

Lab5 Questions

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Lab5.A Shopping

- ▶ Festival is coming and Andrea decides to buy n gifts for her friends. However, n gifts are sold on different days. So Andrea will buy them **in order**. For the i^{th} gift, the price is c_i .
- ▶ In her city, there are only 1 dollar coins and 100 dollar notes. Before shopping, Andrea prepares m coins and plenty of notes (you can assume that she always has enough notes to buy gifts).
- ▶ There is only one cashier in the store and his efficiency depends on the gift he sells. For the i^{th} gift, his efficiency is w_i and he needs $x * w_i$ seconds to check out where x is the total number of the notes and coins he needs to give Andrea. The cashier always minimizes x .
- ▶ Andrea wants to pay in such a way that the total time she needs to check out should be as small as possible.
- ▶ Please help her to find out the minimum time she needs!

Input:

5 34 → the number of gifts
 15 760 755 411 950 → price
 2 2 2 2 2 → efficiency

price	15	760	755	411	950
weight	2	2	2	2	2

34 $\xrightarrow{-15}$ 19 $\xrightarrow{+40}$ 59 $\xrightarrow{-55}$ 4 $\xrightarrow{+89}$ 93 $\xrightarrow{-50}$ 43

total time:
 $40 \cdot 2 + 89 \cdot 2 = 258$

price	15	760	755	411	950
weight	2	2	2	2	2

34 $\xrightarrow{-15}$ 19 $\xrightarrow{+40}$ 59 $\xrightarrow{+45}$ 104 $\xrightarrow{-11}$ 93 $\xrightarrow{-50}$ 43

total time:
 $40 \cdot 2 + 45 \cdot 2 = 170$

Output:

170

Input:

5 193
178 887 466 475 10
816 136 880 340 800



price	178	887	466	475	10
weight	816	136	880	340	800



total time:
 $13 \cdot 136 + 25 \cdot 340 = 10268$

Output:
10268

Lab5.B Voting

- ▶ A monitor election is going to be held in your class. There are $(n + 1)$ students in your class. And you want all your n classmates to vote for you.
- ▶ There exist two ways to convince each of your classmates to vote for you. The first way to convince your i^{th} classmate is to pay him/her c_i coins. The other way is to make m_i other classmates vote for you, and the i^{th} classmate will vote for you for free.
- ▶ It should be noticed that the voting takes places in several steps. For example, if you have four classmates with $m_1 = 1, m_2 = 2, m_3 = m_4 = 3, m_5 = 5$, then if you buy the vote of the 5th classmate, then all your classmates will vote for you. And the set of classmates vote for you changes as: $\{5\} \rightarrow \{5,1\} \rightarrow \{5,1,2\} \rightarrow \{5,1,2,3,4\}$.
- ▶ Please calculate the minimum coins you need to spend so that all your classmates will vote for you.

Test case 1

3

the number of test cases

7

the number of classmates

0 1

3 1

1 1

6 1

1 1

4 1

4 1

3

1 5

2 10

2 8

6

2 6

2 3

2 8

2 7

4 4

5 5

1st classmate $m1 == 0 \leq \text{Number of votes}$

3rd classmate $m3 == 1 \leq \text{Number of votes}$

5th classmate $m5 == 1 \leq \text{Number of votes}$

2nd classmate $m2 == 3 \leq \text{Number of votes}$

6th classmate $m6 == 4 \leq \text{Number of votes}$

7th classmate $m6 == 4 \leq \text{Number of votes}$

4th classmate $m4 == 6 \leq \text{Number of votes}$

the number of classmates

the number of classmates

initial:

Number of votes

0

1

3

4

6

7

Total cost

0

0

0

0

0

0

0

0

Test case 2

3				
7				
0	1			
3	1			
1	1			
6	1			
1	1			
4	1			
4	1			

the number of classmates

3				
1	5			
2	10			
2	8			
6				
2	6			
2	3			
2	8			
2	7			
4	4			
5	5			

Number of votes

initial: 0

1st classmate cost the least → 1

then 3rd classmate cost the least → 2

2nd classmate $m2 == 2 \leq \text{Number of votes}$ → 3

Total cost

0

5

13

13

Not the minimum cost

Number of votes

initial: 0

3rd classmate → 1

1st classmate $m1 == 1 \leq \text{Number of votes}$ → 2

2nd classmate $m2 == 2 \leq \text{Number of votes}$ → 3

Total cost

0

8

8

8

Test case 3

3				
7				
0	1			
3	1			
1	1			
6	1			
1	1			
4	1			
4	1			

Number of votes

initial: 0

6th classmate has the largest m → 1

then 5th classmate → 2

m1,m2,m3,m4==2 <= Number of votes → 6

Total cost

0

5

9

9

Not the minimum cost

3				
1	5			
2	10			
2	8			
6				
2	6			
2	3			
2	8			
2	7			
4	4			
5	5			

the number of classmates

Number of votes

initial: 0

2nd classmate, cost 3 → 1

5th classmate, cost 4 → 2

m1,m3,m4==2 <= Number of votes → 5

m5==5 <= Number of votes → 6

Total cost

0

3

7

7

7