

3) $(f_m)_{m \geq 1}$; $f_m(x) = x \operatorname{arctg}(mx)$ converge uniform on $J = [0, \infty)$

S: $\sum_{m \geq 1} f_m$; $f_m: J \rightarrow \mathbb{R}$ is uniform convergent on his crowd
 convergence $J \Leftrightarrow (\forall) \varepsilon > 0, \exists N(\varepsilon) > 0$ s.t. $\forall m > N(\varepsilon)$;
 $(\forall) x \in J \Rightarrow |f_{m+1}(x) + f_{m+2}(x) + \dots + f_{m+p}(x)| < \varepsilon$, where $p \in \mathbb{N}$
 and $p=1$

$$\left. \begin{array}{l} \text{s.t. } (\forall) m > N(\varepsilon) \\ |f_{m+1}(x)| < \varepsilon \end{array} \right\} \Rightarrow |x \operatorname{arctg}(mx)| < \varepsilon \Big|_{x \in [0, \infty)} \Rightarrow |\operatorname{arctg} x(mx)| < \frac{\varepsilon}{x}$$

$$\Rightarrow \operatorname{arctg} mx < \frac{\varepsilon}{x} \Rightarrow mx < \operatorname{tg} \frac{\varepsilon}{x} \Rightarrow m < \frac{\operatorname{tg} \frac{\varepsilon}{x}}{x}$$

$$N(\varepsilon) = \left[\frac{\operatorname{tg} \frac{\varepsilon}{x}}{x} \right] + 1$$