huge at high luminosity and the ROI selection must be applied to reduce it. The HLT will first use fast online tracking by CDC and ECL information to further reject the residual beam background not found by L1 trigger. Only the events passing this step are considered for the full event reconstruction. Then the information from all detectors except for PXD are fed into the first event builder for full event reconstruction. The event rate is reduced to about 6 kHz by HLT which uses the full reconstruction information to find track-associated hits on PXD, as introduced as ROI before. The workflow of DAQ with HLT is demonstrated in Figure 2-12. The reduced event rate by applying ROI finding on PXD and other detector read-out systems are combined into the second event builder and eventually written to the offline storage.

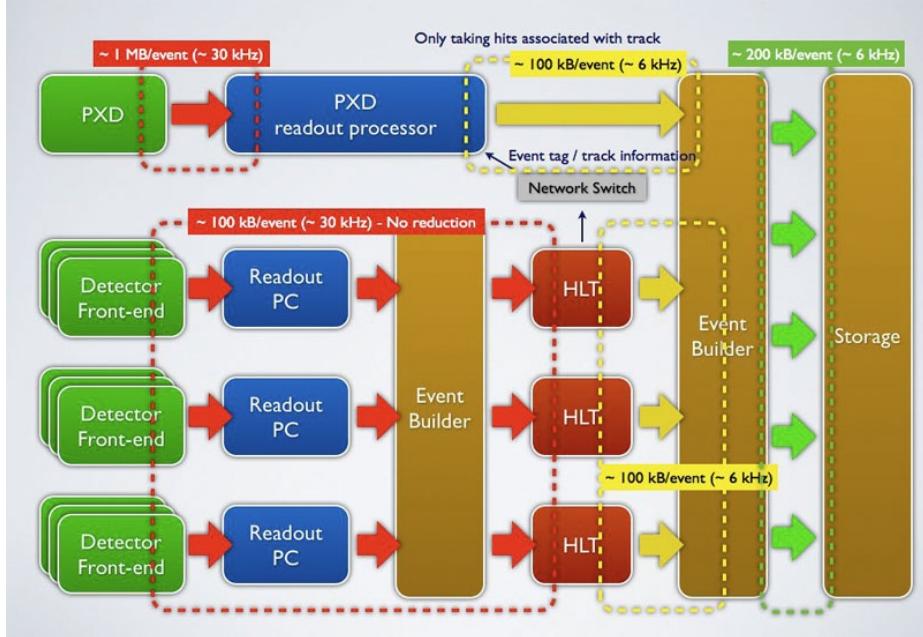


Figure 2-12: The Belle II DAQ workflow with HLT between two event builder to reduce the original 30 kHz event rate down to about 6 kHz for offline storage.

Since the primary goal of the Belle II is focusing on  $B$  physics studies, it is natural that the trigger system should be able to operate over all of the interesting  $B$  physics conditions, with normally 3 or more CDC tracks and large energy deposition in ECL. By studying the efficiency using the simulated events, close to 100%  $B$

decays are recorded by Belle II trigger system. Besides, the Belle II detector is expected to capture many other physics events such as searching for leptonic flavor violation using  $\tau$  decays or dark matter particles, of which the performance is highly affected by the beam background level and trigger efficiency. Therefore, the control of beam background becomes essential, which mainly consists of beam-gas scattering, synchrotron radiation, the radioactive Bhabha scattering, the two-photon process, beam-beam effects, and Touschek effect. Their impacts depend on many factors such as beam current, luminosity and vacuum conditions, etc. One of the featured topology of these beam background events is the combination of two charged tracks in CDC and one or two clusters in ECL. The sources of the main beam backgrounds and their event rates in simulation are listed in Table 2.2.

Table 2.2: Simulated beam background rate [15]

Type	Source	Rate (MHz)
Radiative Bhabha	HER	1320
Radiative Bhabha	LER	1294
Radiative Bhabha(wide angle)	HER	40
Radiative Bhabha (wide angle)	LER	85
Touschek scattering	HER	31
Touschek scattering	LER	83
Beam–gas interactions	HER	1
Beam–gas interactions	LER	156
Two-photon QED	-	206

## 2.8 Analysis software framework

The data acquired by the Belle II experiment or simulation can be processed by the Belle II Analysis Software Framework, called BASF2. It has a good capability to handle multiple tasks for the Belle II data analysis, from the simulated data production to physics events reconstruction. The BASF2 takes the advantage of good efficiency and reliability of C++ as the programming languages, but the use of Python is also

allowed when it shows clear advantages, such as steering the analysis workflow.

### 2.8.1 BASF2 Core Structure

The core structure of BASF2 contains three major parts: the analysis packages required by the needs of analyzing the Belle II data such as finding tracks and combining particles, the external libraries as the third-party software such as ROOT [26], and the tools for configuring and installing BASF2 which are mostly Python and shell scripts. Data analysis is supported by providing a series of modules belonged to BASF2 for appropriate reconstruction based on their specific needs. To realize this, a modular analysis workflow, where each module can handle the event data through an unified method such as ROOT I/O based object persistency, is desired. Other processes, such as data summary table (DST) processing, simulation of each sub-detectors, and data skimming, are done with the packages built for sub-detectors.

The packages are categorized based on the different levels of Belle II detector components, like the packages of base-level system control called “framework”, the package that provides the simulation of each sub-detectors like “svd”, the package for track reconstruction called “tracking”, and the package for post-reconstruction data analysis called “analysis”, etc. Users can work either with compiled binary version of BASF2 installed centrally on working servers, or build from the source based on their own need. Furthermore, the distributed computing is also supported by the installations of BASF2 through the management service provided by DIRAC system [27]. The detail information about the core structure of BASF2 can be found in Ref [28].

### 2.8.2 Event processing workflow

The data from Belle II detector or from the simulation, are organized into a set of runs that are defined by either experimental conditions or simulation conditions. For instance, the simulation data from the condition of a certain detector is packed together, marked with the condition database index used during the simulation. Such

data sample then is divided into different runs based on estimated luminosity from experiment, which can contain the different number of events in each run. This scheme is used for categorizing experimental data as well, so that users can easily know which experiment conditions are used. Thus, when BASF2 processes a data set, the functions are called for every event based on different configurations that are corresponding to the different experiment conditions. For example, in a data set where events are recorded with the different magnetic fields, BASF2 can automatically change the configurations of the magnetic fields event-by-event to provide a better track measurement. Based on this idea, all BASF2 functions (called “modules”) are developed based on a python module class which contains following embedded functions to be called at event-based level:

- initialize: called at the start of processing events to prepare this run, including how many events will be processed and declaration of the buffer space and memory required by this module.
- beginRun: called after the initialization is finished and before the event read-in starts, including setting up database conditions used in this run (run-dependent configurations) or event (event-based configurations).
- event: called when each event is read and start to process. This is the actual processing step, such as perform tracking or combining all daughters to find a mother particle.
- endRun: called at the end of a run, usually to register all processed information to the storage, such as physics variables from all reconstructed particles.
- terminate: called at the end of the processing of all events, release the buffered space and memory.

BASF2 executes a series of modules loaded dynamically to process the data set for analysis purposes, which is shown as Figure 2-13. The selection, configuration and executed order of the modules are defined by a file called “steering file” written in Python. The modules parameters are attributes which can be set during the runtime using the steering file.

The object that interacts with BASF2 I/O is called “DataStore”, as shown in

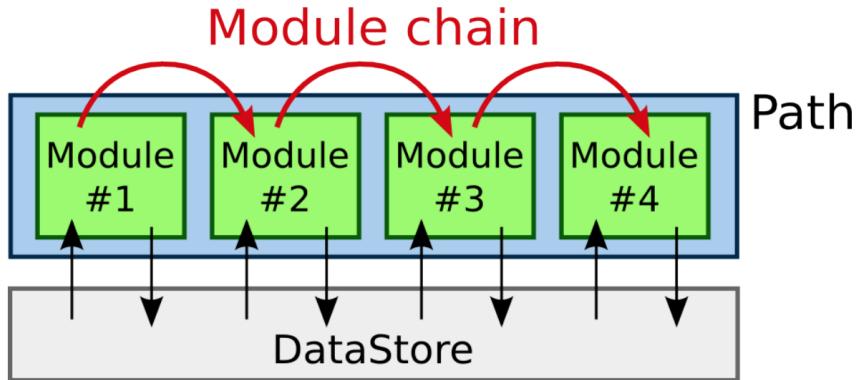


Figure 2-13: The module-based analysis workflow in BASF2.

Figure 2-13. This implementation doesn't depend on the event data model. The only mandatory component is called "EventMetaData" which presents the experiment, run and event number of a event. "Unpacker" module converts the raw digits into digits-based object in BASF2. In simulation, digitization is done by module called "digitizer". The digits-based objects are further processed to form hits or clusters depending on detector types. Higher level functions such as tracking and decay reconstructions are implemented based on these basic information by their packages. Eventually, BASF2 writes out the information based on users' needs, like kinematics variables, to ROOT format files, or simply prints out processing statistics to the standard output.

### 2.8.3 mDST structure

The output of BASF2 processing from the online data contains several detector-specific objects, which are restored as mini data summary table (mDST) type ROOT file. For a mDST level analysis, the goal is usually aimed to find particles from physics processes and reconstruct decay information. A output mDST ROOT file contains the reconstructed objects from each sub-detectors, and the following items are required for  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  analysis.

- Track: object presenting any charged particle trajectory. It's linked to multiple

track fit results using different nominal mass hypotheses as well as their track fit quality to help select good tracks.

- **TrackFitResult**: the fitting result of tracks with different mass hypotheses. It consists of five helix parameters, their covariance matrix and p-value from the fit. It also stores the information of hit pattern on VXD and CDC.
- **V0**: object for the relative long-lived neutral particles that fly out of interaction region but mostly decay or interact inside detector region. In Belle II, these are mostly  $K_S^0$ ,  $\Lambda$  and photon converted to a electron-positron pair. V0 also stores their relation to the charged daughter tracks and track fit results for further selections.
- **PIDLikelihood**: it presents for the possibility of a charged track to be an electron, muon, charged kaon and pion, proton and deuteron provided by particle identification system.
- **MCParticle**: simulated particles and particle-detectors relations are created if simulated particles are correctly reconstructed as tracks or clusters.

#### 2.8.4 Conditional Database

In addition to the physics data, analysis relies on various conditional data that are different calibration of detector, weight files for multi-variate analysis usage like PID and so on. This data is stored in a central database server called central Conditional Database (CDB) [29]. Conditions are made of payloads and each payload has its own “Intervals of Validity” (IoV) which defines in which runs the payload is valid. A collection of the payloads that are produced based on a certain stage of the experiment is packed together and called as a global tag (GT).

Users can create a GT, add objects of payloads to it and commit the GT to the configured database with a user-supplied IoV. This includes the support for run dependency as well. The capability to use a local file-based database allows for easy preparation and validation of new payloads before they are uploaded to the CDB. Only the creator of the payload objects has the right to add, recall, replace and remove the GT from CDB, which guarantees the stability.

## 2.9 Belle II simulation

This section briefly describes simulation (MC) used in the studies presented in this thesis. As this analysis is based on neutral  $B$  meson, which is from the  $\Upsilon(4S)$  events, the simulation is based on the electron -positron collisions at center-of-mass (CMS) energy  $\sqrt{s} = 10.58$  GeV.

In the previous section, it's shown that external packages and functionalities have been integrated with BASF2, including the core components of Belle II simulation in  $B$  decay: *evtgen* as event generator [30] and *GEANT4* as the simulator of detectors [31]. For the simulation and the reconstruction used in this analysis, the latest release of BASF2 (release-05-01-01) was used. Based on the CDB management, BASF2 can utilize the same constants such as the magnetic field distribution for the consistence between simulation and reconstruction.

All simulations start with at least one event generator that configures the physics processes. The *evtgen* requires a decay file that describes the decay chain from a certain mother particle, branching fraction for all processes and decay-related information such as flavor mixing or  $CP$  violation information. MC sample is centrally produced using Belle II grid computing service by DIRAC system and skimmed, of which the output is for physics analysis to create ROOT files. Each round of MC sample is packed and marked by their production index, such as *MC13*, which is the latest MC sample with improvements in PID. In the following content of this thesis, all MC samples are produced in *MC13* if not specifically stated.

For the analysis in this thesis, there are two MC samples included, where one is called *signal MC* and the other is called *generic MC*. *Signal MC*, as its name suggests, is the MC sample that describes the whole decay chain of  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$ . The mother particle of the decay chain is  $\Upsilon(4S)$ , then it decays into a pair of  $B^0 - \bar{B}^0$  at branching fraction of 100%, with the model *EvtVSSMix* [30] describing the decay model. Then, one of the  $B^0$  meson is set to decay into three  $K_S^0$  based on phase-space model (*PHSP*) at 100% branching fraction. The default configuration of *evtgen* can not handle multi-bodies charmless  $B$  decay with TDCPV. A modified decay

Table 2.3: Production cross section for different hadronic flavors from collision at  $\sqrt{s} = 10.58$  GeV used in Belle II *generic MC* [15].

Processes	$\Upsilon(4S)$	$u\bar{u}(\gamma)$	$d\bar{d}(\gamma)$	$s\bar{s}(\gamma)$	$c\bar{c}(\gamma)$
Cross section [nb]	$1.110 \pm 0.008$	1.61	0.40	0.38	1.30

model profile is under-development and not fully validated yet. Thus, MC sample of  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  yields zero  $CP$  violation by default. As for the other  $B$  meson, it decays into all possible final states that are described by the Belle II generic decay file.

As for *generic MC*, all hadronic processes in a  $\sqrt{s} = 10.58$  GeV collision are simulated. The total production cross section receives contributions from not only  $\Upsilon(4S)$  ( $b$ -flavor decay dominated), but also  $u, d, s, c$ . Their relative branching fractions are taken from cross sections at  $\sqrt{s} = 10.58$  GeV as shown in Table 2.3. *Generic MC* sample contains 6 types of MC samples due to this production arrangement, where  $\Upsilon(4S)$  produces *mixed* (neutral) and *charged*  $B$  meson pairs and the rest are other flavor mesons possibly with one extra photon emission named as  $u\bar{u}(\gamma)$ ,  $d\bar{d}(\gamma)$ ,  $s\bar{s}(\gamma)$ , and  $c\bar{c}(\gamma)$ , respectively. In this thesis, the latter 4 types of MC samples are combined and called  $q\bar{q}$  for simplicity. In the mixed MC sample, the branching fraction of  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  is set at  $6 \times 10^{-6}$  and the branching fraction of  $K_S^0 \rightarrow \pi^+ \pi^-$  is set at 0.692. Both values are taken from Particle Data Group (PDG) [32]. As the same as *signal MC*,  $CP$  violation is set to zero for signal events in *generic MC* since they use the same model at generator level.

In addition to the simulation of physics processes, simulated data is produced with at least two beam background conditions, called *BG0* without beam background and *BG1* with one overlay of beam background. The components of them have been discussed briefly in section 2.7. The mixing of simulated beam background to simulated physics events is done by adding simulated hits on each sub-detector output. Possible pile-up of hits is therefore inherently included. The average number of background events of a given type to be added to a single simulated event is determined from the rate  $R_{BG}$  of beam background sample and the time window  $\Delta t$  in which the background is mixed shown in Equation 2.1:

Table 2.4: MC samples with and without beam background used in  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  analysis.

Events number	BG0	BG1
<i>signal MC</i>	$10^6$	$10^6$
<i>generic MC</i>	None	$1 \text{ ab}^{-1}$

$$\bar{N} = s R_{BG} \Delta t \quad (2.1)$$

where  $s$  is an optional scaling factor. The injected background events are based on a Poisson distribution with mean  $\bar{N}$ . Within the timing window, the background events are shifted randomly to simulate contributions from different bunches. To use real experiment background events (data-based beam background), the random triggered events are measured and added to simulated *BG0* MC sample for a more precised background configuration. This method can give a more realistic description of actual beam background but with a possibility to introduce bias due to the pile-up effect of multiple background events in a short timing window. In the early stage of the Belle II, the level of background is not high and the background pile-up effect is small.

In total, there are 2 million events generated in *signal MC*. Half of the *signal MC* (1 million) is produced without beam background for cross-checking the reconstruction performance. For *generic MC*,  $1 \text{ ab}^{-1}$  sample including mixed, charged and  $q\bar{q}$  events are produced with beam background at  $\sqrt{s} = 10.58 \text{ GeV}$ . The MC sample used in this analysis is summarized in Table 2.4

## 2.10 Belle II data taking

The Belle II beam test operation started in 2016 which was focused on the commissioning and test of the SuperKEKB accelerator. Later in 2018, the commissioning of the Belle II detector was accomplished, with partial installation of PXD and full installation of SVD. From 2019 April, the physics run operation has officially started. The rest of the PXD is scheduled to be installed in 2023. By the end of 2020, Belle II

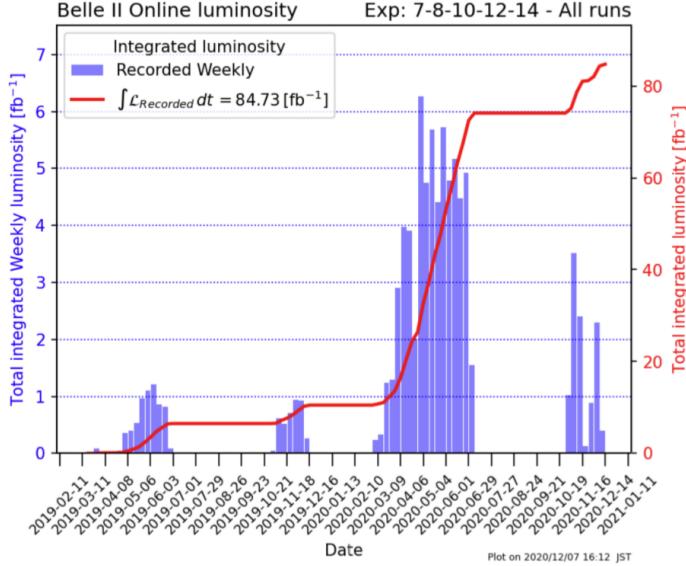


Figure 2-14: Belle II online luminosity from 2019 April to the end of 2020. The experiment 7 and 8 were conducted during 2019 March to June. The experiment 10 was conducted during 2019 October to 2019 November. The experiment 12 was conducted during 2020 February to June. The experiment 14 was conducted during 2020 September to November.

has been operating for 4 total run seasons. The integrated luminosity collected during this period of time is about  $84.73 \text{ fb}^{-1}$ , shown in Figure 2-14. The indices of physics runs are labeled which are experiment 7,8,10 for 2019 data taking and experiment 12 and 14 for 2020 data taking, as shown in Figure 2-14. The data processing is regularly performed along with the data taking. For the analysis reported in this thesis, the experimental data collection from experiment 7, 8, 10 and 12 is used. Correspondingly, the integrated luminosity for offline reconstruction used in this thesis is about  $62.8 \text{ fb}^{-1}$  [33]. The experiment 14 is not used due to the unfinished processing of the latest experiment data.



# Chapter 3

## $K_S^0$ reconstruction study

The final states of  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  only depends on the decay of  $K_S^0$ . The main decay channels of  $K_S^0$  is to either  $\pi^+ \pi^-$  at branching fraction of about 0.692, or to  $\pi^0 \pi^0$  at branching fraction of 0.307, referenced from PDG [32]. The characteristics of these two decays are much different in terms of the response from the Belle II detector. The charged decay that yields  $\pi^+ \pi^-$  leaves two tracks originating from VXD or CDC volumes with the opposite charges. On the other hand, the  $\pi^0$  main decay channel is  $\pi^0 \rightarrow \gamma\gamma$  which typically results in the photon clusters on the ECL. There are mainly two reasons for not selecting  $\pi^0$  as final states. First,  $\pi^0 \rightarrow \gamma\gamma$  can yield a large fraction of fake  $K_S^0$ . The reconstruction of two photons using ECL clusters provides no constrain on  $K_S^0$  vertex so it's almost impossible to suppress the combinatorial background using vertexing information in this case. The photons could be originating from many other resources, such as beam background and charged particles radiation. Besides, the most useful selection is the invariant mass of  $K_S^0$  which is typically distributed around its nominal mass with a few hundred of keV. However, using the mass window of  $K_S^0$  could not effectively reject the noticeable fraction of fake  $K_S^0$ , especially when using photons. Second,  $B^0$  that decays to one or more  $K_S^0$  reconstructed from neutral pions have poorly reconstructed vertices. Even with  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  which only uses  $K_S^0$  from charged pions in the final states, there is no direct charged tracks from IP, which leads to the worse resolution of vertex position compared to the channel like a  $B^0 \rightarrow J/\psi K_S^0$  that has two direct charged

tracks of  $e^+e^-$  or  $\mu^+\mu^-$  from  $J/\psi$ . If one (or more) of  $K_S^0$  has the poor vertexing quality from its decay products, it can further reduce the precision of vertex positions of  $B^0$ , leading to large uncertainties on the vertex positions. Such a degradation of precision of the vertex position eventually results in the large uncertainties in decay time difference, which is the key observable in the time dependent  $CP$  violation (TDCPV) study. Therefore, only  $K_S^0$  reconstructed using charged pions is considered in this analysis.

### 3.1 Cut-based $K_S^0$ Reconstruction

The average life time of  $K_S^0$  is  $(8.954 \pm 0.004) \times 10^{-11}$  s according to the PDG, which corresponds to the average flight length of a few centimeter. Therefore, the flight length of  $K_S^0$  is comparable with the scale of VXD size. In the Belle II energy scale, the range of the flight length of  $K_S^0$  could be from a few  $\mu\text{m}$  away from  $B$  vertex to more than 13.5 cm that is further than the outmost layer of SVD ladders, see Figure 3-1. Due to the different topology of  $B^0$  decay, the average momentum of  $K_S^0$  in *generic MC* is different from the ones of the *signal MC*.

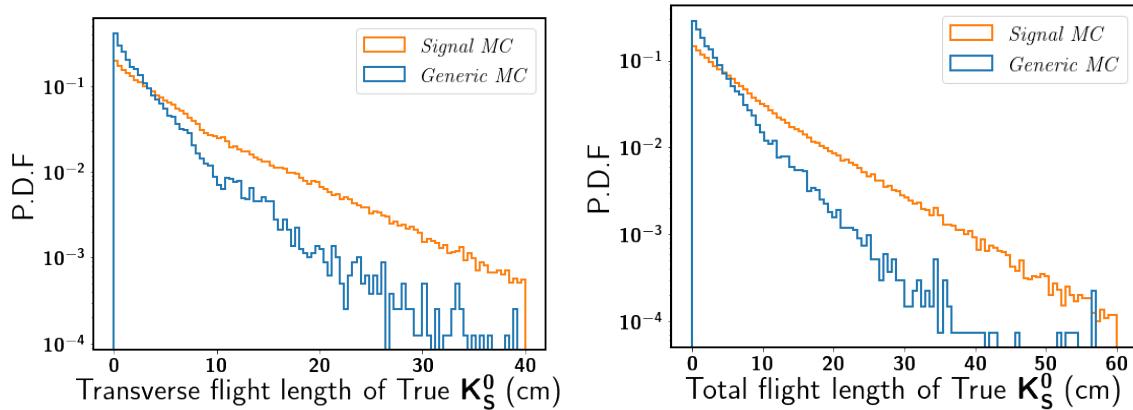


Figure 3-1: The left is the transverse flight length distribution and the right is the total flight length distribution from true  $K_S^0$ . The blue is from *generic MC* and the orange is from *signal MC*. Both plots are normalized.

The cut-based reconstruction for  $K_S^0$  is first performed by the selection of invariant mass from its decay products. After the selection on invariant mass is applied, a vertex

fit for each  $K_S^0$  using two reconstructed charged pions is done without IP constraint. This reconstruction is mainly achieved by using standard a BASF2 particle list, in which two  $K_S^0$  collections are first reconstructed and then merged. We first take all the V0 objects from BASF2 which use 2 online reconstructed charged tracks with opposite charges and a converged fitted vertex. In this step, charged particles with mass hypothesis of  $\pi^\pm$  are used, where the tracks and PID of charged pions are pre-selected by the criteria in Table 3.1. Then the  $K_S^0$  candidates with invariant mass  $M$  between  $0.45 < M < 0.55$  GeV are selected. In addition to these  $K_S^0$  from V0 objects, another  $K_S^0$  collection from offline reconstruction is also formed by using the same selection criteria for pions and  $K_S^0$  invariant mass. The V0 based  $K_S^0$  and offline reconstructed  $K_S^0$  are merged and the vertex fit is performed using *TreeFit* [34]. After the vertex fit, the invariant mass of  $K_S^0$  of the fitted pions is required to be in between  $0.3 \sim 0.7$  GeV to further rejected fake candidates. The duplication of  $K_S^0$  between two  $K_S^0$  collections is possible so that the object indices of two charged pion tracks in BASF2 are compared, from which the identical combinations are removed to avoid duplication. The  $B^0$  reconstruction efficiency is highly sensitive to the efficiency of charged pions because the final state particles are three identical  $K_S^0$  decaying to six charged pions. That's why a very loose selection on  $\pi^\pm$  is applied. The selected  $K_S^0$  collection using cut-based method contains many fake candidates. The distribution of the invariant mass using *signal MC* is shown in Figure 3-2, which shows 39% true  $K_S^0$  and 61% fake  $K_S^0$ .

Table 3.1: Pre-selection criteria of  $\pi^+\pi^-$  for  $K_S^0$  reconstruction.

Selection Criteria	$\theta$	CDC Hits Number	PID
CDC acceptance		$> 20$	pionID $> 0.1$

The reconstruction quality of  $K_S^0$  also depends on the flight distance.  $K_S^0$  that decay in the inner region of VXD yields more hits on the SVD layers associated with the charged tracks of pions, which is critical for providing tracking information together with CDC hits. The Belle II track fitting quality becomes much worse for those without inner detector hits association, especially SVD hits information. To

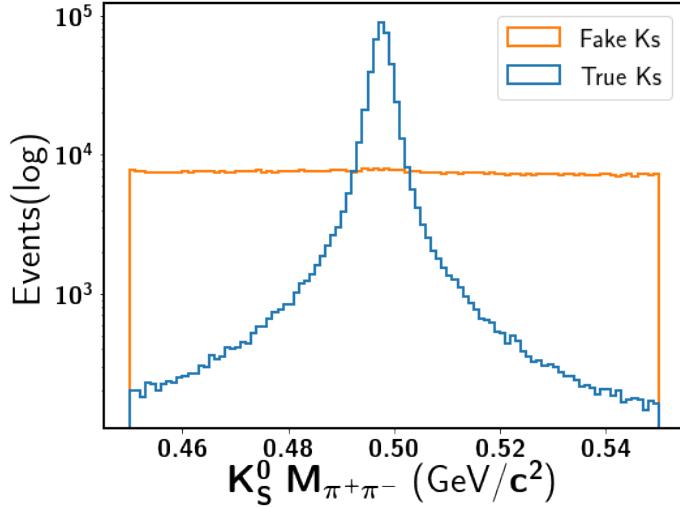


Figure 3-2:  $M$  of  $K_S^0$  from cut-based selection in *signal MC*. The blue line is the true  $K_S^0$  and the orange is the fake  $K_S^0$ . 200000 candidates are used in total.

further study the reconstruction of  $K_S^0$  based on their SVD hits, they are categorized by how many SVD hits their daughter tracks are associated with, in which *SVD10* and *SVD01* stands for  $K_S^0$  that only  $\pi^+$  and  $\pi^-$  has non-zero SVD hits number, *SVD11* and *SVD00* stands for  $K_S^0$  that both or neither charged pions have SVD hit non-zero SVD hits number. The  $K_S^0$  fraction of each category are listed in Table 3.2.

If we compare the distribution of the invariant mass before and after the  $K_S^0$  vertex fit in each category, *SVD00*  $K_S^0$  shows a large dispersion from the  $0.45 \sim 0.55$  GeV to  $0.3 \sim 0.7$  GeV, while *SVD11*  $K_S^0$  shows a much smaller dispersion in Figure 3-3. This indicates that the absence of SVD information leads to the inaccurate  $K_S^0$  reconstruction. Therefore, considering the  $K_S^0$  candidates with different SVD hits, a series of different cuts on invariant mass  $M_{\pi^+\pi^-}$  are applied to improve the purity for well-reconstructed  $K_S^0$  candidates. As shown in Figure 3-4, the sideband regions, where fake  $K_S^0$  is much higher than true  $K_S^0$ , are excluded. The cut windows are listed in Table 3.3.

Fake  $K_S^0$  candidates can cost a large extra processing time and the number of combinatorial backgrounds in  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  becomes high, which significantly reduces the signal significance and introduce bias to the *CP* parameters measurement. Thus, a multi-variate analysis (MVA) based  $K_S^0$  classification package, *KsFinder*, is

developed to further reject the fake  $K_S^0$  from cut-based selected candidates.

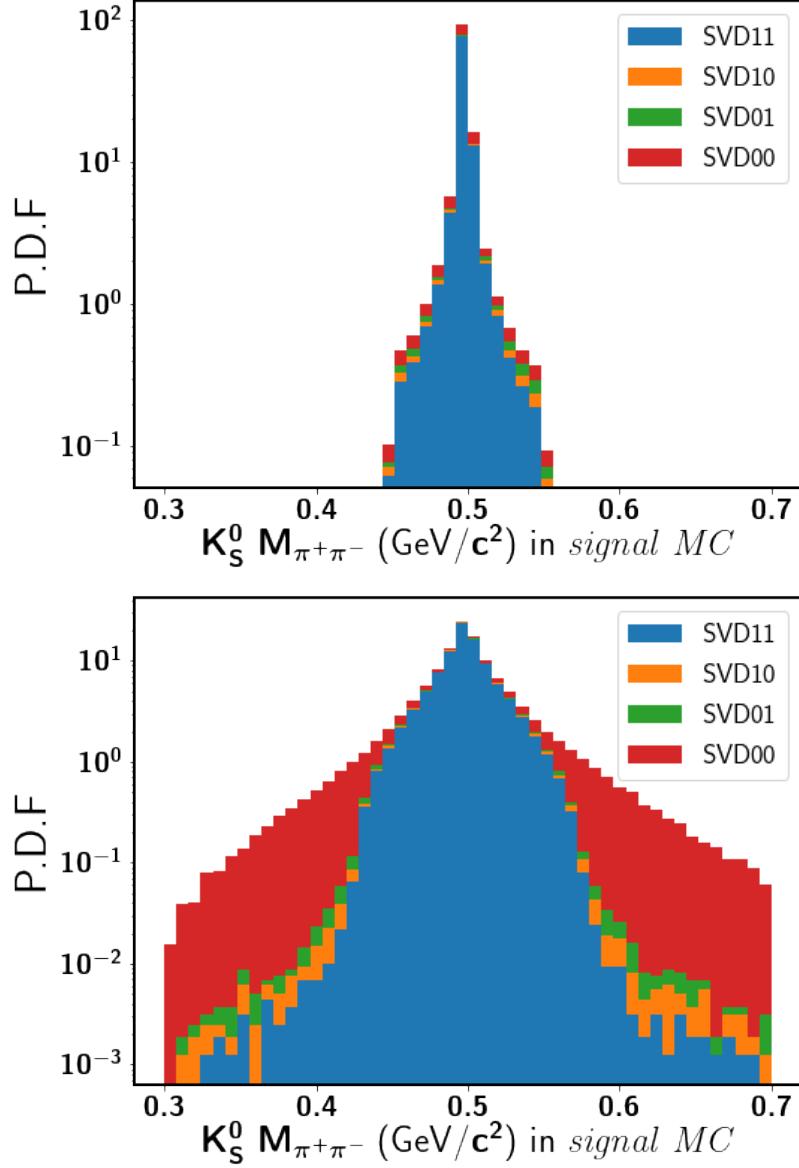


Figure 3-3: The invariant mass before (top) and after (bottom) vertex fit distribution based on SVD types, which shows a clear dispersion in  $SVD00$  particularly, indicating the inaccurate reconstruction of  $K_S^0$  masses without SVD information.

$K_S^0$ type	$SVD11$	$SVD00$	$SVD10$	$SVD01$
% in signal MC	52%	38%	5%	5%

Table 3.2: The fraction of each category of  $K_S^0$  based on pions SVD hits in  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  signal MC.

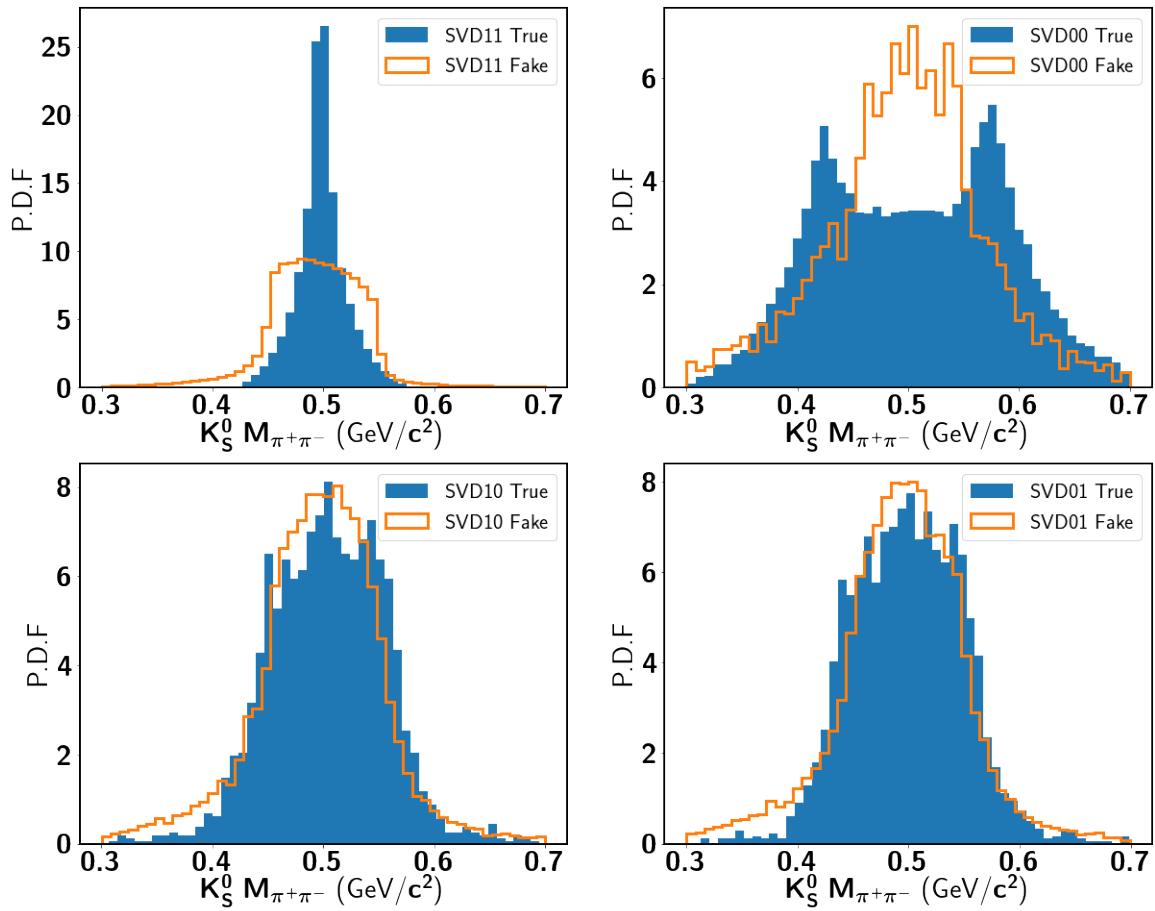


Figure 3-4:  $K_S^0$  invariant mass after vertex fit, where the sideband regions are excluded in these distributions to further reject fake  $K_S^0$

$K_S^0$ type	SVD11	SVD10	SVD01	SVD00
$M_{\pi^+\pi^-}$ window ( $\text{GeV}/c^2$ )	(0.45,0.55)	(0.38,0.7)	(0.38,0.7)	(0.3,0.7)

Table 3.3: The invariant mass windows after  $K_S^0$  vertex fit based on the number of SVD hits in Figure 3-4. The  $K_S^0$  outside these regions are rejected.

## 3.2 MVA-based $K_S^0$ selection

### 3.2.1 Belle II $K_S^0$ classification

The reconstruction of  $K_S^0$  can be treated as a typical classification problem. The input is a set of variables that describes the characteristics of  $K_S^0 \rightarrow \pi^+\pi^-$  decay. The training target is the true or fake flag from the MC truth-matching variable called *isSignal* where *isSignal* = 1 (0) stands for being a true (fake)  $K_S^0$ . The new Belle II  $K_S^0$  classification tool aims to improve the limitations from the similar tool used in Belle.

In Belle, the  $K_S^0$  reconstruction was first done by using cut-based method to select primary candidates, then a MVA-based classifier was implemented by assigning two likelihood indicators to each  $K_S^0$  candidates. The package used by Belle is called *nisKsFinder* [15] which outputs the two likelihood variables based on NeuroBayes algorithm [35]. The Belle tool defines the goodness of  $K_S^0$ , called *nb\_nolam* and *nb\_vlike*. As their names suggest, *nb\_nolam* is the likelihood of not being a  $\Lambda$  particle and *nb\_vlike* is the likelihood of being a V0-like particle. A good  $K_S^0$  candidate from *nisKsFinder* is the one with a low likelihood of being  $\Lambda$  particle and a high likelihood of being a V0-like particle, assuming the major backgrounds for  $K_S^0$  are the mis-identified  $\Lambda$  among V0-like particles. By putting cuts on these two variables, a purification of  $K_S^0$  can be made, shown in Figure 3-5. It can effectively reduce fake  $K_S^0$  from cut-based selected candidates, however, there are disadvantages about this method. First, NeuroBayes is a commercial product that was developed over 10 years ago. The official support and update is stopped nowadays, so it's not an ideal method for an experiment like the Belle II that has a quite long prospective in operation. Second, the classification is based on a joint cut on two variables, which might make the cut values hard to choose, for example, two different cuts might have

very close purity. Besides, the computation speed of NeuroBayes algorithm is not optimized in training large data set.

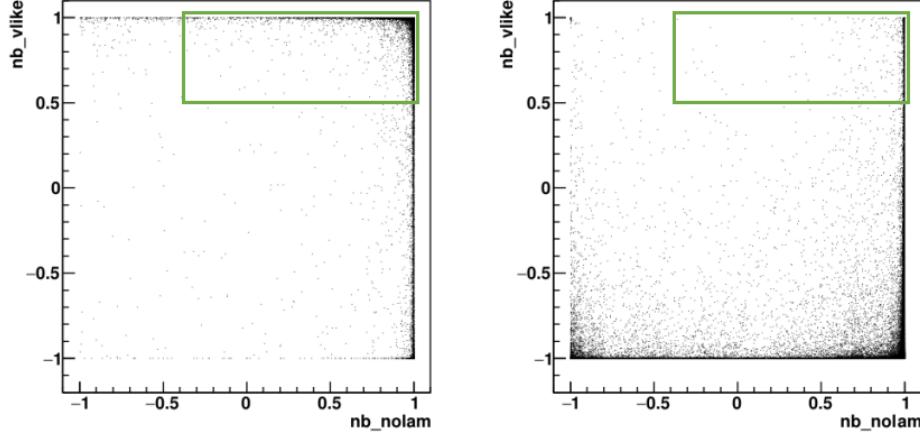


Figure 3-5: The distribution of two variables outputs:  $nb\_nolam$  and  $nb\_vlike$  for  $K_S^0$  candidates from Belle *signal MC*. The left is from true  $K_S^0$  and the right is from the fake  $K_S^0$ . In Belle, the standard cuts for  $K_S^0$  is  $nb\_vlike > 0.5$  and  $nb\_nolam > -0.4$ , which is shown as the green boxes [20].

Such a dedicated  $K_S^0$  classification tool is not implemented yet in BASF2 framework until 2019. Considered the limitation of NeuroBayes, the development of  $K_S^0$  classifier demands another algorithm and structure. The *Boosted Decision Trees* (BDT) is widely employed for multivariate classification and regression tasks in high energy physics field. Particularly, a speed-optimized and cache-friendly implementation of such a method called FastBDT (FBDT) is popularly used [36]. Compared to other popular classification algorithms such as TMVA [37], scikit-learn [38] and XG-Boost [39], FastBDT method is proven to be one order of magnitude faster during the training and applying phases [36]. By using FastBDT algorithm, *KsFinder* in Belle II is expected to give a single output which directly presents the goodness of a candidate of being a true  $K_S^0$ . Since the FastBDT algorithm depends on the variables that are differently distributed in signal and backgrounds, a set of training variables are selected based on  $K_S^0$  decay topology. The  $K_S^0$  variables used in the training of *KsFinder* might be differently distributed in different decay channels, therefore a *KsFinder* trained using MC sample from one channel may not be able to perform a good classification on the other. Thus, *KsFinder* is designed as a general package that pro-

vides a mode-dependent  $K_S^0$  classification which mainly consists of four components: *KsFinderSampler*, *KsFinderTeacher*, *KsFinderApplier* and *KsFinderTest*. *KsFinderSampler* is a function that automatically generates training and/or testing sample from mDST files where the cut-based reconstruction is used as explained in Section 3.1. *KsFinderTeacher* is responsible for extracting variables to perform training of the FastBDT model and generate a weight file containing all the node information in ROOT format, which also provides a function to communicate with BASF2 CDB so that users can share or download other weight file in their own analysis. *KsFinderApplier* can apply the weight file generated by *KsFinderTeacher* (or downloaded from BASF2 CDB) to the independent data sample and assign each  $K_S^0$  candidate a goodness index used as a single cut value in the further analysis. *KsFinderTest* is the evaluation function that can use a test sample to check for over-training, efficiency, and purity. By providing MC samples from certain decay modes, users can easily generate their own weight files of  $K_S^0$  classification that suit different decay modes. Such a design largely improves the flexibility of *KsFinder* compared to Belle MVA tool which indirectly classify  $K_S^0$  with two outputs.

### 3.2.2 Decay Topology of $K_S^0 \rightarrow \pi^+\pi^-$

As introduced in Section 3.2.1, the first step for developing  $K_S^0$  MVA classification is to determine the input variables for FastBDT algorithm that can represent the decay features of  $K_S^0$  against possible backgrounds. The remaining background of  $K_S^0 \rightarrow \pi^+\pi^-$  after the cut-based reconstruction comes from different sources, mainly including the false combination of tracks (including  $\pi^\pm$  misidentification), V0-like particle misidentification and self-looped tracks. For instance, a  $D^0/D^*$  from a  $B$  decaying to  $K\pi$  with  $K$  misidentified as  $\pi$ , could give a false combination of tracks. On the other hand, it's also possible that both of two tracks are correctly identified as  $\pi^\pm$  but they are not from the same mother particle, or the mother is not a  $K_S^0$  particle due to the missing of other daughters, such as  $D^+ \rightarrow K_S^0(\rightarrow \pi^+\pi^-)\pi^+$ . These two cases as the fake  $K_S^0$  are demonstrated in Figure 3-6.

The V0-like particles mainly refer to  $K_S^0$ ,  $\Lambda$  and  $\gamma$ .  $\gamma \rightarrow e^+e^-$  yield is significantly

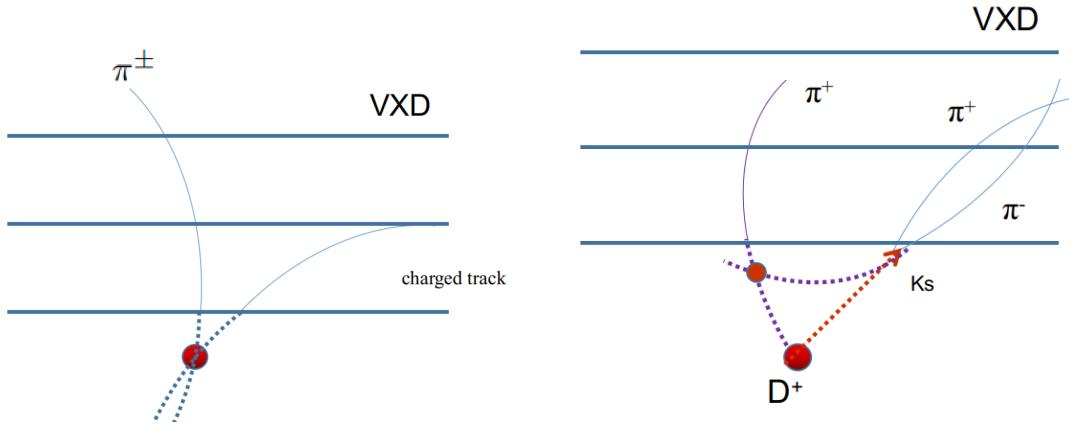


Figure 3-6: The left shows the case when a charged track (not  $\pi^\pm$ ) combined with a charged pion to form a fake  $K_S^0$ , the right shows the case when two daughters are correctly reconstructed as pions but not from the correct mother particle, which is falsely taken as a  $K_S^0$ .

lower than the other two types and the mass difference between pion and electron is very large, so the PID values can be used to well-distinguish them. As for the contribution of  $\Lambda \rightarrow p^+\pi^-$ , it happens when the positive charged tracks (proton track) is wrongly identified as  $\pi^+$ , see Figure 3-7 left. The key observable to distinguish this background is the invariant mass of mother particle, which is 1.115 GeV for  $\Lambda$ , much larger than the  $K_S^0$ . The number of left-over  $\Lambda$  after the cut-based reconstruction in section 3.1 is small, and can be further reduced by rejecting the candidates whose positive charged daughter has  $\text{PID}(\pi^\pm)$  smaller than  $\text{PID}(p)$ .

When a charged pion only carries a minimal of its mother's transverse momentum  $p_T$ , the curvature of its track may form a self-loop of which radius is comparable with the size of Belle II detector (mainly VXD and CDC). In this case, one charge pion could leave two charged tracks candidates with the opposite charge and similar  $p_T$ , with a possibility to form a converged vertex to form a fake  $K_S^0$ , see Figure 3-7 right.

### 3.2.3 Determination of training variables from $K_S^0$ decay

Given the characteristics of  $K_S^0 \rightarrow \pi^+\pi^-$  discussed in the previous section, a set of variables as training features of *KsFinder* can be selected. The set includes variables related to  $K_S^0$  kinematics, decay shape parameters, particle identifications and detec-

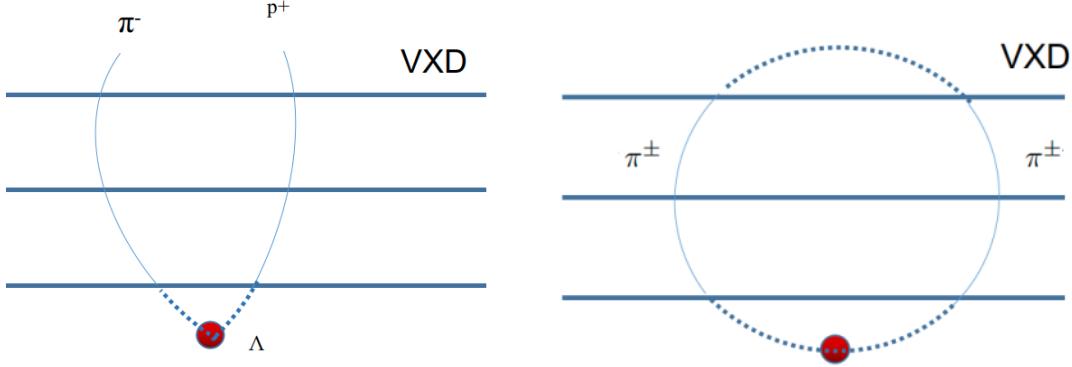


Figure 3-7: The left shows the  $\Lambda \rightarrow p^+\pi^-$  decay shape that can be treated as  $K_S^0$ , the right shows a self-loop formed by a low  $p_T$  charged pion reconstructed as two separated tracks with a vertex.

tor hits information. The summarized information of training variables is listed in Table 3.4.

Table 3.4: Summary of *KsFinder* input variables, where “lab” means angles in lab frame and “ $K_S^0$  CMS” means in  $K_S^0$  rest frame. Other variables are calculated in lab frame by default. The last column shows the number of the variables correspondingly.

$K_S^0$ variables(#)	Meaning	#
cosVertexMomentum	cosine of vertex and momentum direction (lab)	1
flight distance	$K_S^0$ flight distance along its momentum direction	1
significanceOfDistance	flight length from IP divided by relative error	1
cosHelicityAngleMomentum	cosine between $\pi^\pm$ and $K_S^0$ (lab)	1
ImpactXY	Impact parameters in transverse plane for $K_S^0$	1
x, y, z, px, py, pz	$K_S^0$ vertex position and momentum	6
p_D1(p_D2)	momentum magnitude for $\pi^+(\pi^-)$	2
pionID, muonID	PID values of $\pi^\pm$	2
decayAngle_D1(D2) <sup>1</sup>	angle between $\pi^+(\pi^-)$ and $K_S^0$ ( $K_S^0$ CMS)	2
daughterAngle2body	angle between $\pi^\pm$ (lab)	1
daughtersDeltaZ	Z-direction distance of two tracks helix	1
nSVDHits_D1(D2)	SVD detector hits of $\pi^+(\pi^-)$	2
nPXDHits_D1(D2)	PXD detector hits of $\pi^+(\pi^-)$	2
M(InvM)	$K_S^0$ invariant mass before (after) vertex fit	2

The cosine between  $K_S^0$  vertex and momentum direction (named *cosVertexMomentum*) is regarded as the most useful variable to separate true and fake  $K_S^0$ , which is originally used as an extra cut in the first measurement of  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  be-

<sup>1</sup>The decay angle of two daughters are essentially the equivalent variables because they are defined in the mother’s rest frame, which in future will be replaced by only one variable of the positive charged pion decay angle.

fore MVA based  $K_S^0$  classification tool was developed [40]. For instance, if a falsely reconstructed  $K_S^0$  is made of two tracks, it's likely that the momentum direction of the fake  $K_S^0$  is not aligned with the its vertex direction from IP. So the projection of vertex position of  $K_S^0$  on the reconstructed momentum direction could be negative value for fake  $K_S^0$ . While in case of a true  $K_S^0$ , such projection is almost always a positive value, shown in Figure 3-8. This often happens when the two tracks taken as  $\pi^\pm$  are accidentally crossed, or due to the misidentified tracks. The distribution of  $\cos\text{VertexMomentum}$  using *signal MC* is shown in the Figure 3-9. By requiring the cut  $\cos\text{VertexMomentum} > 0.9$ , fake  $K_S^0$  fraction can be reduced to about 20%, which is still not good enough.

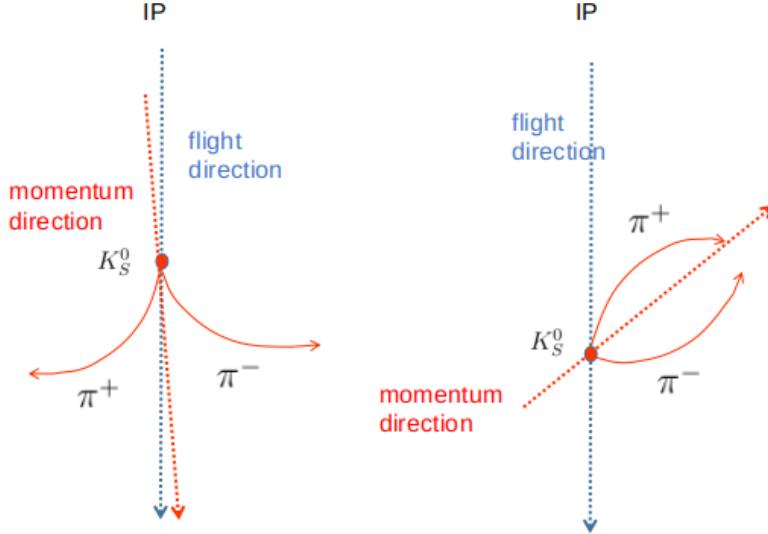


Figure 3-8: The left shows a true  $K_S^0$  decay shape where the cosine angle of  $K_S^0$  vertex position (blue dashed arrow) against reconstructed momentum direction (red dashed arrow) is positive. While the right shows a fake  $K_S^0$  decay shape where the cosine angle of  $K_S^0$  vertex position against the reconstructed momentum direction can be negative.

The other variables in Table 3.4 are not as contributive as  $\cos\text{VertexMomentum}$  in selecting true  $K_S^0$  and reject fake ones at the same time, but still important in increasing the discriminating power of FastBDT model. For instance, the significance of flight distance distribution is shown in Figure 3-10. The fake  $K_S^0$  can have relatively smaller significance because of the larger error of the vertex fit. FastBDT algorithm

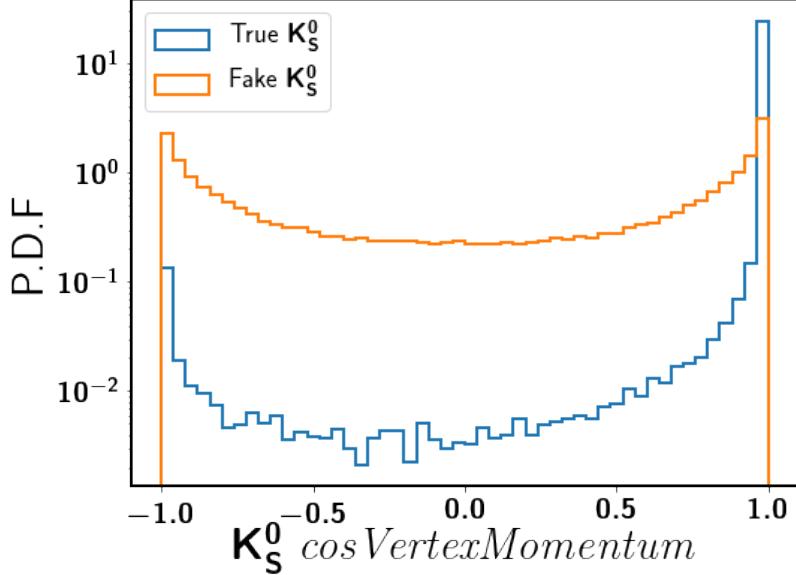


Figure 3-9: The distribution of  $\cos \text{VertexMomentum}$  using *signal MC*. The true and fake  $K_S^0$  ratio is set to be 1:1, where the most true  $K_S^0$  gives  $\cos \text{VertexMomentum} > 0.9$ .

can give the importance of each variable after the training, and the total classification ability of the model depends on the combined power of all input variables. By combining these variables, the rejection of fake  $K_S^0$  is targeted to be as good as the Belle *nisKsFinder*, which should exceed 95%.

Because FastBDT method relies on the distribution of variables to calculate signal and background separation, there are a few points to be checked before feeding the training sample to the model or applying the classification on real data. First, the distribution of the observables should be different in true  $K_S^0$  and the fake ones, so the FastBDT classifier can effectively separate the true and the fake  $K_S^0$  at each node to maximize the separation gain. Second, there will a correlation among the training observables and they should also be different in signal and background. The boosting step will create a sequence of shallow decision trees (DT) whose structures are not the same. Different correlations helps improve the performance of decision trees in tuning of structure. For instance, a true  $K_S^0$  flights longer (flight distance) due to larger momentum in general, so the number of daughter detector hits (nSVDHits\_D1 or nSVDHits\_D2) becomes fewer. Then these two observables have negative correlations

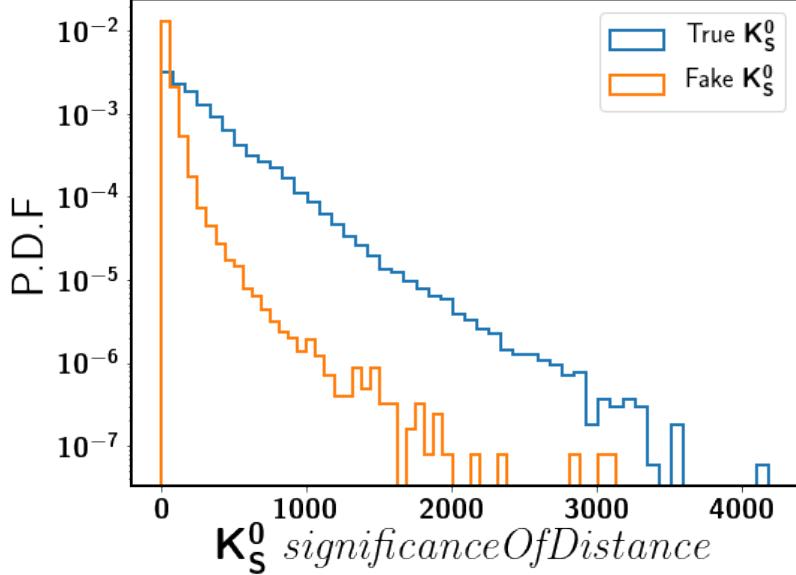


Figure 3-10: The distribution of  $significanceOfDistance$  using *signal MC*. The true and fake  $K_S^0$  ratio is set to be 1:1, where the most fake  $K_S^0$  are distributed in  $significanceOfDistance < 1000$  region.

in true  $K_S^0$ . In case of a fake  $K_S^0$ , the flight length could be a deep outside of VXD but daughters may have full hits on SVD, without strong correlation, see Figure 3-11 . At last, one should also avoid using many observables with too strong correlations, since in this case, many DTs might have a potentially equivalent structure in the boosting step. Therefore, the separation power of many DTs doesn't gain any improvement and the collection of observables might be redundant. The correlation between variables are shown in Figure 3-11.

### 3.2.4 Training, Applying and Testing of *KsFinder*

The variables are internally registered inside the *KsFinder* so it can automatically retrieve their values from a mDST file in BASF2. The Table 3.5 shows the abbreviations of the input variables used in the *KsFinder*. The first step of using *KsFinder* is to call *KsFinderSampler* on a MC sample to generate training and testing data sample. To show the flexibility and stability of *KsFinder* on different modes, *KsFinderSampler* extracts MC data points from both *signal MC* and *generic MC* (see MC definition in section 2.9), respectively. Also, it can separately sample true and fake  $K_S^0$ . In this

Table 3.5: The abbreviations of the input variables used in the training of *KsFinder*.

Observables	Abbreviations
cosVertexMomentum	cosVe
flight distance	fligh
significanceOfDistance	signi
cosHelicityAngleMomentum	cosHe
ImpactXY	Impac
x	x
y	y
z	z
px	px
py	py
pz	pz
p_D1	p_D1
p_D2	p_D2
muonID_pi	muonI
pionID_pi	pionI
decayAngle_D1	decay1
decayAngle_D2	decay2
daughterAngle2body	daugh2
daughtersDeltaZ	daugh1
nSVDHits_D1	nSVDH1
nSVDHits_D2	nSVDH2
nPXDHits_D1	nPXDH1
nPXDHits_D2	nPXDH2
M	M
InvM	InvM

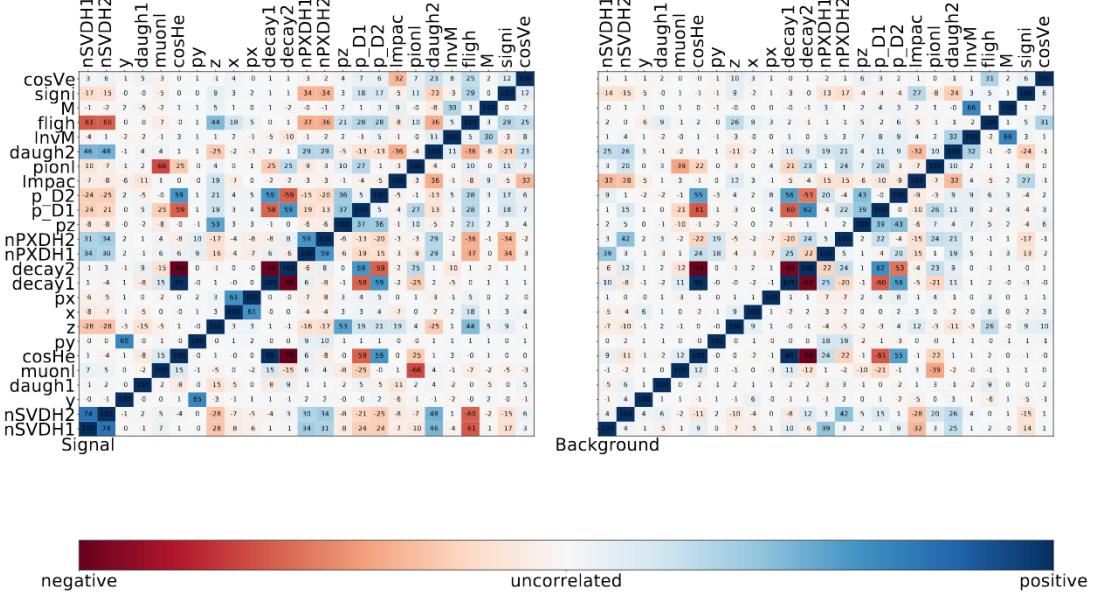


Figure 3-11: The correlation between input variables for *KsFinder*. As the given example, flight length has negative correlation with SVD hits in signal while uncorrelated in background.

analysis, we are looking for the  $K_S^0$  specifically from  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  decay, of which the branching fraction is  $6 \times 10^{-6}$  according to the PDG value. In the *generic MC*, the fraction of  $K_S^0$  from  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  is quite low even among the true  $K_S^0$ . Most of the  $K_S^0$  particles in the *generic MC* are from the decays related to  $c \rightarrow s$  transition. If the true and fake  $K_S^0$  are unbalanced, it may not be optimized for the training of *KsFinder*. Therefore, *KsFinderSampler* is configured to extract true  $K_S^0$  from *signal MC*, where the majority of  $K_S^0$  from  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$ . The true  $K_S^0$  in *signal MC* may contain some candidates from tag-side generic decay, where the fraction is estimated below 5% on average. Hence, there are two types of training samples prepared. First, (a) a true  $K_S^0$  sample is composed of 95000 true  $K_S^0$  from  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  and 5000 true  $K_S^0$  from *generic MC*, to allow the *KsFinder* learn from both cases. Second, (b) we directly sample 100000 true  $K_S^0$  only from *generic MC*. For both cases, the fake  $K_S^0$  are sampled from *generic MC* with the same number as the true  $K_S^0$ . The testing samples corresponding to these two training samples are prepared in the same way. As for the FastBDT training options, the *KsFinder* configures that the depth of each DT is 3, learning rate is 0.3 and the boosting steps is 200.

To train the *KsFinder*, *KsFinderTeacher* function is called and weight files are saved. To apply the classification of  $K_S^0$ , *KsFinderApplier* reads in the testing samples and calculate the output using saved weight files, so that each  $K_S^0$  candidate is assigned with a goodness index named *FBDT\_Ks*. It ranges from 0 to 1 where 1 stands for the best goodness. To evaluate the performance of *KsFinder*, *KsFinderTest* is called which compares the results between the training sample and the testing sample, including the over-training check.

### 3.2.5 The Performance and Over-training check

To evaluate the performance of *KsFinder* on both (a) and (b) samples, signal efficiency, background rejection and purity are calculated by cutting on the different values on *FBDT\_Ks*, as defined:

$$\text{signal efficiency} = \frac{\text{Number of true } K_S^0 \text{ with } FBDT\_Ks > \text{cut value}}{\text{Number of all true } K_S^0}, \quad (3.1)$$

$$\text{background rejection} = \frac{\text{Number of fake } K_S^0 \text{ with } FBDT\_Ks < \text{cut value}}{\text{Number of fake true } K_S^0}, \quad (3.2)$$

$$\text{purity} = \frac{\text{Number of true } K_S^0 \text{ with } FBDT\_Ks > \text{cut value}}{\text{Number of all } K_S^0 \text{ with } FBDT\_Ks > \text{cut value}}. \quad (3.3)$$

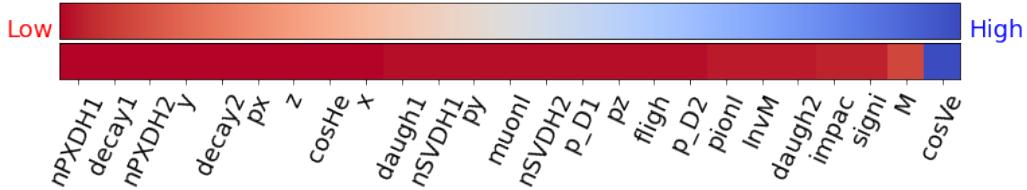


Figure 3-12: The importance rank of the input variables for *KsFinder*. The *cosVertexMomentum* is the most important variable.

The ROC (receiver operating characteristics) curve is usually taken as an indicator of the performance where the curve shows the dependence of background rejection power with respect to the signal efficiency. The larger area under a ROC curve means that the better performance is achieved. The ROC curves as well as the efficiency & purity with respect to the *KsFinder* cut are shown in Figure 3-13 and Figure 3-14,

where the former is for sample (a) and the latter is for sample (b). With increasing the efficiency, the cut on the output of *KsFinder* is getting loose. The background rejection only starts to drop when the efficiency exceeds about 90% in both training and testing sample.

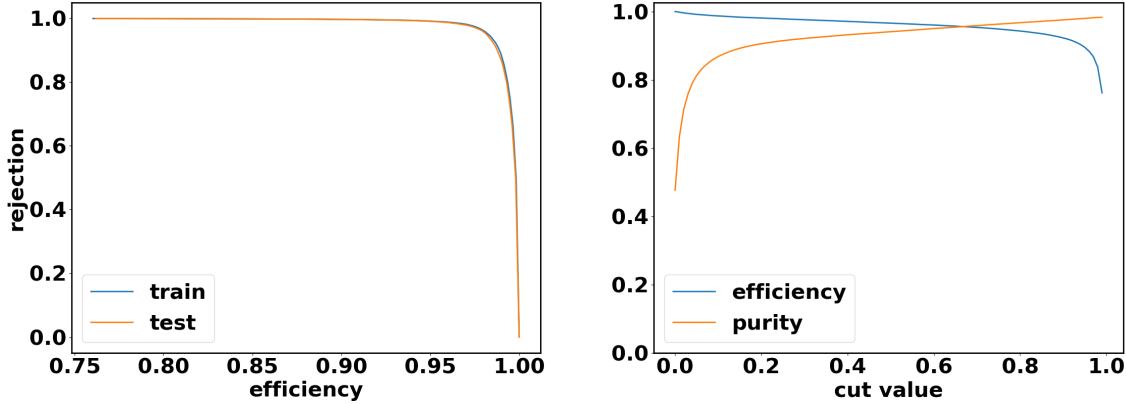


Figure 3-13: The left is ROC curve(blue for training and orange for testing) and the right is efficiency and purity (blue for efficiency and orange for purity) depending on cut of *KsFinder* output. The results are obtained by applying the weight file from training sample (a) to testing sample (a).

Because the ROC curves are consistent in the training and testing samples, it proves the absence of noticeable over-training in classification, however, the detailed check can be made by comparing the distributions of *KsFinder* output on true and fake  $K_S^0$  in training and testing samples. Therefore, the distribution of input variables in the true and fake  $K_S^0$  in training and testing sample with respect to the *KsFinder* output are plotted, where a distinctive separation for both sample (a) and sample (b) are shown and no over-training is found, as shown in Figure 3-15.

The best cut value for *FBDT\_Ks* is determined by maximizing the “Figure of Merit” (FOM), as shown Equation 3.4, where  $S$  and  $B$  is the number of true and fake  $K_S^0$  after the cut, respectively.

$$\text{FOM} = \frac{S}{\sqrt{S + B}} \quad (3.4)$$

The FOM distribution depending on the cut value of *FBDT\_Ks* is shown in Figure

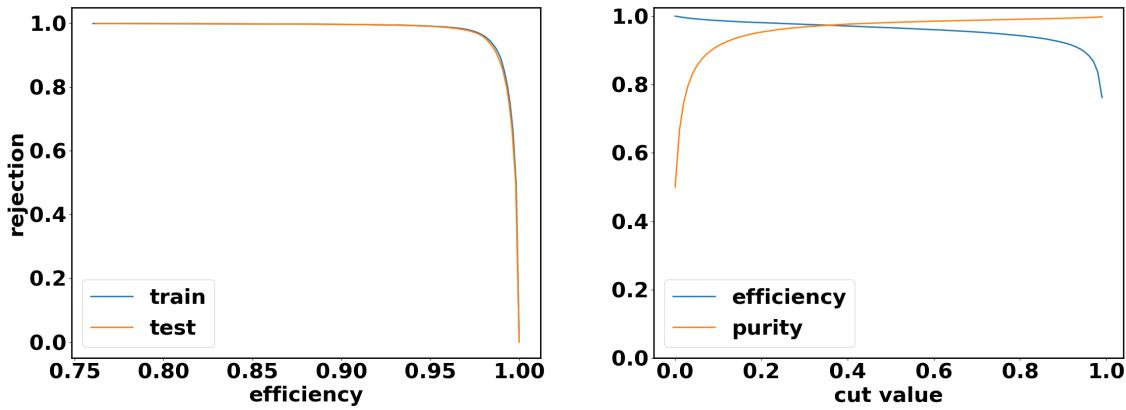
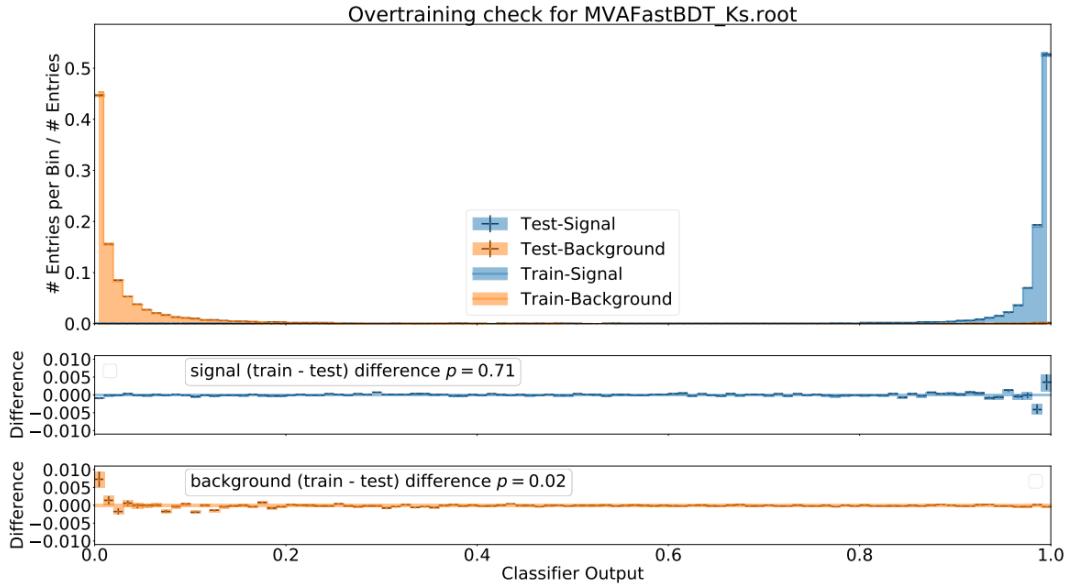


Figure 3-14: The left is ROC curve (blue for training and orange for testing) and the right is efficiency and purity (blue for efficiency and orange for purity) depending on cut of *KsFinder* output. The results are obtained by applying weight file from training sample (b) on testing sample (b).

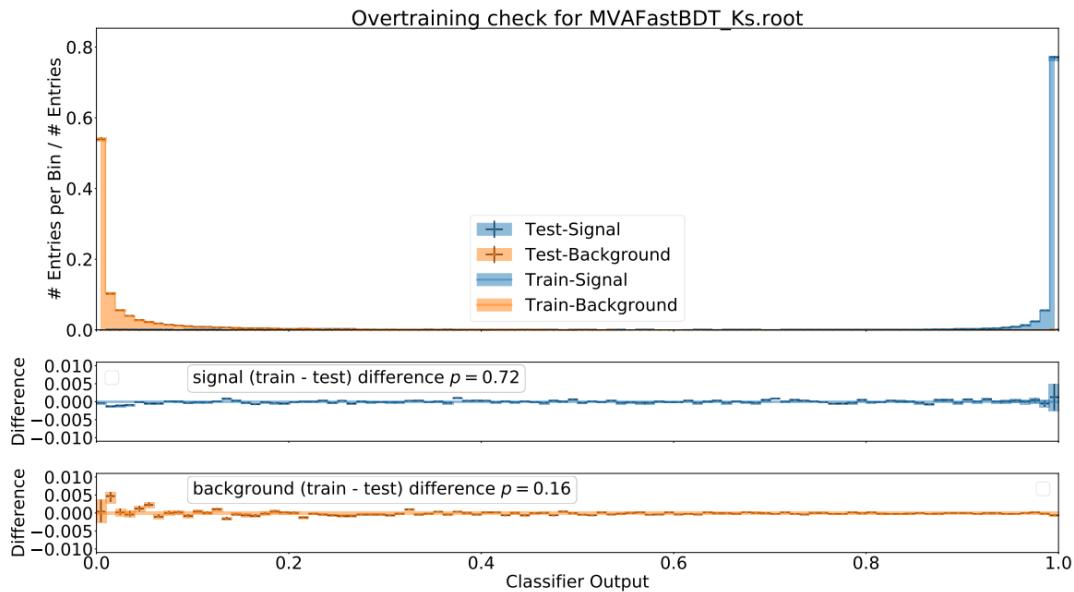
3-16. In this analysis, we primarily focus on the  $K_S^0$  from  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$ , thus the weight file from (a) is chosen to perform  $K_S^0$  classification since it is supposed to learn more on  $K_S^0$  from our analysis channel. The maximum FOM is achieved at *FBDT\_Ks* = 0.74, which is going to be used as the cut value to further reject fake  $K_S^0$ . The FOM curve is not sensitive to the cut value in between 0.5 ~ 0.9, which achieves similar performance on average.

To demonstrate the improvement from using *KsFinder*, the *KsFinder* cut is applied to the cut-based selected  $K_S^0$  sample additionally based on the sample used in Figure 3-2. The true  $K_S^0$  fraction before applying *KsFinder* cut is 39%, and 95% of them are kept after the cut is applied. In the meantime, the fake  $K_S^0$  fraction before applying the cut is 61%, and 98% of them are rejected after the cut is applied. The purity of the  $K_S^0$  candidates is largely improved as shown in Figure 3-17.

The comparison of  $K_S^0$  reconstruction performance using different cuts and approaches is summarized in Table 3.6. It is clear that *KsFinder* can provide a better  $K_S^0$  reconstruction performance using 25 input variables compared to only use cuts on one or two important variables. The importance to the output of *KsFinder* of each variable is obtained from the *KsFinderTest*, where *cosVertexMomentum* has the highest rank, shown in Figure 3-12. From Figure 3-13 and 3-14, the purity can exceed 95%



a) Over-fitting check for sample (a).



b) Over-fitting check for sample (b).

Figure 3-15: The over-training check based on the comparison between training/testing data points in both *signal* and *generic MC*.

Table 3.6: The summarized performance of  $K_S^0$  reconstruction in different approaches. The Belle II results are based on the cut-based reconstruction, with extra cuts from  $\cosVertexMomentum(\text{cosVe})$ ,  $\text{significanceOfDistance}(\text{signi})$  and  $\text{KsFinder}$ .

Cuts	Efficiency	purity	BKG rejection
Belle(default): $\text{nb\_vlike} > 0.5 \& \text{nb\_nolam} > -0.4$	90%	95%	95%
Belle II cut: $\text{cosVe} > 0.9$	96%	82%	80%
Belle II cut: $\text{cosVe} > 0.9 \& \text{signi} > 50$	92%	89%	89%
Belle II $\text{KsFinder}$ cut: $\text{FBDT\_Ks} > 0.74$	95%	97%	97%

by choosing proper cut value. Instead, by only applying  $\cosVertexMomentum > 0.9$  on the cut-based selections, purity can only reach about 80%, demonstrating the necessity of including more variables to improve the power of classification despite that each variable may only weakly discriminate the true and fake  $K_S^0$ .

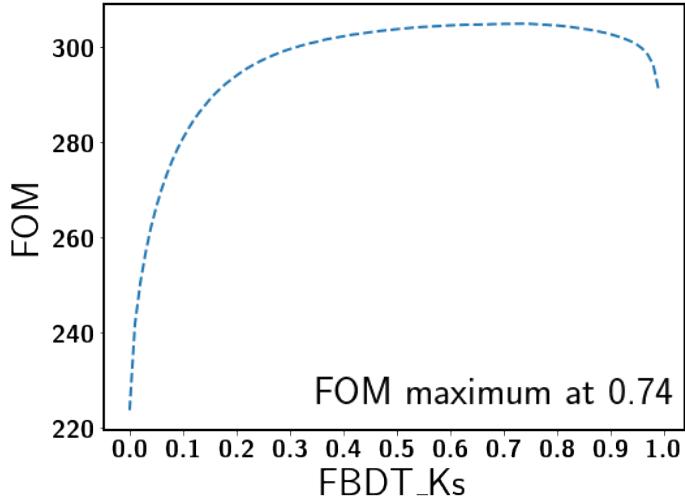


Figure 3-16: FOM of classifier output ( $FBDT\_Ks$ ) in *signal MC*, the maximum value is achieved at 0.74. The FOM curve is almost flat between  $0.5 \sim 0.9$ , which is insensitive to the cut value in this region.

### 3.2.6 Data Validation for $\text{KsFinder}$

The results from MC studies show an excellent performance of  $\text{KsFinder}$ . However, the validation of such a tool on the real experiment data is necessary. Since there's no MC truth on target variable in real data, the FastBDT method is based on variables in MC samples. If these variables shows close distributions among MC and data, the classifier obtained using MC can be applied to the real data with the expectation of

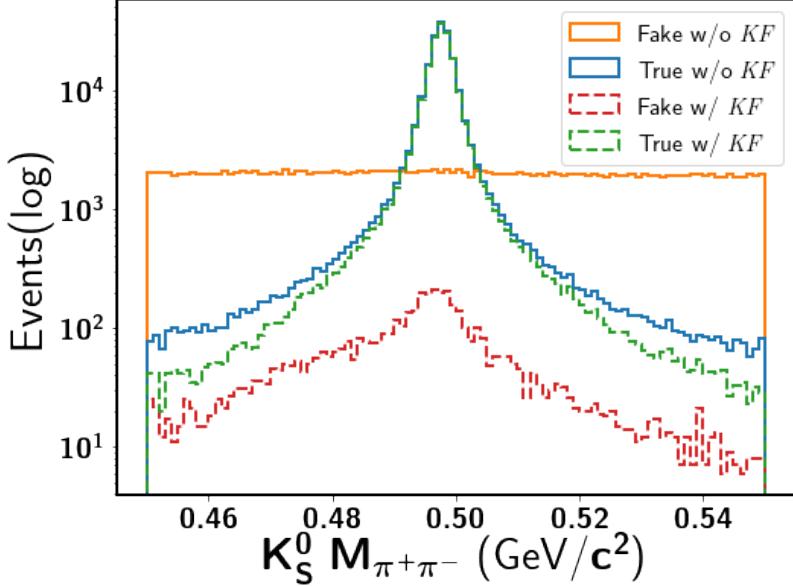


Figure 3-17:  $K_S^0$  purity improvement with  $KsFinder(KF)$  cut at 0.74. The blue solid line is true  $K_S^0$  without  $KsFinder$  and green dashed line is the true  $K_S^0$  with the cut applied. The orange solid line is fake  $K_S^0$  without the cut and the red dashed line is fake  $K_S^0$  with the cut. About 95% of true  $K_S^0$  are kept while 98% of the fake ones are rejected by applying the cut.

the close performance. In addition, due to the fact that  $K_S^0$  candidates are used for the further reconstruction of  $B^0$ , the mass and energy distributions may change after applying the cut, thus it is also required to show that no clear bias on  $B^0$  for signal extraction.

For comparison between MC and data, a small data sample from Belle II experiment 7 and 8 is used. The integral luminosity at  $\Upsilon(4S)$  resonance for this data sample is  $5.17 \text{ fb}^{-1}$ . The MC sample is extracted from *generic MC* with equivalent luminosity. Data and MC events are filled in the binned histogram of each variables to check the consistency. The number of events in each bin is assumed to follow the *Poisson Distribution*, which is approximately equivalent to the *Gaussian* distribution when the number of events is large enough according to the *Central Limit Theorem*. Therefore the standard deviation of each bin is calculated as  $\sqrt{N_i}$  using *Poisson* distribution property, where  $N_i$  is the event number in the  $i$ -th bin. We use three times the standard deviation in each bin as a conventional reference in the drawing error bars. For example, the Figure 3-18 shows the invariant mass and momentum distri-

butions from data and MC samples. The *generic MC* is shown in blue solid lines with no *KsFinder* cut used. Similarly, data without using *KsFinder* is shown in yellow dots, which are closely distributed as the *generic MC*, indicating a good data-MC consistency. The purple solid lines are presenting the  $K_S^0$  distribution in *generic MC* with *KsFinder* cut at 0.74, while the red dots are the  $K_S^0$  in data after using the same *KsFinder* cut. To compare the number of events ratio between data and MC, a ratio distribution is also produced for each variable below the main comparison plot, where the blue circle dots are the data/MC ratio without *KsFinder* cut and red reverse-triangle dots are the ones with *KsFinder*. The distribution plots of invariant mass and momentum are shown in Figure 3-18. After applying *KsFinder* cut, it shows about 20% difference on the data/MC ratio, indicating the data is reduced more than the *generic MC* on the *KsFinder* cut. The distribution plots of *cosVertexMomentum* is shown in Figure 3-19. The ratio plot of *cosVertexMomentum* shows a discrepancy in the background dominated region ( $\text{cosVertexMomentum} < 0.0$ ), while remains close to 1 for the signal dominated region ( $\text{cosVertexMomentum} > 0.5$ ) after the *KsFinder* cut. These discrepancies will be monitored and improved in future by the better data and MC match-up. The full distributions comparison between data and *generic MC* by using *KsFinder* cut are included in the Appendix A.

Not only the similar distributions of the input variables are important for applying *KsFinder* trained from MC to the real data, the correlations between these variables should also be similar between data and MC. This requires the comparison of the correlation matrices using true and fake  $K_S^0$ . However, because it is hard to precisely know whether a  $K_S^0$  from data is definitely a true candidate or not, it is difficult to directly compare the correlation among data and MC in true and fake  $K_S^0$  separately. One possible solution to obtain the true  $K_S^0$  sample in real data is to use other control channels which contain at least one  $K_S^0$  in the decay chain and have very high purity even without *KsFinder*. In the early stage of the Belle II, the preparation of such clean control samples is not ready, especially for the multi-body hadronic  $B$  decays that are similar to  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  with more than one  $K_S^0$ . This will be an advanced topic for widely validating *KsFinder* in the future, which is not implemented in this

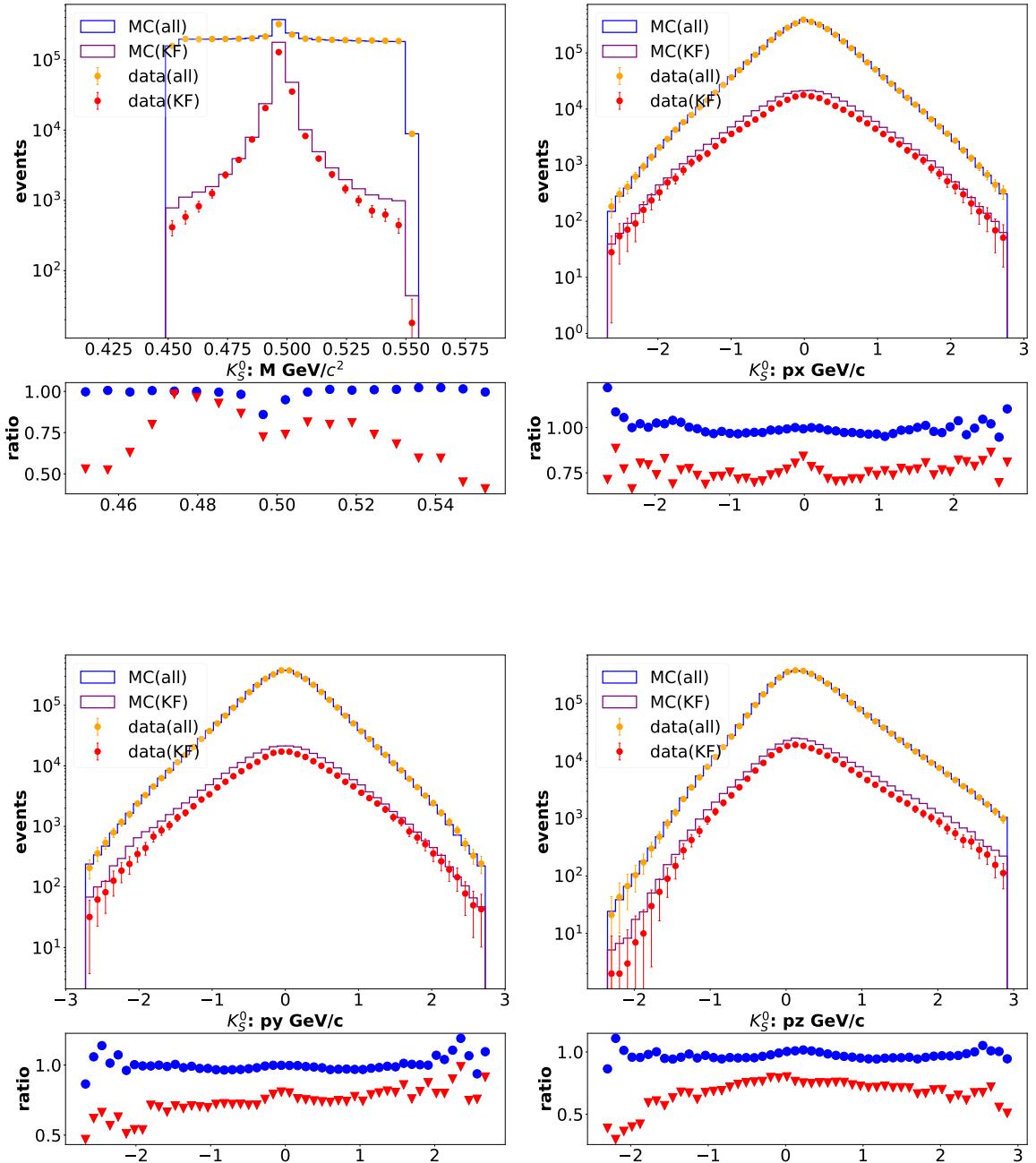


Figure 3-18: The distribution of invariant mass from charged pions and the momentum of  $K_S^0$  in  $x, y, z$  directions. The blue line is from all *generic MC* and the purple line is the  $K_S^0$  after *KsFinder* (KF). The yellow dots are data with no *KsFinder* (KF) cut applied and the solid red dots are data after applying the same cut. The bottom sub-plots are the data/MC ratio before and after applying *KsFinder* in data (blue) and *generic MC* (red).

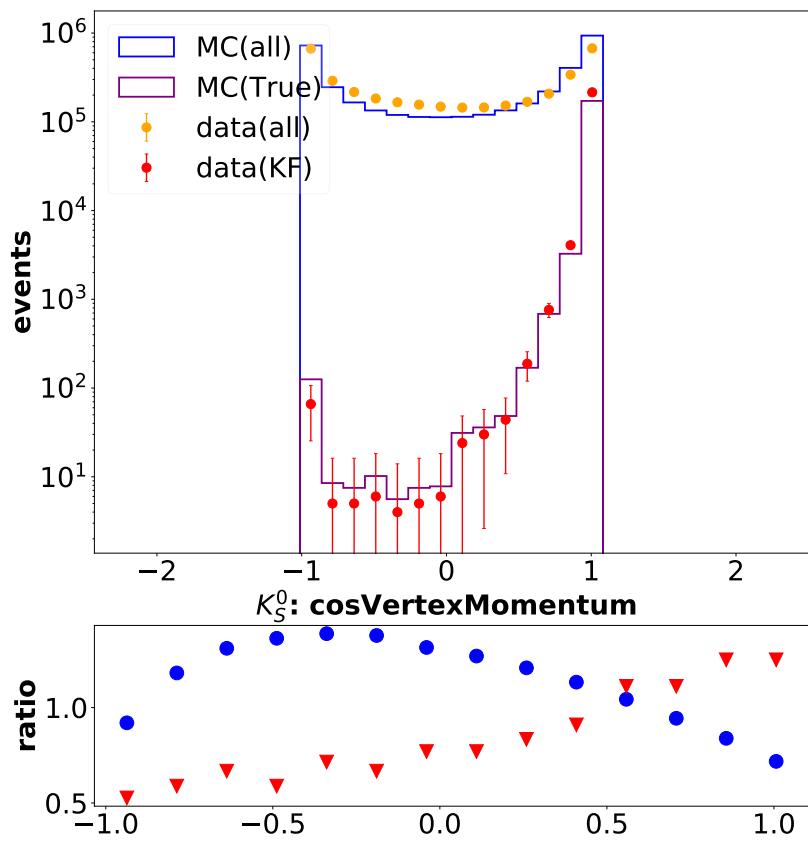


Figure 3-19: The distribution of  $\text{cosVertexMomentum}$  in data and MC with or without  $KsFinder$  cut applied.

thesis. Hence, instead of using clean control samples containing very high purity  $K_S^0$  collections, we just compare the correlation matrices for both true and fake  $K_S^0$  together in data and *generic MC*, where the correlation in data is divided by the correlation in MC, as shown in Figure 3-20. The most of the variables present the close correlation factor between data and MC, while the  $z$  momentum presents a largely different correlation with the daughter tracks distance in  $z$  direction. The *cosVertex-Momentum* only shows a different correlation with the  $y$ -direction momentum, which is acceptable due to the low importance of the  $y$ -direction momentum. The differently correlated variables are mostly low ranked, and no appearance of the large difference among the high ranked variables is observed. In the future, such discrepancies will be monitored with improved simulation along with the data recording.

### 3.2.7 Data and MC correction by *KsFinder*

As the previous section shows, implementing *KsFinder* cut on data may induce bias on the event numbers for  $K_S^0$  because the training set of *KsFinder* is extracted from MC. To compensate such potential effect, a ratio as the data and MC correction is calculated based on the expected signal yield after using *KsFinder*. A maximum likelihood fit on invariant mass for  $K_S^0$  with  $FBDT_{Ks} > 0.74$  is performed, where signal shape is modeled as a triple-Gaussian and background shape is modeled as a Chebyshev polynomial. The signal yield fraction is defined as:

$$f_{K_S} = \frac{N_{sig}}{N_{tot}}, \quad (3.5)$$

where  $N_{sig}$  is the signal number from the fit result and  $N_{tot}$  is the total events number. The fit is performed on both *generic MC* and data to obtain  $f_{K_S}$ , respectively, as shown in Figure 3-21, where the left is for data and the right is for *generic MC*. The fit results are  $0.933 \pm 0.008$  for *generic MC* and  $0.924 \pm 0.006$  for data. The fraction of the true  $K_S^0$  in *generic MC* sample is 0.939, consistent with the fit result. The  $\mathcal{R}_{K_S}$  is defined as the ratio of signal yield fraction  $f_{K_S}$  from *generic MC* and data as

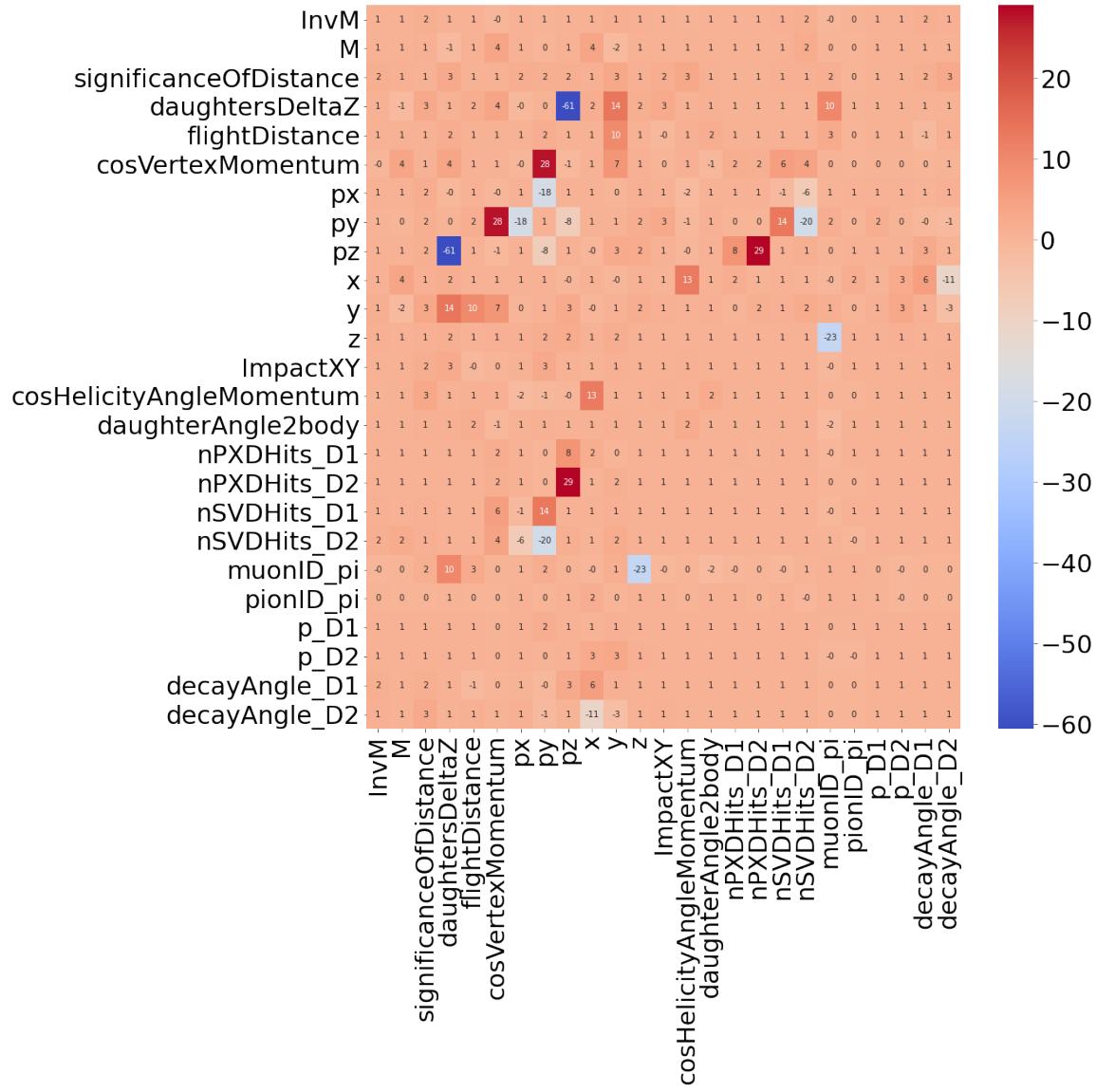


Figure 3-20: The correlation ratio between *KsFinder* input variables, where the value is calculated by using the one from data divided by that from *generic MC*.

shown in Equation 3.6.

$$\mathcal{R}_{K_S} = \frac{f_{K_S}^{MC}}{f_{K_S}^{data}} \quad (3.6)$$

By applying the *KsFinder* cut at 0.74, the  $\mathcal{R}_{K_S}$  is calculated to be  $1.009 \pm 0.011$  from the  $f_{K_S}$ . Similarly, the ratio for data and *generic MC* in terms of the number of  $B^0$  can be defined as:

$$\mathcal{R}_{B^0} = \frac{f_{B^0}^{MC}}{f_{B^0}^{data}} \simeq \mathcal{R}_{K_S}^3, \quad (3.7)$$

Since the final state consists of three  $K_S^0$ , the  $\mathcal{R}_{B^0}$  is expected to be the cube of  $\mathcal{R}_{K_S}$ , with the uncertainty propagated from the uncertainty of  $\mathcal{R}_{K_S}$ . By using  $\mathcal{R}_{K_S} = 1.009 \pm 0.011$ , the result of  $\mathcal{R}_{B^0}$  is  $1.027 \pm 0.033$ , which is close to one within its uncertainty. Hence, the correction  $\mathcal{R}_{B^0}$  is not applied in signal extraction of  $B^0$ , but the impact is taken into account as a possible source of systematic uncertainty. We take the larger one among the center value shift of  $\mathcal{R}_{B^0}$  (0.027) and the uncertainty of  $\mathcal{R}_{B^0}$  (0.033) as the systematic uncertainty source in the *CP* measurement. Thus, the  $\mathcal{R}_{B^0} = 1.033$  and  $\mathcal{R}_{B^0} = 0.967$  are applied to the calculation of the signal fraction when performing the systematic uncertainty evaluation in *CP* violation measurement.

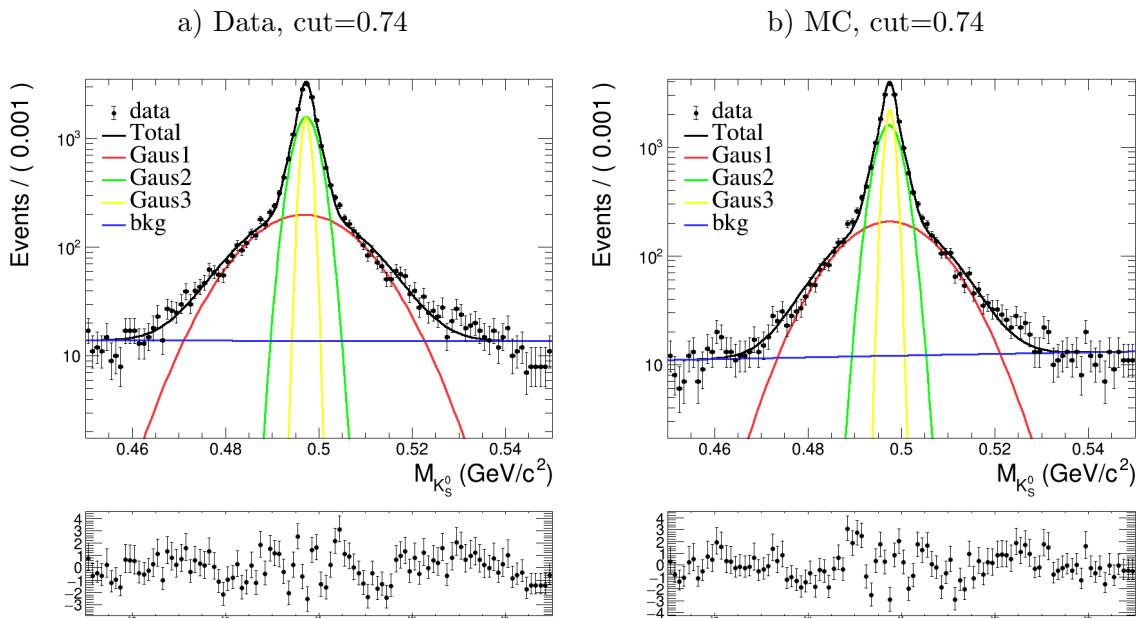


Figure 3-21: The fit on invariant mass  $M_{K_s^0}$  where signal component is modeled as a triple-Gaussian and background component is modeled as a Chebyshev polynomial. The bottom plots are the pull of the fitted lines and data points. The signal fraction is slight higher in *generic MC* compared to that in data.



# Chapter 4

## $B^0$ reconstruction and event selection

As introduced in section 2.9, the branching fraction of  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  is  $6.0 \times 10^{-6}$ . The simulation sets the  $\Upsilon(4S)$  as the mother particle then  $\Upsilon(4S)$  decays into two scalar  $B^0$  mesons with mixing.  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  decay process is simulated based on the possible phase-space the final state particles could obtain, where no  $CP$  violation is implemented in the generator level, meaning that the input of  $\mathcal{S}(\sin 2\phi_1)$  and  $\mathcal{A}$  are both zero.

### 4.1 $K_S^0$ Selection

$K_S^0$  is first reconstructed by the cut-based method using two charged pions which contains a large fraction of fake candidates, as discussed in chapter 3 and Table 3.1. In addition, a cut on  $K_S^0$  is used considering momentum distribution of  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$ , where the huge fake  $K_S^0$  appear in low momentum region. Only the  $K_S^0$  candidates with momentum larger than 0.05 GeV are selected, as shown in Figure 4-1. To further reduce the fake candidates in  $K_S^0$  using *KsFinder*, only  $K_S^0$  with *FBDT\_Ks* larger than 0.74 are kept.

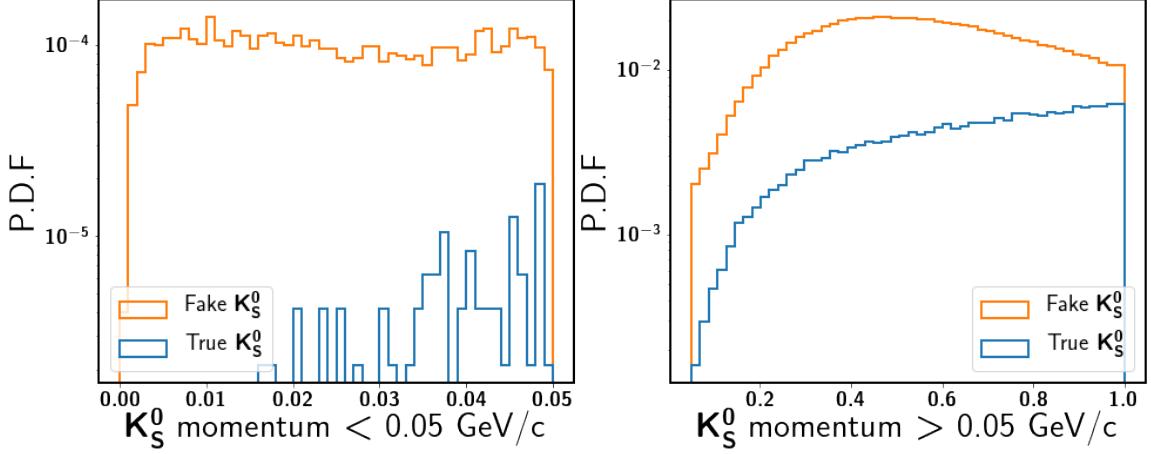


Figure 4-1: The distribution of  $K_S^0$  momentum. Candidates smaller than  $0.05\text{GeV}/c$  are rejected.

## 4.2 $B^0$ Reconstruction

By combining three  $K_S^0$  particles from selected  $K_S^0$  candidates,  $B^0$  candidates can be reconstructed. The beam-constraint mass  $M_{bc}$  and energy difference  $\Delta E$  are used to extract signal, as defined in Equation 4.1 and 4.2, respectively.

$$M_{bc} = \sqrt{\frac{s}{4} - p_B^{*2}} \quad (4.1)$$

$$\Delta E = E_B^* - \frac{\sqrt{s}}{2} \quad (4.2)$$

For  $M_{bc}$ ,  $\sqrt{s}$  is defined as the invariant mass of the center-of-mass which is calculated from the beam energies and  $p_B^*$  is the reconstructed  $B$  momentum in the center-of-mass frame. For  $\Delta E$ ,  $E_B^*$  is the reconstructed energy in the center-of-mass frame. These two variables are quite useful for discriminating signal and background events for hadronic  $B$  decay with fully reconstructed final states.

In Belle II, the  $B^0$  candidates with  $M_{bc} > 5.2 \text{ GeV}$  and  $|\Delta E| < 0.2 \text{ GeV}$  are required. The vertex information of the fully reconstructed  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$ , called as  $CP$ -side, is obtained by the vertex fit using *TreeFit* and the  $\chi^2$  probability of the fit is calculated. Only  $B^0$  candidates with converged vertex fit results are kept by a very loose cut of  $P(\chi^2) > 0.001$ . On the other hand, the  $CP$  violation measurement

does not require the certain decay mode of the other  $B^0$  meson in the Rest-Of-Event. The  $B$  meson in the Rest-Of-Event is called as tag-side  $B$  since this  $B$  is used to tag the flavor of  $CP$ -side  $B$ . Thus, no full  $B^0$  reconstruction on the tag-side is performed, meaning that the vertex information can not be obtained by the specific final states. Considering this strategy, the vertex fit on the tag-side is done by *KFit* that only takes advantage of well-reconstructed charged particle tracks. The vertex on the tag-side are required to be located inside the standard PXD region, despite that PXD is not fully installed yet. In future, such requirement is subjected to be modified by the PXD hits requirements.

After performing the vertex fit for both  $CP$ -side and tag-side, we check the potential impact of applying *KsFinder* on the reconstructed vertex positions, as well as the impact on the  $M_{bc}$  and  $\Delta E$ . It is necessary for mainly two reasons. First, the *KsFinder* might change the original distributions of  $M_{bc}$  and  $\Delta E$  of  $B^0$  candidates, which are used for the signal extraction. The signal extraction will provide the signal fraction information that is used during the  $CP$  parameters measurement. Second, the *KsFinder* might introduce the bias on the distribution of the vertex positions of  $B^0$ . The  $K_S^0$  candidates with less SVD hits on their daughter pion tracks usually have poorer reconstruction quality and more likely to be rejected as fake candidates. Therefore, we check the distribution of  $M_{bc}$  and  $\Delta E$  before and after the applying *KsFinder*, as well as the distribution of vertex positions on the  $z$ -axis. The details about the comparison can be found in the Appendix E. In conclusion, applying *KsFinder* have a negligible impact on  $M_{bc}$ ,  $\Delta E$  and the vertex positions on the  $z$ -axis. The contribution of *KsFinder* as a possible systematic uncertainty source mainly comes from the different data and MC responses of the  $K_S^0$  classification, as discussed in the section 3.2.7.

When multiple  $B^0$  candidates are obtained in a single event, the best candidates selection (BCS) is performed by ranking their  $\chi^2$  of the  $CP$ -side vertex fit. Since the BCS is based on the  $\chi^2$  that might introduce bias in the vertex positions for  $CP$  fit, we check the distribution of the vertex  $\chi^2$ , as shown in Figure 4-2 top left where the data and *generic MC* present a good consistence within  $1\sigma$  on average. The

distribution of the candidate number per event without BCS is shown in top right of Figure 4-2 as well, showing an agreement between data and *generic MC* within  $1\sigma$ . The distribution of the candidate number per event from the *signal MC* is also in the bottom left of Figure 4-2. The 2D distribution of  $M_{bc}$  and  $\Delta E$  from  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  *signal MC* is shown in Figure 4-2 bottom right, where the correlation factor is about 15% between two observables.

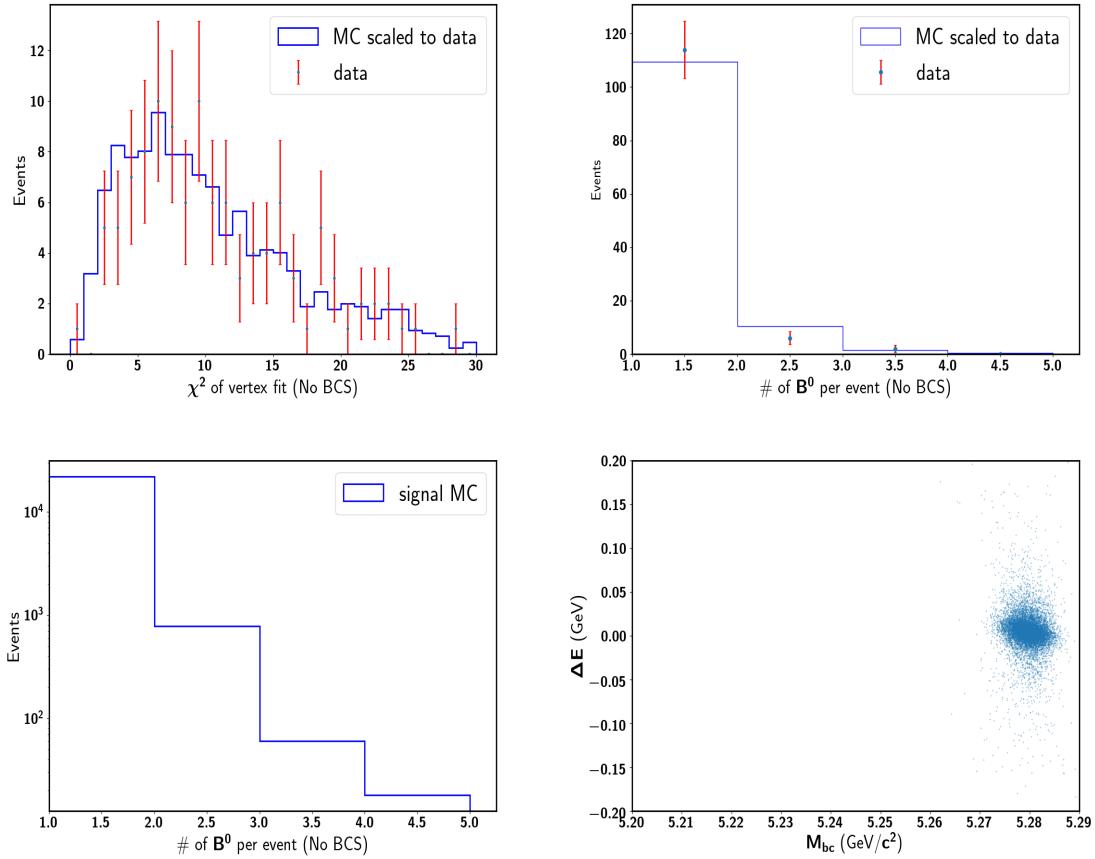


Figure 4-2: Top left is the  $\chi^2$  for data and *generic MC* before BCS. Top Right is the  $B^0$  candidates per event in data and *generic MC* before the BCS. Bottom left is the number of  $B^0$  candidates per event from *signal MC*. Bottom right is the 2D  $M_{bc}$  and  $\Delta E$  distribution from *signal MC*.

## 4.3 Continuum Suppression

The generic decay of  $\Upsilon(4S)$  produces neutral and charged  $B$  mesons, as well as other flavor mesons  $q\bar{q}$ . Since the branching fraction of  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  is relatively low, the  $B^0$  candidates after the reconstruction contains a large fraction of fake ones if no special reduction on  $q\bar{q}$  is applied. The  $q\bar{q}$  background events are distributed as a continuum-like shape in the distribution of  $M_{bc}$  and  $\Delta E$ . This calls a demand to distinguish  $B\bar{B}$  decay events from  $q\bar{q}$  events, which is called as continuum suppression (CS). The rejection is essential because it's the dominated background in this analysis. The most useful information to reject  $q\bar{q}$  events is to use the event shape information. In a  $B\bar{B}$  event, two mesons are produced almost at rest in the CMS frame since the resonance state  $\Upsilon(4S)$  is just slightly lighter than the beam energy. As a result, decay products are emitted more isotropically compared to continuum background events which are more jet-like, back-to-back flying out from the interaction region. The ARGUS and CLEO collaboration [41] developed a set of variables to suppress the continuum background, which has also been implemented into BASF2 framework. The two major sets of variables are the CLEO cone momentum and the modified Super Fox-wolfram momentum.

CLEO cone momentum can be presented as Equation 4.3, where  $p_i$  is momentum of i-th particle in the Rest-Of-Event. The particles used in a reconstructed  $CP$ -side  $B^0$  are therefore excluded. The  $\theta_i$  is an angle against momentum thrust of reconstructed  $CP$ -side  $B$  meson. The angle is divided into the binned intervals in nine cones of 10 degrees around the thrust. The  $L_n$  stands for the combination that includes particles in a certain cone.

$$L_n = \sum_{i \in ROE} p_i \times |\cos\theta_i| \quad (4.3)$$

The modified Super Fox-wolfram momentum (KSFW momentum) can be defined as shown in Equation 4.4.

$$KSFW = \sum_{l=0}^4 (R_l^{so} + R_l^{oo}) + \gamma \sum_{n=1}^{N_t} |P(t)_n| \quad (4.4)$$

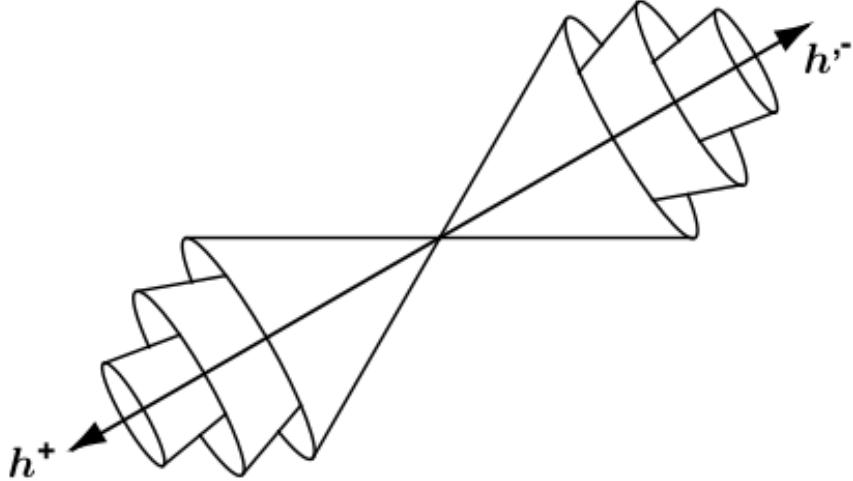


Figure 4-3: A graphical illustration of the CLEO cone. The  $h^+$  and  $h'^-$  present the hadronic tracks from a  $B$  decay. The first three cones are drawn [41]. The nine CLEO cone momentum can be calculated using the particles in each cone.

The  $R_l^{so}$  and  $R_l^{oo}$  are the functions which depend on both  $CP$  and tag-side particles. Their values are also affected by whether  $l$  is even or odd. The  $P(t)_n$  is the scalar sum of the transverse momentum of each particle multiplied by a free parameter  $\gamma$  and  $N_t$  is the total number of particles. The detailed definition for each KSFW momentum is described in Ref [42].

In addition to the CLEO cone and KSFW momentum, a few other variables that are related to the event-shape topology are also used in the Belle II CS framework in order to obtain a better continuum background rejection performance. This includes  $R_2$ ,  $\cos TBz$ ,  $\cos TBTO$ ,  $thrustOm$ , and  $thrustBm$ .  $R_2$  is defined as the normalized second Fox-Wolfram moment ratio, which is widely used in the decay shape studies. The  $\cos TBTO$  is cosine of angle between thrust axis of the  $CP$ -side  $B$  meson and thrust axis of Rest-Of-Event. The  $\cos TBz$  is cosine of angle between thrust axis of the  $CP$ -side  $B$  meson and  $z$ -axis. The  $thrustOm$  and  $thrustBm$  are the magnitude of the  $CP$ -side  $B$  thrust axis and Rest-Of-Event thrust axis, respectively.

For the Belle II CS strategy, the default method is to use the above variables as an input for a FastBDT classifier to discriminating the signal and continuum

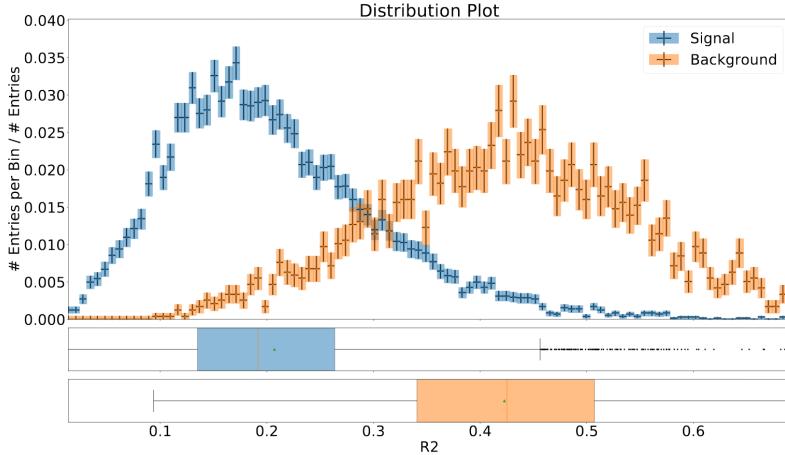


Figure 4-4:  $R_2$  is the ratio of the second to the zeroth KSFW momentum in Equation 4.4 of which the distribution in *signal MC* sample which serves as the highest weight as a variable in discriminating the continuum events, having a quite different distribution between signal and background.

background. Such function is implemented by the BASF2. For the specific decay mode  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$ , the training and testing sample prepared from *signal MC* and *generic MC* are used. The target variable of the training is the continuum event truth named *NotContinuumEvent*, where for signal(continuum background) the value is 1(0). The same events reconstruction procedures for  $B^0$  is applied for both MC samples. Events passing the selection using  $M_{bc}$  and  $\Delta E$  are used for training the CS classifier. The fraction of signal and background is set to 1:1. The output of CS classifier is called *FBDT\_CS*. We determine the cut value at 0.66 based on the maximum of *FOM* curve, as shown in Figure 4-5. The input variables are listed in Table 4.1 with their abbreviations in the training. After the training, the importance of the input variables can be evaluated, shown as Figure 4-6.

The correlation between these training variables are shown in Figure 4-7 which are varied between signal and continuum background events. The ROC curve and the efficiency/purity with respect to the classifier output are shown in Figure 4-8, yielding a close performance.

The Overtraining check is made by comparing the distribution of signal and background depending on the classifier output in both training and testing samples. The testing samples show about 1% lower in each bin for both signal and background

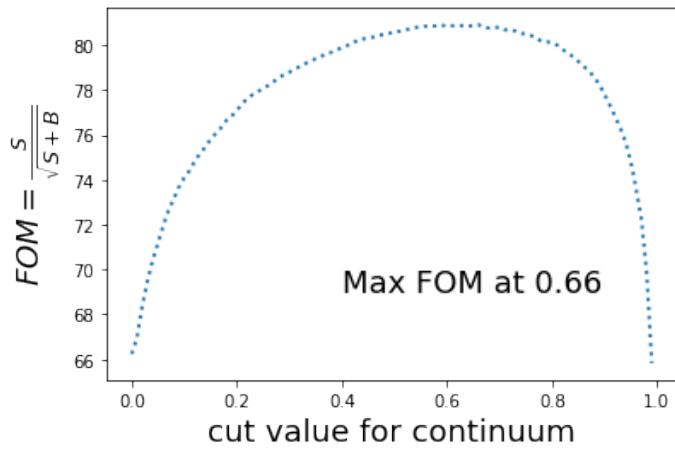


Figure 4-5:  $FOM$  depending on the cut value of continuum classifier output, cut value at 0.66 is used for continuum suppression.

Figure 4-6: The importance rank of the input variables for the Belle II CS framework.

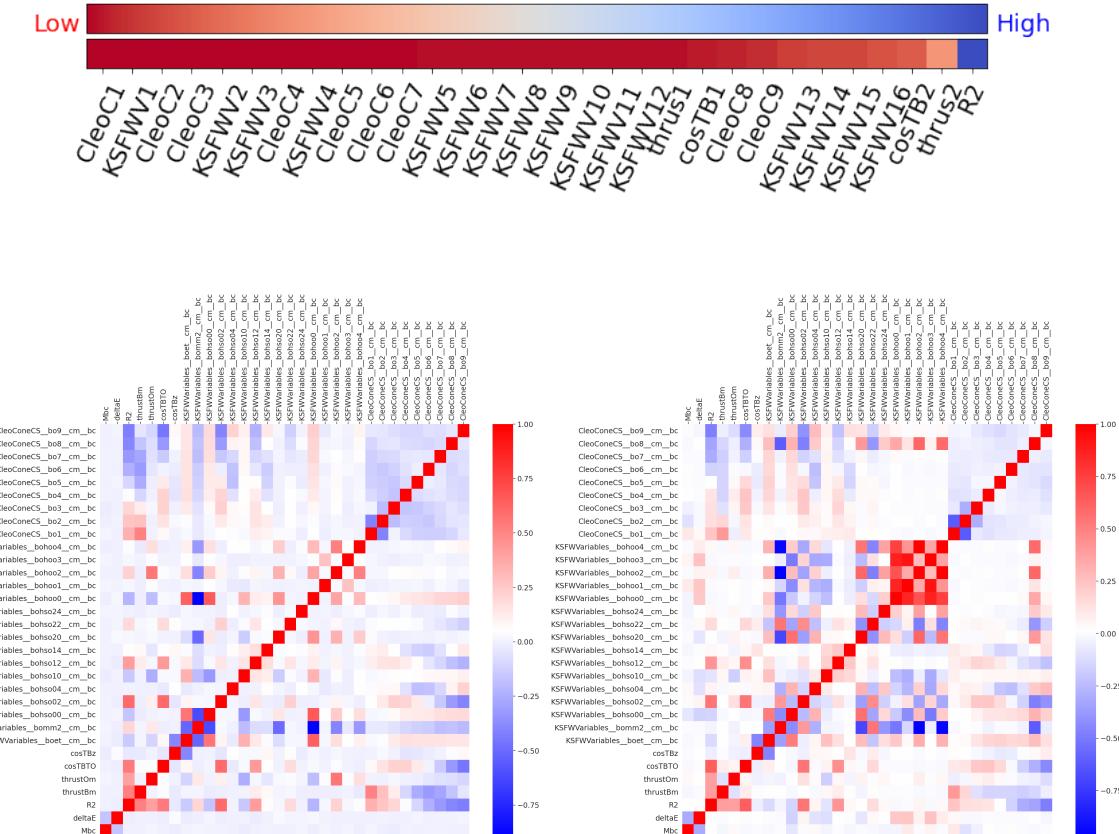


Figure 4-7: The correlation in variables for continuum suppression. The left is for signal and the right is for background.

Table 4.1: Input variables and the abbreviations in the continuum suppression framework of BASF2.

Observables	Abbreviations
CleoConeCS(9,)	CleoC1
KSFWVariables(hoo1,)	KSFWV1
CleoConeCS(7,)	CleoC2
CleoConeCS(5,)	CleoC3
KSFWVariables(hso22,)	KSFWV2
KSFWVariables(hoo3,)	KSFWV3
CleoConeCS(4,)	CleoC4
KSFWVariables(hoo4,)	KSFWV4
CleoConeCS(3,)	CleoC5
CleoConeCS(6,)	CleoC6
CleoConeCS(8,)	CleoC7
KSFWVariables(hso14,)	KSFWV5
KSFWVariables(hso00,)	KSFWV6
KSFWVariables(et,)	KSFWV7
KSFWVariables(hso24,)	KSFWV8
KSFWVariables(hso04,)	KSFWV9
KSFWVariables(hso20,)	KSFWV10
KSFWVariables(mm2,)	KSFWV11
KSFWVariables(hoo2,)	KSFWV12
thrustOm	thrus1
cosTBz	cosTB1
CleoConeCS(1,)	CleoC8
CleoConeCS(2,)	CleoC9
KSFWVariables(hso02,)	KSFWV13
KSFWVariables(hoo0,)	KSFWV14
KSFWVariables(hso12,)	KSFWV15
KSFWVariables(hso10,)	KSFWV16
cosTBTO	cosTB2
thrustBm	thrus2
R2	R2

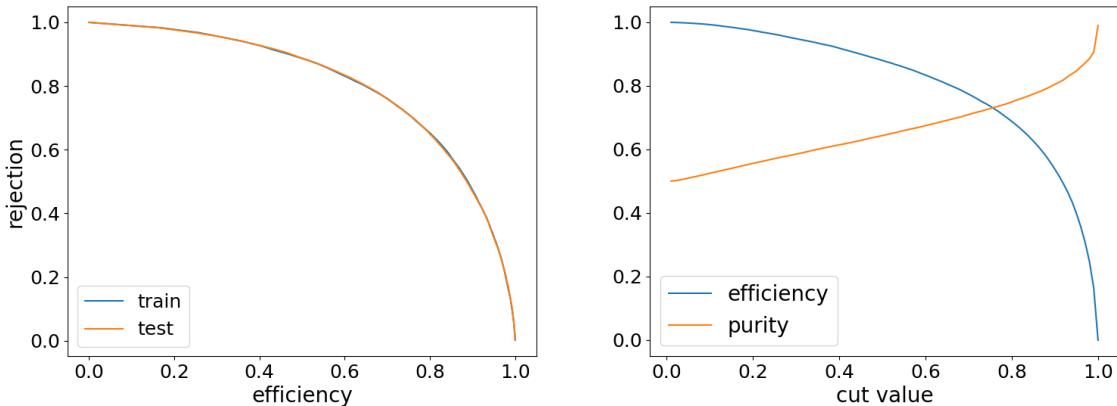


Figure 4-8: The left is the ROC curve (blue for training and orange for testing) and the right is the efficiency(blue) and purity(orange) regarding the classifier output *FBDT\_CS*.

events, which is within the acceptable range.

#### 4.3.1 Event selection summary

The summary of Event selections is listed in Table 4.2, including the application of *KsFinder* (by *FBDT\_Ks*) and continuum suppression (by *FBDT\_CS*).

$B^0$	$M_{bc}(\text{GeV}/c^2)$	$\Delta E(\text{GeV})$	$P(\chi^2)$	Rank	<i>FBDT_CS</i>	<i>FBDT_Ks</i>
Criteria	$> 5.20 \& < 5.29$	$ \Delta E  < 0.2$	$> 0.001$	= 1	$> 0.66$	$> 0.74$

Table 4.2:  $B^0$  selection criteria,  $P(\chi^2)$  is from  $B^0$  *CP*-side vertex fit and *Rank* is from the BCS

Combined with the previous paragraph, the reconstruction performance of  $B^0$  is summarized in Table 4.3. The efficiency, purity, fraction of multiplicity events and best candidates fraction of  $B^0$  are slightly improved in the Belle II compared to the ones referenced from Belle.

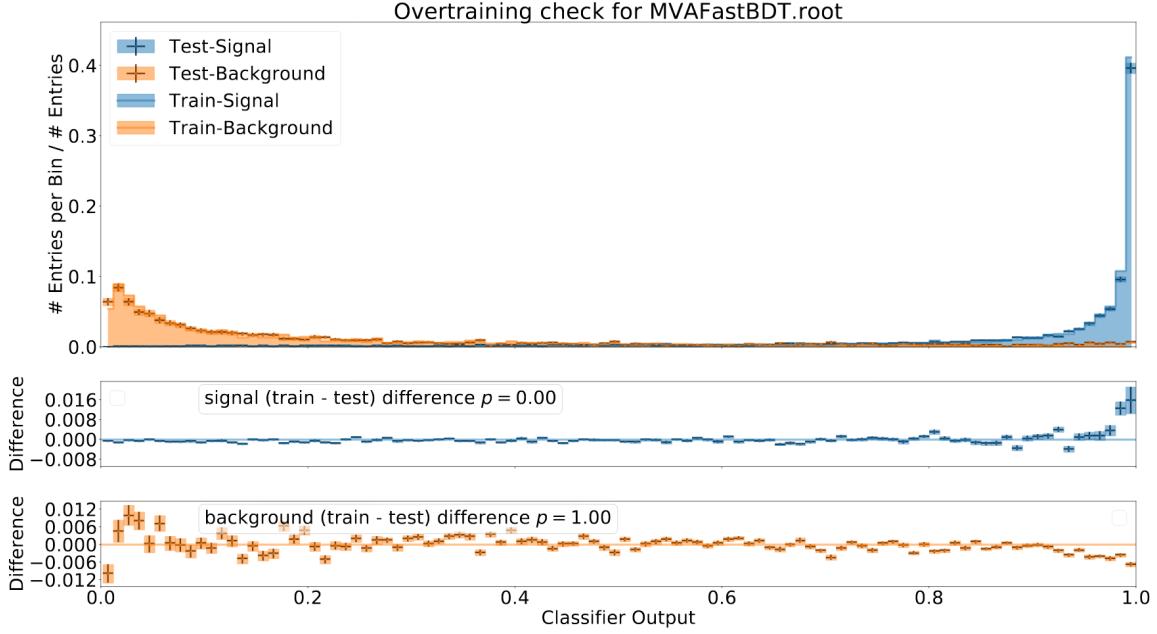


Figure 4-9: Over-training check of continuum classifier, where a very small difference in training and testing (1%) is shown.

event selection	efficiency	purity	$f_{MB}$	BCS
Belle Standard	35%(33%)	96%(99%)	6%(6%)	83%(96%)
Belle II ( $BG1$ )	36%(34%)	96%(98%)	4%(4%)	95%(96%)
Belle II ( $BG0$ )	40%(36%)	96%(99%)	3%(3%)	97%(97%)

Table 4.3: The efficiency is defined by the fraction of best candidates among the MC input number. Purity is the fraction of true  $B^0$  in best candidates.  $f_{MB}$  stands for multiple  $B^0$  events fraction in true signal events. BCS is the fraction of best candidates being a true signal. All values in the parenthesis are calculated in  $|M_{bc}| - 5.28 < 0.1$  and  $|\Delta E| < 0.1$ , called as “signal region” where efficiency is lower but purity is higher, compared to the full range of  $M_{bc}$  and  $\Delta E$  in Table 4.2.

## 4.4 Resonance Background

The  $CP$  eigenvalue of  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  is  $\eta_f = +1$  if it is a loop-level  $b \rightarrow s$  transition, called  $CP$ -even. However, the charmonium resonances from  $b \rightarrow c$  tree-level transition can give an odd  $CP$  eigenvalue ( $\eta_f = -1$ ) while producing the same final states as  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$ . This would cause the contamination to the  $CP$  measurement due to

the fact that  $\mathcal{S} = -\eta_f \sin(2\phi_1)$ . The loop-level  $CP$ -even processes are demonstrated in the left and middle diagrams of Figure 1-5, including the phase-space based decay and resonance decays. Both are considered as the signal events. The tree-level  $CP$ -odd process is shown in the right diagram of Figure 1-5, which is usually referred as the resonance background and can be rejected by applying cut on the invariant mass of two  $K_S^0$  around the possible charmonium resonant states. Therefore, to check whether a resonance decay is a signal or background event, a list of possible  $B^0 \rightarrow X(\rightarrow K_S^0 K_S^0) K_S^0$  processes are considered. For the resonance decays of signal events,  $X$  could be  $f_2(1270)$ ,  $f_0(1500)$ ,  $f'_2(1525)$ ,  $f_0(980)$ ,  $f_0(1710)$  and  $f_2(2010)$ . For resonance background,  $X$  could be  $D^0$ ,  $J/\psi$ ,  $\psi(2S)$ ,  $\chi_{c0}$ ,  $\chi_{c1}$ , and  $\chi_{c2}$ . The branching fraction of these decay modes in the PDG and the Belle II decay profile are both checked and compared, where some of them are not yet measured or not implemented in the Belle II simulation. Thus it is hard to precisely evaluate all the contributions from these decay modes. The expected contributions are calculated by using  $2.14 \times 10^8 B\bar{B}$  pairs as shown in the Table 4.4. The main contribution from the resonance background is  $B^0 \rightarrow \chi_{c0} K_S^0$  and the main contribution from the resonant signal is  $B^0 \rightarrow f_0(980) K_S^0$ . Given the very limited statistics of data accumulation we used in this analysis, the contribution of  $CP$ -odd resonance background should be smaller than one event. Besides, the comparison of two  $K_S^0$  invariant mass using data and *generic MC* is performed, while the small number of reconstructed events in data can not provide reasonable information on the distribution, see Appendix C. Hence, currently there is no veto of two  $K_S^0$  invariant mass is applied to avoid potential bias in this low statistics scenario. In the future with more data collected, the veto will be first checked by the proper comparison between data and MC, then applied according to mass of the main contributive resonance states.

## 4.5 $B\bar{B}$ background

Another possible contribution of background comes from  $B\bar{B}$  events. Both neutral and charged  $B\bar{B}$  pairs could produce the background events. Compared to the event

Table 4.4: Expected yield for signal and background resonances  $2.14 \times 10^8 B\bar{B}$  in *generic MC*. The branching fraction of  $B \rightarrow XK_S$  and  $X \rightarrow 2K_S$  are listed from both the PDG values and the values used in Belle II generic decay profile. The number of events from  $CP$ -odd resonance background is expected to be smaller than one at current luminosity  $62.8 \text{ fb}^{-1}$ .

Resonances	$\text{Br}(B \rightarrow XK_S)$ PDG	$\text{Br}(X \rightarrow 2K_S)$	$\text{Br}(B \rightarrow XK_S)\text{Dec.}$	$\text{Br}(X \rightarrow 2K_S)\text{Dec.}$	$B\bar{B}$ pairs	Expected yields
$D^0 K_S$	$2.6 \times 10^{-5}$	$1.7 \times 10^{-4}$	$2.6 \times 10^{-5}$	$1.8 \times 10^{-4}$	$2.14 \times 10^8$	0.134
$\eta K_S$	$3.45 \times 10^{-4}$	$< 3.1 \times 10^{-4}$	$4 \times 10^{-4}$	No Value	$2.14 \times 10^8$	No Value
$J/\psi K_S$	$4.35 \times 10^{-4}$	$< 1.4 \times 10^{-8}$	$4.35 \times 10^{-4}$	0	$2.14 \times 10^8$	0
$\psi(2S)K_S$	$2.9 \times 10^{-4}$	$< 4.6 \times 10^{-6}$	$2.9 \times 10^{-4}$	0	$2.14 \times 10^8$	0
$\chi_{c0} K_S$	$7.3 \times 10^{-5}$	$3.16 \times 10^{-3}$	$7.35 \times 10^{-5}$	$3.1 \times 10^{-3}$	$2.14 \times 10^8$	6.21
$\chi_{c1} K_S$	$1.96 \times 10^{-4}$	$6 \times 10^{-5}$	$1.96 \times 10^{-4}$	$1 \times 10^{-5}$	$2.14 \times 10^8$	0.05
$\chi_{c2} K_S$	$7.5 \times 10^{-6}$	$2.6 \times 10^{-4}$	$7.5 \times 10^{-6}$	$5.5 \times 10 - 4$	$2.14 \times 10^8$	0.11
$f_2(1270)K_S$	$1.35 \times 10^{-6}$	$1.15 \times 10^{-2}$	$1.35 \times 10^{-6}$	$1.15 \times 10^{-2}$	$2.14 \times 10^8$	0.42
$f'_2(1525)K_S$	$1.5 \times 10^{-7}$	$2.22 \times 10^{-2}$	No value	0.22	$2.14 \times 10^8$	No Value
$f_2(2010)K_S$	$5 \times 10^{-7}$	No Value	No Value	No Value	$2.14 \times 10^8$	No Value
$f_6(980)K_S$	$2.7 \times 10^{-6}$	No Value	$2.75 \times 10^{-6}$	No Value	$2.14 \times 10^8$	43.3
$f_0(1710)K_S$	$5 \times 10^{-7}$	No Value	No Value	No Value	$2.14 \times 10^8$	No Value
$f_0(1500)K_S$	$6.5 \times 10^{-5}$	0.022	No Value	0.022	$2.14 \times 10^8$	No Value
Total	-	-	-	-	-	$\simeq 50$

number from the continuum background, the number of  $B\bar{B}$  background is much fewer. By counting the background event number from  $B\bar{B}$  and  $q\bar{q}$  using *generic MC*, the fraction of  $B\bar{B}$  takes about 3% among all background events, and no special treatment is implemented.

## 4.6 Signal Extraction

The event selections defined in Table 4.2 is applied to *signal MC*, *generic MC* and experiment data for extracting signal events. The integral luminosity in *generic MC* is  $1 \text{ ab}^{-1}$  and experiment data used in this analysis is  $62.8 \text{ fb}^{-1}$  from the latest official processing. The distribution of  $M_{bc}$  and  $\Delta E$  from *generic MC* are shown in Figure 4-10 which contains 328 signal events, 702 continuum background events and 35  $B\bar{B}$  background events. The distribution of  $M_{bc}$  and  $\Delta E$  from data are also shown in Figure 4-10.

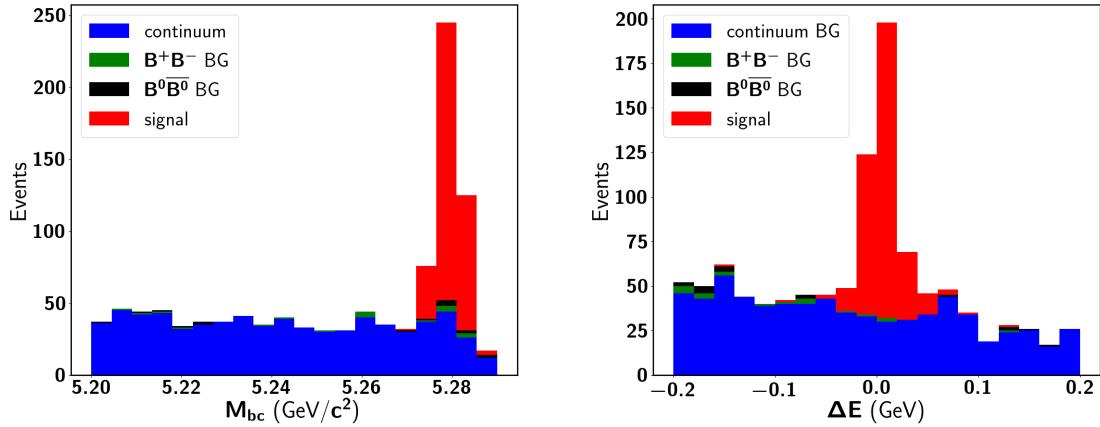


Figure 4-10: The distribution of  $M_{bc}$  and  $\Delta E$  for selected events from *generic MC*, where each background components are stacked with signal. The blue component is the continuum background. The green and the black are the background from charged and neutral  $B\bar{B}$  events. The red component is the signal component by checking MC truth matching.

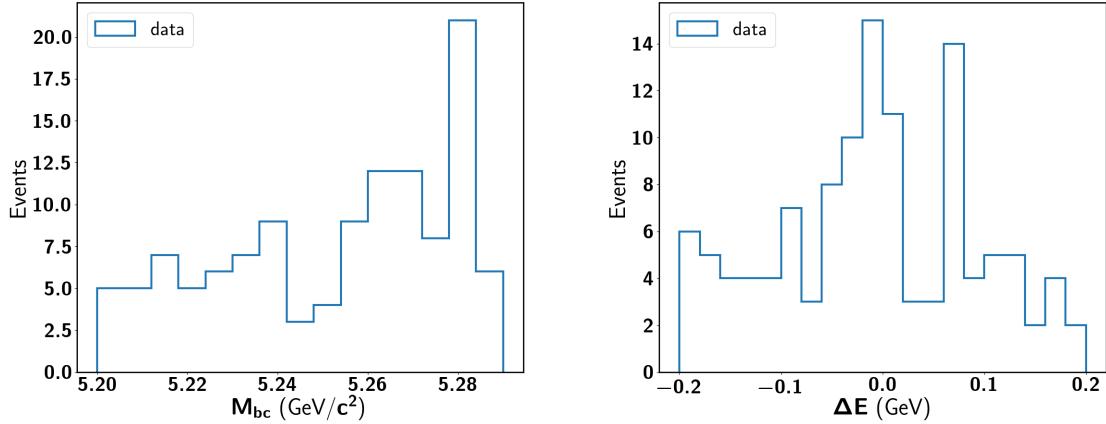


Figure 4-11: The distribution of  $M_{bc}$  and  $\Delta E$  for selected events from data.

The unbinned maximum likelihood fit using RooFit is performed to extract the signal. The 2D fit using both  $M_{bc}$  and  $\Delta E$  are done by taking the probability density function:

$$\mathcal{P}(M_{bc}, \Delta E) = f_{sig} \times \mathcal{P}_{sig}^{M_{bc}} \times \mathcal{P}_{sig}^{\Delta E} + (1 - f_{sig}) \mathcal{P}_{bkg}^{M_{bc}} \times \mathcal{P}_{bkg}^{\Delta E}, \quad (4.5)$$

where  $\mathcal{P}_{sig}^{M_{bc}}$  and  $\mathcal{P}_{sig}^{\Delta E}$  are the probability density function (P.D.F) for the distributions of  $M_{bc}$  and  $\Delta E$ . The  $f_{sig}$  is the fraction of signal events. We use the single Gaussian function as  $\mathcal{P}_{sig}^{M_{bc}}$  in the distribution of  $M_{bc}$  and triple Gaussian functions as  $\mathcal{P}_{sig}^{\Delta E}$  in the distribution of  $\Delta E$  to model the signal component.

On the other hand, the dominated background comes from the continuum events, which is modeled as the Argus distribution [43] in the distribution of  $M_{bc}$ :

$$\mathcal{P}_{bkg}^{M_{bc}}(x; c, \chi) = \frac{\chi^3}{\sqrt{2\pi}\Psi(\chi)} \cdot \frac{x}{c^2} \sqrt{1 - \frac{x^2}{c^2}} \cdot \exp \left\{ -\frac{1}{2}\chi^2(1 - \frac{x^2}{c^2}) \right\}, \quad (4.6)$$

where  $x$  presenting  $M_{bc}$  is defined in  $0 < x < c$  with a preset mass threshold at  $c = 5.29$  GeV. The  $\chi$  is parameter of the distribution. The  $\Psi(\chi) = \Phi(\chi) - \chi\phi(\chi) - \frac{1}{2}$  where  $\Phi(\chi)$  and  $\phi(\chi)$  are cumulative distribution and probability density function of the standard normal distribution, respectively. The  $\Delta E$  distribution of continuum

events is modeled by the first order Chebyshev polynomial function.

The unbinned maximum likelihood fit is first performed to obtain the parameters for signal functions using *signal MC*, and then fixed them as the constants latter for 2D fit. The fit results on *signal MC* are shown in Figure 4-12. The continuum background is fitted by using  $q\bar{q}$  events from *generic MC* to determine the shapes then fix them as the constants latter for 2D fit. The fit results on  $q\bar{q}$  events are shown in Figure 4-13.

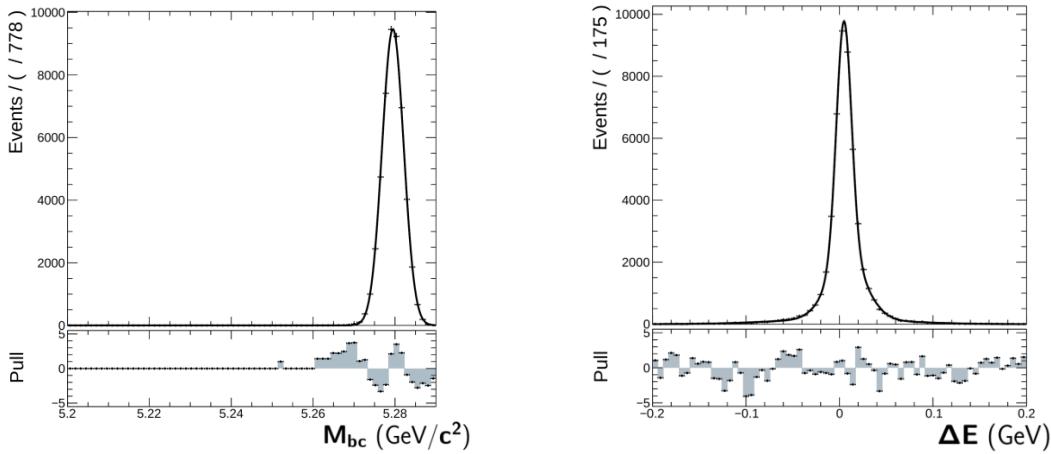


Figure 4-12: The distribution of  $M_{bc}$  and  $\Delta E$  of *signal MC* of  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  fitted with single and triple Gaussian functions respectively. The bottom plots are the pull of the data points and the fit result.

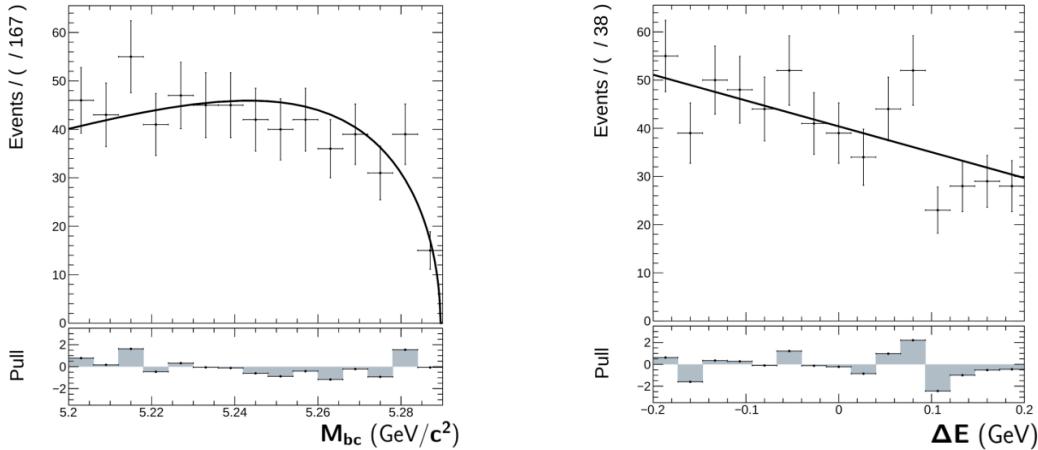


Figure 4-13: The distribution of  $M_{bc}$  and  $\Delta E$  of continuum events in *generic MC* fitted with Argus and Chebyshev polynomial functions, respectively. The bottom plots are the pull of the data points and the fit result.

Then we set the events number for signal and background as floating parameters and use Equation 4.5 as the 2D model to fit on  $1 \text{ ab}^{-1}$  *generic MC* as shown in the Figure 4-14.

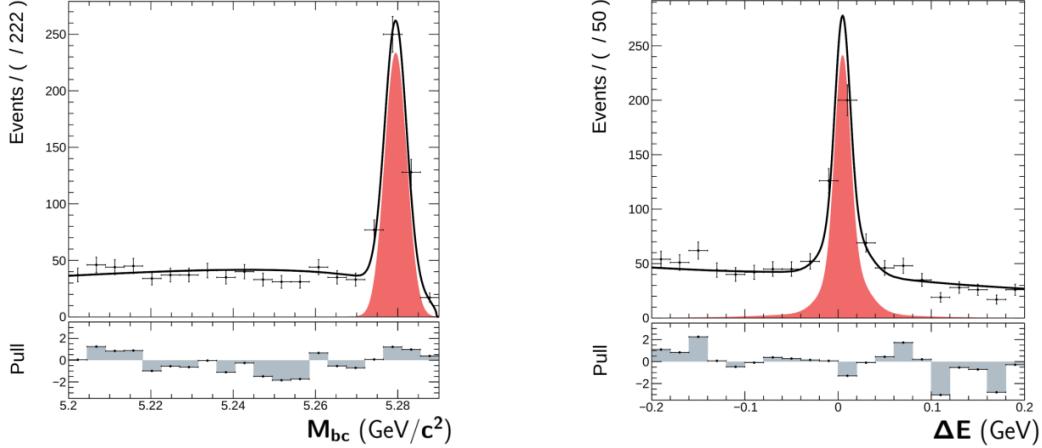


Figure 4-14: Top is the stacked plots for *generic MC* of  $M_{bc}$  and  $\Delta E$ , where each background components are stacked with signal. The bottom is the 2D fit on  $1 \text{ ab}^{-1}$  *generic MC* projected on  $M_{bc}(\text{GeV}/c^2)$  and  $\Delta E(\text{GeV})$ , the red is signal component from the fit result in both plots.

Before perform 2D fit on experiment data, the distribution of  $K_S^0$  invariant mass from the reconstructed  $B^0$  candidates is compared between *generic MC* and experiment data. The selection criteria in Table 4.2 are applied to both samples. The distributions are shown in Figure 4-15, where the *generic MC* is scaled to the luminosity of experiment data and an agreement within  $\sim 1\sigma$  is observed.

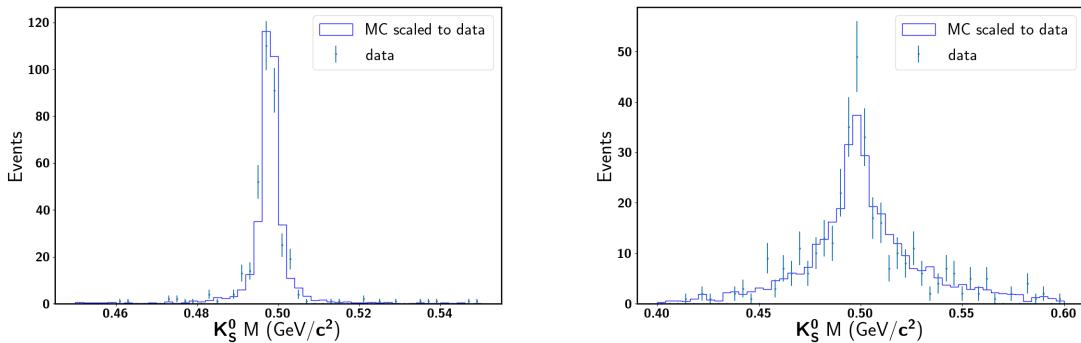


Figure 4-15: Invariant mass before (left) and after (right)  $B^0$  vertex fit from *generic MC* and experiment data.

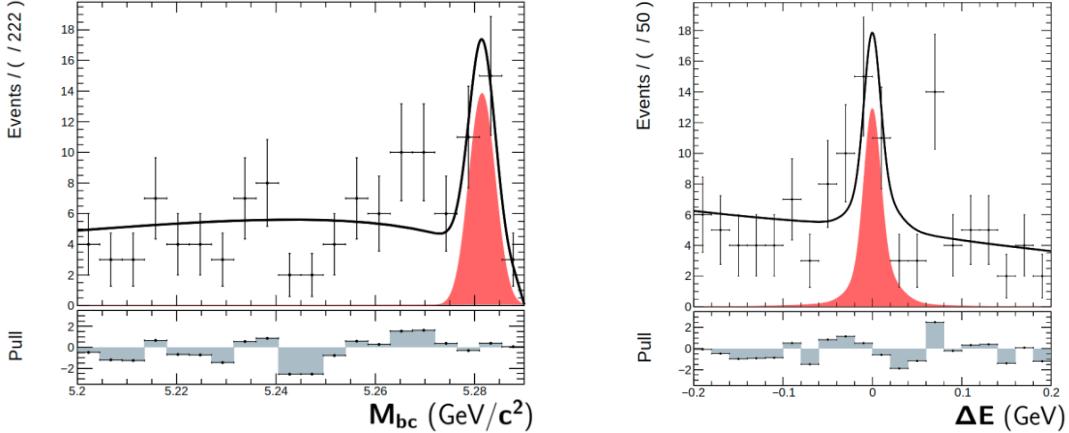


Figure 4-16:  $M_{bc}$ (GeV) and  $\Delta E$ (GeV) 2D fit on  $62.8 \text{ fb}^{-1}$  data, the red is the signal component.

Same as the fit procedure for the *generic MC*, the 2D fit of the experiment data is done and the distributions projected on  $M_{bc}$  and  $\Delta E$  are shown in Figure 4-16. The number of signal events is extracted by the integral of fit model over the signal region which is defined as  $5.27 < M_{bc} < 5.29 \text{ GeV}$  and  $-0.1 < \Delta E < 0.1 \text{ GeV}$ . Using Equation 4.7:

$$N_{sig} = \mathcal{B}(B^0 \rightarrow K_S^0 K_S^0 K_S^0) \times \mathcal{B}(K_S^0 \rightarrow \pi^+ \pi^-)^3 \times \epsilon_{rec} \times N_{B\bar{B}} \times 2 , \quad (4.7)$$

the estimated signal event number can be calculated, where the  $N_{B\bar{B}}$  is the number of neutral  $B$  meson pairs calculated from the integrated luminosity and  $\epsilon_{rec}$  is the reconstruction efficiency. The factor 2 accounts for the fact that both  $B^0$  and  $\overline{B^0}$  can decay to three  $K_S^0$  in the final states.

Using  $62.8 \text{ fb}^{-1}$  data from the Belle II, we extract the number of signal events to be  $N_{sig} = 17.4 \pm 4.2$  from the signal region. The number of background events in the signal region is  $7.2 \pm 3.6$ . The number of signal and background events from the same amount of *generic MC* is calculated to be  $\sim 20.6$  and  $\sim 4.1$ . These values are summarized in Table 4.5. If we directly count the number of events from the data, there are 30 events in the signal region and 60 events in the sideband region which is defined as  $M_{bc} < 5.26 \text{ GeV}/c^2$ . The events in the signal region will be used as the input data points for the  $CP$  parameters measurement latter.

Table 4.5: Reconstructed signal and background events using  $M_{bc}$  and  $\Delta E$  2D fit, compared with expected numbers from *generic MC*.

Events (signal region)	Signal	Background
62.8 $\text{fb}^{-1}$ <i>generic MC</i>	$\sim 20.6$	$\sim 4.1$
62.8 $\text{fb}^{-1}$ data	$17.4 \pm 4.2$	$7.2 \pm 3.6$

To check reliability of the number of events fitted from the  $M_{bc}$  and  $\Delta E$  in this low statistics case, we test the 2D fit result, by merging the continuum events and the different number of signal events, to check the linearity of the input and output. From the 2D fit on *generic MC*, the expected number of continuum events in the full range of  $M_{bc}$  and  $\Delta E$  is  $\sim 46$  at  $62.8 \text{ fb}^{-1}$ , which is set to be the constant number of continuum events used in the linearity test. Then the number of signal events from 5 to 30 with 5 events per step are injected into the continuum events, to perform the  $M_{bc}$  and  $\Delta E$  2D fit to obtain the output signal events number. The  $M_{bc}$  and  $\Delta E$  distributions and fit in each injection test are shown in Figure 4-17. The output signal and background events depending on the injected number of the signal events are presented in Figure 4-18, where the dependence on both signal and background events are fitted with linear function  $y = ax + b$ . The error bar on each data point is taken from the statistical uncertainty of the number of signal or continuum events of the 2D fit results. The fit results show a good linearity on the input and output of the number of signal events while the number of continuum events remain close the constant 46 as the input number. The signal events yield from the current luminosity is considered as a reliable result.

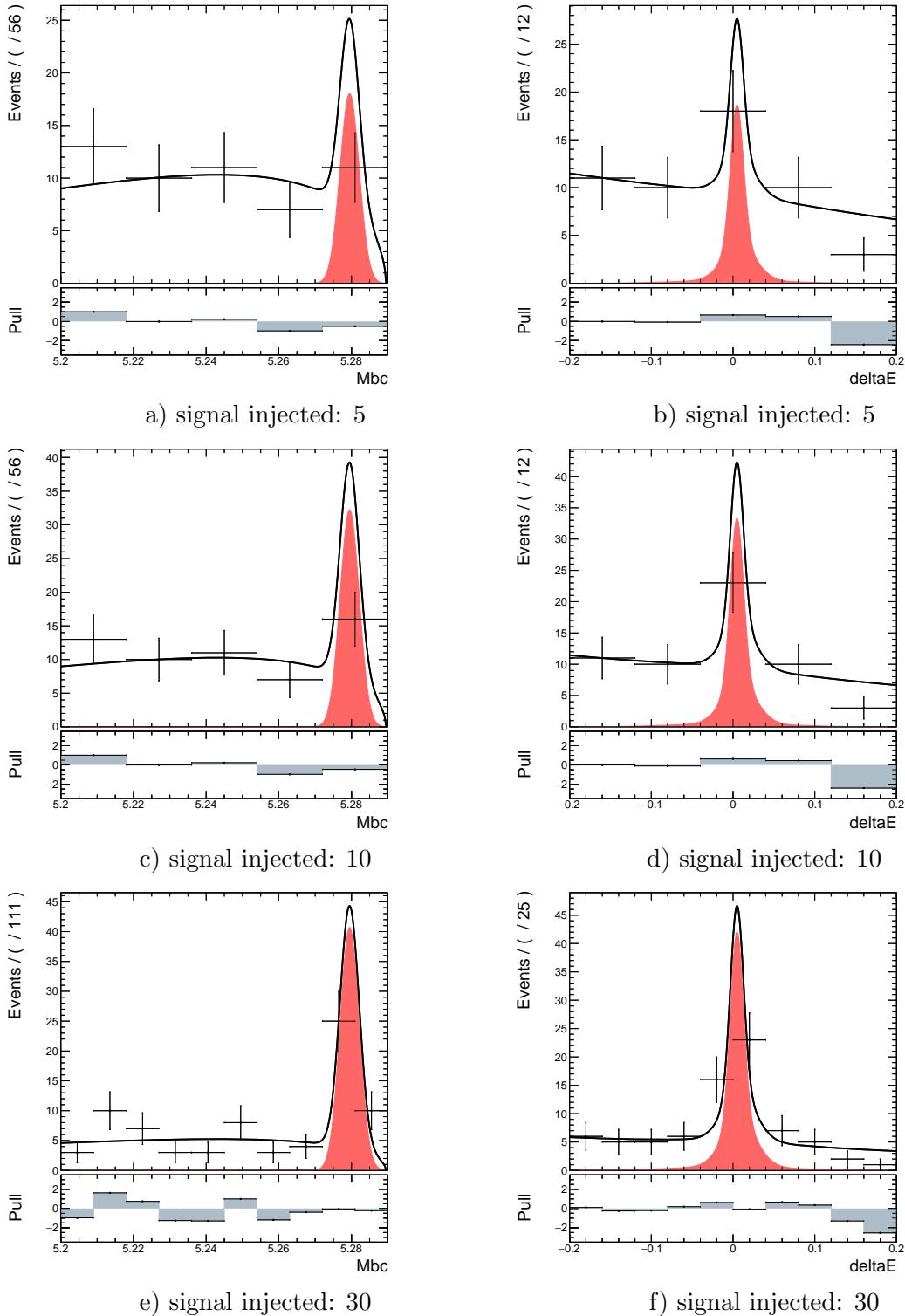


Figure 4-17: The fit results of  $M_{bc}$  and  $\Delta E$  in signal injection test, where the number of signal events of 5, 10, and 30, injected with 46 continuum events, are shown. The full results including other values of the number of signal events are included in the Appendix D.

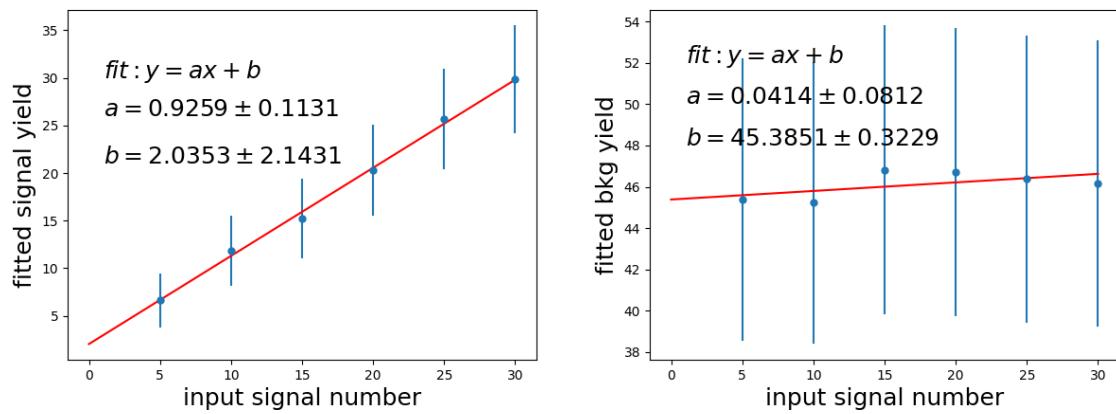


Figure 4-18: Injection test for signal extraction. The linearity is clear between input and output signal events number. The error bar on each point is taken from the statistical uncertainty of the number of signal or continuum events from 2D fit results.



# Chapter 5

## $CP$ parameter measurement

The measurement of  $CP$  parameters  $\mathcal{S}$  and  $\mathcal{A}$  is performed by fitting Equation 5.1 to the distribution of the decay time difference  $\Delta t$  of events with flavor  $q$ , where  $\Delta t = t_{CP} - t_{tag}$  and  $q = +1$  ( $-1$ ) when the tag-side  $B$  meson is  $B^0$  ( $\bar{B}^0$ ).

$$\mathcal{P}_{sig}(\Delta t, q) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} \left\{ 1 + q \cdot \left[ \mathcal{S} \cdot \sin(\Delta M_d \Delta t) + \mathcal{A} \cdot \cos(\Delta M_d \Delta t) \right] \right\} \quad (5.1)$$

The Equation 5.1 describes the distribution of signal events only with  $\tau_{B^0}$  and  $\Delta M_d$  as physics parameters. To perform the unbinned maximum likelihood fit on data, a complete model for  $i$ -th event that takes into account background and outlier components is defined as Equation:

$$\begin{aligned} \mathcal{P}(\Delta t_i, q_i, f_i^{sig}, \mathcal{S}, \mathcal{A}) &= (1 - f_{ol}) \left[ f_{sig} \mathcal{P}_{sig}(\Delta t_i, q_i, \mathcal{S}, \mathcal{A}) + (1 - f_{sig}) \mathcal{P}_{bkg}(\Delta t_i) \right] \\ &\quad + f_{ol} \mathcal{P}_{ol}(\Delta t_i) , \end{aligned} \quad (5.2)$$

where  $f_{sig}$  and  $f_{ol}$  are the fractions of signal and outlier components, respectively. The  $\mathcal{P}_{bkg}$  and  $\mathcal{P}_{ol}$  are defined as

$$\mathcal{P}_{bkg}(\Delta t_i) = f_{bkg}^\delta \delta(\Delta t_i - \mu_{bkg}^\delta) + (1 - f_{bkg}^\delta) \frac{1}{2\tau_{bkg}} e^{-|\Delta t_i - \mu_{bkg}^\delta|/\tau_{bkg}} , \quad (5.3)$$

$$\mathcal{P}_{ol}(\Delta t_i) = G(\Delta t_i, \sigma_{ol}) , \quad (5.4)$$

where  $\delta(\Delta t_i - \mu_{bkg}^\delta)$  is a Dirac  $\delta$  function and  $G$  is single Gaussian. The outlier component is to improve the fit quality with large  $\Delta t$  events.

## 5.1 Vertex Resolution Model

The Equation 5.2 presents an ideal distribution of  $\Delta t_i$  for each event without considering the difference between measured and the true position of the vertex. The difference can be described by introducing resolution functions, turning Equation 5.2 into Equation 5.5.

$$\begin{aligned} \mathcal{P}(\Delta t_i, q_i, f_i^{sig}, \mathcal{S}, \mathcal{A}) = & (1 - f_{ol})[f_{sig} \mathcal{P}_{sig}(\Delta t_i) \otimes R_{sig}(\Delta t_i) \\ & + (1 - f_{sig}) \mathcal{P}_{bkg}(\Delta t_i) \otimes R_{bkg}(\Delta t_i)] \\ & + f_{ol} \mathcal{P}_{ol}(\Delta t_i) \otimes R_{ol}(\Delta t_i) \end{aligned} \quad (5.5)$$

The  $R_{sig}$  stands for the resolution function for signal events, which receives smearing effect from  $CP$ -side and tag-side separately, namely  $R_{cp}$  and  $R_{tag}$ . The treatment of  $CP$ -side and tag-side is different because of the varied vertexing strategies. For  $CP$  side, vertex of  $B^0$  is reconstructed by fitting all the daughter particles using *TreeFit*. Instead, in tag-side, there is no full reconstruction of  $B^0$  so that a vertex fit is applied for the selected charged tracks in the Rest-Of-Event using *KFit*. The background events have its own resolution model which is independent from  $CP$  violation parameters. The outlier is used to smooth fit for large  $\Delta t$  events. In the low statistics case like the current luminosity, the outlier is excluded in the fit model of Equation 5.5.

For signal events, the resolution functions are studied for  $CP$ -side and tag-side based on each possible degradation such as detector resolutions, the effect of tracks from non-primary  $B$  vertex and so on. Such approaches have been used in Belle analyses. Details are summarized in Ref [44]. The vertex position difference  $\Delta z$  for signal events can be broken down to

$$\Delta z = \Delta z' + (z_{cp} - z'_{cp}) - (z_{tag} - z'_{tag}) , \quad (5.6)$$

where the primed ones stand for physics truth of the position and the non-primed one are the measured value. The resolution function receives contribution from both *CP* and tag-side effects. Thus, the resolution functions on both sides depend on the applied IP constraints. Considering that the fine structure of IP profile is not yet fully understood and small discrepancies have been observed between data and simulation [45], there is no IP constraint applied for both sides in vertex fit, which avoids potential bias from IP profile under this low statistical situation. From the Equation 5.6, the total vertex resolution of signal events can be presented as the sum of the two random variables which stand for the resolution effects on the both side. Therefore, the vertex resolution function of signal events is defined as

$$R_{sig} = R_{cp} \otimes R_{tag} \quad (5.7)$$

where  $R_{cp}$  and  $R_{tag}$  are the vertex resolution functions for *CP*-side and tag-side, respectively. The determination of these two components are described in the section 5.1.1 and 5.1.2.

### 5.1.1 *CP*-side resolution function

A *CP*-side vertex position is obtained by *TreeFit* with all tracks from a reconstructed  $B^0$ , thus the resolution models only depend on the performance of the Belle II detectors, such as the vertexing and tracking accuracy affected by the detector hardware and software. Hence, the resolution effect for each event can be different based on event-by-event reconstruction quality, primarily presented by the reduced  $\chi^2$  called  $\chi^2/N$  from *TreeFit*, which  $N$  is the degree of freedom of the fit. The distribution of  $\chi^2/N$  in data are shown in Figure 5-1.

Therefore, we model the resolution function  $R_{cp}$  on *CP*-side by using a double Gaussian function, where the mean is fixed to zero and the standard deviation is the error of reconstructed vertex  $\sigma_{z_{cp}}$  scaled by  $\chi^2/N$ :

$$R_{cp}(\delta z_{cp}) = (1 - f_{cp}^{tail})G(0, s_{cp}^{main}) + f_{cp}^{tail}G(0, s_{cp}^{tail}) , \quad (5.8)$$

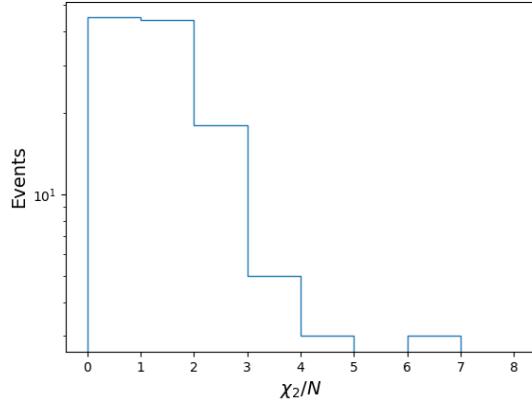


Figure 5-1:  $\chi^2/N$  of selected events from data.

where  $s_{cp}^{main}$  and  $s_{cp}^{tail}$  are

$$\begin{aligned} s_{cp}^{main} &= (s_0^{main} + s_1^{main} \cdot \chi_{cp}^2/N) \cdot \sigma_{z_{cp}} , \\ s_{cp}^{tail} &= (s_0^{tail} + s_1^{tail} \cdot \chi_{cp}^2/N) \cdot \sigma_{z_{cp}} . \end{aligned} \quad (5.9)$$

The Figure 5-2 shows the distribution of the  $z_{cp} - z'_{cp}$  as the residual with the dependence of the  $\chi^2/N$ , where the first plot is for the range of  $0 < \chi^2/N < 10$ , covering all of the selected events. The rest plots are the distributions in the sliced range of  $\chi^2/N$ , which show a slight increase of the deviation with respect to the increasing of  $\chi^2/N$  range. This validates the necessity to include the  $\chi^2/N$  as a conditional parameter in  $R_{cp}$  so that for a poorly reconstructed  $B^0$  the resolution functions should yield relatively larger deviation.

Restrictively speaking, the  $CP$ -side resolution for  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  is slight different from  $B^0 \rightarrow J/\psi K_S^0$  due to the absence of the direct tracks of the charged particles from the  $B^0$  vertex. The modification of the resolution function on  $CP$ -side will be further studied when more data becomes available in future. Given the current low statistics, the Equation 5.8 works well as an approximation. By fitting the resolution function using *signal MC* on  $CP$ -side, the parameters are obtained and listed in Table 5.1.

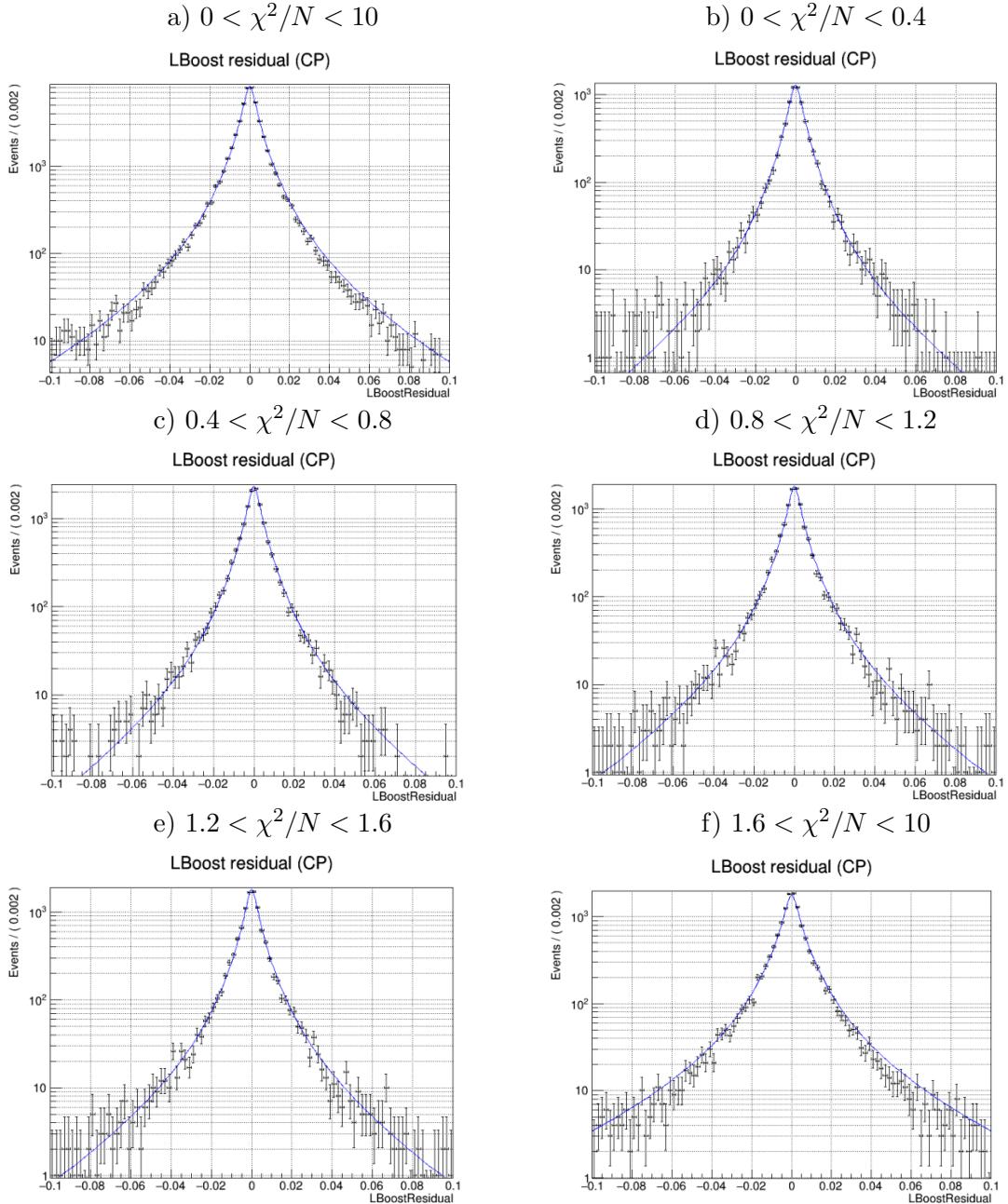


Figure 5-2: The  $z$  position residual of  $B^0$  vertices on  $CP$ -side, which is dependent on the  $\chi^2/N$ . The first plot is the fit in the full range and the rest of the plots are the fit in each sliced range of  $\chi^2/N$ . The events are the true candidates taken from the *signal MC*.

Table 5.1: Parameters in  $R_{cp}$ .

$f_{cp}^{tail}$	$0.07424 \pm 0.0008$
$s_0^{main}$	$0.9151 \pm 0.0077$
$s_1^{main}$	$0.2142 \pm 0.0064$
$s_0^{tail}$	$2.0477 \pm 0.0779$
$s_1^{tail}$	$1.3470 \pm 0.0720$

### 5.1.2 Tag-side resolution function

For the tag-side, the vertexing is done by using *KFit* and no IP constraint used. Since the tag-side vertex reconstruction takes into account the tracks of the charged particles which may not be directly from the tag-side  $B^0$  decay, the vertex position could be affected by both detector effects like the *CP*-side and the degradation of the secondary vertex. This effect is demonstrated in Figure 5-3. where the tag-side vertex fit will give a estimated positions around the range of orange meshed area while the actual position of the primary vertex should be in the area of the blue circle.

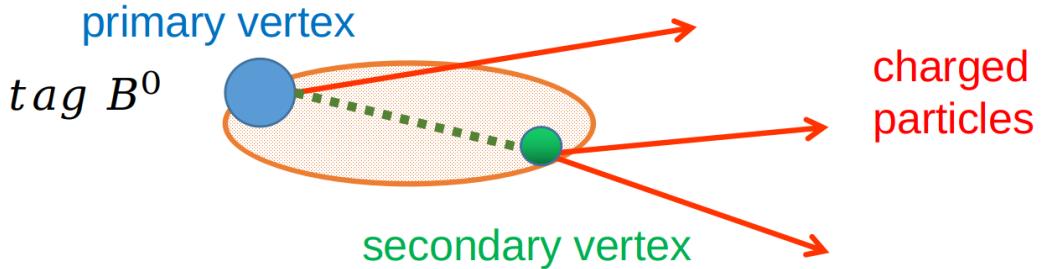


Figure 5-3: The illustration of the tag-side  $B^0$  vertex resolution affected by the non-primary tracks from the secondary vertex. The red arrows present the charged particles used for the tag-side vertex reconstruction, where one is from primary vertex of  $B^0$  and two are from the secondary vertex.

To the contrary, if all tracks that are used for tag-side vertexing are primary tracks, the resolution will only be affected by the detector effects. The vertex position difference from the MC truth can be written as Equation 5.10, where  $\delta z_{tag}^{det}$  and  $\delta z_{tag}^{np}$  are the position shifts caused by the detector effects and the vertex fit using non-primary tracks, respectively. Therefore, the effects from both detectors and non-

primary tracks contributes to the total resolution on tag-side as shown in Equation 5.11.

$$\begin{aligned} z_{tag} - z'_{tag} &= (z'_{tag} + \delta z_{tag}^{det} + \delta z_{tag}^{np}) - z'_{tag} \\ &= \delta z_{tag}^{det} + \delta z_{tag}^{np} \end{aligned} \quad (5.10)$$

$$R_{tag}(z_{tag} - z'_{tag}) = R_{det}^{tag}(\delta z_{tag}^{det}) \otimes R_{np}^{tag}(\delta z_{tag}^{np}) \quad (5.11)$$

Similarly to the *CP*-side resolution function, detector effects are presented as

$$R_{det}^{tag}(\delta z_{tag}^{det}) = (1 - f_{tag}^{tail})G(0, s_{tag}^{main} \cdot \sigma_{z_{tag}}) + f_{tag}^{tail}G(0, s_{tag}^{tail} \cdot \sigma_{z_{tag}}), \quad (5.12)$$

where the main and tail Gaussian functions have the same central value at zero, but the standard deviation is scaled by  $\chi^2_{tag}/N$  on the tag-side:

$$s_{tag}^{main/tail} = s_0^{main/tail} + s_1^{main/tail} \cdot \chi^2_{tag}/N. \quad (5.13)$$

$R_{det}^{tag}$  can be obtained with MC samples of which tag-side tracks are all from a primary vertex.

The fit model of  $R_{np}^{tag}$  is shown in Equation 5.14 which consists of three functions, including one Dirac  $\delta$  function and two single-side exponential functions  $E_p$  and  $E_n$ . The  $E_p(x|y_p) = (1/y_p)e^{-x/y_p}$  when  $x > 0$  and the  $E_n(x|y_n) = (1/y_n)e^{x/y_n}$  when  $x < 0$ . The exponential factors in both positive and negative components are scaled by the tag-side vertex uncertainty  $\sigma_{z_{tag}}$ .

$$R_{np}^{tag}(\delta z_{tag}^{np}) = f_\delta \delta(\delta z_{tag}^{np}) + (1 - f_\delta)[f_p E_p(\delta z_{tag}^{np}, \tau_p \cdot \sigma_{z_{tag}}) + (1 - f_p)E_n(\delta z_{tag}^{np}, \tau_n \cdot \sigma_{z_{tag}})] \quad (5.14)$$

Since tag-side has no dependence on how *CP*-side is reconstructed, the resolution functions on tag-side are almost mode-independent. Thus these parameters are obtained by fitting to the control sample reconstructed from the MC. The control sample consists of multiple exclusive  $D^{(*)}$  hadronic decays, of which the details are summarized in Appendix B. The results are referenced from the  $B^0 \rightarrow J/\psi K_S^0$  study [45].

The fit plots for tag-side resolution functions are shown in Figure 5-4 and 5-5. The parameters obtained from the fit are listed in Table 5.2 and Table 5.3.

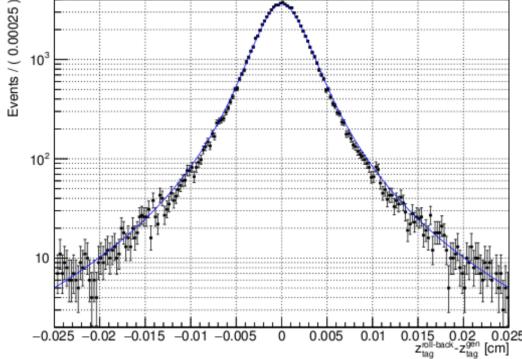


Figure 5-4:  $R_{det}^{tag}$  fit

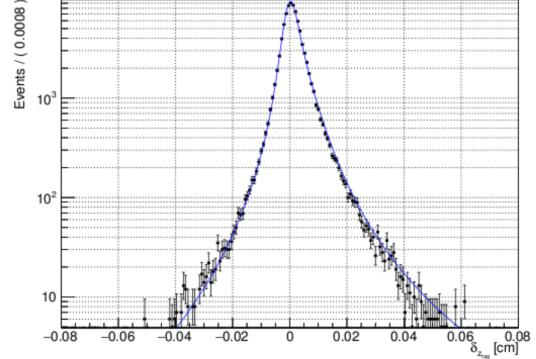


Figure 5-5:  $R_{np}^{tag}$  fit

Table 5.2: Parameters in  $R_{det}^{tag}$

$f_{tag}^{tail}$	$0.0523 \pm 0.0025$
$s_0^{main}$	$1.1446 \pm 0.0061$
$s_1^{main}$	$0.0443 \pm 0.0022$
$s_0^{tail}$	$3.4480 \pm 0.0897$
$s_1^{tail}$	$0.2666 \pm 0.0276$

Table 5.3: Parameters in  $R_{np}^{tag}$

$f_\delta$	$0.6256 \pm 0.0049$
$f_p$	$0.8316 \pm 0.0051$
$\tau_n$	$2.9141 \pm 0.0758$
$\tau_p$	$2.4846 \pm 0.0269$

The boost direction is not exactly same in each event, while we use  $\Delta t_i = \Delta z / \beta \gamma c$  as an universal relation to calculate the decay time difference for all the events, assuming the boosted direction of the CMS frame to the laboratory frame is always precisely along the  $z$ -direction for each event. It will cause a small additional contribution to the resolution of  $\Delta t_i$ . This effect could be reduced by two approaches. First, instead of using the vertex position difference along the  $z$ -axis, we use the the relative distance between two vertices along the boosting direction calculated for each event during the vertex reconstruction. The second approach is to still use vertex position difference along the  $z$ -axis but introduce another resolution function called  $R_k$  into Equation 5.5 for the kinematic correction of both signal and background events [46]. In the current stage of the Belle II, the dedicated study of  $R_k$  is not ready because

it requires a good understanding to the beam conditions and alignment in the event basis. Thus, the first approach is used in this thesis.

### 5.1.3 Background events $\Delta t$ distribution

The  $R_{bkg}$  model is approximately uncorrelated to vertex reconstruction method. Because the background component mainly comes from continuum events passing the selection, it is reasonable to model the vertex resolution of the background events by a Gaussian-like function. In this case, a double-Gaussian functions with the standard deviations scaled by the measured uncertainties from both  $CP$ - and tag-sides is used as shown in Equation 5.15.

$$R_{bkg} = (1 - f_{tail}^{bkg})G(\Delta t_i, \sigma_{main}^{bkg} \sqrt{\sigma_{z_{cp}}^2 + \sigma_{z_{tag}}^2}) + f_{tail}^{bkg}G(\Delta t_i, \sigma_{tail}^{bkg} \sqrt{\sigma_{z_{cp}}^2 + \sigma_{z_{tag}}^2}) \quad (5.15)$$

where the  $\sigma_{z_{cp}}$  and  $\sigma_{z_{tag}}$  are the measured uncertainties of the vertex position in  $CP$ - and tag-sides. The  $\sigma_{main}^{bkg}$  and  $\sigma_{tail}^{bkg}$  are the non-unit scaling parameters which control the standard deviations of the main and tail Gaussian functions.

The shape of  $\mathcal{P}_{bkg} \otimes R_{bkg}$  can be determined by fitting to the side-band data. The sideband region is defined as  $M_{bc} < 5.26$  GeV, according to section 4.6. The requirement of  $\Delta E$  is not used in the current definition of the sideband in order to increase the number of events, which will be added in future when more data is collected. Figure 5-6 shows the fit result using 60 sideband data. There are totally seven floating parameters which are listed in Table 5.4.

$\mu_{\delta}^{bkg}$	$0.1310 \pm 0.1902$
$\mu_l^{bkg}$	$0.1638 \pm 0.5030$
$\tau_{bkg}$	$1.0541 \pm 0.4370$
$f_{\delta}^{bkg}$	$0.5861 \pm 0.2570$
$f_{tail}^{bkg}$	$0.0417 \pm 0.0408$
$\sigma_{main}^{bkg}$	$1.4348 \pm 0.3940$
$\sigma_{tail}^{bkg}$	$28.0930 \pm 8.8221$

Table 5.4: Parameters in Background  $\Delta t$  distribution.

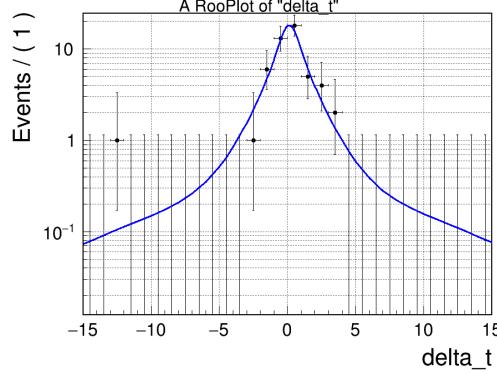


Figure 5-6:  $\mathcal{P}_{bkg} \otimes R_{bkg}$  fit using 60 sideband events at  $M_{bc} < 5.26$  GeV.

## 5.2 Flavor Tagging

In order to determine the flavor of tag side  $B^0$ , flavor tagging algorithm is being developed. The flavor tagging uses information from  $\mu^\pm, \pi^\pm, K^\pm$  and  $\Lambda$  which are categorized into 13 different types as illustrated in Figure 5-7.

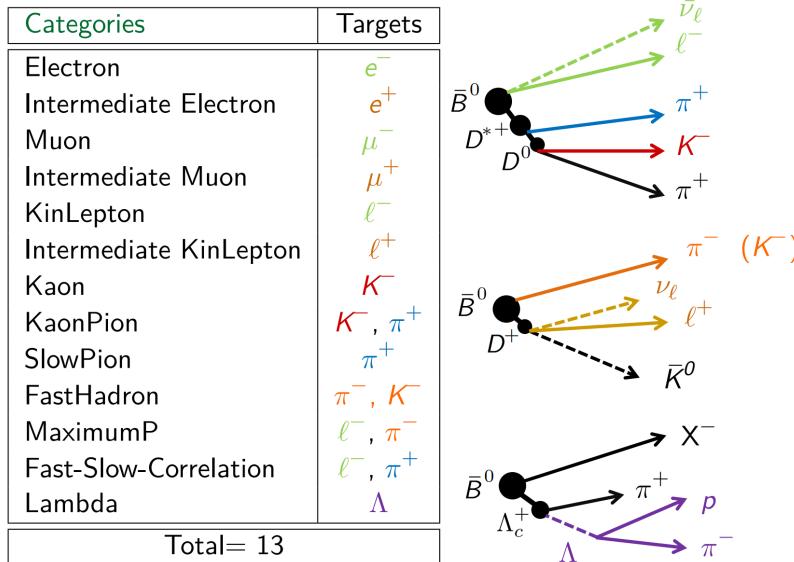


Figure 5-7: Particles and their categories used in flavor tagging algorithm[47].

For each particle that has been used from above categories, PID and kinematics information are extracted and feed to the combiner as training variables, to obtain a classifier response corresponding to each category. Then for all responses from these categories, a total classifier is trained to present the likelihood of flavor  $q$ .

This algorithm is called category-based method and used in this thesis. After the reconstruction on the  $CP$ -side  $B^0$  is done, the rest-of-events tracks used to form the particle lists are selected<sup>5-7</sup>. The FastBDT as the back-end algorithm is chosen for performing training on the classifier of flavor tagging. Targeted variable is true  $q$  of tag-side neutral  $B$  in MC. To minimize impact of the reconstruction performance on  $CP$ -side, MC sample of  $B^0 \rightarrow \nu\nu$  is used as the training sample where the final state in  $CP$ -side are completely invisible.

Considering the limited power of flavor tagging accuracy, there is a certain fraction of events that are wrongly tagged among all that can be flavor tagged using the final state particles in the rest-of-event. Thus, the flavor tagging efficiency  $\epsilon$  and wrong tag fraction  $w$  are defined, respectively. Taking into account of the performance of flavor tagging, the observed distribution of Equation 5.2 becomes Equation 5.16.

$$\mathcal{P}_{sig}^{obs}(\Delta t, q, \epsilon, w) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} \epsilon \left\{ 1 - q \cdot \Delta w + q(1 - 2w) \cdot [\mathcal{S} \sin(\Delta M_d \Delta t) + \mathcal{A} \cos(\Delta M_d \Delta t)] \right\} \quad (5.16)$$

Compared to the original, the term with  $\mathcal{S}$  and  $\mathcal{A}$  is scaled by factor  $r \equiv |1 - 2w|$ , defined as the dilution factor. The statistical uncertainty of  $\mathcal{S}$  now becomes dependent to the tagging efficiency  $\epsilon$  and wrong tag fraction  $w$ . The uncertainty of  $w$  is much larger than  $\epsilon$  which makes  $w$  an important source of systematic uncertainty, too. The validation of flavor tagger using flavor specific decay modes in 2019 Belle II data is summarized here[48]. The  $w$  for each single event is defined as a probability of being wrongly flavor tagged which can be presented by the average wrong tag fraction in a binned interval of the dilution factor. The binned values of dilution factor  $r$  is defined for the calculation of  $w$  as  $[0.0, 0.1, 0.25, 0.5, 0.625, 0.75, 0.875, 1.0]$ , also named as  $r$ -bin. For all events that have been successful tagged, they are projected into histogram of  $r$ -bin, and  $w$  is calculated in each bin by the fraction of events with  $q \cdot r$  opposite to its MC flavor. The distribution of  $q \cdot r$  is shown in Figure 5-8 using *signal MC* of  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$ .

Besides,  $w$  can be different between  $B^0$  and  $\bar{B^0}$ , where  $\bar{w} = (w_{B^0} + w_{\bar{B^0}})/2$  and  $\Delta w = w_{B^0} - w_{\bar{B^0}}$ . Due to the small value of  $\Delta w$ , the contribution from  $\Delta w$  is treated

as zero in Equation 5.16 in this analysis. Similarly, for  $\epsilon$ , the values calculated based on each  $r$ -bin are summed and used in Equation 5.16, where the total efficiency is  $(99.72 \pm 0.02)\%$ , treated as 1. The difference  $\mu = \epsilon_{B^0} - \epsilon_{\bar{B}^0}$  is about 1 % to 2 % in each  $r$ -bin, thus treated as zero. The distributions of  $w$ ,  $\Delta w$ ,  $\epsilon$ , and  $\mu$  in each  $r$ -bin are shown in Figure 5-9. The values obtained from *signal MC* are agreed with those from the control sample study[48]. Thus the values from control samples are used for *CP* fit.

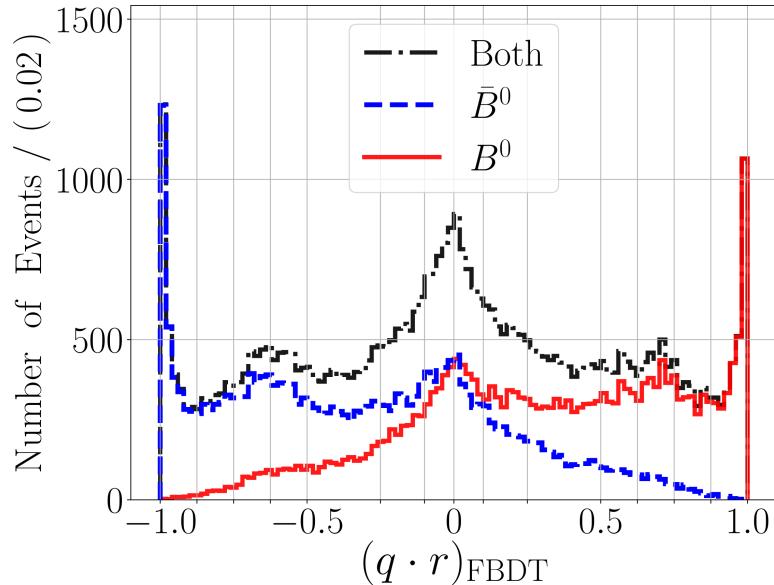


Figure 5-8: The distribution of flavor tagger output ( $q \cdot r$ ) for both tag-side of  $B^0$  and  $\bar{B}^0$

### 5.3 *CP* Fitter

The parameters that are needed for measuring  $\mathcal{S}$  and  $\mathcal{A}$  are studied and obtainable. Using observed  $\Delta t$  distribution from selected events, Equation 5.5 can be fitted using unbinned maximum likelihood fit which takes  $\Delta t$ , signal fraction  $f_{sig}$ , the flavor charge  $q$  as observables. In the meantime the vertexing error  $\sigma_{z_{cp}}$ ,  $\sigma_{z_{tag}}$  and  $\chi^2/N$  are used as event-by-event conditional variables that are accessed during the fitting. For Belle II, a new *CP* fitter is developed based on Python and RooFit, which is naturally easy to use and maintained with BASF2. The fitter requires a configuration files which

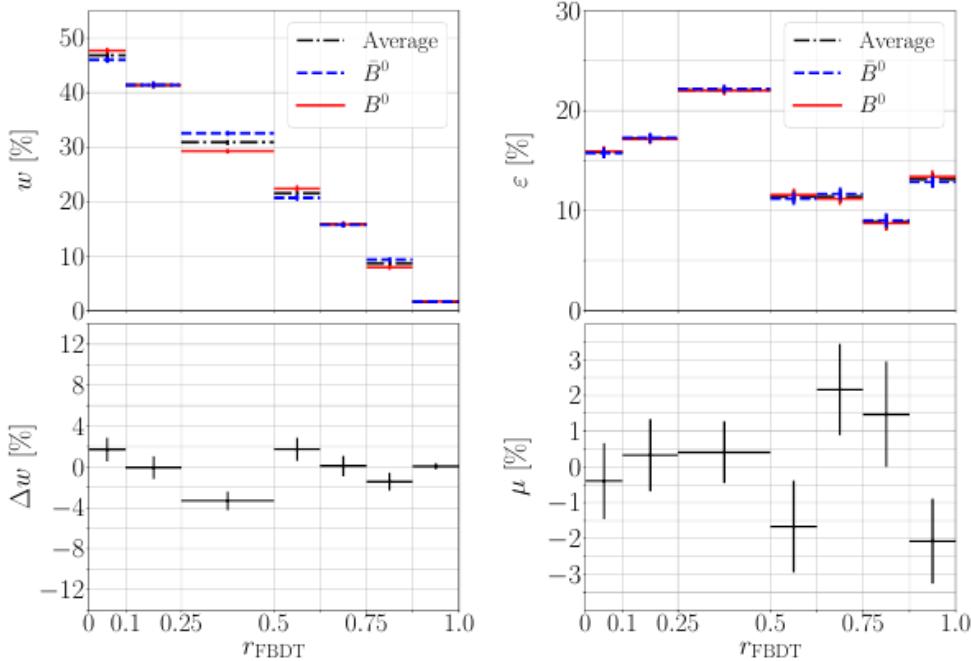


Figure 5-9: The flavor tagging efficiency, wrong tagging fraction, and their difference between different flavors sorted in each  $r$ -bin.

contains all the parameters' definitions including their ranges, initial values, floating states and uncertainties.

## 5.4 Blind analysis and fit

As a required procedure to make sure the  $CP$  parameters are measured without bias due to the preconceived results, a blind analysis procedure is conducted before the fit is actually performed using the experimental data. The blind fit procedure includes the  $CP$  fit on *signal MC* and *generic MC*, with different number of events used. To check the reliability of fit result from  $CP$  fitter, a linearity test and toy MC study are also performed.

### 5.4.1 $CP$ fit on MC samples

Using  $CP$  fitter, we first perform the  $CP$  fit on events in *signal MC* and *generic MC*. The *signal MC* and *generic MC* are generated with phase-space model which

Observables	Selections
$\Delta t$	$-70 < \Delta t < 70$ ps
$CP\text{-side } \chi^2/N$	$0 < (\chi^2/N)_{cp} < 8$
tag-side $\chi^2/N$	$0 < (\chi^2/N)_{tag} < 50$
$\sigma_{z_{tag}}$	$\sigma_{z_{tag}} < 0.1$ cm
signal region	$5.27 < M_{bc} < 5.29$ GeV and $ \Delta E  < 0.1$ GeV

Table 5.5: The selection criteria for events that are used for  $CP$  parameters fit.

contains zero  $CP$  violation ( $\mathcal{S} = \mathcal{A} = 0$ ). The events that pass the selections in Table 5.5 are used for  $CP$  parameters fit. We have 10000 (8873 passing selections) events from signal sample and 415 (373 passing selections) events from  $1 \text{ ab}^{-1}$  generic MC to fit  $CP$  parameters. To mimic the events number expected in data sample, 30 events randomly taken from generic MC are used to perform the fit as well. The plots are shown in Figure 5-10, 5-11 and 5-12. The fit results of  $\mathcal{S}$  and  $\mathcal{A}$  are summarized in Table 5.6.

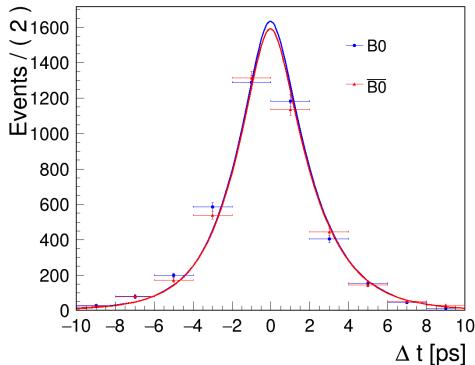


Figure 5-10:  $CP$  fit on 8873 signal MC.

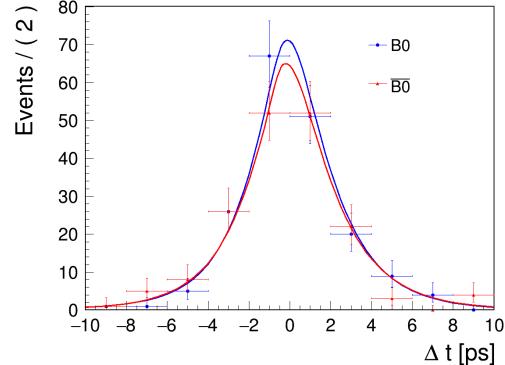


Figure 5-11:  $CP$  fit on 373 generic MC.

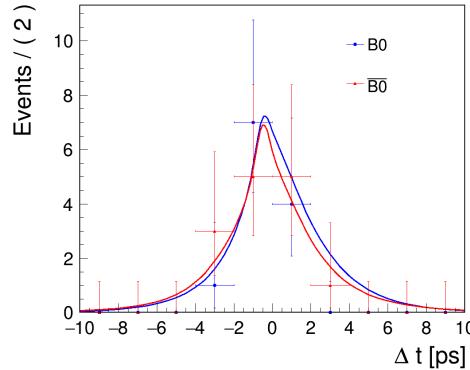


Figure 5-12:  $CP$  fit on 30 generic MC.

Table 5.6: The  $CP$  fit results using *signal MC* and *generic MC* with only statistical uncertainties.

Sample (events)	$\mathcal{S}$	$\mathcal{A}$
<i>signal MC</i> (8873)	$\sin(2\phi_1) = 0.00 \pm 0.04$	$\mathcal{A} = -0.01 \pm 0.02$
<i>generic MC</i> (373)	$\sin(2\phi_1) = 0.00 \pm 0.21$	$\mathcal{A} = -0.05 \pm 0.07$
<i>generic MC</i> (30)	$\sin(2\phi_1) = 0.20 \pm 0.85$	$\mathcal{A} = -0.06 \pm 0.30$

The fit results are consistent with expectation in non- $CP$  violation from MC input, and the statistical uncertainties has the tendency  $\delta \propto 1/\sqrt{N}$  as poission distribution, where  $N$  is events number used for  $CP$  fit. To test fit on non-zero  $CP$  violating MC, the fit on  $B^0 \rightarrow J/\psi K_S^0$  *signal MC* is also done, the details of events selection as well as fit model determination can be found[45]. The fit result over 10000 events is shown in Figure 5-13, which results in  $\sin(2\phi_1) = 0.70 \pm 0.05$  and  $\mathcal{A} = -0.01 \pm 0.02$ . The results agree with the input.

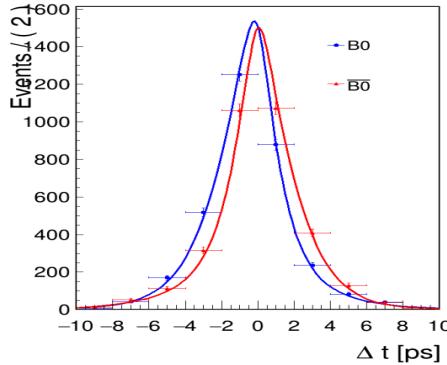


Figure 5-13:  $CP$  fit over 10000  $B^0 \rightarrow J/\psi K_S^0$  *signal MC*.

### 5.4.2 Linearity Test

To validate the  $CP$  fit linearity, a series of toy MC samples is generated, which the  $\chi^2$  from vertex fit, events number  $N$  and vertex errors on  $CP$  and tag-side are sampled from the distribution of *signal MC*. The resolution functions parameters are kept as same as  $CP$  fit on *generic MC*. The input  $\mathcal{A}$  is set to zero while the input value of  $\sin(2\phi_1)$  is running from 0.1 to 0.9. Each dataset contains 10000 events. The dependence between input and output are shown in Figure 5-14. The linearity fit shows a good agreement between input and output.

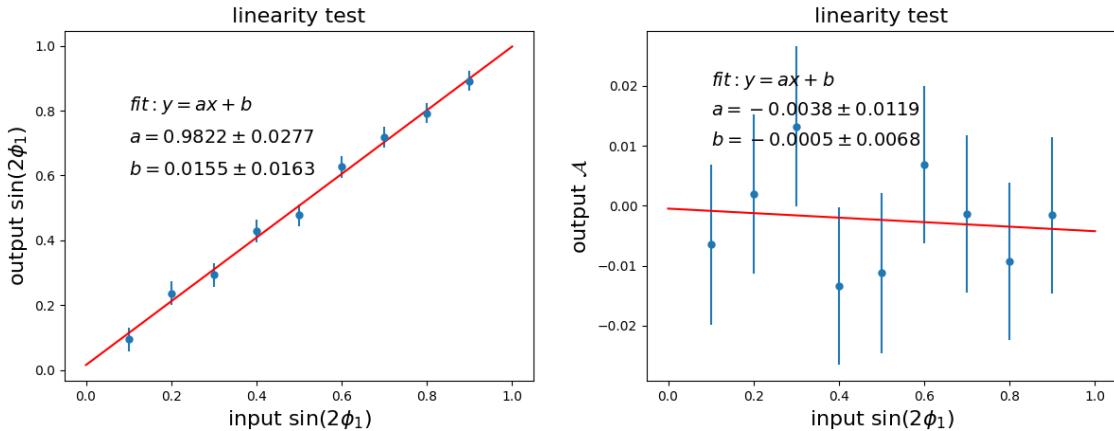


Figure 5-14: Linearity test of  $CP$  fit.

Also, we fix  $\sin(2\phi_1)$  at zero while floating  $\mathcal{A}$  from 0.1 to 0.9, the dependence between input and output are as Figure 5-15 shows. The linearity fit shows a good agreement as well.

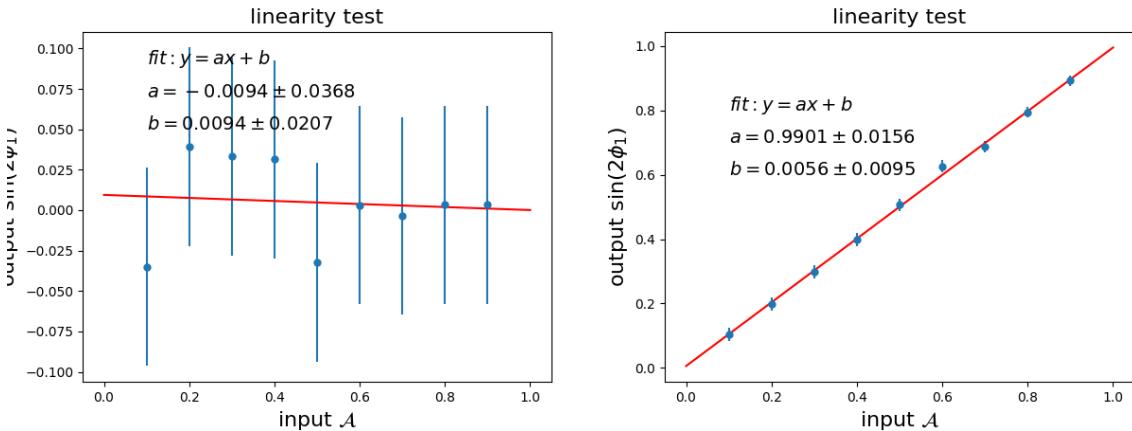


Figure 5-15: Linearity test of  $CP$  fit.

### 5.4.3 Toy MC Fit Pull

In order to check the fit bias with input-output method, a series of 1000 dataset of toy MC has been created containing about 26 events in each. The event number is set based on the expected number from signal region in data after the selection. The  $\chi^2$  from vertex fit, events number  $N$  and vertex errors on  $CP$  and tag-side are sampled from the distribution of data. The fit to dataset is performed with zero input  $\sin(2\phi_1)$

and  $\mathcal{A}$  as floating parameters. We expect to use the normal distribution to fit the pull of  $\sin(2\phi_1)$  and  $\mathcal{A}$ .

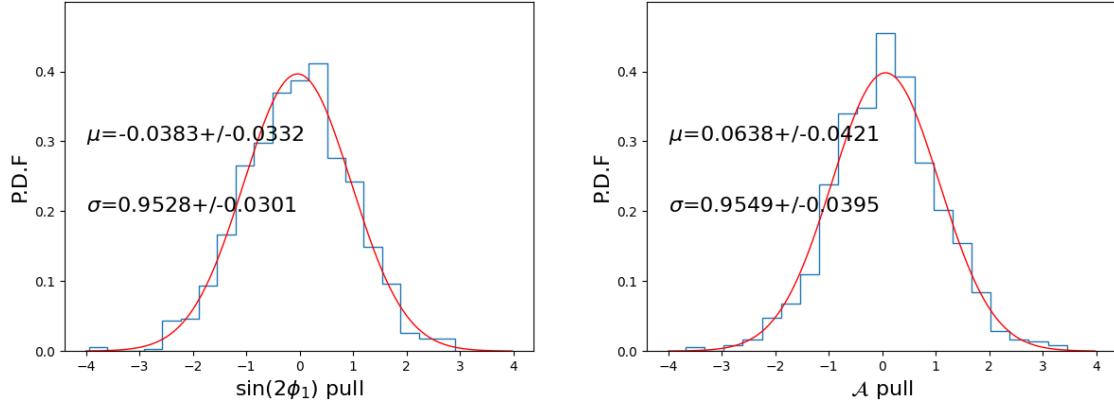


Figure 5-16: Pull of  $\sin(2\phi_1)$  and  $\mathcal{A}$  fitted with the standard normal distribution.

The fit results shows a good recovery of input  $\sin(2\phi_1)$  and  $\mathcal{A}$  with no clear bias is spotted.

#### 5.4.4 Lifetime and $\Delta m_d$ Fit

Before looking at  $CP$  parameters in data, we need to check if the physics parameters are consistent when setting the  $CP$  fitter to fit them in float. To test lifetime fit, first we use 10000 *signal MC* events which is generated by  $\tau_{B^0} = 1.520$  from PDG value. The  $\sin(2\phi_1)$  and  $\mathcal{A}$  are fixed at zero during the fit, for which the generator level  $CP$  violation is zero. This is equivalent fit to Equation 5.17.

$$\mathcal{P}(\Delta t, \tau_{B^0}) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} \quad (5.17)$$

The fit result on *signal MC* is  $1.537 \pm 0.024$  ps which is consistent with the input. We perform the lifetime fit on data in signal region, and the  $CP$  parameters are fixed based on PDG values to:  $\sin(2\phi_1) = 0.69$  and  $\mathcal{A} = 0$ . The fitted lifetime from  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  is  $1.431 \pm 0.382$  ps. The result is consistent with PDG value. The distribution of  $\Delta t$  in lifetime fit is shown as Figure 5-17. The  $B^0$  and  $B^+$  lifetime fit

using control sample is also performed and summarized in here[45]. The results are consistent with PDG values as input in MC generator.

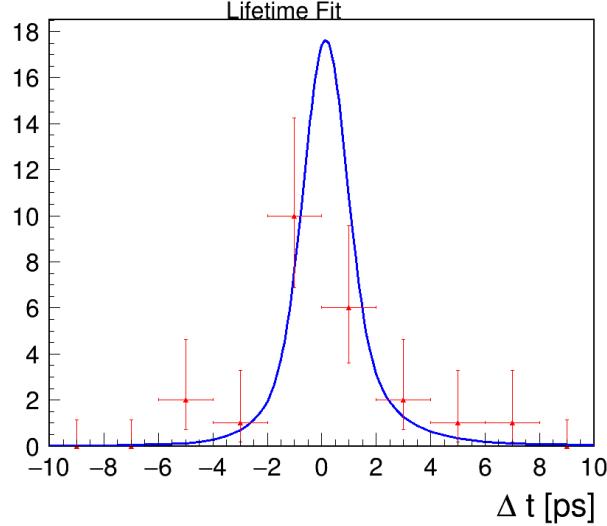


Figure 5-17: Lifetime fit on data

To test the fit on physics parameter  $\Delta m_d$ , we generate 200 toy MC sets of  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  with input  $\Delta m_d = 0.507 \text{ GeV}/c^2$  where each set contains 26 events as same as data. The fit result is close to normal distribution and the pull of  $\Delta m_d$  is shown in Figure 5-18.

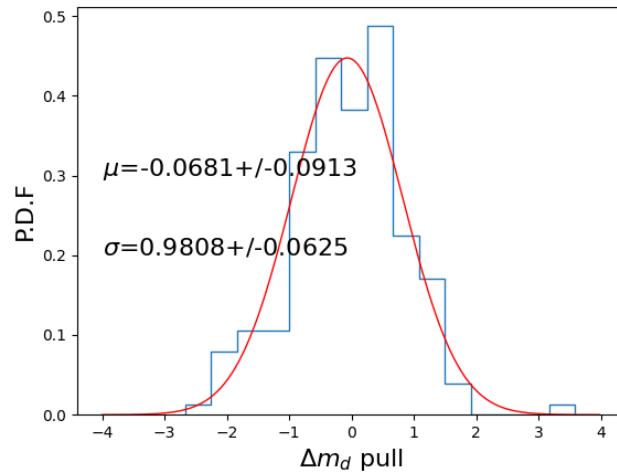


Figure 5-18: Pull of  $\Delta m_d$

## 5.5 $CP$ fit on data

After the  $CP$  fit procedures are reviewed by Belle II collaboration, the permission of measuring  $CP$  parameters using  $62.8 \text{ fb}^{-1}$  Belle II data is granted. The events number used for the  $CP$  fit is 26, and the fit result is shown Figure 5-19.

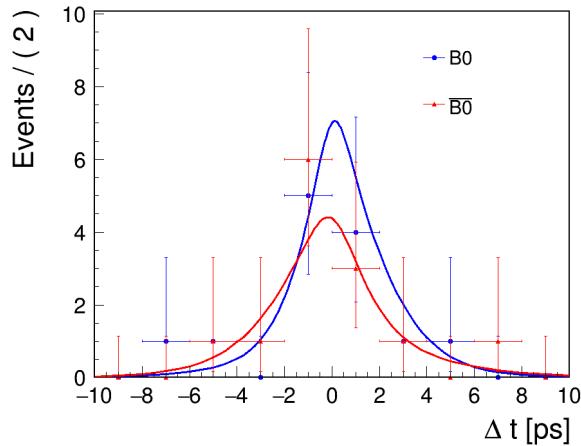


Figure 5-19: The  $CP$  fit from data.

The results of  $CP$  parameters are:

$$\begin{aligned} \sin(2\phi_1) &= 0.82 \pm 0.85(\text{stat}) \\ \mathcal{A} &= -0.21 \pm 0.28(\text{stat}) \end{aligned} \tag{5.18}$$

## 5.6 Systematic Uncertainty

The systematic uncertainty that affects the fit results may come from many aspects of the measurement setup. Currently there is no estimation on systematic uncertainty from the tag-side interference in the Belle II, which is caused by the interference between CKM-favored or CKM-suppressed tree-level decays. The Belle results suggested the contribution is  $\sim 0.001$ [49] which is trivial at current systematic uncertainty. As shown in Table 5.7 to 5.11, the total contribution from each source is calculated by adding-in-quadrature using each systematic uncertainty caused by the fit model parameters belonging to that category. To be specific, in each category if the param-

eters are defined with MC study, we float the value by  $\pm 2\sigma$ , and if the parameters are defined by data, we float the value by  $\pm 1\sigma$ , where  $\sigma$  is the uncertainty of the parameters. The impact on the  $CP$  fit results from every parameter in each category is therefore marked as  $\pm \delta\mathcal{S}$  and  $\pm \delta\mathcal{A}$ , where the signs present the difference caused by positively or negatively floating values. On the other hand, from Table 5.12 to 5.14, the contributions are not directly from the parameters of the fit model, but events number in fit bias test, *KsFinder* correction factor and vertex reconstruction options, we modified their values and repeat the fit to obtain the systematic uncertainties. After obtaining the  $\delta\mathcal{S}$  and  $\delta\mathcal{A}$  from each category, the total systematic uncertainty is calculated by add-in-quadrature again from all the sources, as shown in Table 5.16.

The signal resolution functions' parameters are determined from MC study for signal component. The impact on fit results is summarized as follows Table 5.7. The background  $\Delta t$  shapes' parameters are determined from data sideband  $M_{bc} <$

Table 5.7: Systematic uncertainty from signal  $\Delta t$  shapes

source	$+\delta\mathcal{S}$	$+\delta\mathcal{A}$	$-\delta\mathcal{S}$	$-\delta\mathcal{A}$
$f_{cp}^{tail}$	-0.000096	-0.000057	0.000014	0.000056
$s_{0CP}^{main}$	0.005443	0.001299	-0.005675	-0.001404
$s_{1CP}^{main}$	0.019934	-0.000903	-0.020204	0.000633
$s_{0CP}^{tail}$	-0.003233	-0.001623	0.003270	0.001596
$s_{1CP}^{tail}$	-0.002044	-0.000063	0.002009	0.000048
$f_{tag}^{tail}$	0.003140	-0.001257	-0.003117	0.001266
$s_{0tag}^{main}$	0.002011	-0.001395	-0.001956	0.001398
$s_{1tag}^{main}$	0.005059	-0.000840	-0.004969	0.000825
$s_{0tag}^{tail}$	-0.000135	-0.000393	0.000101	0.000435
$s_{1tag}^{tail}$	0.000101	0.000027	-0.000472	0.000129
$f_\delta$	-0.007248	-0.000552	0.007231	0.000591
$f_p$	0.003037	0.004347	-0.003069	-0.004314
$\tau_n$	-0.001010	-0.002841	0.000937	0.002940
$\tau_p$	0.004497	0.002502	-0.004648	-0.002478
Total	$\delta\mathcal{S} = 0.033793$		$\delta\mathcal{A} = 0.009283$	

5.26 GeV. The impact on fit results is summarized in Table 5.8. The flavor tagging parameters wrong tagging fraction  $w$  in each rbin is determined by applying flavor tagging on control sample. The impact in each rbin on fit results is summarized in Table 5.9: The physics parameters  $\Delta m_d$  and  $\tau_{B^0}$  uncertainties are included using the

Table 5.8: Systematic uncertainty from background  $\Delta t$  shapes

source	$+\delta\mathcal{S}$	$+\delta\mathcal{A}$	$-\delta\mathcal{S}$	$-\delta\mathcal{A}$
$\mu_{\delta}^{bkg}$	-0.014294	-0.016581	0.006758	0.006537
$\mu_l^{bkg}$	-0.002798	-0.012567	0.003789	0.012783
$\tau_{bkg}$	0.001377	0.001689	-0.004159	0.000085
$f_{\delta}^{bkg}$	-0.011315	0.001365	0.011187	-0.001395
$f_{tail}^{bkg}$	-0.002661	0.001530	0.002480	-0.001368
$\sigma_{main}^{bkg}$	0.020702	0.022041	-0.023618	-0.015690
$\sigma_{tail}^{bkg}$	-0.000275	-0.000159	0.000179	0.000141
Total	$\delta\mathcal{S} = 0.039430$		$\delta\mathcal{A} = 0.037269$	

Table 5.9: Systematic uncertainty from wrong tagging fraction

source	$+\delta\mathcal{S}$	$+\delta\mathcal{A}$	$-\delta\mathcal{S}$	$-\delta\mathcal{A}$
$w_1$	-0.001892	0.001911	0.001855	-0.002004
$w_2$	-0.001645	0.001104	0.001609	-0.001155
$w_3$	-0.000490	0.001344	0.000473	-0.001341
$w_4$	0.000656	0.000264	-0.000654	-0.000255
$w_5$	-0.000123	0.000204	0.000123	-0.000195
$w_6$	0.000095	0.000054	0.000096	-0.000045
$w_7$	0.000191	-0.000396	-0.000191	0.000402
Total	$\delta\mathcal{S} = 0.003709$		$\delta\mathcal{A} = 0.003790$	

PDG average value. The impact on fit results is summarized in Table 5.10. The signal

Table 5.10: Systematic uncertainty from physics parameters

source	$+\delta\mathcal{S}$	$+\delta\mathcal{A}$	$-\delta\mathcal{S}$	$-\delta\mathcal{A}$
$\Delta m_d$	-0.001767	-0.000687	0.001778	0.000696
$\tau_{B^0}$	-0.004561	-0.000546	0.004565	0.000555
Total	$\delta\mathcal{S} = 0.006923$	$\delta\mathcal{A} = 0.001250$		

fraction is determined using 2D fit results of  $M_{bc}$  and  $\Delta E$  from data. The impact on fit results is summarized in Table 5.11.

Table 5.11: Systematic uncertainty from signal fraction

source	$+\delta\mathcal{S}$	$+\delta\mathcal{A}$	$-\delta\mathcal{S}$	$-\delta\mathcal{A}$
mu1_mbc	0.000822	-0.003888	-0.000797	0.003849
sigma1_mbc	0.000476	0.008442	-0.000628	-0.008733
m0_argus	-0.000707	0.004140	0.001448	-0.005781
c_argus	-0.005544	0.001449	0.000922	-0.000078
f1_de	0.027826	0.020589	-0.019237	-0.008409
f2_de	0.020809	0.017649	-0.016129	-0.007005
mu1_de	-0.000443	-0.000153	0.000496	0.000088
mu2_de	-0.000563	0.001446	0.000591	-0.001446
mu3_de	-0.003164	-0.000834	0.003354	0.000981
sigma1_de	-0.000172	-0.000966	0.000206	0.000906
sigma2_de	-0.003150	0.002958	0.002635	-0.002475
sigma3_de	-0.001926	-0.002550	0.002470	0.002985
a0_cheb	0.000952	0.000057	-0.000893	-0.000102
N_sig_f	-0.004640	0.003987	0.004922	-0.003504
Total	$\delta\mathcal{S} = 0.044387$	$\delta\mathcal{A} = 0.033932$		

The fit bias uncertainties are determined by taking the larger ones among the fit error of 300000 *signal MC* events with zero  $CP$  violation and the difference between input and output of the center value. The fit result is  $\mathcal{S} = 0.000127 \pm 0.009817$  and  $\mathcal{A} = 0.000265 \pm 0.005702$ . So the values of fit errors are used as listed in Table 5.12.

Table 5.12: Systematic uncertainty from fit bias

source	$\delta\mathcal{S}$	$\delta\mathcal{A}$
fit bias	0.009817	0.005702

Applying *KsFinder* cut at 0.74 based on MC study may introduce small impact on data due to the different response on the classifier between data and MC. Therefore

the contribution of systematic uncertainty from KsFinder is considered. At cut value 0.74, the  $\mathcal{R}_{B'}$  presenting MC and data signal yield ratio is  $\mathcal{R}_{B^0} = 1.027 \pm 0.033$ , where the upper and lower limit is 1.060 and 0.994, respectively. These two ratios are applied on the signal fraction obtained by data to repeat the fit, and the difference of fit results compared to the original values are used as systematic uncertainty, see Table 5.13.

Table 5.13: Systematic uncertainty from *KsFinder*.

source	$\delta\mathcal{S}$	$\delta\mathcal{A}$
$\mathcal{R}_{B^0} = 1.06$	0.004826	-0.000606
$\mathcal{R}_{B^0} = 0.994$	-0.000508	0.000007
Total	0.004852	0.000606

For the contributions from vertex reconstruction, the impacts from the selections in Table 5.5 are considered. Given the fact that cut values in Table 5.5 are very loose and the statistics from data is very limited, the changing of the these values doesn't affect events collected from data so that systematic uncertainty can not be reflected correctly. Therefore,  $1 \text{ ab}^{-1}$  *generic MC* is used with the modified ranges to estimate the potential systematic uncertainty from vertex reconstruction. Besides, due to the absence of IP constraint in vertex fit, the impact from the IP constraint options as well as the potential bias are not considered. The summarized systematic uncertainties are listed in Table 5.14, where the zero values appear due to the unchanged events input under the modified ranges.

The detailed study of the tag-side interference is not available from the current Belle II thus the Belle result  $\delta\mathcal{S} \sim 0.001$  and  $\delta\mathcal{A} \sim 0.008$  are referenced[49], as shown in Table 5.15.

The contributions at the current stage of Belle II are summarized based on the all the above sources, as shown Table 5.16.

Table 5.14: Systematic uncertainty from vertex reconstruction

source	$\delta\mathcal{S}$	$\delta\mathcal{A}$
$\sigma_{z_{tag}} < 0.05$ cm	0.004369	-0.003599
$\sigma_{z_{tag}} < 0.15$ cm	0.000000	0.000000
$\chi^2/N(CP) < 3$	0.018197	-0.020242
$\chi^2/N(CP) < 13$	0.000000	0.000000
$\chi^2/N(tag) < 40$	0.000000	0.000000
$\chi^2/N(tag) < 60$	0.000000	0.000000
$ \Delta t  < 50$ ps	0.003325	-0.000396
$ \Delta t  < 90$ ps	0.000000	0.000000
IP constraint	0.000000	0.000000
Total	0.019007	0.020563

Table 5.15: Systematic uncertainty of the tag-side interference .

Sources	$\delta\mathcal{S}$	$\delta\mathcal{A}$
tag-side interference	0.001000	0.008000

Table 5.16: The contributions of each source and the total of systematic uncertainty.

Sources	$\delta\mathcal{S}$	$\delta\mathcal{A}$
signal fraction	0.044387	0.033932
background $\Delta t$ shapes	0.039430	0.037269
signal $\Delta t$ shapes	0.033793	0.009283
wrong tag fraction	0.003709	0.003790
fit bias	0.009817	0.005702
physics parameters	0.006923	0.001250
<i>KsFinder</i> impact on data	0.004852	0.000606
vertex reconstruction	0.019007	0.020563
tag-side interference	0.001000	0.008000
Total	0.072186	0.056233

# Chapter 6

## Conclusion, discussion and prospect

The  $CP$  parameters measurement is performed based on the validation of analysis strategies by blind analysis. In the MC study, the fit is performed which shows a consistent result for  $CP$  parameters compared to the simulation input. The linearity and pull of the  $CP$  fit are checked to validate the reliability of the fit procedures. The fit result on  $B^0$  lifetime using experiment data is also agreed with the current value in PDG with a relatively large statistical uncertainty due to the low statistics from data.

After the  $CP$  fit procedures are validated, the  $CP$  parameters  $\mathcal{S}$  and  $\mathcal{A}$  using the Belle II early data with  $62.8 \text{ ab}^{-1}$  in 2019 and 2020 spring and summer is performed. The result is shown in Equation 6.1.

$$\begin{aligned}\mathcal{S} &= -\sin(2\phi_1) = -0.82 \pm 0.85(\text{stat}) \pm 0.07(\text{syst}) \\ \mathcal{A} &= -0.21 \pm 0.28(\text{stat}) \pm 0.06(\text{syst})\end{aligned}\tag{6.1}$$

The result agrees with the prediction of the Standard Model and the previous results from Belle[20] and BaBar[50]. The systematics study is performed considering the main contributing sources at the moment. The measurement precision of  $CP$

parameters in this study is majorly limited due to the large statistical uncertainties from low statistics, which leads to no clear evidence or hint on the NP effects.

In this thesis, the analysis strategies that aim to maximize the efficiency and purity are developed and a conservative measurement approach is taken for the Belle II early data. The newly developed *KsFinder* contributes much in improving the signal significance by effectively rejecting fake  $K_S^0$ , which is also useful in background rejection for other channels with  $K_S^0$  in the final state. The model of the resolution of vertex positions has been studied using MC sample and sideband data, which is benefiting from the understanding of vertex reconstruction performance in the current Belle II detectors. To make a proper use of the reconstructed vertex information and perform a  $CP$  fit compactly, a new  $CP$  fitter is built and being validated, which will serve as a multi-functional analysis tool for the Belle II  $CP$  violation study in future.

## 6.1 Improvements on statistical uncertainty

This study has shown a good potential of performing  $CP$  measurement in Belle II for the incoming years with more data recorded. The precision on  $\mathcal{S}$  requires the large luminosity as shown in Figure 1-6 and the statistical uncertainty in this thesis fits in the scale. With  $50 \text{ ab}^{-1}$  luminosity from the full Belle II data sample in future, the statistical uncertainty is expected to be reduced. The  $CP$  fit on the MC sample with different amount of events used reflects that the statistical uncertainty is reduced proportionally around factor of  $\frac{1}{\sqrt{N}}$ , where  $N$  is the events used in  $CP$  fit. Also, due to the flavor tagging accuracy limitation, the expected statistics of tagged events could be increased as well, however, at this moment no clear sign of large boosting on flavor tagging efficiency or reduction of wrong tagging fraction is foreseen. Therefore, the expected reduction of statistical uncertainty is mostly due to the increased data sample, with current reconstruction efficiency assumed, which is shown in Figure 6-2. As the current luminosity is quite far away from  $50 \text{ ab}^{-1}$ , it is hard to precisely predict the uncertainty in full Belle II luminosity. Given that the expected sensitivity of  $\Delta S$  is in a precision level of three decimal places for both  $\eta' K_S^0$  and  $\phi K_S^0$ [15], therefore

such a precision is taken to estimate the future uncertainties based on the current results. The estimated statistical uncertainty is  $\sim 0.030$  as shown in Figure 6-2.

From Table 4.3, the current  $B^0$  reconstruction efficiency is about 35% which could be further optimized mainly by improving  $K_S^0$  efficiency. As discussed in chapter 3, the  $K_S^0$  reconstruction efficiency and quality becomes worse for long-flight ones. This is mainly due to the limitation of CDC-only tracking and the hit filters on the SVD layers. The current Belle II track finding algorithm rises a requirement for SVD hits that at least two or more SVD hits have to be considered from a same track so that they can be used together during tracking. If a  $K_S^0$  decay outside of layer 5 at 10.4 cm, even though the daughter tracks pass the SVD layer 6, unless they hit the overlapping region of the SVD edges which will create two hits instead of one, otherwise only SVD hits information is missing and such a track become a CDC-only track. This effect is shown in Figure 6-1, where *SVD00* type  $K_S^0$  start to appear at SVD layer 5. Such a algorithm is to suppress the beam background and SVD noise strips that create a large fraction of random single hits. Thus, the actual sensitivity volume of SVD is reduced and the  $K_S^0$  efficiency is negatively affected. In future, the improvement of tracking algorithm is expected to remove this requirement while still be able to effectively reduce single hits background.

In general, the expected  $B^0$  signal yield can be improved in future and help to further reduce the statistical uncertainty. From Figure 6-2, the extrapolated statistical uncertainty at  $0.711 \text{ ab}^{-1}$  using current value is comparable with the Belle result. When the integrated luminosity reaches about  $9 \text{ ab}^{-1}$ , the statistical uncertainty is reduced to  $\sim 0.072$  which is equivalent to the current systematic uncertainty. At  $50 \text{ ab}^{-1}$  integrated luminosity, the major contribution will be systematic uncertainty if no improvement is assumed. We take the extrapolated statistical uncertainty  $\sim 0.030$  at  $50 \text{ ab}^{-1}$  as a conservative value for estimating total uncertainty later.

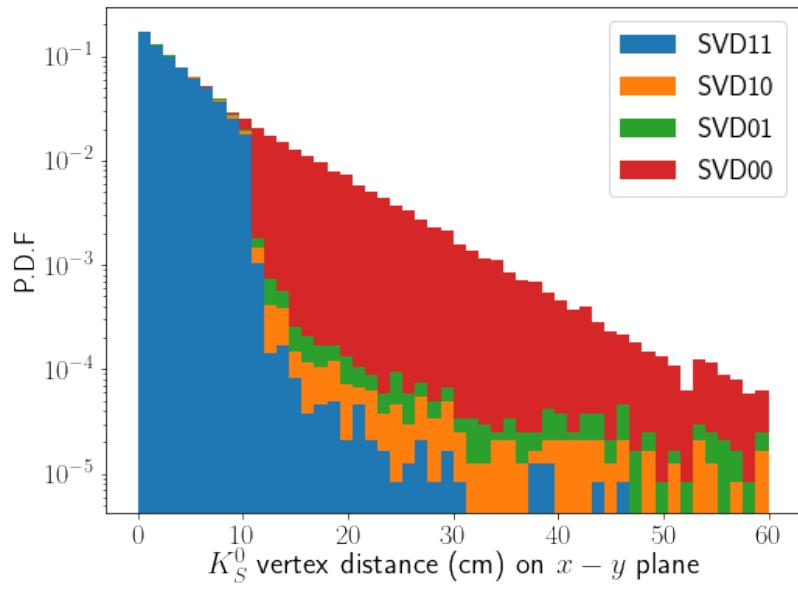


Figure 6-1:  $K_S^0$  flight length on  $x - y$  plane for each category of  $K_S^0$ , where  $SVD00$  type  $K_S^0$  start to appear at about SVD layer 5.

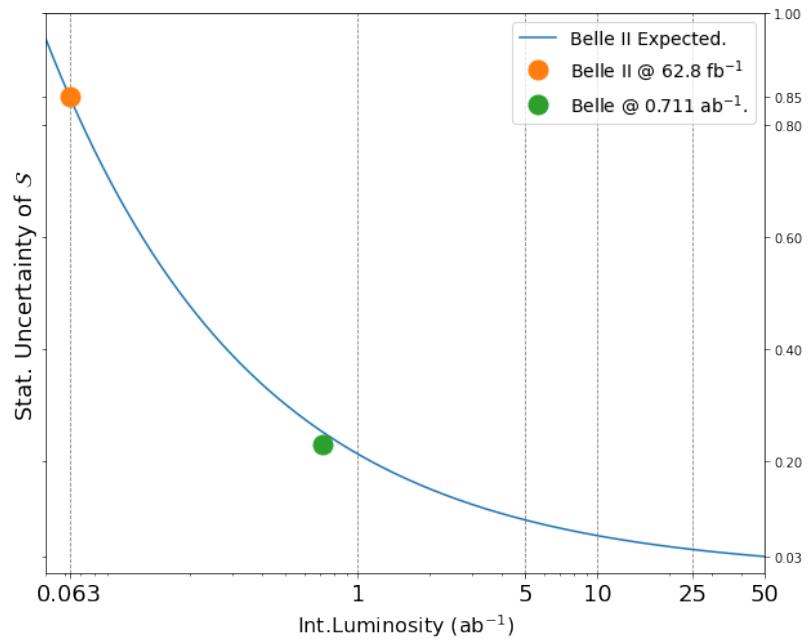


Figure 6-2: Statistical uncertainty of  $\mathcal{S}$  extrapolation based on the current result of  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  in Belle II, where the orange is the current value and the green is the Belle result at  $0.711 \text{ ab}^{-1}$   $\Upsilon(4S)$  data.

## 6.2 Improvements on systematic uncertainty

As discussed in the introduction chapter, the NP effects that potentially contributes to the  $B^0 \rightarrow \phi K_S^0$  could also affect  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$ . In the current SM correction, the QCD factorization (QCDF) scan approach suggests the expected upper-limit for  $\Delta\mathcal{S}$  is about 0.05[15], and the “add-in-quadrature” QCDF predicts the  $\Delta S = 0.01 \sim 0.02$ [15]. In this scale, it’s important to evaluate the reducible and irreducible systematic uncertainties in  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  for future data collection based on the current measurement result. The irreducible sources mainly refer to the terms that are not scaled or improved with increased luminosity, such as the irreducible vertexing related terms and tag-side interference[15]. The reducible sources are mainly the signal  $\Delta t$  shape , the signal fraction, the background  $\Delta t$  shape, the flavor tagging, and the fit bias. As an initial study in early operation with very low statistics, it’s summed that the reducible terms are achieved from the increased future luminosity where the reduction of parameters’ uncertainties are scaled by the fraction of squared-root of increased events statistically. If no improvement on systematic uncertainty is expected from the current evaluation, with the full Belle II data it is still challenging to validate the evidence of the NP effects against the small theoretical predictions. In the Belle II original prospect, the new PXD detector would be contributive to the reduction of vertexing related systematic uncertainties by 50% on average. However, the PXD is not fully installed at the current Belle II and the vertex reconstruction in this analysis doesn’t include IP constraint options. Hence the conservative scenario that systematic uncertainties do not change due to the largely improved vertexing quality is assumed, which makes the increased luminosity the major factor for precision improvements. To show the estimated systematic uncertainties in future, the data collection as well as MC simulation at  $50 \text{ ab}^{-1}$  is taken as reference. Similar to the discussion in statistical uncertainties, the precision level of the estimation is set to three decimal places[15].

For signal  $\Delta t$  shape, we assumed that the  $CP$ -side resolution functions parameters can optimized by increased *signal MC* and better vertex reconstruction. The current

contribution from  $CP$ -side resolution parameters is 0.029946. The overall 50% reduction in the uncertainties of  $CP$  side resolution parameters is assumed, which can be calculated to be 0.015 by using the  $CP$ -side related terms in the Table 5.7. The current tag-side parameters contribution is 0.015658. The tag-side parameters are determined from  $2 \text{ ab}^{-1}$  control sample MC which could be further reduced at the Belle II  $50 \text{ ab}^{-1}$  luminosity so the reduced uncertainties are expected to be about 20% of the current value, which is  $\sim 0.003$ . In Table 6.1, the improvement where both  $CP$  and tag side uncertainties are reduced is calculated to be 0.015 while a conservative case that  $CP$  side resolution remain as the present ones is also considered, which is  $\sim 0.030$ .

Table 6.1: Signal  $\Delta t$  shape systematic uncertainties of  $\mathcal{S}$  expected at  $50 \text{ ab}^{-1}$ . The second and third columns are the expected reduced systematic uncertainties for both  $CP$ /tag-side improvements or only tag-side improvement.

Luminosity ( $50 \text{ ab}^{-1}$ )	both ( $CP$ /tag) improved	only tag-side improved
signal $\Delta t$ shape	$\sim 0.015$	$\sim 0.030$

For the signal fraction contribution which is the largest term in the systematic uncertainties currently, it mainly suffers from the very low statistics in data that causes the inaccurate description of signal shape against background. The signal fraction is determined event-by-event using  $M_{bc}$  and  $\Delta E$  2D fit shape in Figure 4-16. Hence, the uncertainties of signal fraction parameters are expected to be reduced quickly with the increased data collection in future. Using  $1 \text{ ab}^{-1}$  generic MC, the signal fraction contribution is estimated for comparison, where the combined contribution on  $\mathcal{S}$  uncertainty by floating  $\pm 1\sigma$  for each parameter is  $\sim 0.013$ . This estimation is close to the observed systematic uncertainty from signal fraction in the Belle data which is  $\sim 0.015$ [20] and the data scaled value  $\sim 0.011$ , both with  $\mathcal{O}(0.01)$  level difference. Therefore, the current contribution is taken as the baseline to extrapolate the reduced systematic uncertainty in  $50 \text{ ab}^{-1}$  Belle II data, reduced by luminosity ratio to  $\sim 0.002$ , listed in Table 6.2.

For the background  $\Delta t$  shape, it can be reduced by the increased luminosity since

Table 6.2: Signal fraction systematic uncertainties of  $\mathcal{S}$  expected at  $50 \text{ ab}^{-1}$ .

Luminosity ( $50 \text{ ab}^{-1}$ )	Improved uncertainty
Signal fraction	$\sim 0.002$

the current parameters are determined by sideband data with very low statistics. Therefore, the systematic uncertainty from background  $\Delta t$  shape is reduced by factor  $\sim 28$  calculated from  $\sqrt{50/0.063}$  to be  $\sim 0.001$  as listed in Table 6.3. This estimation is checked by comparing the background  $\Delta t$  shape uncertainties in between the Belle result and the one in this analysis, where the background  $\Delta t$  shape contribution in the Belle result is 0.017[20] with a tighter sideband region used, which is consistent with scaled luminosity of the Belle data.

Table 6.3: Background  $\Delta t$  shape systematic uncertainties of  $\mathcal{S}$  expected at  $50 \text{ ab}^{-1}$ .

Luminosity ( $50 \text{ ab}^{-1}$ )	Improved uncertainty
Background $\Delta t$ shape	$\sim 0.001$

For the contributions of wrong tag fraction, the flavor tagging related information is expected to be determined by experimental data using flavor-specific decay modes with increased the Belle II data in future. To estimate the expected uncertainties from the Belle II future data, the results on  $w$  in each  $r$ -bin by using about  $8.7 \text{ fb}^{-1}$  Belle II in 2019 are compared with the Belle results[48]. The flavor tagging performance studied by Belle II early data presented a close efficiency and wrong tag fraction values compared to the Belle results. In each  $r$ -bin, the uncertainties of  $w$  is reduced averagely by factor of  $\sim 11$ , which is consistent with the squared root of the luminosity ratio. Hence, the expected uncertainties at  $50 \text{ ab}^{-1}$  Belle II data is assumed to be  $\sim 7$  times smaller than those from the Belle result[20], which is about  $\sim 0.002$  as listed in Table 6.4.

Table 6.4: Wrong tag fraction systematic uncertainties of  $\mathcal{S}$  expected at  $50 \text{ ab}^{-1}$ .

Luminosity ( $50 \text{ ab}^{-1}$ )	Improved uncertainty
wrong tag fraction	$\sim 0.002$

For the fit bias contribution as systematic uncertainty, currently the values are

taken by the statistical fit error using 300000 *signal MC*. In future, the fit bias contribution is expected to be estimated by taking the larger one among the fit statistical error using more MC sample and the center value difference between the input and output. Thus, if MC sample used in fit could be at least 100 times more than one million in future, then the fit error is possible to be smaller than input-output difference. From the current MC production plan of Belle II, the *signal MC* sample recommended by MC production group is typically in a range of several millions. So the foreseen systematic uncertainty is still going to be the fit error, where we take a 50% reduction of the value 0.009817 from Tabel 5.12 as an estimation similar to the one used in *CP*-side resolution functions, listed in Table 6.5.

Table 6.5: Fit bias systematic uncertainties of  $\mathcal{S}$  expected at 50 ab $^{-1}$ .

Luminosity (50 ab $^{-1}$ )	Improved uncertainty
fit bias	$\sim 0.005$

Concluded from the above discussion, the reducible systematic uncertainties by using increased MC and data in the full Belle II luminosity are estimated and summarized in Table 6.6. It is clear that the dominated contribution in future Belle II data for systematic uncertainty is the *CP* side resolution, indicating the finer study on *CP* side resolution model for no IP-originated tracks is necessary with much larger data sample. In addition, the impact of using *KsFinder* receives contribution from the data MC mismatch on signal purity, which is expected to be improved by better data MC consistency in future. For physics parameters  $\Delta m_d$  and  $\tau_{B^0}$ , the uncertainties could be further reduced by better physics input. Finally, vertex reconstruction options are not contributing much in this analysis mostly because of the very loose cuts and no IP constraint used. However, this does not mean their contributions are missing since the resolution function parameters obtained under such loose IP conditions receives more inaccuracies than the ones from using tighter cuts and IP constraint. The signal  $\Delta t$  shape contribution partially absorbs the expected uncertainties from vertex reconstruction options. In future, by using proper IP constraint and tighter vertex cuts, the signal  $\Delta t$  shape will contribute less and vertex reconstruction will

contribute more to systematic uncertainties. The current systematic uncertainty from the tag-side interference is referenced as  $\sim 0.001$  as a negligible term from the Belle study of  $B^0 \rightarrow (c\bar{c}K^0)$ [49]. In the full Belle II data, such a value is still not considered as an large contribution. We keep it as 0.001 considering it's an irreducible source. The current estimations from *KsFinder*(0.004852), physics parameters(0.006923), the vertex reconstruction(0.019007) and tag-side interference( $\sim 0.001$ ) are unchanged in the  $50 \text{ ab}^{-1}$  Belle II luminosity to have a conservative expectation on  $\mathcal{S}$  systematic uncertainty, shown in Table 6.7.

Table 6.6: Improved systematic uncertainties of  $\mathcal{S}$  expected at  $50 \text{ ab}^{-1}$ . The value in the parenthesis stands for the case that only tag-side resolution is improved and no improvement on  $CP$  side resolution is implemented.

Sources	Improved uncertainty ( $50 \text{ ab}^{-1}$ )
signal $\Delta t$ shape	$\sim 0.015(\sim 0.030)$
Signal fraction	$\sim 0.002$
Background $\Delta t$ shape	$\sim 0.001$
wrong tag fraction	$\sim 0.002$
fit bias	$\sim 0.005$
Total	$\sim 0.016(0.031)$

Table 6.7: The unchanged systematic uncertainties at  $50 \text{ ab}^{-1}$  based on the current luminosity of the Belle II data.

Sources	Unchanged uncertainty ( $50 \text{ ab}^{-1}$ )
<i>KsFinder</i>	0.004852
physics parameters	0.006923
vertex reconstruction	0.019007
tag-side interference	$\sim 0.001$
Total	0.020826

### 6.3 Total uncertainty of $\Delta\mathcal{S}$ at $50 \text{ ab}^{-1}$

The total systematic uncertainty of  $\mathcal{S}$  in the  $50 \text{ ab}^{-1}$  Belle II luminosity is estimated based on the improved terms from Table 6.6 and the unchanged ones from Table 6.7. If  $CP$  side resolution is not improved, the systematic uncertainty is  $\sim 0.037$ . If the  $CP$  side resolution functions is 50% improved, the systematic uncertainty is reduced to

$\sim 0.026$ . Both are shown in Table 6.8 where the major contribution is from signal  $\Delta t$  shapes and the vertex reconstruction options which are both related to the vertexing quality.

Table 6.8: The systematic uncertainty expected in  $50 \text{ ab}^{-1}$  Belle II luminosity. The first column is the current value of systematic uncertainty of  $\mathcal{S}$  in  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$ . The second and third columns are the systematic uncertainties for both  $CP/\text{tag-side}$  improvements or only tag-side improvement used in the combined estimation.

Luminosity( $\text{ab}^{-1}$ )	current( $\sim 0.063$ )	$CP/\text{tag}(50)$	only-tag(50)
Syst.Uncert.( $\mathcal{S}$ )	$\sim 0.072$	$\sim 0.026$	$\sim 0.037$

By adding in quadrature using estimated statistical and systematic uncertainties, the total uncertainty for  $\mathcal{S}$  in  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  in  $50 \text{ ab}^{-1}$  Belle II luminosity is estimated, as shown in Table 6.9. With no  $CP$  vertex resolution improvement, total uncertainty of  $\sim 0.048$  is expected. On the other hand, the total uncertainty will be at  $\sim 0.040$  if 50%  $CP$ -side resolution improvement is assumed, which is a conservative estimation considering that the current  $CP$ -side vertexing performance is not optimized and some unchanged systematic uncertainties could possibly be improved. Given the total uncertainty from  $B^0 \rightarrow J/\psi K_S^0$  at that time is expected to be  $\sim 0.005$ [15],  $\Delta S$  sensitivity is dominated by the total uncertainty in  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$ . The current Belle result from  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  on  $\Delta S$  is  $\sim 0.05$  without taking into account any uncertainty, which is close to the theoretical predicted upper-limit. In general, a total uncertainty at about  $0.040 \sim 0.048$  for  $\Delta S$  at Belle II full luminosity is expected to be a much better probe for addressing whether the NP effects in  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  exist.

Table 6.9: The total uncertainty of  $\mathcal{S}$  in  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  expected in  $50 \text{ ab}^{-1}$  Belle II luminosity, calculated from the expected statistical and systematic uncertainties. The second and third columns are the total uncertainties for both  $CP/\text{tag-side}$  improvements or only tag-side improvement used in the combined estimation.

Luminosity ( $\text{ab}^{-1}$ )	current( $\sim 0.063$ )	$CP/\text{tag}(50)$	only-tag(50)
Tot.Ucert.( $\mathcal{S}$ )	$\sim 0.853$	$\sim 0.040$	$\sim 0.048$

## 6.4 *KsFinder* importance

While monitoring the uncertainties of the  $CP$  parameters is crucial in searching the hidden NP effects, avoiding bias in the measurement is also critical. If a total uncertainty at  $\sim 0.03$  is achieved in future, however, the center value of  $\mathcal{S}_{3K_S^0}$  is biased and shifted away from  $\mathcal{S}_{J/\psi K_S^0}$ , it can lead to a very wrong conclusion about the discovery of the NP effects. The *KsFinder* contributes to improve the signal purity for measuring  $CP$  parameters, which is essential in controlling the potential bias introduced by the large fraction of background events that yield random  $CP$  asymmetry due to the statistical fluctuation. The larger background events without using *KsFinder* cut in Table 4.2 can produce the wrongly estimated signal fraction ( $f_{sig}$ ) in Equation 5.5 so that the  $CP$  parameters are biased using the biased fit model. Especially when the luminosity is increased in future, the signal fraction uncertainty is expected to be largely reduced, such a biased signal fraction will be treated as a large contribution to the systematic uncertainty compared to the correct ones. To demonstrate the effect, the signal extraction and  $CP$  fit on the  $1 \text{ ab}^{-1}$  *generic MC* sample without *KsFinder* are performed. In this case, we remove the *KsFinder* cut in Table 4.2 and apply the cut  $\text{cosVertexMomentum} > 0.9$  which can only achieve  $\sim 82\%$  purity for  $K_S^0$  in *signal MC*. The signal significance in  $M_{bc}$  and  $\Delta E$  2D fit is considerably lower than the ones with using *KsFinder*. The stacked histograms of  $M_{bc}$  and  $\Delta E$  with much higher background are shown in Figure 6-3 where the red component is signal. There are 352 true signal events and 543 background events inside the signal region by count. In the meanwhile, the 2D fit on  $M_{bc}$  and  $\Delta E$  are shown in Figure 6-4. From the 2D fit, the signal events number is  $389 \pm 19$  and background events number is  $502 \pm 15$ . Clearly the signal fraction defined by the 2D fit in the latter case is biased from the MC truth, which shows a positively biased signal fraction on average, as summarized in Table 6.10.

From Table 6.10, by using *KsFinder*, the true average signal fraction in signal region from  $1 \text{ ab}^{-1}$  *generic MC* is  $83.2\%$ , and the fit result is  $(84.8 \pm 3.7)\%$ . To contrary, by only using  $\text{cosVertexMomentum} > 0.9$ , the true average signal fraction

Table 6.10: The signal and background events using different  $K_S^0$  selection cuts compared with the *generic MC* counts, showing that signal events reconstructed using *KsFinder* is more precise to the MC truth.

Selection	signal	background
<i>FBDT_Ks</i> > 0.74 (fit)	$341 \pm 20$	$61 \pm 17$
<i>FBDT_Ks</i> > 0.74 (MC)	336	68
<i>cosVertexMomentum</i> > 0.9 (fit)	$389 \pm 19$	$502 \pm 15$
<i>cosVertexMomentum</i> > 0.9 (MC)	352	543

is 39.3% and the fit result is  $(43.7 \pm 1.4)\%$ , which shows over  $3\sigma$  deviation as a strong bias. If such a bias is taken into account as the systematic uncertainty, signal fraction difference is used as a floating value to check the impact on the  $CP$  fit results, which leads to an extra systematic uncertainty from the biased  $f_{sig}$  at level of  $\sim 0.006$ , already larger than any other reducible source except for the signal  $\Delta t$  shapes as listed in Table 6.6. Therefore, the development of *KsFinder* is particularly important in the precised  $CP$  measurement for  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$ . The current performance of *KsFinder* is presenting a purity about 95% in  $K_S^0$  reconstruction which means there is still small room for improvements, as well as the background rejection power. The targeted purity and background rejection power of *KsFinder* in future is  $\sim 99\%$  on average. The data/MC consistency should also be improved so the current correction ratio  $R_{B^0}$  is expected to be reduced to  $\sim 1.00 \pm 0.01$ . Thus the systematic uncertainty from different *KsFinder* responses in between data and MC is assumed to be  $\mathcal{O}(0.001)$  as a negligible contribution.

## 6.5 Prospect

Even though the current result on  $CP$  parameters are dominated by the large uncertainty, mostly from the statistical one, the previous discussions about the future uncertainties have shown a good potential of searching for the NP effects in  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$  based on the current analysis in this thesis. At integral luminosity at  $50 \text{ ab}^{-1}$ , the uncertainty on  $\mathcal{S}$  would be reduced to a comparable value around  $0.040 \sim 0.048$  realistically, as shown in Figure 6-5, where the statistical and reducible systematic

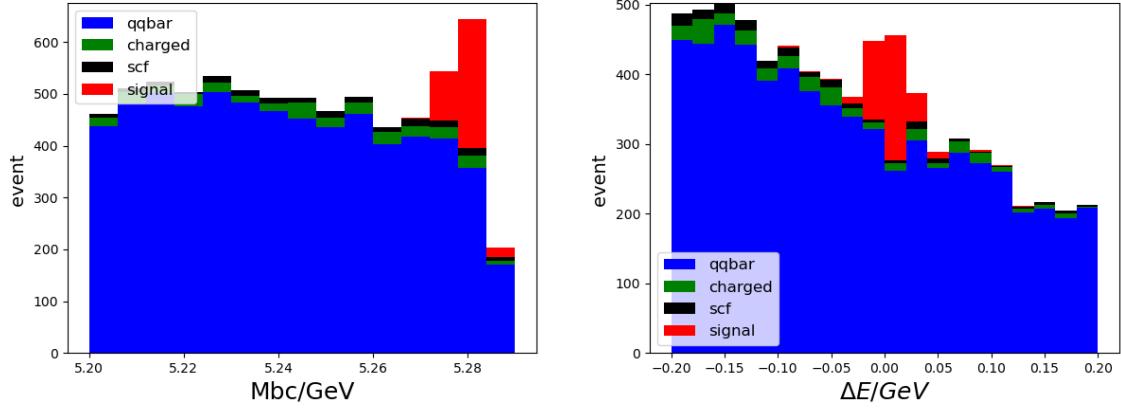


Figure 6-3:  $M_{bc}$  and  $\Delta E$  stacked histogram of  $1 \text{ ab}^{-1}$  generic MC sample replacing  $FBDT\_Ks > 0.74$  by  $\text{cosVertexMomentum} > 0.9$  in Table 4.2 as a selection criteria, showing a much worse signal significance.

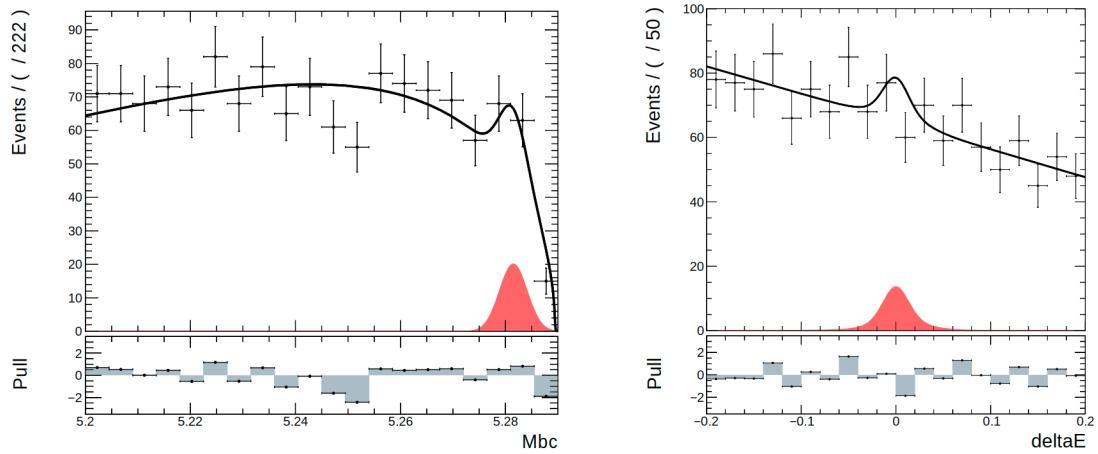


Figure 6-4:  $M_{bc}$  and  $\Delta E$  2D fit on  $1 \text{ ab}^{-1}$  generic MC sample, replacing  $FBDT\_Ks > 0.74$  by  $\text{cosVertexMomentum} > 0.9$  in Table 4.2. The red is signal component.

uncertainties are assumed to be scaled by the squared root of the integrated luminosity. The expected sensitivity in full Belle II data is proven to be competitive and the analysis workflow is built which will be further improved along with the future Belle II data taking and MC production. In conclusion, the progress that has been made so far in this thesis paves a well-constructed and solid path for searching the NP effects in time dependent  $CP$  violation study of  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$ .

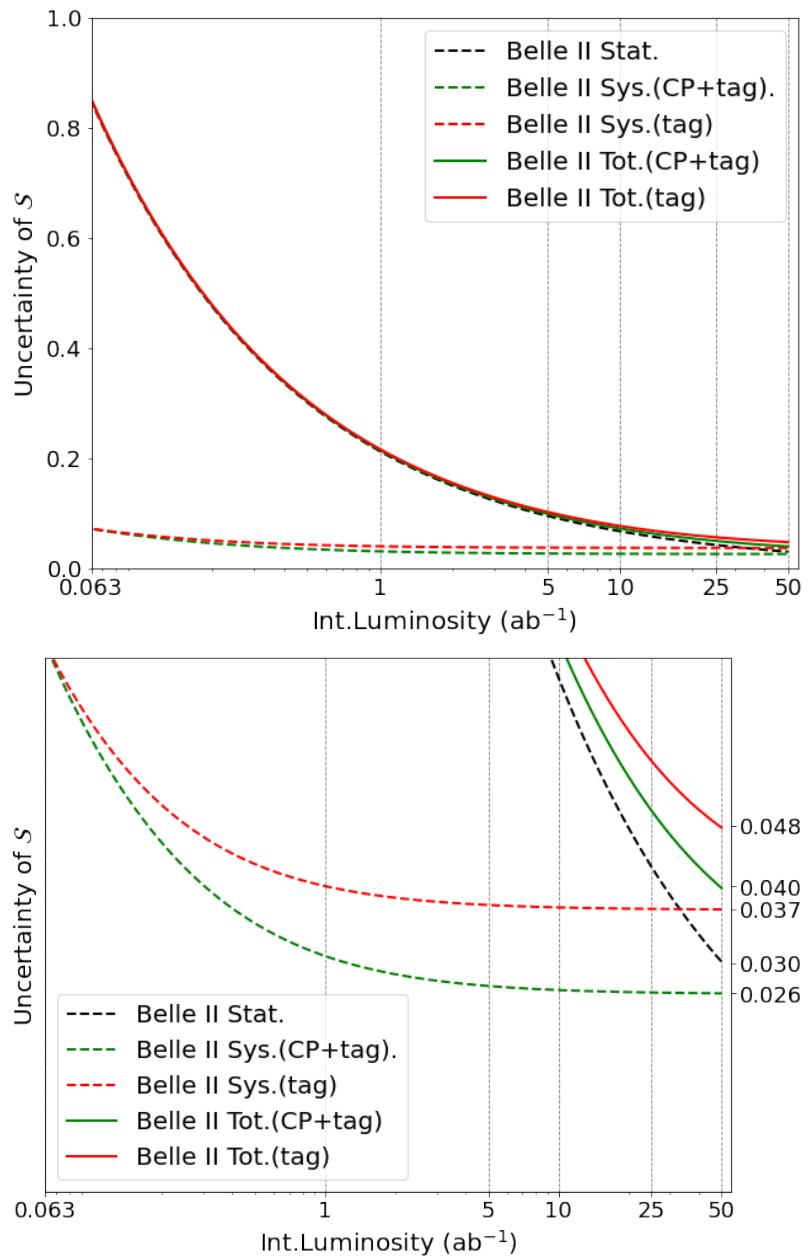


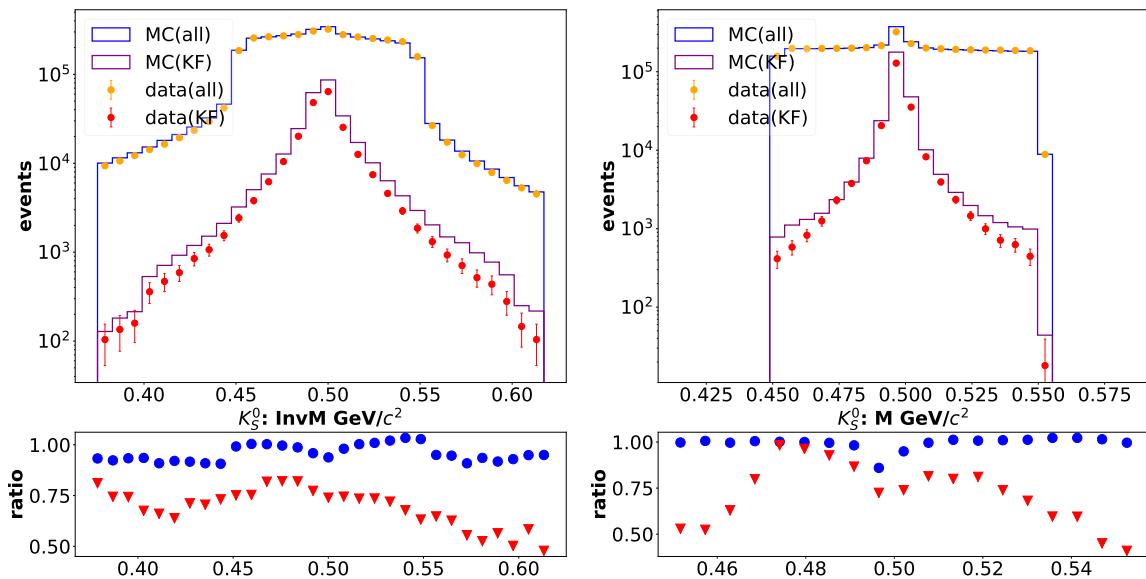
Figure 6-5: The expected total uncertainty of  $\mathcal{S}$  in  $B^0 \rightarrow K_S^0 K_S^0 K_S^0$ , where the dashed lines are the statistical(black),  $CP$ /tag-side improved systematic(green) and only tag-side improved systematic(red) uncertainties, with the corresponding solid lines as the total uncertainties. The top is the overview for the whole Belle II luminosity range from now, and the bottom is  $y$ -axis zoom-in.

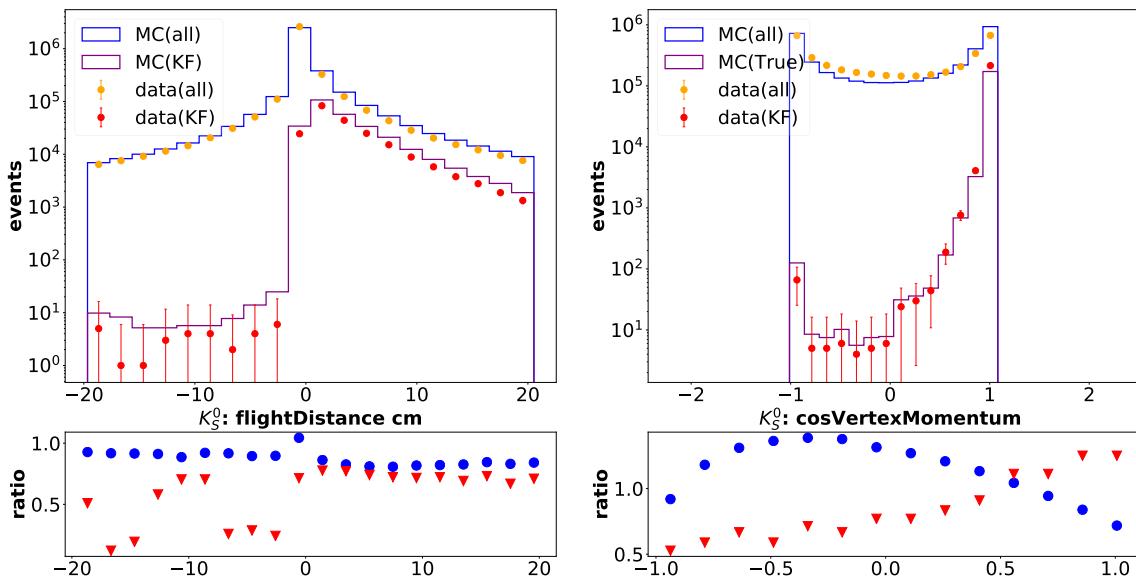
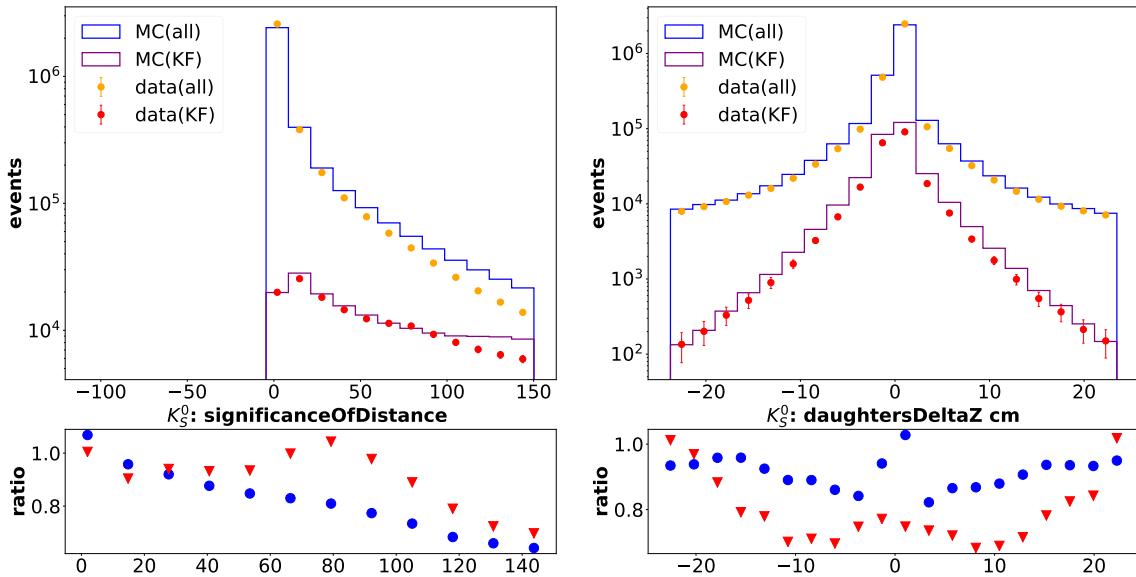


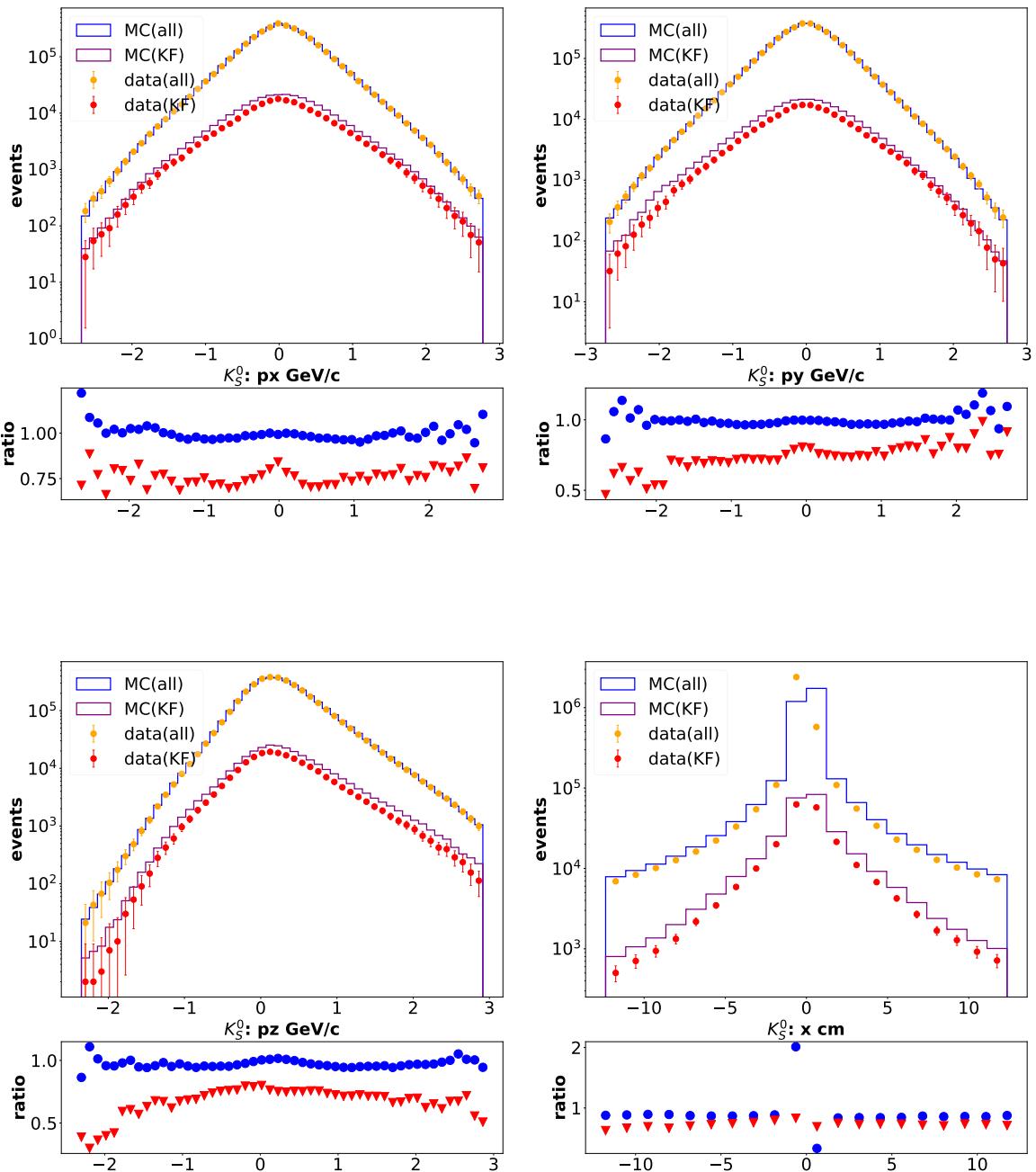
# Appendix A

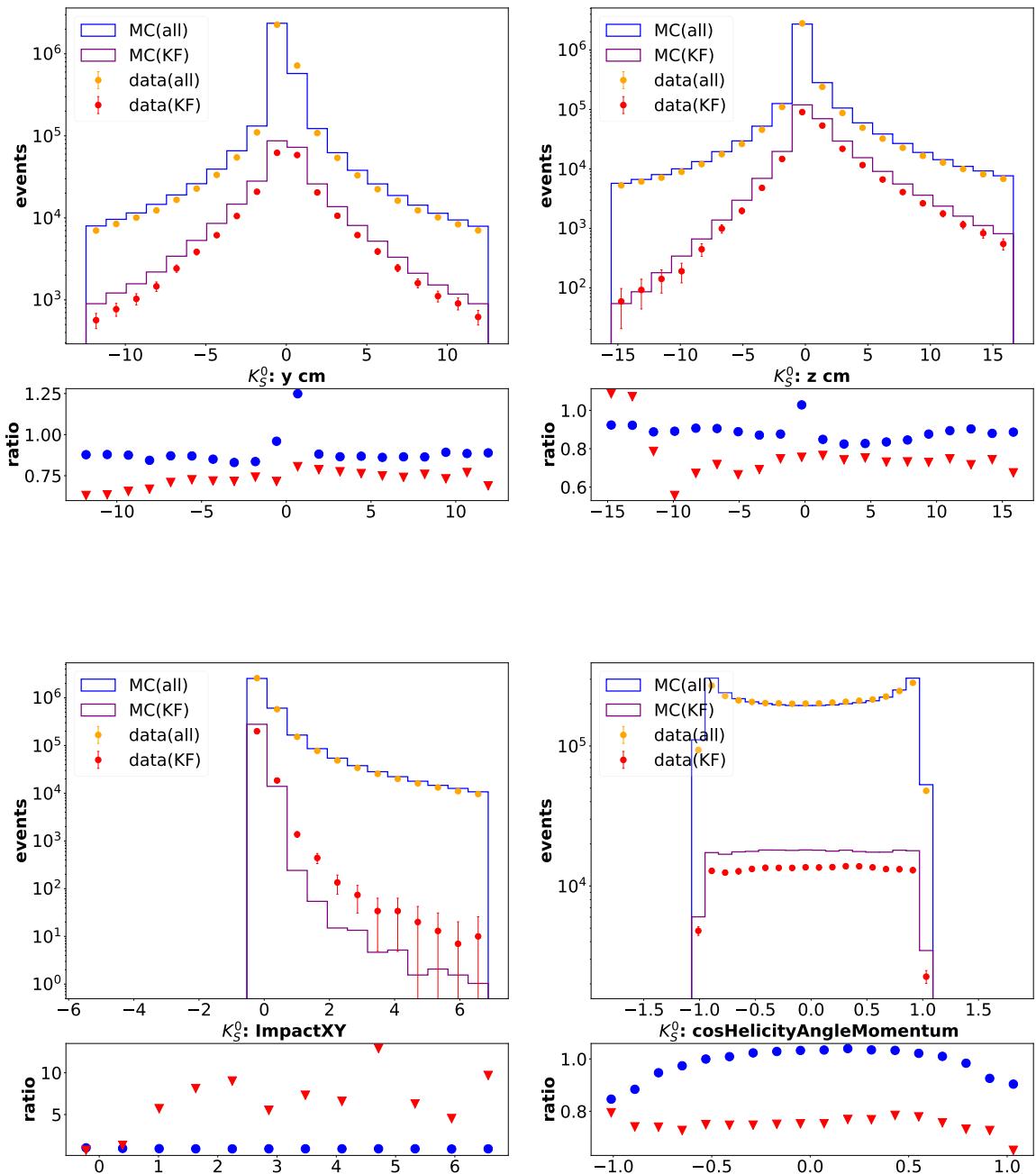
## Data Validation Plots for $K_S^0$

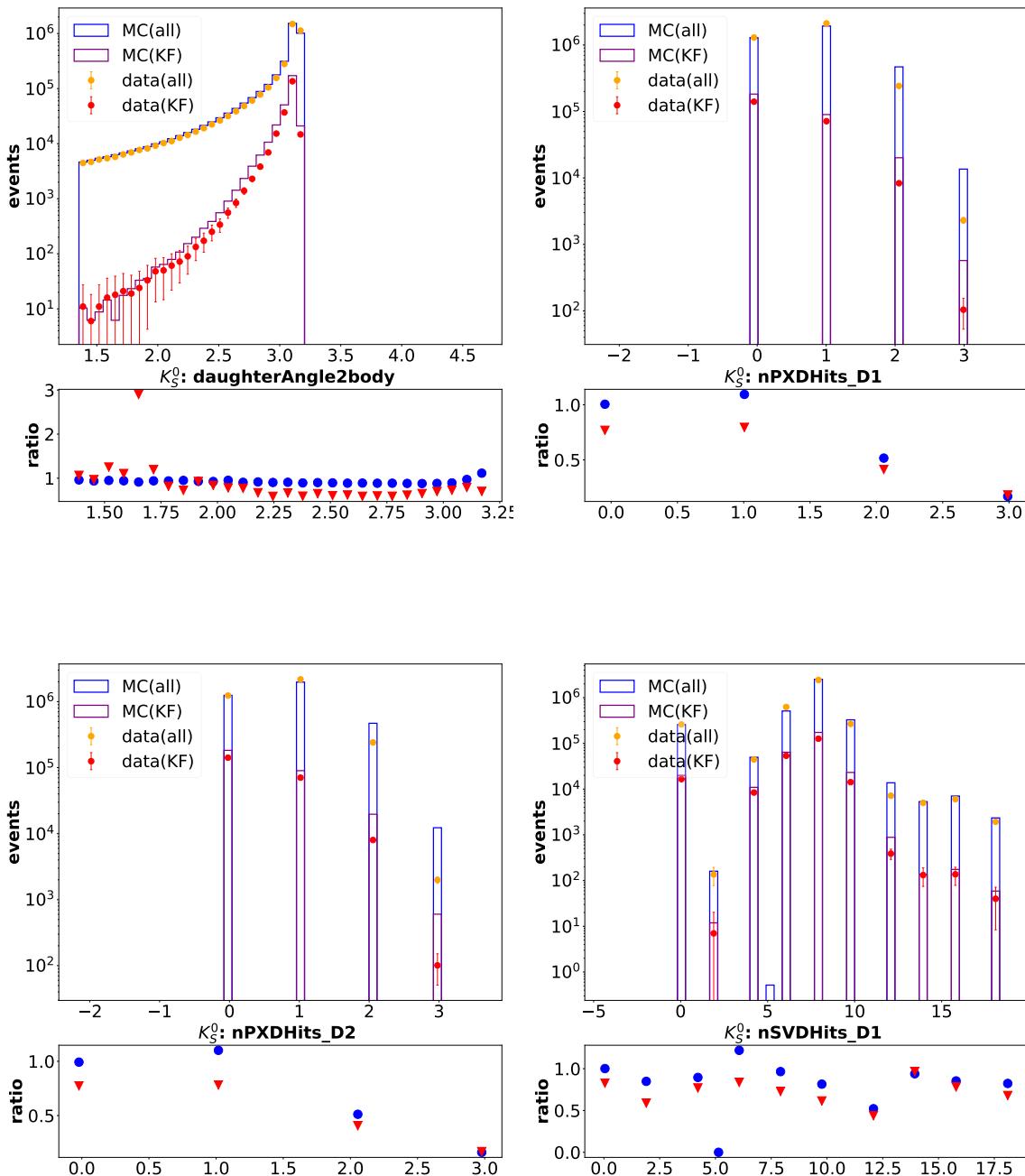
Figure A-1: The distribution of the training variables in KsFinder. The blue and purple solid lines are the total and true  $K_S^0$  distributions from generic MC, respectively. The yellow and red dots are the data distribution before and after applying KsFinder cut. The uncertainties in data are taken as three times the Poisson standard deviation.

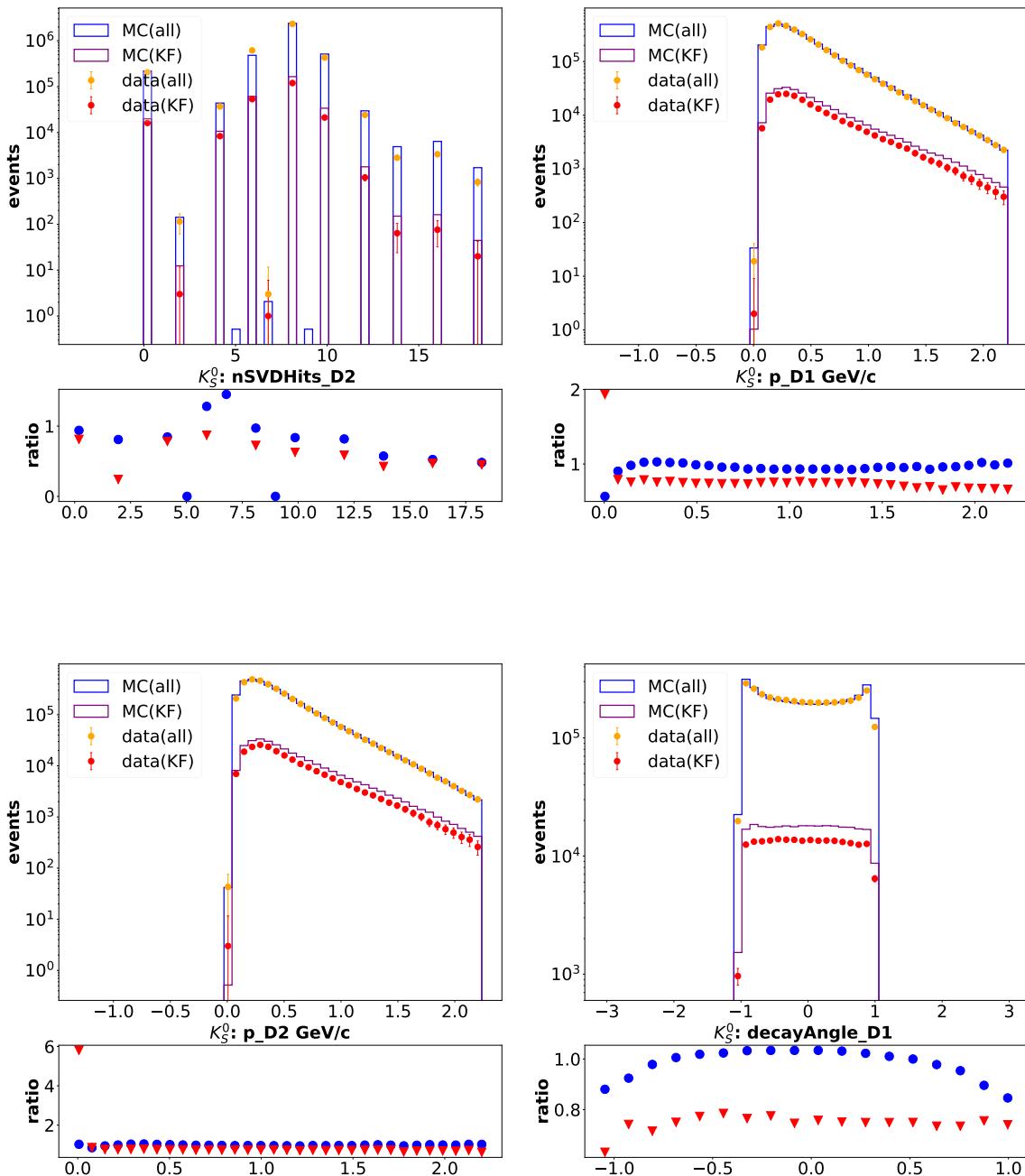


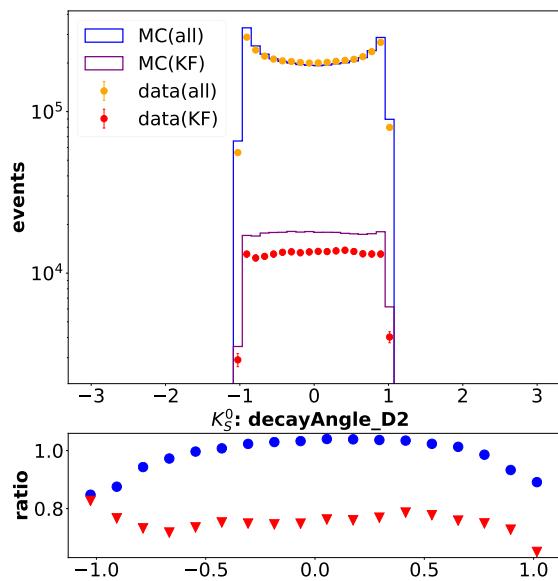














# **Appendix B**

## **Control Samples**

Table B.1: Hadronic control sample reconstruction criteria. The first column stands for the  $B$  decay to neutral and charged  $D$  or  $D^*$ . The second column stands for the  $D$  decay as intermediate states of the  $B$  decay, which includes  $D^{*+} \rightarrow D^0\pi^+$ ,  $D^0 \rightarrow K^-\pi^+, K^-\pi^+\pi^0, K^-\pi^+\pi^-\pi^+$  and  $\rho^+ \rightarrow \pi^+\pi^0$ [45].

$B$ decay	$D$ decay	$ M_{Kn\pi} - M_D $	$\Delta M_{D^*}$	$R_2$	$\cos\theta_{th}$
$B^+ \rightarrow \bar{D}^0\pi^+$	$D^0 \rightarrow K^-\pi^+$	$< 4\sigma$	-	-	-
	$D^0 \rightarrow K^-\pi^+\pi^0$	$< 3\sigma$	-	$< 0.45$	-
	$D^0 \rightarrow K^-\pi^+\pi^-\pi^+$	$< 2\sigma$	-	$< 0.45$	-
$B^0 \rightarrow D^{*-}\pi^+$	$D^0 \rightarrow K^-\pi^+$	$< 10\sigma$	$< 5 \text{ MeV}/c^2$	-	-
	$D^0 \rightarrow K^-\pi^+\pi^0$	$< 3.5\sigma$	$< 3 \text{ MeV}/c^2$	-	$< 0.98$
	$D^0 \rightarrow K^-\pi^+\pi^-\pi^+$	$< 4\sigma$	$< 4 \text{ MeV}/c^2$	$< 0.6$	-
$B^0 \rightarrow D^{*-}\rho^+$	$D^0 \rightarrow K^-\pi^+$	$< 7\sigma$	$< 4 \text{ MeV}/c^2$	$< 0.6$	$< 0.95$
	$D^0 \rightarrow K^-\pi^+\pi^0$	$< 3.5\sigma$	$< 12 \text{ MeV}/c^2$	-	$< 0.98$
	$D^0 \rightarrow K^-\pi^+\pi^-\pi^+$	$< 3.5\sigma$	$< 3 \text{ MeV}/c^2$	-	$< 0.92$
$B^0 \rightarrow D^-\pi^+$	$D^+ \rightarrow K^-\pi^+\pi^-$	$< 2\sigma$	-	$< 0.5$	$< 0.995$

## Appendix C

$2K_S^0$  invariant mass distribution  
where A,B and C are in the  
increasing order of momentum

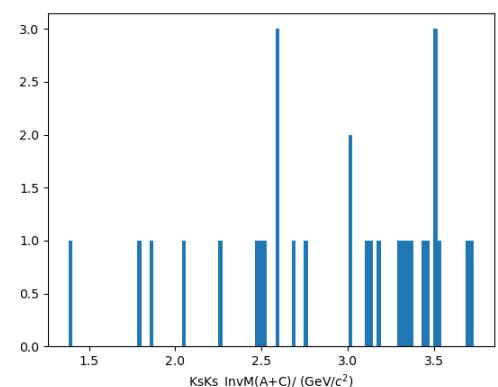
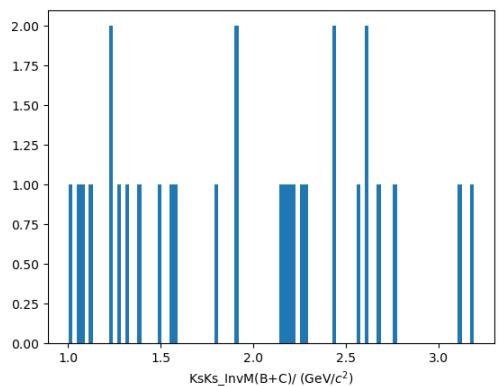
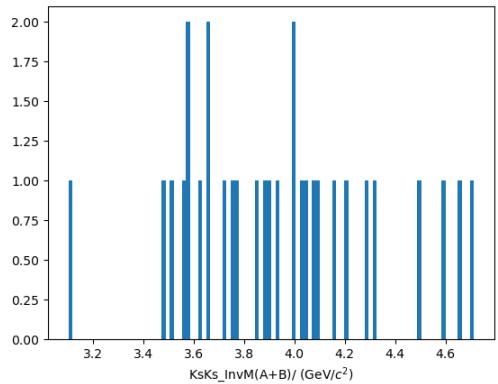


Figure C-1: Data in signal region

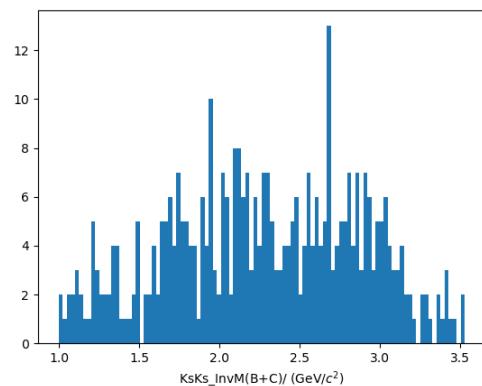
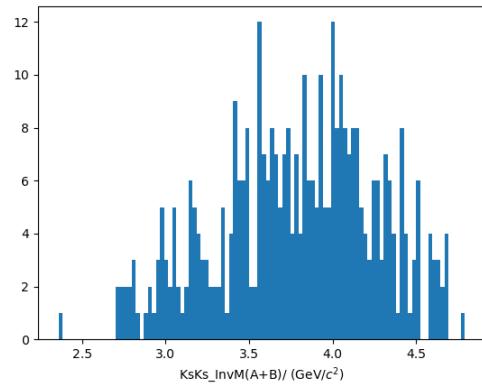
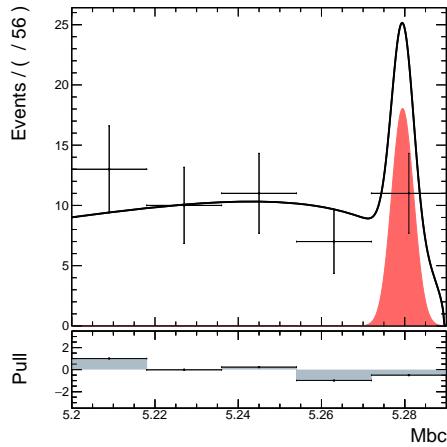


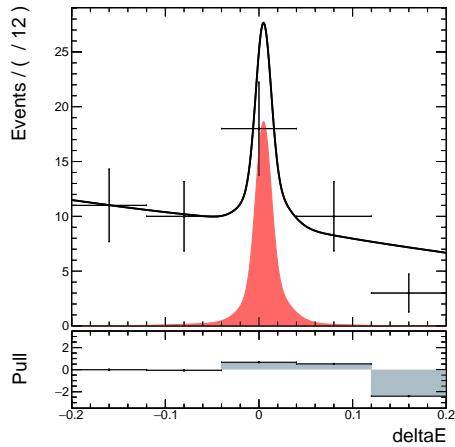
Figure C-2: Generic MC in signal region.

## Appendix D

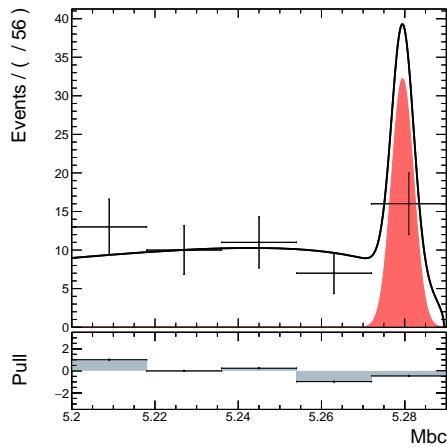
### Injection test for $B^0$ signal yield



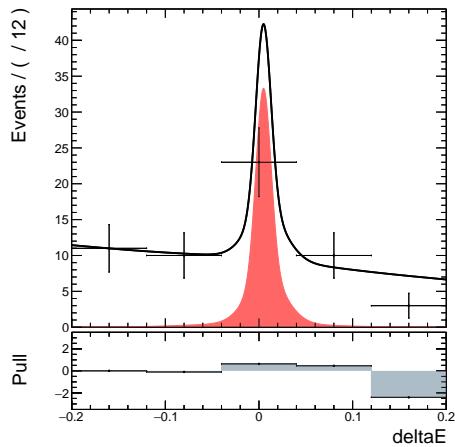
a) signal injected: 5



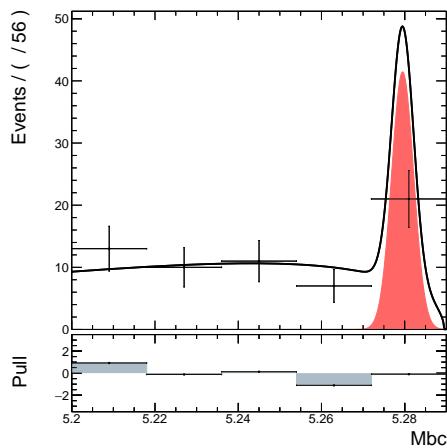
b) signal injected: 5



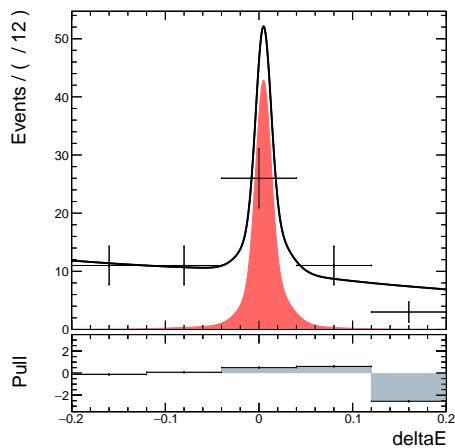
c) signal injected: 10



d) signal injected: 10



e) signal injected: 15



f) signal injected: 15

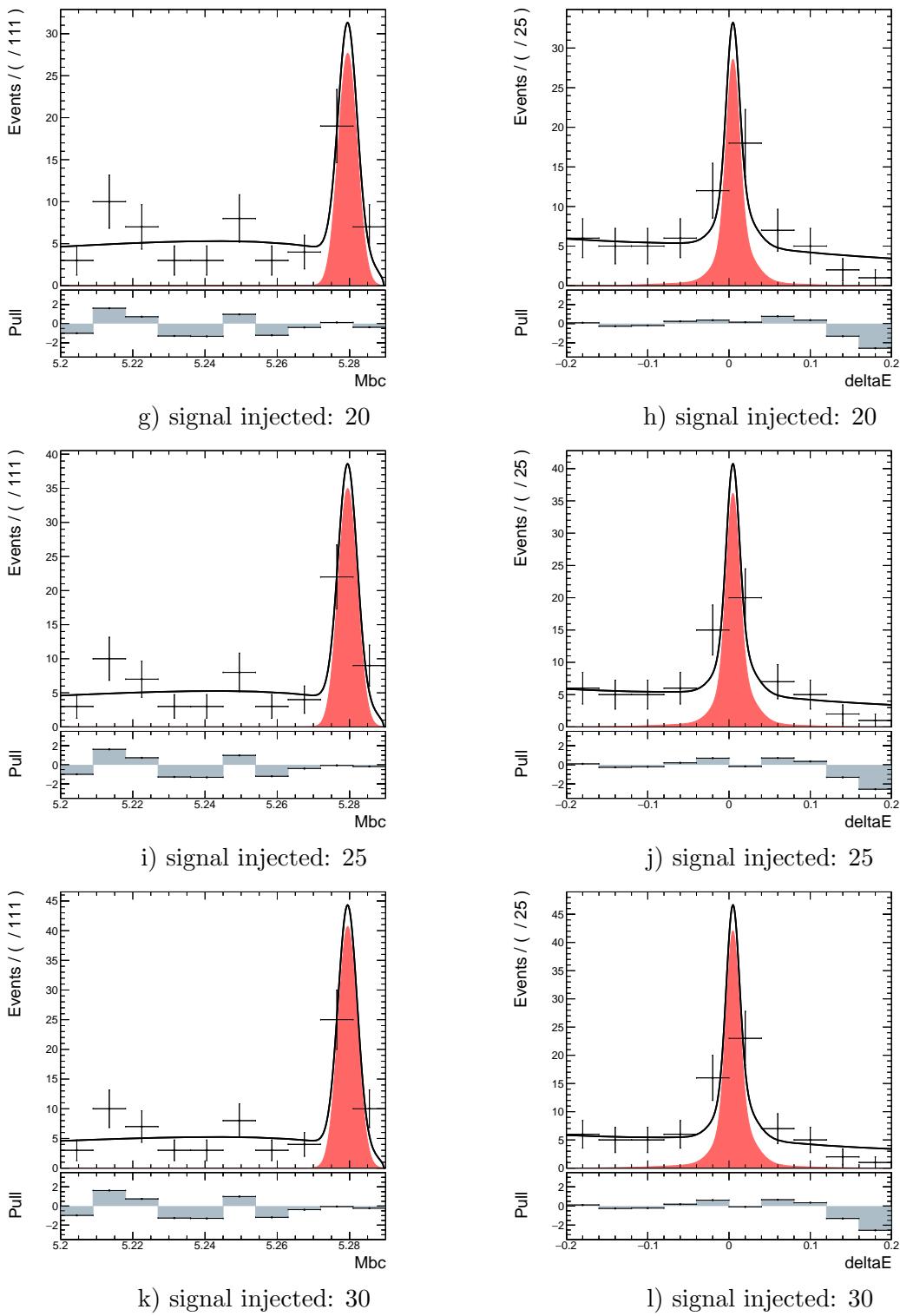


Figure D-1: The fit results of  $M_{bc}$  and  $\Delta E$  in signal injection test, where signal events from 5 to 30 with 5 per step are injected with 46 continuum events.



## Appendix E

### The *KsFinder* impact on $M_{bc}$ , $\Delta E$ and vertex positions.

*KsFinder* provides a classification variable  $FBDT_{Ks}$  to be used as a cut to improve the purity of the  $K_S^0$  and  $B^0$ . Thus, it's essential to check the potential impact on  $M_{bc}$  and  $\Delta E$ , as well as vertex positions on  $z$ -axis of  $B^0$  after applying *KsFinder*. The  $K_S^0$  classification uses information such as invariant mass and decay vertex positions which may propagate bias into  $B^0$  signal extraction, eventually may affect the measurement of  $CP$  parameters.

For  $K_S^0$  candidates with full SVD hits from their daughter pion tracks, the *KsFinder* can perform a better classification on whether it's a true  $K_S^0$  or not, compared to those  $K_S^0$  candidates with less SVD hits information. This is because the tracking quality and invariant mass from the fit is highly dependent on the SVD hits information, which plays an important role in calculating input variables used in the *KsFinder*. For example, a true  $K_S^0$  is more likely to be wrongly classified if all of its daughter pions have no SVD hits, so the reconstruction can only be done by using 6 CDC-only tracks. Rejecting these candidates might introduce biases. Therefore, given each type of  $B^0$  based on how many CDC-only tracks it has in the final states, the comparison on  $M_{bc}$  and  $\Delta E$  with or without *KsFinder* is performed by fitting the distribution in *signal MC*.  $M_{bc}$  and  $\Delta E$  are modeled by signal and double Gaussian functions, respectively. Comparing corresponding fit results, no clear bias on  $M_{bc}$  and

$\Delta E$  is found by using *KsFinder* where fit results are agreed well within one standard deviation. The fit results are shown in Figure E-1 and E-2.

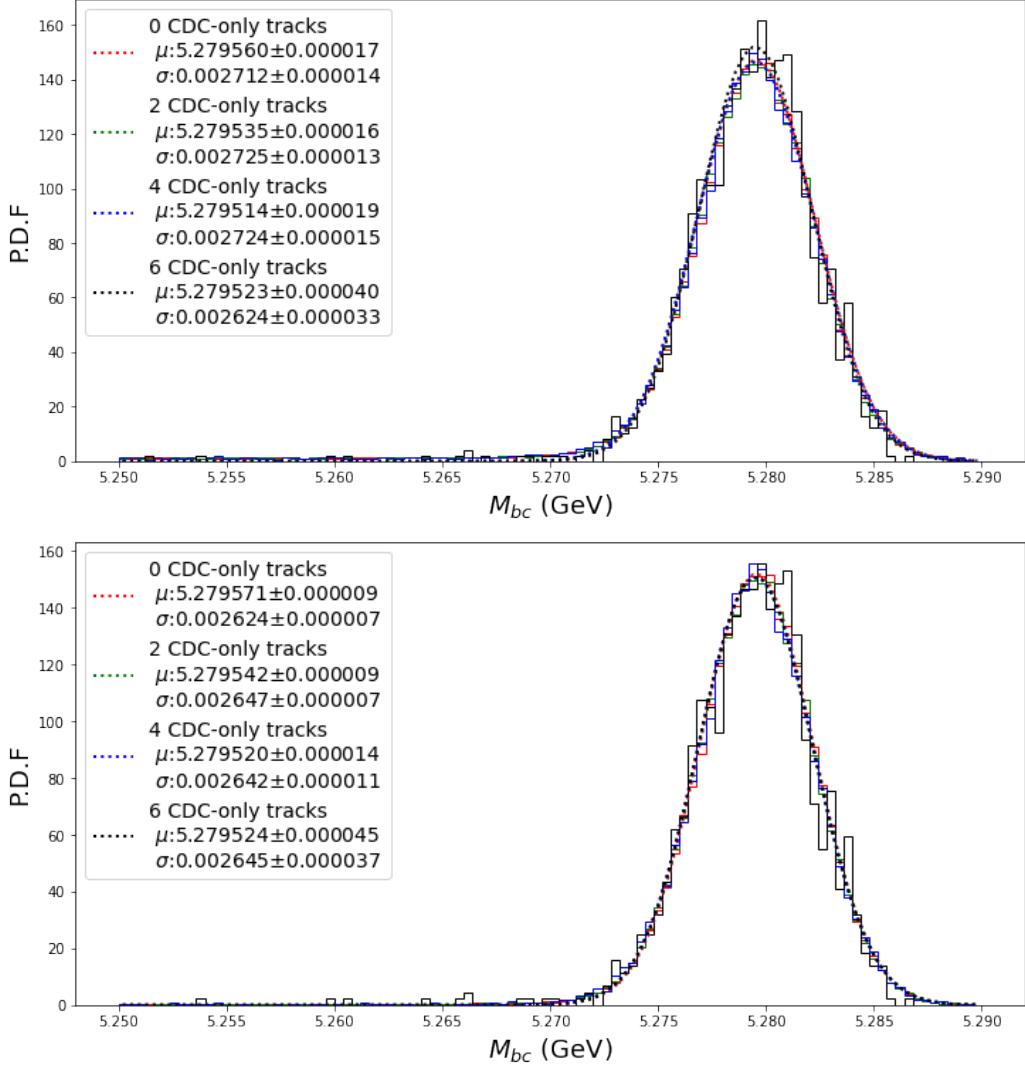


Figure E-1:  $M_{bc}$  distribution based on the number of CDC-only tracks in final states. Top: no *KsFinder* used; Bottom: *KsFinder* used. The  $\mu$  and  $\sigma$  are the mean and standard deviation of the Gaussian function.

Similar to the comparison of  $M_{bc}$  and  $\Delta E$ , the  $z$  direction vertex position and the vertex position difference  $\Delta z$  between *CP* and tag sides are also checked, in which no clear bias are found either. The  $z$  and  $\Delta z$  are modeled using single Gaussian with the same mean but different standard deviation. The results are shown in Figure E-3 and E-4. It is obvious that in Figure E-3, the *CP*-side resolution of vertex on  $z$ -axis is wider when the final states of  $B^0$  have more CDC-only tracks, especially when all

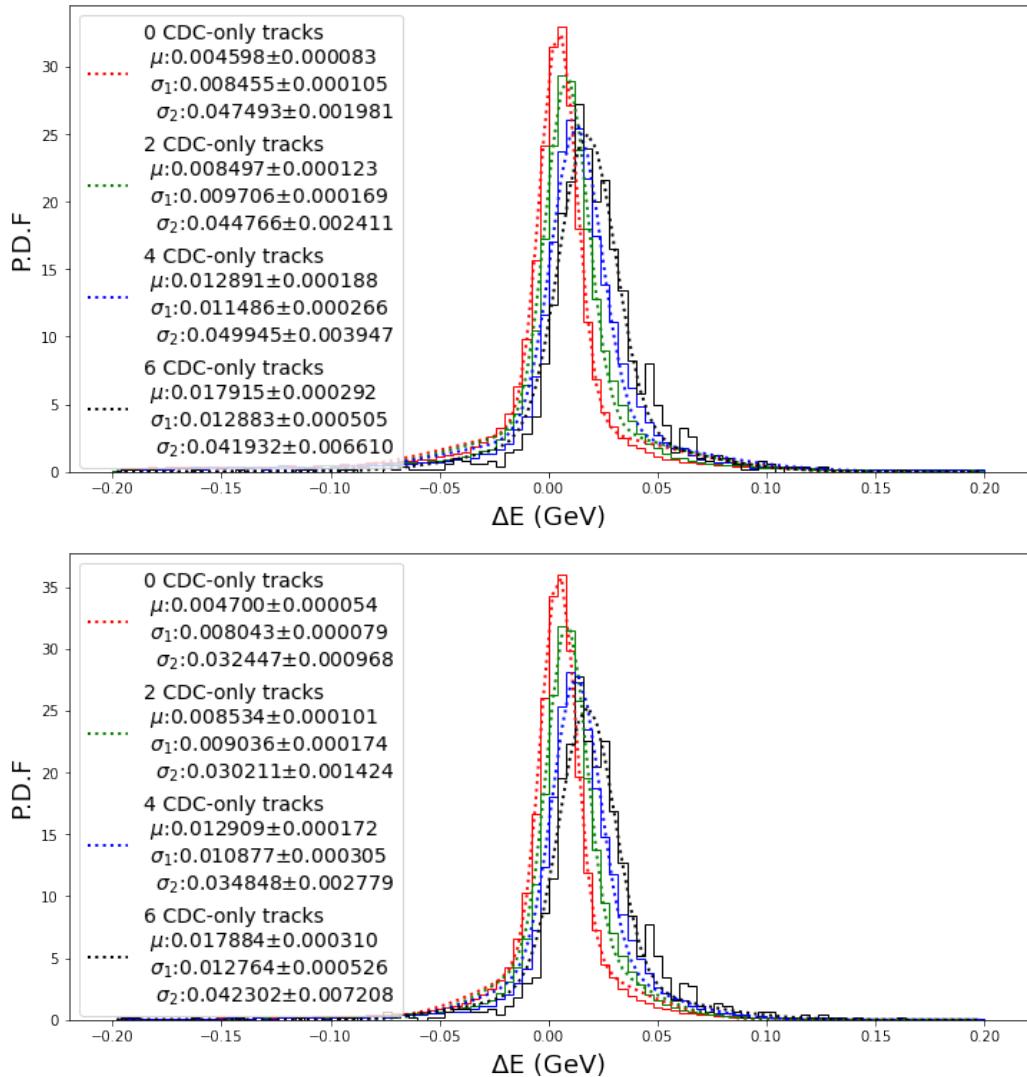


Figure E-2:  $\Delta E$  distribution based on the number of CDC-only tracks in final states. Top: no *KsFinder*; Bottom: *KsFinder* used. The  $\mu$  is the common mean for double Gaussian. The  $\sigma_1$  and  $\sigma_2$  are the standard deviations of the Gaussian function.

the tracks only contains CDC hits (6 CDC-only tracks).

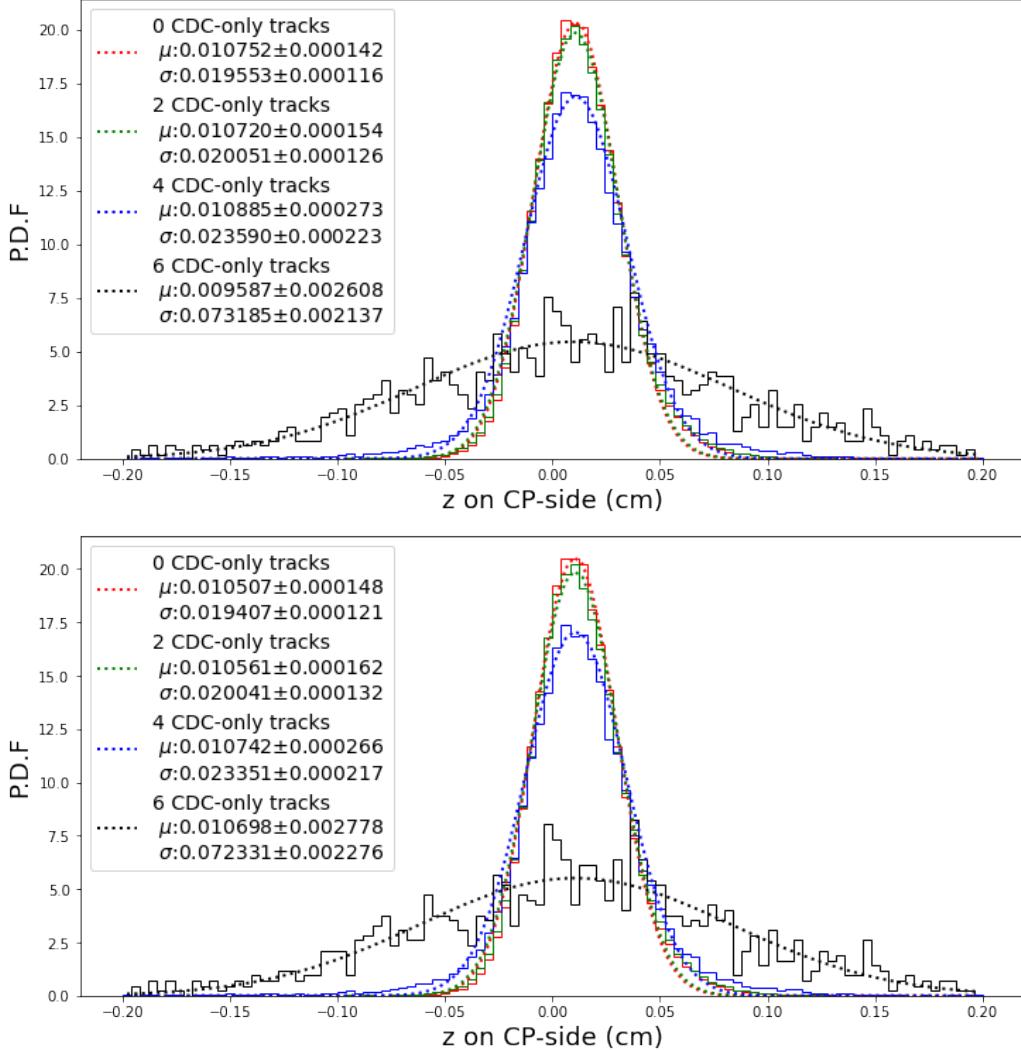


Figure E-3:  $\Delta z$  distribution based on the number of CDC-only tracks in final states. Top: no *KsFinder*; Bottom: *KsFinder* used. The  $\mu$  and  $\sigma$  are the mean and standard deviation of the Gaussian function.

Above all, no clear appearance of bias on  $M_{bc}$  and  $\Delta E$  distributions, as well as vertex positions from using *KsFinder* has been found, *KsFinder* may implement a small shift on the vertex position which is negligible compared to the large statistical uncertainty due to the current low luminosity. Hence, there's no correction on these observables are applied in this analysis, and the systematic uncertainty from *KsFinder* is evaluated by taking into account of  $R_{B^0}$  in signal fraction calculation which comes from the potential discrepancy of *KsFinder* responses among data and MC.

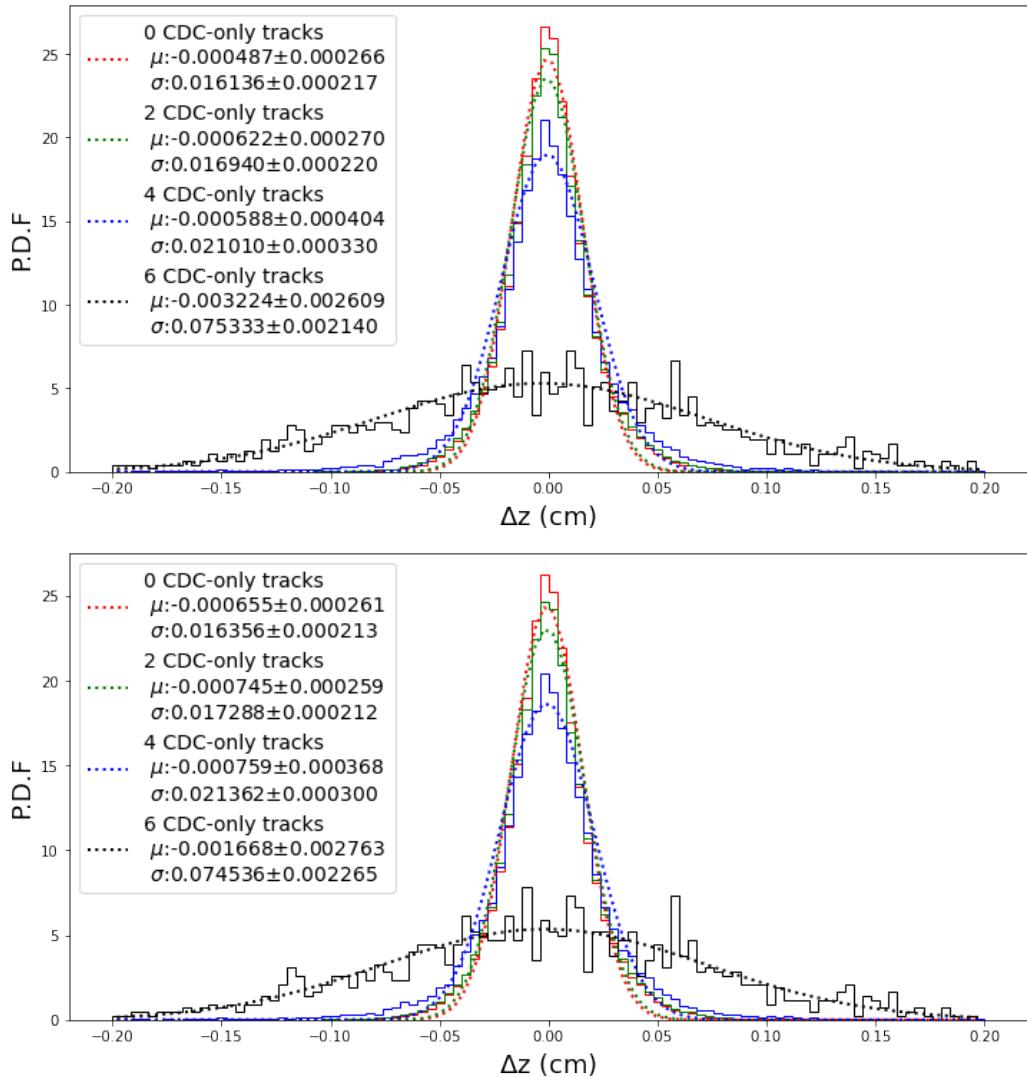


Figure E-4:  $\Delta z$  distribution based on the number of CDC-only tracks in final states. Top: no *KsFinder*; Bottom: *KsFinder* used. The  $\mu$  and  $\sigma$  are the mean and standard deviation of each Gaussian function.



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