```
cd ../../../pqnl1
addpath(genpath(pwd))
cd ../experiments/help_spgl1/modifying/task17mmv/
m = 50; n = 128;
                                    % Measurement matrix is m x n
k = 14;
                                    % Set sparsity level x0
A = randn(m,n);
                                    % Random encoding matrix
[Q,R] = qr(A',0); A = Q';
% group sparse X0
p = 2; nn = n/2;
X0 = zeros(nn,p);
pp = randperm(nn); pp = pp(1:k);
XO(pp,:) = 1e-3*randn(k,p);
B = A * vec(X0); % + 0.005 * randn(m,1);
b = B(:);
groups = p;
options.project = @(x,weight,tau) NormL12_project(groups,x,weight,tau);
options.primal_norm = @(x,weight ) NormL12_primal(groups,x,weight);
options.dual_norm
                 = @(x,weight
                                 ) NormL12_dual(groups,x,weight);
% cd ../task7
% addpath(genpath(pwd))
% cd ../task8
% tau = mixNorm(X0,1,2);
tau = 0;
%sigma = 1e-3;
sigma = 0;
[x_spg,r_spg,g_spg,info_spg] = spgl1(A,B(:),tau,sigma,zeros(size(A,2),1),options);
[x_pqn1, r_pqn1, g_pqn1, info_pqn1] = pqn11_2(A,B(:),tau,sigma,zeros(size(A,2),1),opt)
figure;
subplot(3,1,1); plot(vec(X0));title('X0')
subplot(3,1,2); plot(vec(x_spg)); title('x_spg')
subplot(3,1,3); plot(vec(x_pqn1)); title('x_pqn')
title('Multiple Measurement Vector Basis Pursuit');
info_spg
info pqn1
        ______
```

SPGL1\_SLIM v. 46 (Tue, 14 Jun 2011) based on v.1017

No. rows : 50 No. columns : 128

Initial tau : 0.00e+00 Two-norm of b : 3.27e-03

Optimality tol : 1.00e-04 Target objective : 0.00e+00

Basis	pursuit tol	: 1.00e-06	Maximum I	iterations	:	500
Iter	<i>Objective</i>	Relative Gap	Rel Error	gNorm	stepG	nnzX
0	3.2722461e-03	0.0000000e+00	3.27e-03	1.027e-03	0.0	0
1	2.8844048e-03	9.0474168e-06	2.88e-03	8.403e-04	-0.3	2
2	1.2846925e-03	1.7225185e-06	1.28e-03	3.385e-04	0.0	3
3	1.1489742e-03	4.3876574e-07	1.15e-03	2.323e-04	0.0	3
4	1.1131523e-03	3.3177933e-07	1.11e-03	2.186e-04	0.0	3
5	1.0676105e-03	3.8298416e-07	1.07e-03	2.168e-04	0.0	5
6	1.0782715e-03	7.3583675e-07	1.08e-03	2.556e-04	0.0	4
7	1.0854393e-03	1.3382518e-06	1.09e-03	2.918e-04	0.0	4
8	1.0402680e-03	7.4461407e-08	1.04e-03	1.872e-04	0.0	5
9	1.0387735e-03	5.5290799e-08	1.04e-03	1.857e-04	0.0	6
10	1.0378834e-03	4.2721939e-08	1.04e-03	1.846e-04	0.0	6
11	1.0372591e-03	1.1677787e-07	1.04e-03	1.894e-04	0.0	5
12	1.0372757e-03	1.0457073e-07	1.04e-03	1.910e-04	-0.3	5
13	2.3226185e-04	5.1509904e-07	2.32e-04	5.398e-05	0.0	9
14	2.0225401e-04	1.1810539e-07	2.02e-04	3.712e-05	0.0	9
15	1.9408727e-04	1.2504745e-07	1.94e-04	3.611e-05	0.0	9
16	1.7567201e-04	2.0564929e-07	1.76e-04	3.756e-05	0.0	9
17	1.9760337e-04	4.0337298e-07	1.98e-04	4.669e-05	-0.3	9
18	1.6274726e-04	1.4646406e-07	1.63e-04	3.294e-05	0.0	9
19	1.5501895e-04	7.4198366e-08	1.55e-04	2.777e-05	0.0	9
20	1.5350836e-04	6.0948796e-08	1.54e-04	2.687e-05	0.0	9
21	1.4733059e-04	4.1297953e-08	1.47e-04	2.458e-05	0.0	9
22	1.4519535e-04	2.2333522e-07	1.45e-04	3.459e-05	-0.3	9
23	1.3815473e-04	3.6357218e-08	1.38e-04	2.330e-05	-0.3	9
24	1.3653341e-04	3.7628548e-08	1.37e-04	2.304e-05	0.0	9
25	1.3596637e-04	1.9359035e-08	1.36e-04	2.182e-05	0.0	9
26	1.3478333e-04	3.0420847e-08	1.35e-04	2.219e-05	0.0	9
27	1.3619740e-04	1.0128464e-07	1.36e-04	2.658e-05	-0.3	8
28	1.3566097e-04	8.8481798e-08	1.36e-04	2.554e-05	0.0	8
29	1.3288199e-04	1.0576499e-08	1.33e-04	2.083e-05	0.0	8
30	1.3272240e-04	1.0800349e-08	1.33e-04	2.079e-05	0.0	8
31	1.3153915e-04	1.2975383e-08	1.32e-04	2.057e-05	0.0	8
32	1.3133006e-04	3.2077354e-08	1.31e-04	2.183e-05	-0.3	8
33	1.3143470e-04	6.9677172e-08	1.31e-04	2.400e-05	0.0	8
34	1.3082253e-04	3.4106682e-08	1.31e-04	2.188e-05	0.0	8
35	1.3053279e-04	7.5210900e-09	1.31e-04	2.021e-05	0.0	8
36	1.3043823e-04	9.2781545e-09	1.30e-04	2.028e-05	0.0	8
37	1.2963278e-04	1.5906114e-08	1.30e-04	2.031e-05	0.0	8
38	1.2967806e-04	4.2095237e-08	1.30e-04	2.221e-05	-0.3	8
39	1.2939055e-04	2.4043783e-08	1.29e-04	2.088e-05	0.0	8
40	1.2923457e-04	1.2728896e-08	1.29e-04	2.023e-05	0.0	8
41	1.2916840e-04	8.3379887e-09	1.29e-04	1.995e-05	0.0	8
42	1.2893117e-04	9.4424514e-09	1.29e-04	1.994e-05	0.0	8
43	1.2884096e-04	2.1392050e-08	1.29e-04	2.064e-05	-0.3	8
44	1.2875955e-04	2.2832142e-08	1.29e-04	2.075e-05	-0.3	8
45	1.2863095e-04	8.8222892e-09	1.29e-04	1.989e-05	0.0	8
46	1.2858284e-04	8.2969939e-09	1.29e-04	1.983e-05	0.0	8
47	1.2848098e-04	5.9229707e-09	1.28e-04	1.966e-05	0.0	8
48	1.2839146e-04	3.8373249e-08	1.28e-04	2.126e-05	-0.3	8
49	1.2794427e-04	1.1794438e-08	1.28e-04	1.981e-05	-0.3	8
50	1.2783861e-04	7.6504556e-09	1.28e-04	1.957e-05	0.0	8

```
51 1.2780421e-04 6.5239624e-09 1.28e-04 1.952e-05
                                                    0.0
                                                             8
   52 1.2753848e-04 1.0744087e-08 1.28e-04 1.964e-05
                                                    0.0
                                                             8
   53 1.2774333e-04 3.4339417e-08 1.28e-04 2.130e-05
                                                    -0.3
                                                             8
   54 1.2757437e-04 2.1838869e-08 1.28e-04 2.028e-05
                                                    0.0
                                                             8
   55 1.2738923e-04 3.8461405e-09 1.27e-04 1.927e-05
                                                    0.0
                                                             8
   56 1.2737178e-04 5.7482976e-09 1.27e-04 1.938e-05
                                                    0.0
   57 1.2729833e-04 3.7915472e-09 1.27e-04 1.923e-05
                                                    0.0
                                                             8
   58 1.2730150e-04 4.4870048e-08 1.27e-04 2.149e-05 -0.3
   59 8.3539597e-05 4.3971577e-07 8.35e-05 2.645e-05
                                                             8
                                                    -0.3
EXIT -- Found a root
Products with A
                :
                      82
                               Total time (secs): 0.6
Products with A' :
                      60
                               Project time (secs) :
                                                    0.1
Newton iterations :
                      3
                               Mat-vec time (secs) :
                                                      0.2
Line search its :
                      27
                               Subspace iterations :
                                                      0
______
PQNL1 SLIM v. 46 (Tue, 14 Jun 2011) based on v.1017
______
No. rows
                      50
                                No. columns
                                                        128
Initial tau
                  : 0.00e+00
                               Two-norm of b
                                                  : 3.27e-03
                               Target objective
Optimality tol
                   : 1.00e-04
                                                   : 0.00e+00
                               Maximum iterations
Basis pursuit tol
                                                         500
                  : 1.00e-06
    0 3.2722461e-03 0.0000000e+00 3.27e-03 1.027e-03
                                                    0.0
                                                             0
Inside of minConf_PQN
Iteration FunEvals Projections
                               Step Length
                                                 rNorm2
                                                             0
       1
                7
                         4
                               1.00000e+00
                                            1.39147e-03
                                                          2.672
       2
                1
                         10
                               1.00000e+00
                                            1.25964e-03
                                                          1.702
       3
                        19
                               1.00000e+00
                                           1.15903e-03
                                                          8.968
                1
       4
                1
                        28
                               1.00000e+00
                                            1.12229e-03
                                                          7.301
                                                          5.099
       5
                1
                        37
                               1.00000e+00
                                            1.08727e-03
                                                         3.984
                        48
                               1.00000e+00
       6
                1
                                            1.06912e-03
       7
                1
                        64
                              1.00000e+00
                                           1.05631e-03
                                                         3.850
                1
                        77
                               1.00000e+00
                                            1.04778e-03
                                                         3.106
       8
       9
                1
                        88
                               1.00000e+00
                                            1.04027e-03
                                                          1.588
                               1.00000e+00
                                           1.03796e-03
                                                         1.043
      10
                1
                        100
                               1.00000e+00
                                                          7.199
      11
                1
                        112
                                           1.03737e-03
      12
                        121
                               1.00000e+00
                                           1.03695e-03
                                                          3.785
                7
break of testUpdateTau, exit minConf_PQN
   12 1.0369517e-03 3.1459615e-08 1.04e-03 1.827e-04 0.0
                                                             6
Inside of minConf PQN
Iteration FunEvals Projections
                               Step Length
                                                             0
                                                 rNorm2
      13
                7
                         4
                               1.00000e+00
                                            2.15489e-04
                                                          5.157
      14
                 1
                        10
                               1.00000e+00
                                            1.98623e-04
                                                          4.200
      15
                               1.00000e+00
                                            1.65810e-04
                                                          2.553
                1
                        18
                        29
                                                          2.158
                                            1.54803e-04
      16
                1
                               1.00000e+00
      17
                1
                        38
                              1.00000e+00
                                           1.42846e-04
                                                         1.683
                        54
                              1.00000e+00
                                                         1.572
      18
                                           1.35172e-04
                7
      19
                1
                        69
                               1.00000e+00
                                            1.27800e-04
                                                          1.387
```

3

```
1.00000e+00
        20
                   1
                             90
                                                     1.19861e-04
        21
                    1
                             110
                                     1.00000e+00
                                                     1.15506e-04
        22
                    1
                             130
                                     1.00000e+00
                                                     1.10453e-04
        23
                    1
                             154
                                     1.00000e+00
                                                     1.05201e-04
        24
                    1
                             169
                                     1.00000e+00
                                                     1.02293e-04
        25
                    1
                             183
                                     1.00000e+00
                                                     9.95981e-05
find BP solution
EXIT -- Found a root
Products with A
                          28
                                      Total time
                                                   (secs) :
Products with A'
                          28
                                     Project time (secs) :
Newton iterations
                            2
                                      Mat-vec time (secs) :
info\_spg =
            tau: 0.0168
         rNorm: 8.3540e-05
          rGap: 4.3972e-07
         gNorm: 2.6447e-05
          stat: 1
          iter: 59
        nProdA: 82
       nProdAt: 60
       nNewton: 3
    timeProject: 0.0702
    timeMatProd: 0.1657
       itnLSQR: 0
       options: [1x1 struct]
      timeTotal: 0.5606
        xNorm1: [59x1 double]
        rNorm2: [59x1 double]
         lambda: [59x1 double]
info pqn1 =
            tau: 0.0163
         rNorm: 9.9598e-05
          rGap: 3.5332e-08
         gNorm: 1.6659e-05
          stat: 1
           iter: 25
        nProdA: 28
        nProdAt: 28
       nNewton: 2
    timeProject: 1.0130
    timeMatProd: 0.0766
        itnLSQR: 0
```

1.330

1.270

1.167 1.060

8.042

6.582

1.2

1.0

0.1

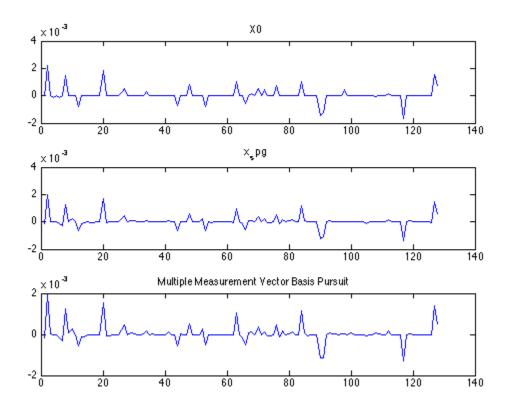
4

options: [1x1 struct]

xNorm1: [25x1 double]
rNorm2: [25x1 double]

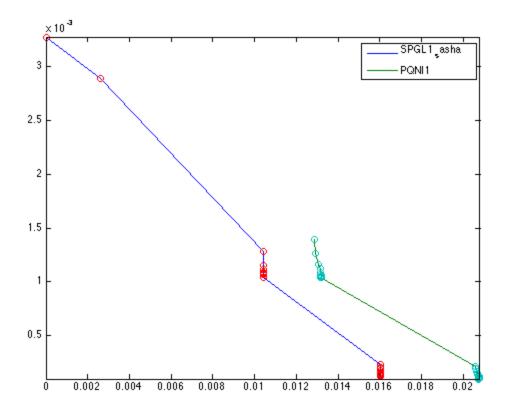
timeTotal: 1.1783

## lambda: [25x1 double]



## show result

```
figure('Name','Solution paths')
plot(info_spg.xNorm1,info_spg.rNorm2,info_pqn1.xNorm1,info_pqn1.rNorm2);hold on
scatter(info_spg.xNorm1,info_spg.rNorm2);
scatter(info_pqn1.xNorm1,info_pqn1.rNorm2);hold off
legend('SPGL1_sasha','PQN11')
axis tight
```



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