

# 1995 IMO P1

LIN LIU

November 23, 2021

## Problem

Let  $A, B, C, D$  be four distinct points on a line, in that order. The circles with diameters  $AC$  and  $BD$  intersect at  $X$  and  $Y$ . The line  $XY$  meets  $BC$  at  $Z$ . Let  $P$  be a point on the line  $XY$  other than  $Z$ . The line  $CP$  intersects the circle with diameter  $AC$  at  $C$  and  $M$ , and the line  $BP$  intersects the circle with diameter  $BD$  at  $B$  and  $N$ . Prove that the lines  $AM, DN, XY$  are concurrent.

## Solution

It remains to prove that quadrilateral  $AMND$  so that we can use the radical axis theorem and finish the problem. Notice that quadrilateral  $MBCN$  is cyclic. Now we do an angle chase.

$$\begin{aligned}\angle MND &= \angle MNB + 90^\circ = \angle MCB + 90^\circ = \angle MCA + 90^\circ \\ &= 90 - \angle MAC + 90 = 180 - \angle MAC = 180 - \angle MAD. \quad \blacksquare\end{aligned}$$