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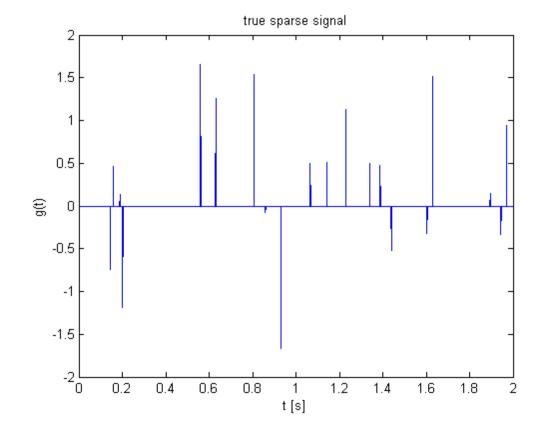
# add working path of tools and functions

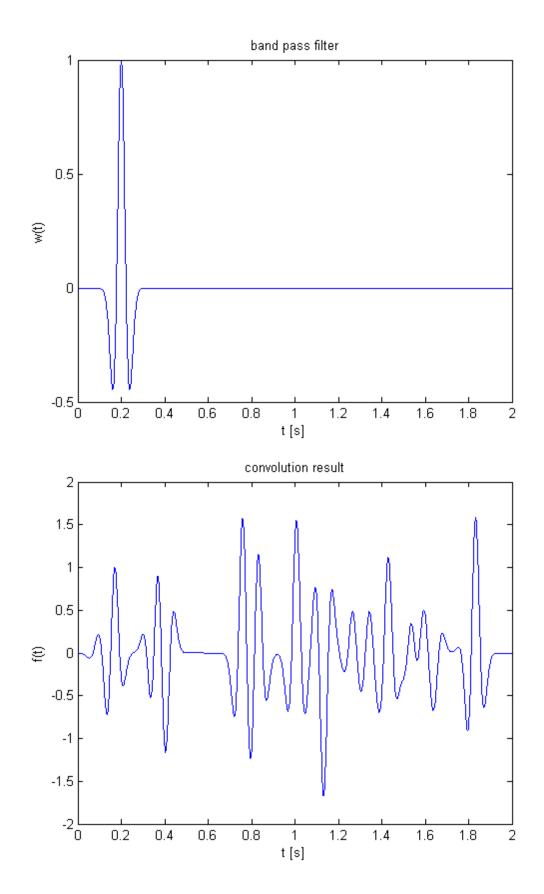
```
%addpath(genpath('e:\research\Tools\spot-slim'))
% addpath(genpath('e:\research\Tools\pSPOT'))
cd ../../../pqnl1;
addpath(genpath(pwd))
rmpath(genpath('./minConF'))
cd ../experiments/help_spgl1/modifying/task12illconditioned
addpath(genpath(pwd))
cd ./convolution
rmpath('/Volumes/Users/linamiao/Dropbox/PQN/pqnl1/minConF/')
Warning: ".\minConF" not found in path.
Warning: ".\minConF\html" not found in path.
Warning: "\Volumes\Users\linamiao\Dropbox\PQN\pqnl1\minConF" not
found in path.
```

## problem setting

```
time axis
t = [0:.001:2]';
N = length(t);
% true signal g has approx k spikes with random amplitudes
k = 20;
q = zeros(N,1);
g(randi(N,k,1)) = randn(k,1);
w = (1-2*1e3*(t-.2).^2).*exp(-1e3*(t-.2).^2);
% plot
figure;
plot(t,g);
xlabel('t [s]');ylabel('g(t)');
title('true sparse signal')
figure;
plot(t,w);
xlabel('t [s]');ylabel('w(t)');
title('band pass filter')
% fourier transform of w
```

```
wf = fft(w);
% SPOT operator to perform convolution.
C = opDFT(N)'*opDiag(wf)*opDFT(N);
f = C*g;
% plot
figure;
plot(t,f);
xlabel('t [s]');ylabel('f(t)');
title('convolution result')
```





## spgl1 and pqnl1

opts.iterations = 100;

tau = norm(g,1);

### lasso

```
[x_spg,r_spg,g_spg,info_spg] = spgl1(C, f, tau, [], zeros(size(g)), opts);
   [x_pqn,r_pqn,g_pqn,info_pqn] = pqnl1_2(C, f, tau, [], zeros(size(g)), opts);
   figure;
   subplot(3,1,1); plot(g); title('original sparse signal')
   subplot(3,1,2); plot(x_spg);title('x_spg')
   subplot(3,1,3); plot(x_pqn);title('x_pqn')
______
SPGL1_SLIM v. 46 (Tue, 14 Jun 2011) based on v.1017
______
                                   No. columns
No. rows
                          2001
                                                              2001
                   : 1.56e+001
                                   Two-norm of b
Initial tau
                                                         : 2.26e+001
                                    Target one-norm of x : 1.56e+001
Optimality tol
                    : 1.00e-004
                   : 1.00e-006
Basis pursuit tol
                                    Maximum iterations
 Iter
          Objective
                     Relative Gap
                                      gNorm
                                              stepG
                                                       nnzX
                                                              nnzG
                                                 0.0
                                                          0
      2.2645313e+001 2.9494325e+000
                                    4.85e+001
                                                                   0
   1
      1.8776891e+001
                     4.8799941e+000
                                    4.75e+001
                                                 -0.3
                                                          23
                                                                   0
      1.9394462e+001
                     7.5596761e+000
                                     7.46e+001
                                                  0.0
                                                         368
      1.6045261e+001
                     7.7725249e+000
                                    5.35e+001
                                                  0.0
                                                         762
                                                                   0
      4.8711421e+000
                     1.2167068e+001
                                    1.18e+001
                                                  0.0
                                                         1119
                                                                   Ω
      3.4119268e+000
                     4.7277531e+000
                                    4.11e+000
                                                 0.0
                                                        1063
      3.0042147e+000
                     4.4646305e+000
                                    3.34e+000
                                                 0.0
                                                        1007
                                                                   0
      1.9739365e+000
                     7.9157751e+000
                                    2.18e+000
                                                 0.0
                                                         842
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      2.0682892e+000
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                                    3.48e+000
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                                    9.59e+000
                                                  0.0
                                                         859
   10
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                                     1.85e+000
                                                  0.0
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      1.3754619e+000
                                                  0.0
                     7.1049805e+000
                                    1.37e+000
                                                         780
                                                                   0
   11
      1.3322292e+000
                                    1.33e+000
                     7.1134280e+000
                                                 0.0
                                                         765
                                                 0.0
                                                         688
      1.1398846e+000
                     7.4482398e+000
                                    1.24e+000
      1.0949871e+000
                     8.6926827e+000 1.30e+000
                                                                   0
                                                 -0.3
                                                         683
                                                 0.0
                                                         674
                                                                   0
      1.0661115e+000
                     1.1982020e+001
                                    1.48e+000
                     5.1162391e+000
      1.0388838e+000
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                                                         669
                                                                   0
   16
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                     5.0139361e+000
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                                                  0.0
                                                         664
   18
      9.9566608e-001
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                                                         661
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                                                         641
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                                     1.64e+000
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                                                         509
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                                                         507
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      6.0059862e-001
                     1.2714380e+000
                                    4.37e-001
                                                 0.0
                                                         507
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                     1.6548856e+000
                                    4.58e-001
                                                  0.0
                                                         503
                                    1.05e+000
                                                                   0
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                     1.1248513e+001
                                                  0.0
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                     3.3893330e+000
                                    5.54e-001
                                                 -0.3
                                                         511
                                                                   0
      5.4636270e-001
                                                  0.0
                                                         506
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                                     3.97e-001
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                                                         503
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                                                  0.0
   34
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                     1.9913246e+000
                                    4.45e-001
                                                         500
                                                                   0
  35 5.2914537e-001 3.9012734e+000 5.65e-001
                                                 -0.3
                                                         499
                                                                   0
```

36	5.4120367e-001	1.1657952e+001	1.05e+000	0.0	501	0
37	5.2307154e-001	4.1205431e+000	5.76e-001	0.0	497	0
38	5.1723605e-001	1.0250733e+000	3.72e-001	0.0	498	0
39	5.1536067e-001	8.9308973e-001	3.61e-001	0.0	498	0
40	4.8601558e-001	1.0126047e+000	3.55e-001	0.0	494	0
41	4.9172175e-001	9.1044765e+000	8.30e-001	-0.3	498	0
42	4.8010762e-001	3.5303543e+000	5.01e-001	-0.3	493	0
43	4.7517898e-001	1.5423907e+000	3.69e-001	0.0	494	0
44	4.7350303e-001	9.2211230e-001	3.29e-001	0.0	493	0
45	4.6954363e-001	6.9186986e-001	3.13e-001	0.0	492	0
46	4.5332590e-001	1.2906648e+001	1.03e+000	0.0	474	0
47	4.7046384e-001	1.2852216e+001	1.08e+000	-0.3	481	0
48	4.2454221e-001	3.0273691e+000	4.32e-001	0.0	477	0
49	4.1997155e-001	6.2320463e-001	2.72e-001	0.0	477 476	
50	4.1858119e-001	6.7045367e-001	2.72e-001 2.72e-001	0.0	476	0
51	4.0626870e-001	2.0445869e+000	3.52e-001	0.0	469	0
51 52	4.1611190e-001	6.4343625e+000	6.01e-001	-0.3	40 <i>9</i> 471	
52 53	4.0271255e-001	3.1572940e+000	4.28e-001	0.0	467	0
53 54	3.9520887e-001	1.3209422e+000	2.92e-001		468	0
				0.0		
55 56	3.9392899e-001 3.9236141e-001	7.6808916e-001 4.8433808e-001	2.57e-001 2.37e-001	0.0 0.0	469 469	0
50 57	3.7428314e-001	2.3546791e+000	3.50e-001	0.0		0
	3.7426314e-001 3.7443408e-001	3.3572585e+000	3.99e-001		455	
58 50				-0.3	458 455	0
59	3.6954026e-001	1.0533078e+000	2.61e-001	0.0	455	0
60	3.6850003e-001	4.7552958e-001	2.19e-001	0.0	455	0
61	3.6755264e-001	4.9816460e-001	2.20e-001	0.0	455	0
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63	3.6794970e-001	5.9901184e+000	5.74e-001	-0.3	449	0
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65	3.5006704e-001	6.8403235e-001	2.20e-001	0.0	448	0
66	3.4945448e-001	4.7928156e-001	2.05e-001	0.0	448	0
67	3.4623251e-001	4.8693773e-001	2.03e-001	0.0	447	0
68	3.4469985e-001	1.9790504e+000	2.94e-001	-0.3	448	0
69 70	3.4515734e-001	1.7423995e+000	2.84e-001	-0.3	444	0
70	3.4202089e-001	1.1578532e+000	2.43e-001	0.0	445	0
71	3.4125379e-001	4.1466166e-001	1.95e-001	0.0	445	0
72	3.4051593e-001	3.9603100e-001	1.93e-001	0.0	445	0
73	3.0491475e-001	3.2767023e+000	3.52e-001	0.0	425	0
74 75	3.0562183e-001 2.9545390e-001	3.2170111e+000	3.43e-001	-0.3	434	0
75 76		1.3513436e+000	2.31e-001	0.0	427	0
76	2.9343348e-001	5.9842678e-001 4.8922161e-001	1.75e-001	0.0	429	0
77	2.9290749e-001		1.67e-001	0.0	428	0
7 <i>8</i>	2.9015425e-001	4.2245474e-001	1.54e-001	0.0	429	0
79	2.9062132e-001	1.8774976e+000 2.9798518e+000	2.65e-001	-0.3	427	0
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82	2.8610950e-001			0.0	427	0
83	2.8572767e-001	2.9149238e-001	1.46e-001 1.61e-001	0.0	426	0
84 05	2.7892935e-001	6.3525255e-001	2.64e-001	0.0	424 422	
85	2.8069205e-001	2.1761998e+000		-0.3		0
86 87	2.7732659e-001	7.0767514e-001	1.72e-001 1.56e-001	-0.3 0.0	421 421	0
88	2.7623102e-001	5.4451913e-001		0.0	421 421	
	2.7585576e-001	2.4821454e-001	1.38e-001			0
89 90	2.7526080e-001	2.6860777e-001	1.38e-001 2.33e-001	0.0	421 417	0
90 91	2.7338176e-001	1.6736696e+000		0.0 -0.3	417 418	0
	2.6830446e-001	1.0641051e+000	1.82e-001			0
92 93	2.6745271e-001 2.6718283e-001	3.7933332e-001 3.0577791e-001	1.40e-001	0.0 0.0	418	0
93 94		3.05///91e-001 3.5359478e-001	1.34e-001		418 417	
94 95	2.6651313e-001 2.6590882e-001	1.8026232e+000	1.37e-001 2.21e-001	0.0 -0.3	417 417	0
95 96	2.6344037e-001	6.2650185e-001	1.58e-001	-0.3	417	0
96 97	2.6344037e-001 2.6296169e-001	3.3103893e-001	1.34e-001	0.0	416 416	0
97 98	2.6270367e-001	3.1316992e-001	1.33e-001	0.0	416	0
90 99	2.6141106e-001	4.1182473e-001	1.36e-001	0.0	415	0
<b>ラ</b> フ	2.01411006-001	7.11024/3E-001	1.306-001	0.0	413	U

```
100 2.6121201e-001 1.1436003e+000 1.89e-001 -0.3
                                                           413
ERROR EXIT -- Too many iterations
Products with A
                         140
                                    Total time
                                               (secs) :
                                                             0.7
                                   Project time (secs) :
Products with A'
                         101
                                                            0.1
Newton iterations
                          0
                                   Mat-vec time (secs) :
                                                             0.5
                   :
Line search its
                          71
                                   Subspace iterations :
______
PQNL1_SLIM v. 46 (Tue, 14 Jun 2011) based on v.1017
______
                    : 2001
                                    No. columns : 2001
Two-norm of b : 2.26e+001
No. rows
Initial tau
                    : 1.56e+001
Optimality tol
                                     Target one-norm of x : 1.56e+001
                    : 1.00e-004
Basis pursuit tol
                    : 1.00e-006
                                     Maximum iterations
          Objective
                      Relative Gap
                                       gNorm
                                              stepG
                                                       nnzX
                                                               nnzG
    0 2.2645313e+001 2.9494325e+000 4.85e+001
                                                  0.0
                                                         0
Inside of minConf_PQN
          FunEvals Projections
                                   Step Length
                                                        rNorm2
                                                                     Opt Cond
Iteration
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Ω

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                              3358
                                       1.00000e+000
                                                         2.02382e-001
                                                                          4.24092e+000
        54
                     1
                              3431
                                       1.00000e+000
                                                         1.99498e-001
                                                                          3.57918e+000
        55
                     1
                              3484
                                       1.00000e+000
                                                         1.96936e-001
                                                                          3.17061e+000
                                                                          3.79097e+000
                     1
                                                         1.93877e-001
        56
                              3569
                                       1.00000e+000
        57
                     1
                              3603
                                       1.00000e+000
                                                         1.92137e-001
                                                                          3.41969e+000
        58
                     1
                              3696
                                       1.00000e+000
                                                         1.88206e-001
                                                                          3.01527e+000
        59
                     1
                              3793
                                                         1.84486e-001
                                                                          3.17005e+000
                                       1.00000e+000
        60
                     1
                              3813
                                       1.00000e+000
                                                         1.83013e-001
                                                                          2.73076e+000
                     1
                                       1.00000e+000
                                                         1.81119e-001
       61
                              3871
                                                                          3.25828e+000
                     1
        62
                              3940
                                       1.00000e+000
                                                         1.79604e-001
                                                                          3.53079e+000
       63
                     1
                              4009
                                       1.00000e+000
                                                         1.77164e-001
                                                                          3.26749e+000
       64
                     1
                              4066
                                       1.00000e+000
                                                         1.75353e-001
                                                                          3.08693e+000
        65
                     1
                              4130
                                       1.00000e+000
                                                         1.73632e-001
                                                                          3.22444e+000
                     1
        66
                              4197
                                       1.00000e+000
                                                         1.71655e-001
                                                                          3.33909e+000
        67
                     1
                                       1.00000e+000
                                                         1.70256e-001
                              4263
                                                                          2.72990e+000
        68
                     1
                              4317
                                       1.00000e+000
                                                         1.69089e-001
                                                                          2.13853e+000
        69
                     1
                              4369
                                       1.00000e+000
                                                         1.68266e-001
                                                                          2.72189e+000
        70
                     1
                                                         1.67154e-001
                              4413
                                       1.00000e+000
                                                                          3.83586e+000
        71
                     1
                              4455
                                                         1.66239e-001
                                       1.00000e+000
                                                                          3.82867e+000
        72
                     1
                              4523
                                       1.00000e+000
                                                         1.64247e-001
                                                                          2.56957e+000
        73
                     1
                              4564
                                       1.00000e+000
                                                         1.62921e-001
                                                                          2.35973e+000
                     1
        74
                              4630
                                       1.00000e+000
                                                         1.61320e-001
                                                                          1.91743e+000
        75
                     1
                              4680
                                       1.00000e+000
                                                         1.59438e-001
                                                                          1.83681e+000
        76
                     1
                              4719
                                       1.00000e+000
                                                         1.58639e-001
                                                                          1.93105e+000
       77
                     1
                              4776
                                       1.00000e+000
                                                         1.57796e-001
                                                                          2.14427e+000
        78
                     1
                              4820
                                                         1.57024e-001
                                       1.00000e+000
                                                                          1.79408e+000
        79
                     1
                              4900
                                       1.00000e+000
                                                         1.55538e-001
                                                                          1.67845e+000
                                       1.00000e+000
        80
                     1
                              4997
                                                         1.52174e-001
                                                                          2.09069e+000
                     1
        81
                              5170
                                       1.00000e+000
                                                         1.46937e-001
                                                                          2.66195e+000
                                                         1.41216e-001
        82
                     1
                              5323
                                       1.00000e+000
                                                                          2.70069e+000
                     1
        83
                              5366
                                       1.00000e+000
                                                         1.39591e-001
                                                                          2.00095e+000
        84
                     1
                              5425
                                       1.00000e+000
                                                         1.38485e-001
                                                                          1.60459e+000
       85
                     1
                              5452
                                                         1.38079e-001
                                       1.00000e+000
                                                                          1.46284e+000
       86
                     1
                              5524
                                       1.00000e+000
                                                         1.36615e-001
                                                                          3.35872e+000
        87
                     1
                              5531
                                       1.00000e+000
                                                         1.36332e-001
                                                                          1.88522e+000
        88
                     1
                              5574
                                       1.00000e+000
                                                         1.35495e-001
                                                                          1.33698e+000
       89
                     1
                                                         1.34990e-001
                              5618
                                       1.00000e+000
                                                                          1.45858e+000
        90
                     1
                              5692
                                       1.00000e+000
                                                         1.33691e-001
                                                                          1.65416e+000
        91
                     1
                              5724
                                       1.00000e+000
                                                         1.33109e-001
                                                                          1.67949e+000
        92
                     1
                              5785
                                       1.00000e+000
                                                         1.32199e-001
                                                                          1.54889e+000
                                                         1.30856e-001
        93
                     1
                              5828
                                       1.00000e+000
                                                                          1.51711e+000
        94
                     1
                              5839
                                       1.00000e+000
                                                         1.30611e-001
                                                                          1.14289e+000
        95
                     1
                              5883
                                       1.00000e+000
                                                         1.29657e-001
                                                                          1.58833e+000
                     1
        96
                              5899
                                       1.00000e+000
                                                         1.29396e-001
                                                                          1.10613e+000
        97
                                                                          1.40269e+000
                     1
                              5972
                                       1.00000e+000
                                                         1.27827e-001
                     1
        98
                              6115
                                       1.00000e+000
                                                         1.25013e-001
                                                                          1.60522e+000
        99
                     1
                                       1.00000e+000
                              6143
                                                         1.24412e-001
                                                                          1.19403e+000
       100
                     1
                              6185
                                       1.00000e+000
                                                         1.23720e-001
                                                                          1.17072e+000
       1.2372032e-001
                         1.3654918e-001 4.32e-002
                                                           0.0
                                                                               0
                                                                    362
ERROR EXIT -- Too many iterations
                             104
                                                                     16.3
Products with A
                                         Total time
                                                        (secs):
```

Project time

Mat-vec time (secs) :

(secs)

1.00000e+000

2.53572e-001

14.7

0.5

4.11459e+000

43

Products with A'

Newton iterations

1

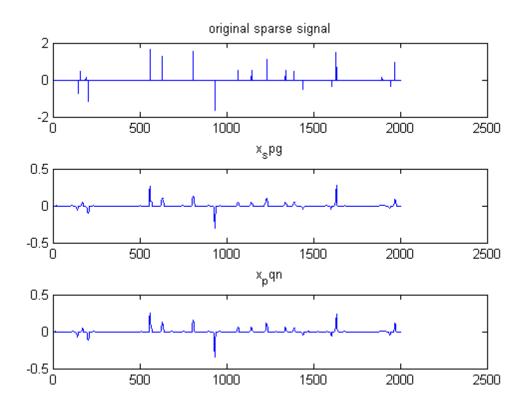
2482

7

104

0

:



#### **BPDN**

```
noisy signal
```

```
f = C*g+ le-2*randn(N,1);

% plot
figure;
plot(t,f);
xlabel('t [s]');ylabel('f(t)');
title('convolution result')

opts.iterations = 100;

[x_spg,r_spg,g_spg,info_spg] = spgll(C, f, 0, le-2, zeros(size(g)), opts);
[x_pqn,r_pqn,g_pqn,info_pqn] = pqnll_2(C, f, 0, 1-2, zeros(size(g)), opts);

figure;
subplot(3,1,1); plot(g); title('original sparse signal')
subplot(3,1,2); plot(x_spg);title('x_spg')
subplot(3,1,3); plot(x_pqn);title('x_pqn')

figure('Name','Solution paths')
plot(info_spg.xNorml,info_spg.rNorm2,info_pqn.xNorm1,info_pqn.rNorm2);hold on
scatter(info_pqn.xNorml,info_pqn.rNorm2);
scatter(info_pqn.xNorml,info_pqn.rNorm2);hold off
```

legend('spg','pqn')
axis tight

SPGL1\_SLIM v. 46 (Tue, 14 Jun 2011) based on v.1017 \_\_\_\_\_\_ No. rows 2001 No. columns 2001 Two-norm of b Initial tau : 0.00e+000 : 2.27e+001 Optimality tol Target objective : 1.00e-002 : 1.00e-004 Basis pursuit tol : 1.00e-006 Maximum iterations Iter *Objective* Relative Gap Rel Error gNorm stepG nnzXnnzG 0 2.2653829e+001 0.0000000e+000 1.00e+000 4.857e+001 0.0 0 2.1539742e+001 2.5053147e+000 1.00e+000 4.755e+001 -0.31 1 4.5039507e+000 2.1945525e+001 1.00e+000 6.067e+001 0.0 64 9.99e-001 3 1.3015228e+001 2.7336742e+000 2.707e+001 238 -0.3 4 8.9481166e+000 3.4466186e+000 9.99e-001 1.756e+001 0.0 453 9.99e-001 1.320e+001 5 7.6772763e+000 1.8196608e+000 0.0 444 6 7.0711798e+000 2.0411517e+000 9.99e-001 1.214e+001 0.0 413 7 6.5625362e+000 1.3708150e+000 9.98e-001 1.075e+001 0.0 378 1.470e+001 9.98e-001 6.4224922e+000 3.7827647e+000 0.0 351 8 2.9081220e+000 9.98e-001 6.3378483e+000 1.336e+001 0.0 320 9.98e-001 10 6.1671065e+000 1.5393709e+000 1.054e+001 0.0 329 6.1283601e+000 8.1179270e-001 9.98e-001 9.217e+000 0.0 318 7 7 6.0684023e+000 7.4350472e-001 9.98e-001 9.046e+000 0.0 299 12 0.0 5.8955071e+000 1.3759245e+000 9.98e-001 9.948e+000 196 13 9.98e-001 9.048e+000 14 5.7943583e+000 9.0793147e-001 -0.3 212 4.5987525e-001 5.7510872e+000 9.98e-001 8.490e+000 0.0 207 15 5.7390312e+000 2.9508745e-001 9.98e-001 8.170e+000 0.0 203 16 5.7232635e+000 3.0532273e-001 9.98e-001 8.178e+000 0.0 201 17 9.98e-001 5.7213778e+000 18 2.0532600e+000 1.068e+001 0.0 183 5.6866066e+000 2.3590914e-001 9.98e-001 7.995e+000 19 -0.3 211 20 5.6793217e+000 3.5216926e-001 9.98e-001 8.158e+000 0.0 198 21 5.6712292e+000 2.7335622e-001 9.98e-001 8.045e+000 0.0 192 0.0 7.0342383e-001 9.98e-001 8.602e+000 172 22 5.6556886e+000 5.6485594e+000 23 2.0366325e-001 9.98e-001 7.911e+000 -0.3 177 2.1630401e-001 9.98e-001 7.908e+000 172 24 5.6442907e+000 0.0 25 5.6397189e+000 1.9905938e-001 9.98e-001 7.890e+000 0.0 171 9.98e-001 26 5.6229640e+000 6.7155804e-001 8.541e+000 0.0 162 27 5.6252771e+000 2.9233220e-001 9.98e-001 8.037e+000 -0.3 169 2.8217972e-001 9.98e-001 7.975e+000 28 5.6140753e+000 0.0 161 7.803e+000 29 5.6114538e+000 1.6027372e-001 9.98e-001 0.0 159 5.6053517e+000 9.98e-001 7.768e+000 155 30 1.4196301e-001 0.0 31 5.5722997e+000 1.2453964e+000 9.98e-001 9.242e+000 -0.3 125 5.5613695e+000 5.8866510e-001 9.98e-001 8.294e+000 -0.3 138 9.98e-001 5.5406642e+000 3.5814175e-001 8.025e+000 0.0 33 131 5.5379695e+000 1.2432341e-001 9.98e-001 7.663e+000 0.0 34 126 35 5.5366953e+000 9.6422682e-002 9.98e-001 7.626e+000 0.0 128 36 5.5301037e+000 2.7880167e-001 9.98e-001 7.875e+000 0.0 124 37 5.5300422e+000 2.0436936e-001 9.98e-001 7.800e+000 -0.3 127 2.0874012e+001 9.96e-001 4.164e+000 38 2.5030243e+000 0.0 538 39 1.9900975e+000 9.3735668e+000 9.95e-001 3.045e+000 0.0 838 9.94e-001 40 1.7084173e+000 1.1276363e+001 2.108e+000 0.0 740 9.94e-001 1.914e+000 736 41 1.6419438e+000 9.4318367e+000 0.0 42 1.5324760e+000 9.0884197e+000 9.93e-001 1.812e+000 0.0 689 9.93e-001 43 1.4105912e+000 3.4845627e+001 3.355e+000 0.0 547 1.3293368e+000 6.5315443e+000 9.92e-001 1.477e+000 -0.3 554 44 1.3095864e+000 4.5738073e+000 9.92e-001 0.0 45 1.328e+000 542 1.2950123e+000 2.8765273e+000 9.92e-001 1.201e+000 0.0 540 46 1.2378355e+000 8.7045155e+000 9.92e-001 1.556e+000 0.0 496 1.3007029e+000 3.0844659e+001 9.92e-001 3.087e+000 490 48 -0.3 2.568e+000 49 1.2577326e+000 2.3570587e+001 9.92e-001 0.0 482 50 1.2033508e+000 4.6429863e+000 9.92e-001 1.264e+000 0.0 475

```
51 1.1973516e+000 2.7606393e+000 9.92e-001 1.125e+000
                                                          0.0
52 1.1872620e+000 2.6206209e+000 9.92e-001 1.107e+000
                                                          0.0
                                                                   462
   1.1307990e+000
                   1.5887124e+001
                                             1.971e+000
                                  9.91e-001
                                                           0.0
                                                                   337
5.3
                                                         -0.3
    1.1066290e+000
                   7.0454559e+000
                                   9.91e-001
                                             1.405e+000
                                                                   346
55
    1.0895973e+000
                   4.1964280e+000
                                   9.91e-001
                                             1.173e+000
                                                           0.0
                                                                   336
                                  9.91e-001
56
    1.0851709e+000
                   1.2213389e+000
                                             9.650e-001
                                                           0.0
                                                                   334
57
    1.0828656e+000
                   1.1972088e+000
                                  9.91e-001 9.578e-001
                                                           0.0
                                                                   331
   1.0669274e+000
                   5.5060804e+000
                                   9.91e-001 1.226e+000
                                                          0.0
                                                                   328
                                   9.91e-001
59
   1.0662451e+000
                   6.1906129e+000
                                             1.277e+000
                                                          -0.3
                                                                   326
   1.0620657e+000
                                   9.91e-001
                                                          0.0
60
                   3.7805691e+000
                                             1.111e+000
                                                                   328
    1.0596490e+000
                                             9.525e-001
61
                   1.5376901e+000
                                   9.91e-001
                                                           0.0
                                                                   321
    1.0582505e+000
                   1.0966667e+000
                                   9.91e-001
                                             9.220e-001
                                                           0.0
                                                                   320
   1.0437502e+000
                                             1.011e+000
63
                   2.5248775e+000
                                  9.90e-001
                                                          0.0
                                                                   312
                   1.0341956e+001 9.90e-001
   1.0494401e+000
                                             1.559e+000
                                                          -0.3
                                                                   313
   1.0529689e+000
                   1.1102447e+001 9.91e-001 1.605e+000
                                                          0.0
                                                                   303
   1.0378969e+000
                   2.6053913e+000 9.90e-001
                                            1.021e+000
                                                          0.0
                                                                   308
                   1.1113317e+000
                                  9.90e-001
                                             9.123e-001
                                                          0.0
   1.0358707e+000
                                                                   308
67
                                                          0.0
68
    1.0345859e+000
                   1.0803532e+000
                                   9.90e-001
                                             9.090e-001
                                                                   307
    1.0100182e+000
                   5.4351502e+000
                                   9.90e-001
                                             1.254e+000
69
                                                           0.0
                                                                   266
    9.9294631e-001
                                                         -0.3
70
                   3.6824102e+000
                                   9.83e-001
                                             1.091e+000
                                                                   268
71 9.8296626e-001
                                                          0.0
                   3.3244990e+000
                                   9.73e-001
                                             1.043e+000
                                                                   265
72 9.7967681e-001
                   1.4402224e+000
                                  9.70e-001
                                            9.147e-001
                                                           0.0
                                                                   265
                   7.5514084e-001
                                   9.68e-001 8.627e-001
73 9.7833766e-001
                                                           0.0
                                                                   265
74
   9.7576340e-001
                   8.1060745e-001
                                   9.66e-001
                                             8.628e-001
                                                          0.0
                                                                   263
   9.7519971e-001
                                             1.316e+000
75
                   7.5291769e+000
                                   9.65e-001
                                                          0.0
                                                                   259
76
    9.6835172e-001
                   9.4105252e-001
                                   9.58e-001
                                             8.739e-001
                                                          -0.3
                                                                   257
                                                          0.0
77
    9.6695920e-001
                   1.2534387e+000
                                   9.57e-001
                                             8.862e-001
                                                                   257
78 9.6585036e-001
                                  9.56e-001
                                                           0.0
                   6.9930414e-001
                                             8.475e-001
                                                                   256
   9.6125114e-001
                   1.0795349e+000 9.51e-001 8.642e-001
79
                                                          0.0
                                                                   253
80
   9.5991242e-001
                   2.0840159e+000 9.50e-001 9.464e-001
                                                          -0.3
                                                                   252
   9.6194278e-001
                   7.3780610e+000 9.52e-001 1.296e+000
                                                         -0.3
                                                                   253
   9.5759164e-001
                                  9.48e-001
                                             9.529e-001
                                                          0.0
82
                   2.2120235e+000
                                                                   251
                   1.3222274e+000
                                                          0.0
    9.5445143e-001
                                   9.44e-001
                                             8.805e-001
                                                                   251
8.3
84
    9.5381269e-001
                   6.6290617e-001
                                   9.44e-001
                                             8.345e-001
                                                           0.0
                                                                   251
85
    9.5156471e-001
                   8.3952199e-001
                                   9.42e-001
                                             8.468e-001
                                                           0.0
                                                                   249
                                                          -0.3
   9.4991006e-001
                   3.5507123e+000
                                   9.40e-001
                                             1.026e+000
                                                                   248
86
87
   9.4801263e-001
                   1.1268133e+000
                                  9.38e-001 8.646e-001
                                                          -0.3
                                                                   248
   9.4735026e-001
                   7.9674917e-001
                                   9.37e-001 8.396e-001
                                                          0.0
                                                                   248
                                   9.36e-001
89
   9.4643154e-001
                   6.7615153e-001
                                             8.318e-001
                                                          0.0
                                                                   247
   9.4329576e-001
                   5.7559944e+000
                                   9.33e-001
90
                                             1.173e+000
                                                          0.0
                                                                   238
                   5.6211564e+000
91
    9.4405378e-001
                                   9.34e-001
                                             1.176e+000
                                                          -0.3
                                                                   239
                                                          0.0
    9.3939482e-001
                   1.7954881e+000
                                   9.29e-001
                                             9.035e-001
                                                                   238
                  5.8425965e-001
   9.3860944e-001
                                  9.29e-001
                                             8.186e-001
93
                                                                   237
   9.3809984e-001 5.8439282e-001 9.28e-001 8.184e-001
94
                                                           0.0
                                                                   237
    9.2655311e-001 3.8033969e+000 9.17e-001
                                             1.066e+000
                                                          0.0
                                                                   223
96
   9.3008758e-001 8.9404482e+000 9.20e-001
                                            1.375e+000
                                                         -0.3
                                                                  225
    9.2712345e-001 6.4216582e+000 9.17e-001
                                             1.219e+000
                                                          0.0
97
                                                                   228
                   3.5761182e+000
                                             1.015e+000
                                                          0.0
98
    9.1414281e-001
                                  9.04e-001
                                                                   223
    9.1182405e-001
                   6.8432291e-001
                                   9.02e-001
                                             8.090e-001
99
                                                           0.0
                                                                   224
                   5.2656535e-001 9.01e-001
                                             7.969e-001
100
    9.1133996e-001
                                                           0.0
                                                                   224
```

474

#### ERROR EXIT -- Too many iterations

Products with A 143 Total time (secs): 0.8 101 Products with A' Project time (secs) : : 0.1 Mat-vec time (secs) : Newton iterations : 2 0.5 72 Subspace iterations : Line search its :

PQNL1 SLIM v. 46 (Tue, 14 Jun 2011) based on v.1017

\_\_\_\_\_\_ No. rows : 2001 No. columns : 2001 Initial tau : 0.00e+000 Two-norm of b : 2.27e+001

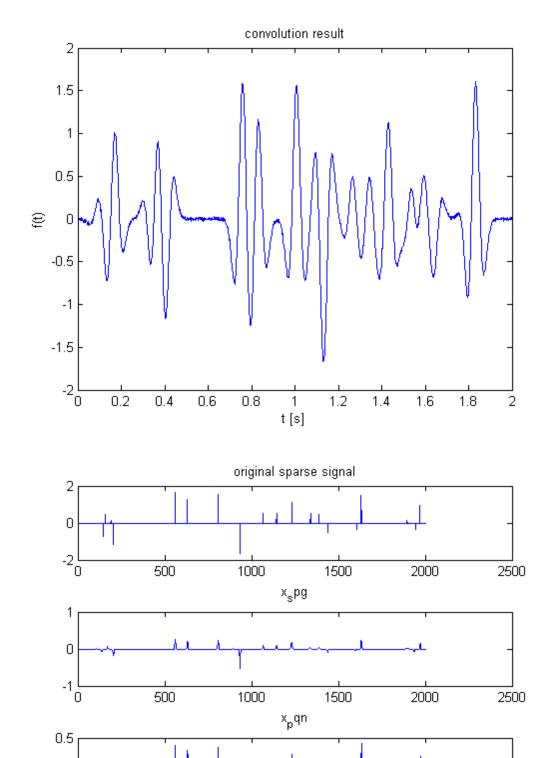
\_\_\_\_\_\_

Optimality tol : 1.00e-004 Target objective : -1.00e+000 Basis pursuit tol : 1.00e-006 Maximum iterations : 100

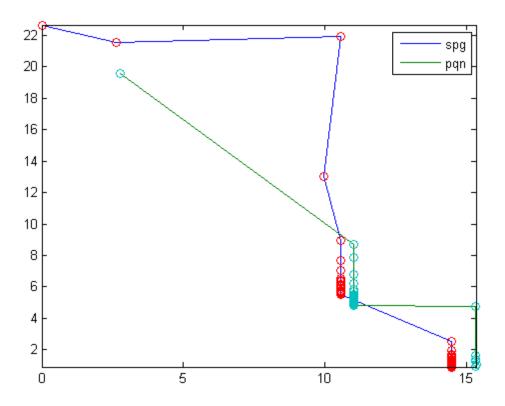
0 2.2653829e+001 0.0000000e+000 1.04e+000 4.857e+001 0.0 0

0 2.2	653829e+001	1 0.0000000e+	000 1.04e+000	4.857e+001	0.0	0
Inside of m		_ , , , ,				
Iteration		Projections	Step Length	rNorm2	_	Opt Cond
1	1	4	2.50000e-001	1.95410e+001		.37914e+001
2	1	37	1.00000e+000	8.72147e+000		.01963e+001
3	1	60	1.00000e+000	7.87001e+000		.04149e+001
4	1	89	1.00000e+000	6.80721e+000		.99116e+001
5	1	116	1.00000e+000	6.18932e+000	1	.73701e+001
6	1	143	1.00000e+000	5.86912e+000	1	.69641e+001
7	1	170	1.00000e+000	5.68653e+000	1	.73610e+001
8	1	195	1.00000e+000	5.54593e+000	1	.64133e+001
9	1	216	1.00000e+000	5.43221e+000	1	.39788e+001
10	1	240	1.00000e+000	5.36403e+000	1	.36777e+001
11	1	266	1.00000e+000	5.30710e+000	1	.31236e+001
12	1	290	1.00000e+000	5.25375e+000		.24564e+001
13	1	316	1.00000e+000	5.21921e+000		.17837e+001
14	1	348	1.00000e+000	5.17607e+000		.04996e+001
15	1	37 <i>2</i>	1.00000e+000	5.15471e+000		.06717e+001
16	1	408	1.00000e+000	5.12554e+000		.06730e+001
17	1	436	1.00000e+000	5.09687e+000		.80724e+000
18	1	462	1.00000e+000	5.07937e+000		.03638e+000
19	1	496	1.00000e+000	5.06779e+000		.83850e+000
20	1	522	1.00000e+000	5.05410e+000		.28314e+000
21	1	560	1.00000e+000	5.02884e+000		.88169e+000
22	1	594	1.00000e+000	5.01403e+000		.85173e+000
23	1	628	1.00000e+000	5.00301e+000		.27836e+000
24	1	656	1.00000e+000	4.99622e+000		.39837e+000
25	1	696	1.00000e+000	4.98468e+000		.74229e+000
26	1	734	1.00000e+000	4.97695e+000		.96922e+000
27	1	779	1.00000e+000	4.96448e+000		.11239e+000
28	1	817	1.00000e+000	4.95806e+000		.50045e+000
29	1	865	1.00000e+000	4.94659e+000		.20714e+000
30	1	906	1.00000e+000	4.94183e+000		.56886e+000
31	1	961	1.00000e+000	4.93514e+000		.64929e+000
32	1	993	1.00000e+000	4.93137e+000	7	.23914e+000
33	1	1027	1.00000e+000	4.92590e+000	7	.21247e+000
34	1	1065	1.00000e+000	4.92302e+000	6	.80827e+000
35	1	1146	1.00000e+000	4.91488e+000	7	.66149e+000
36	1	1187	1.00000e+000	4.91063e+000	8	.24783e+000
37	1	1240	1.00000e+000	4.90279e+000	9	.36629e+000
38	1	1284	1.00000e+000	4.89884e+000	9	.22215e+000
39	1	1327	1.00000e+000	4.89451e+000	8	.25664e+000
40	1	1379	1.00000e+000	4.89004e+000	6	.42364e+000
41	1	1420	1.00000e+000	4.88460e+000	7	.25058e+000
42	1	1475	1.00000e+000	4.87941e+000	9	.09805e+000
43	1	1515	1.00000e+000	4.87753e+000	8	.73137e+000
44	1	1565	1.00000e+000	4.87412e+000	8	.24319e+000
45	1	1594	1.00000e+000	4.87288e+000		.72510e+000
46	1	1637	1.00000e+000	4.87004e+000	5	.80899e+000
47	1	1713	1.00000e+000	4.86608e+000		.17227e+000
48	1	1753	1.00000e+000	4.86492e+000		.64816e+000
49	1	1846	1.00000e+000	4.86087e+000		.91781e+000
50	1	1912	1.00000e+000	4.85840e+000		.53143e+000
51	1	1977	1.00000e+000	4.85398e+000		.75271e+000
51 52	1	2129	1.00000e+000 1.00000e+000	4.84570e+000		.19297e+000
52 53	1	2129 2162	1.00000e+000	4.84570E+000 4.84411e+000		.192976+000 .29876e+000
				4.84411e+000 4.84219e+000		.00265e+000
5 <i>4</i>	1	2214	1.00000e+000 1.00000e+000			
55 56	1	2257		4.84069e+000		.56476e+000
56	1	2308	1.00000e+000	4.83869e+000		.96414e+000
57	1	2369	1.00000e+000	4.83679e+000	/	.11867e+000

F	. 0	7	2431	1.00000e+000	4 0252201000	7.89737e+000
	8	1			4.83533e+000	
	9	1	2528	1.00000e+000	4.83319e+000	9.43801e+000
	0	1	2601	1.00000e+000	4.83154e+000	8.94404e+000
	1	1	2633	1.00000e+000	4.83037e+000	7.37479e+000
6	2	1	2687	1.00000e+000	4.82843e+000	5.42102e+000
6	3	1	2728	1.00000e+000	4.82754e+000	4.93113e+000
	4	1	2780	1.00000e+000	4.82652e+000	6.36848e+000
	5	1	2874	1.00000e+000	4.82497e+000	9.03994e+000
	6	1	2905	1.00000e+000	4.82420e+000	8.57085e+000
	7	1	2965	1.00000e+000	4.82199e+000	5.13524e+000
	8	1	3032	1.00000e+000	4.82064e+000	6.01275e+000
	9	1	3070	1.00000e+000	4.82005e+000	5.68687e+000
	0	1	3097	1.00000e+000	4.81958e+000	4.21729e+000
	1	1	3125	1.00000e+000	4.81914e+000	3.66839e+000
7	2	1	3162	1.00000e+000	4.81880e+000	3.28373e+000
7	3	1	3188	1.00000e+000	4.81852e+000	3.04400e+000
7	4	1	3234	1.00000e+000	4.81767e+000	5.05706e+000
	5	1	3290	1.00000e+000	4.81714e+000	7.01630e+000
	6	1	3356	1.00000e+000	4.81646e+000	7.66806e+000
	7	1	3520	1.00000e+000	4.81411e+000	8.34056e+000
	8	1	3590	1.00000e+000	4.81191e+000	6.89912e+000
	9					5.25305e+000
		1	3628	1.00000e+000	4.81094e+000	
	0	1	3668	1.00000e+000	4.81044e+000	4.80736e+000
	1	1	3708	1.00000e+000	4.80970e+000	4.98176e+000
	2	1	3795	1.00000e+000	4.80876e+000	6.01965e+000
	3	1	3835	1.00000e+000	4.80835e+000	5.28667e+000
	4	1	3898	1.00000e+000	4.80725e+000	5.59141e+000
8	5	1	3933	1.00000e+000	4.80677e+000	6.04866e+000
8	6	1	4066	1.00000e+000	4.80408e+000	6.59174e+000
8	7	1	4145	1.00000e+000	4.80304e+000	5.87872e+000
	8	1	4213	1.00000e+000	4.80152e+000	4.70528e+000
	9	1	4254	1.00000e+000	4.80048e+000	4.49987e+000
	0	1	4298	1.00000e+000	4.80012e+000	4.43804e+000
	1	1	4360	1.00000e+000	4.79928e+000	4.74935e+000
	2	1	4421	1.00000e+000	4.79872e+000	4.35972e+000
	3	1	4460	1.00000e+000	4.79825e+000	2.95317e+000
	4	1	4497	1.00000e+000	4.79803e+000	2.50413e+000
94 4	.7980302e+0	000 8.5	020529e-	002 1.21e+000	6.462e+000	0.0 76
	minConf_P(					
Iteratio		ls Proje		Step Length	rNorm2	Opt Cond
9	5	1	4	1.00000e+000	4.77164e+000	3.06768e+001
9	16	1	65	1.00000e+000	1.67227e+000	3.03111e+001
9	7	1	104	1.00000e+000	1.41041e+000	2.76955e+001
	8	1	143	1.00000e+000	1.23687e+000	2.35533e+001
_	9	1	203	1.00000e+000		1.65658e+001
10		1	255	1.00000e+000	9.38798e-001	1.87036e+001
10	-	=				
ERROR EX	CIT Too r	many ite	rations			
Droduct	i+h 7		105	Total time	(gogg) - 12	0
Products		:	105		(secs): 12	
	with A'		105	Project time		
Newton 1	terations	:	2	Mat-vec time	(secs):	. 5



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