

Module:
Assignment 2

INT102

1. Assessment

The tasks contribute 10% to the overall assessment of INT102

2. Submission

Please complete the assessment tasks using Microsoft Word and submit it in PDF via Learning. Please including **your name and student ID** on the cover page and name your file as **name_student ID**.

3. Deadline

26-May- 2021, Wednesday, 24:00. Time zone in Beijing, China (GMT+8)

Question 7 is compulsory.

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Question 1

1. A: $5-1-3=1$

G: $5-1-2=2$

C: 5

T: $5-1-1=3$

A	G	C	T	-
1	2	5	3	5

2.

A	G	C	A	A	T	G	A	A
A	T	G	A	A				
	A	T	G	A	A			
				A	T	G	A	A

So the number of comparisons is 9.

Question 2

a	b	c	d	e
0	∞	∞	∞	∞
0	4	∞	∞	∞
0	4	5	∞	∞
0	4	5	12	∞
0	4	5	12	6
0	4	5	12	-2
0	0	5	12	-2
0	0	5	8	-2

So the shortest path length from a to a is 0,

the shortest path length from a to b is 0,

the shortest path length from a to c is 5,

the shortest path length from a to d is 8,

the shortest path length from a to e is -2.

Question 3

1.

	""	G	A	G	T
""	0	0	0	0	0
A	0	$\uparrow 0$	$\nwarrow 1$	$\leftarrow 1$	$\leftarrow 1$
G	0	$\nwarrow 1$	$\uparrow 1$	$\nwarrow 2$	$\leftarrow 2$
C	0	$\uparrow 1$	$\uparrow 1$	$\uparrow 2$	$\uparrow 2$
C	0	$\uparrow 1$	$\uparrow 1$	$\uparrow 2$	$\uparrow 2$
C	0	$\uparrow 1$	$\uparrow 1$	$\uparrow 2$	$\uparrow 2$
T	0	$\uparrow 1$	$\uparrow 1$	$\uparrow 2$	$\nwarrow 3$

So the length of the Longest Common Subsequence between sequences of GAGT and AGCCCT is 3.

2.

	""	G	A	G	T
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""	0	0	0	0	0
A	0	↑0	↖1	←1	←1
G	0	↖1	↑1	↖2	←2
C	0	↑1	↑1	↑2	↑2
C	0	↑1	↑1	↑2	↑2
C	0	↑1	↑1	↑2	↑2
T	0	↑1	↑1	↑2	↖3

So one of the longest common subsequences of GAGT and AGCCCT is AGT.

Question 4

1.a.

Complete the following table using the formula

$F(i,j) = \max(F(i-1,j-1) + s(x_i, y_j), F(i-1,j) + d, F(i,j+1) + d)$

and set $F(0,0)=0, F(i,0)=i*d, F(0,j)=j*d$

		G	A	G	T
	0	←-1	←-2	←-3	←-4
A	↑-1	↖↑←-2	↖0	←-1	←-2
G	↑-2	↖0	↑←-1	↖1	←0
A	↑-3	↑-1	↖1	↑←0	↑←-1
C	↑-4	↑-2	↑0	↑←-1	↖↑←-2
C	↑-5	↑-1	↑-1	↑←-2	↖↑←-3
T	↑-6	↑-2	↑-2	↑←-3	↖-1

b.

An optimal global alignment of GAGT and AGACCT:

- GA - - GT

AGACC -T

2.a.

Complete the following table using the formula

$F(i,j) = \max(F(i-1,j-1) + s(x_i, y_j), F(i-1,j) - d, F(i,j+1) - d, 0)$

and set $F(0,0)=0$

		G	A	G	T
	0	0	0	0	0
A	0	0	↖1	0	0
G	0	↖1	0	↖2	←1
A	0	0	↖2	↑1	0
C	0	0	0	0	0
C	0	0	0	0	0
T	0	0	0	0	↖1

b.

An optimal local alignment of GAGT and AGACCT are found:

A G

A G

Question 5

a b c d e
a0 4 5 2 1
b4 0 4 3 1
c5 4 0 1 8
d2 3 1 0 6
e1 1 8 6 0

To reduce the complexity, we can assume that, d is before e in the tour. The lower bound for each node can be computed by

$$\text{Node 0: lb} = \lceil [(1+2) + (1+3) + (1+4) + (1+2) + (1+1)] / 2 \rceil = 9$$

$$\text{Node 1: lb} = \lceil [(4+1) + (4+1) + (4+1) + (2+1) + (1+1)] / 2 \rceil = 10$$

$$\text{Node 2: lb} = \lceil [(5+1) + (3+1) + (5+1) + (2+1) + (1+1)] / 2 \rceil = 11$$

$$\text{Node 3: lb} = \lceil [(2+1) + (3+1) + (4+1) + (2+1) + (1+1)] / 2 \rceil = 9$$

Node 4: ignored as d is not before e.

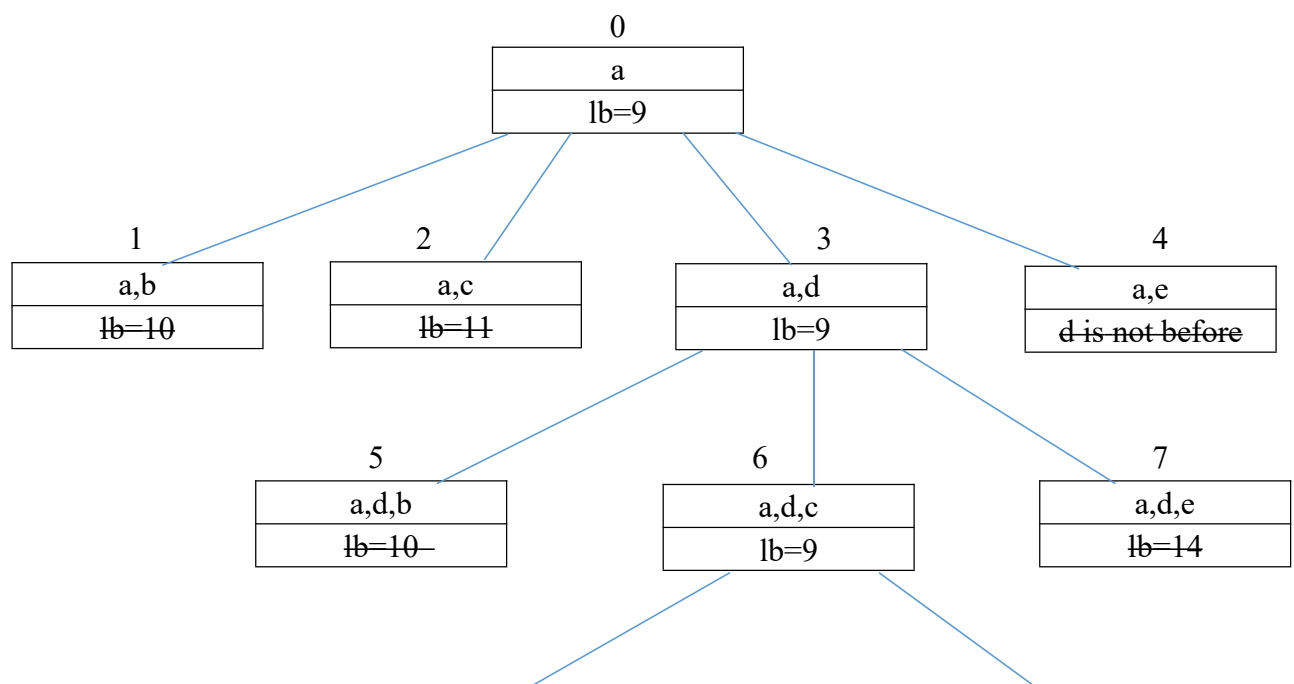
$$\text{Node 5: lb} = \lceil [(2+1) + (3+1) + (4+1) + (2+3) + (1+1)] / 2 \rceil = 10$$

$$\text{Node 6: lb} = \lceil [(2+1) + (3+1) + (4+1) + (2+1) + (1+1)] / 2 \rceil = 9$$

$$\text{Node 7: lb} = \lceil [(2+1) + (3+1) + (4+1) + (6+2) + (6+1)] / 2 \rceil = 14$$

$$\text{Node 8: lb} = \lceil [(2+1) + (4+1) + (4+1) + (2+1) + (1+1)] / 2 \rceil = 9$$

$$\text{Node 9: lb} = \lceil [(4+2) + (4+1) + (1+8) + (2+1) + (1+8)] / 2 \rceil = 16$$



8

a,d,c,b,(e,a)
lb=9(optimal tour)

9

a,d,c,e,(b,a)
lb=16(inferior tour)

Solutions: a,d,c,b,e,a

Question 6

P problem is all decision problems that can be solved in worst-case polynomial time.

NP problem is all problems that can be verified in polynomial time.

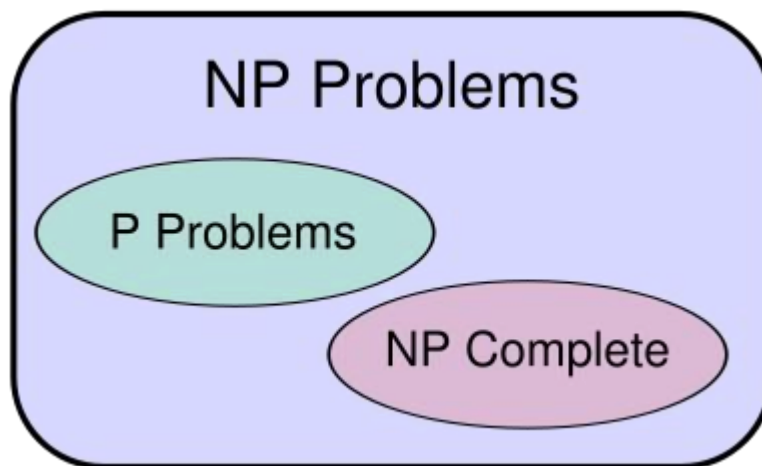
All P problem can be verified in polynomial time, so $P=NP$ or $P \subset NP (P \neq NP)$.

Problem A is NP-complete if

- Problem A is in NP
- For any Problem A' in NP, A' is reducible to A in polynomial time

So $NPC \subset NP$, P problem is not NPC problem.

As a result, we can get the diagram as shown below:



1. contradict

$NP=NPC$ is wrong.

2. not contradict

3. contradict

$NP=P \cup NPC$ is wrong.

4. contradict

$P \cap NPC \neq \{\}$ is wrong

5. not contradict

Question 7

Yes, I do.