

2019 ISL G1

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September 26, 2021

Problem

Let ABC be a triangle. Circle Γ passes through A , meets segments AB and AC again at points D and E respectively, and intersects segment BC at F and G such that F lies between B and G . The tangent to circle BDF at F and the tangent to circle CEG at G meet at point T . Suppose that points A and T are distinct. Prove that line AT is parallel to BC .

Claim 2. $ATGF$ is an isosceles trapezoid.

Proof. Obvious. □

Because all trapezoids have their bases parallel, we are done.