# Algorithm Design and Analysis

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#### Administrative Stuff

Lectures: Yuhui Shi

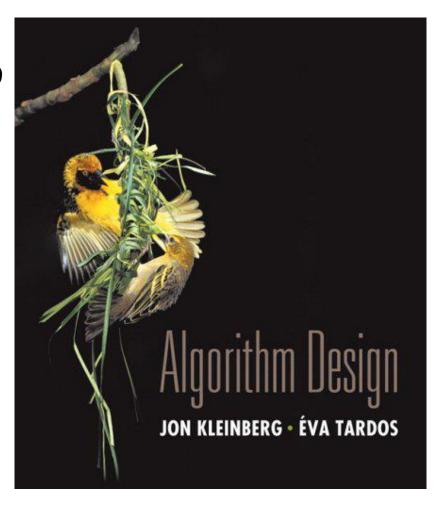
Tuesday 10:20-12:10/19:00-20:50

Attendance is expected.

Lab: Yao Zhao & Weiyu Wang

Prerequisite. CS203

Textbook. Algorithm Design by Jon Kleinberg and Éva Tardos.



Open Office Hours: 14:00 - 17:00PM, on Tuesday of every teaching week at my office (521 West Wing, South Tower, CoE Building)

#### Grades

#### Course grades.

Final Exam: 40%

Lab: 30%

Homework: 20%

Attendance: 10%

- We will ask you to sign online during lecture time in several teaching weeks;
- or We will ask you to sign your names on a piece of paper during lecture time in several teaching weeks;
- Do not sign for others. If caught, first time, 0 point for the Attendance part; second time, 0 point for the whole course;
- No excuse will be accepted for not attending classes unless I have been notified by an official permission for absence at the university level (approved) in advance.

# Algorithms

#### Algorithm.

- [webster.com] A procedure for solving a mathematical problem (as of finding the greatest common divisor) in a finite number of steps that frequently involves repetition of an operation.
- [Knuth, TAOCP] An algorithm is a finite, definite, effective procedure, with some input and some output.

Great algorithms are the poetry of computation. Just like verse, they can be terse, allusive, dense, and even mysterious. But once unlocked, they cast a brilliant new light on some aspect of computing. - Francis Sullivan

# Definition of Algorithm

must have a well-established structure in terms of the order of their execution, but not necessary in a sequencing. E.g. parallel algorithms, GPU, Interrupt

# An algorithm is an ordered set of unambiguous, executable steps that defines a terminating process.

The information in the state of the process must be sufficient to determine uniquely and completely the actions required by each step

Make a list of all the positive integers

The execution of an algorithm must lead to an end

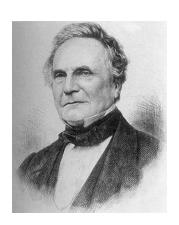
# Etymology

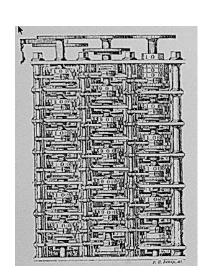
#### Etymology [eti maladzi]. [Knuth, TAOCP]

- Algorism = process of doing arithmetic using Arabic numerals.
- A misperception: algiros [painful] + arithmos [number].
- True origin: Abu 'Abd Allah Muhammad ibn Musa al-Khwarizm was a famous 9th century Persian textbook author who wrote *Kitab al-jabr wa'l-muqabala*, which evolved into today's high school algebra text.

# Theory of Algorithms

"As soon as an Analytic Engine exists, it will necessarily guide the future course of the science. Whenever any result is sought by its aid, the question will arise - By what course of calculation can these results be arrived at by the machine in the shortest time? - Charles Babbage

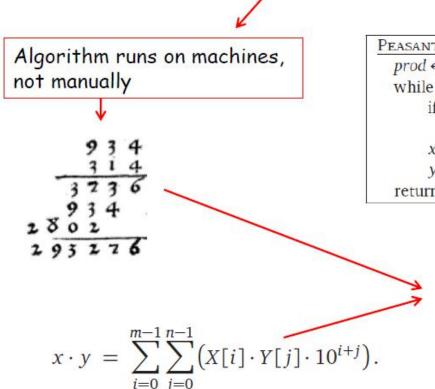




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$$x \cdot y = \begin{cases} 0 & \text{if } x = 0 \\ \lfloor x/2 \rfloor \cdot (y+y) & \text{if } x \text{ is even} \\ \lfloor x/2 \rfloor \cdot (y+y) + y & \text{if } x \text{ is odd} \end{cases}$$



#### Multiplication by duplation and mediation In Eastern Europe

PEASANTMULTIPLY $(x, y)$ :
$prod \leftarrow 0$
while $x > 0$
if $x$ is odd
$prod \leftarrow prod + y$
$x \leftarrow \lfloor x/2 \rfloor$
$y \leftarrow y + y$
return prod

prod		y	X
0			
456	=	+456	123
1368	=	+912	61
		1824	30
5016	=	+3648	15
12312	=	+7296	7
26904	=	+14592	3
56088	=	+29184	1

FIBONA	CCIMULTIPLY( $X[0m-1], Y[0n-1]$ ):
hold .	<b>←</b> 0
for k	$\leftarrow 0$ to $n+m-1$
f	for all $i$ and $j$ such that $i + j = k$
	$hold \leftarrow hold + X[i] \cdot Y[j]$
2	$Z[k] \leftarrow hold \mod 10$
ŀ	$nold \leftarrow \lfloor hold/10 \rfloor$
retur	n Z[0m+n-1]

# Design and Analysis of Algorithms

The skills required to effectively design and analyze algorithms are entangled with the skills required to effectively describe algorithms. A complete description of any algorithm has four components [Jeff Erickson]:

- What: A precise specification of the problem that the algorithm solves.
- How: A precise description of the algorithm itself.
- Why: A proof that the algorithm solves the problem it is supposed to solve.
- · How fast: An analysis of the running time of the algorithm.

Computer programs are concrete representations of algorithms, but algorithms are not programs.

# Algorithmic Paradigms

#### Design and analysis of computer algorithms.

- Greedy.
- Divide-and-conquer.
- Dynamic programming.
- Network flow.
- Randomized algorithms.
- Intractability.
- Coping with intractability.

Critical thinking and problem-solving.

# **Applications**

#### Wide range of applications.

- Caching.
- Compilers.
- Databases.
- Scheduling.
- Networking.
- Data analysis.
- Signal processing.
- Computer graphics.
- Scientific computing.
- Operations research.
- Artificial intelligence.
- Computational biology.

**.** . . .

We focus on algorithms and techniques that are useful in practice.