Introduction to Nuclear and Particle Physics

Decays

Half-Lives and Applications of Some Radioactive Isotopes

Radioactive Isotope	Half-Life	Typical Uses		
hydrogen-3 (tritium)	12.32 yr	biochemical tracer		
carbon-11	20.33 min	positron emission tomography		
carbon-14	5.70 × 103 yr	dating of artifacts		
sodium-24	14.951 h	cardiovascular system tracer		
phosphorus-32	14.26 days	biochemical tracer		
potassium-40	1.248 × 109 yr	dating of rocks		
iron-59	44.495 days	red blood cell lifetime tracer		
cobalt-60	5.2712 yr	radiation therapy for cancer		
technetium-99m*	6.006 h	biomedical imaging		
iodine-131	8.0207 days	thyroid studies tracer		
radium-226	1.600 × 103 yr	radiation therapy for cancer		
uranium-238	4.468 × 109 yr	dating of rocks and Earth's crust		
americium-241	432.2 yr	smoke detectors		
*The m denotes metastable, where an excited state nucleus decays to the ground state of the same isotope.				

Decays

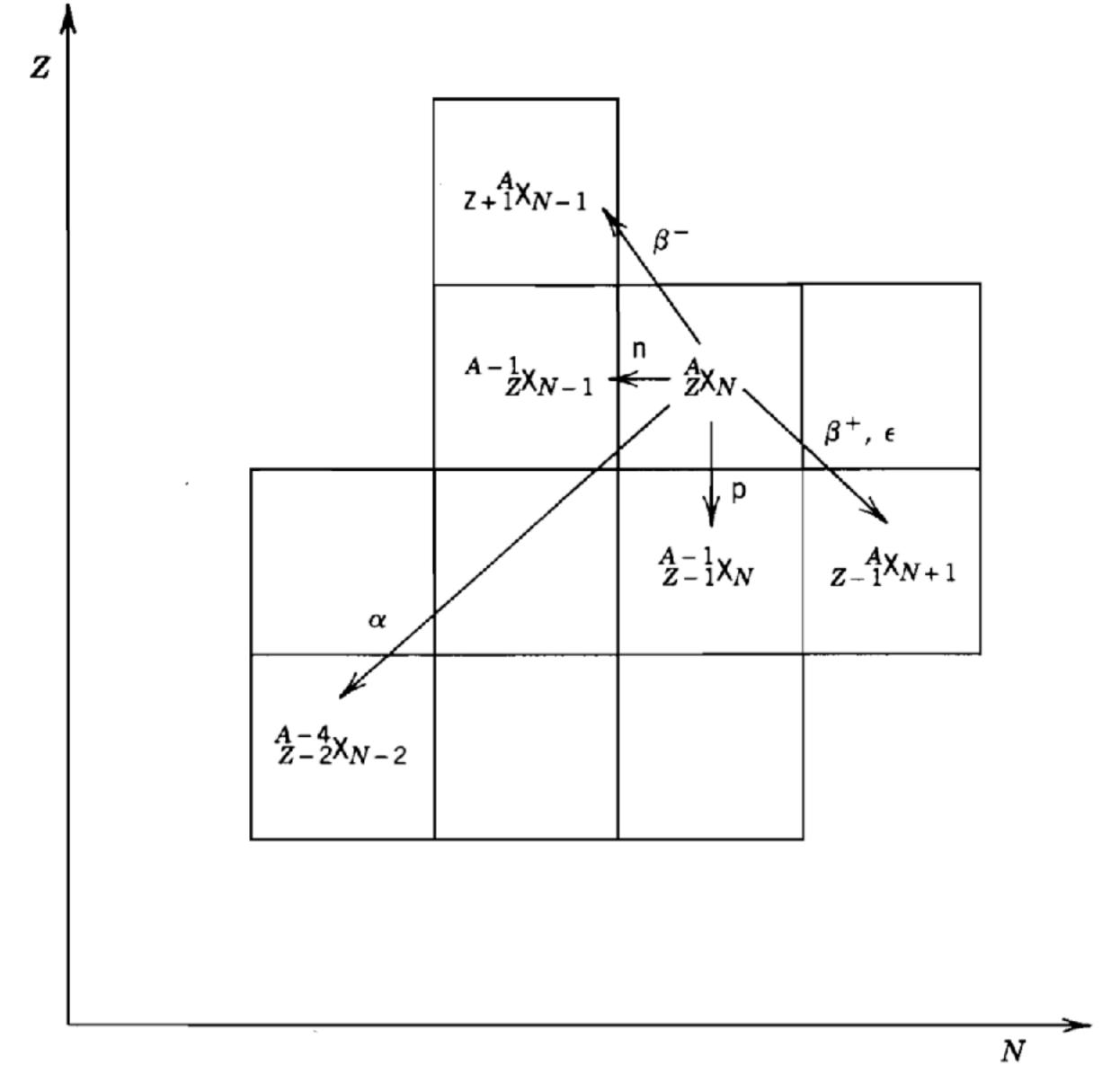


Figure 6.9 The initial nucleus ${}_{Z}^{A}X_{N}$ can reach different final nuclei through a variety of possible decay processes.

Q vs. half-life

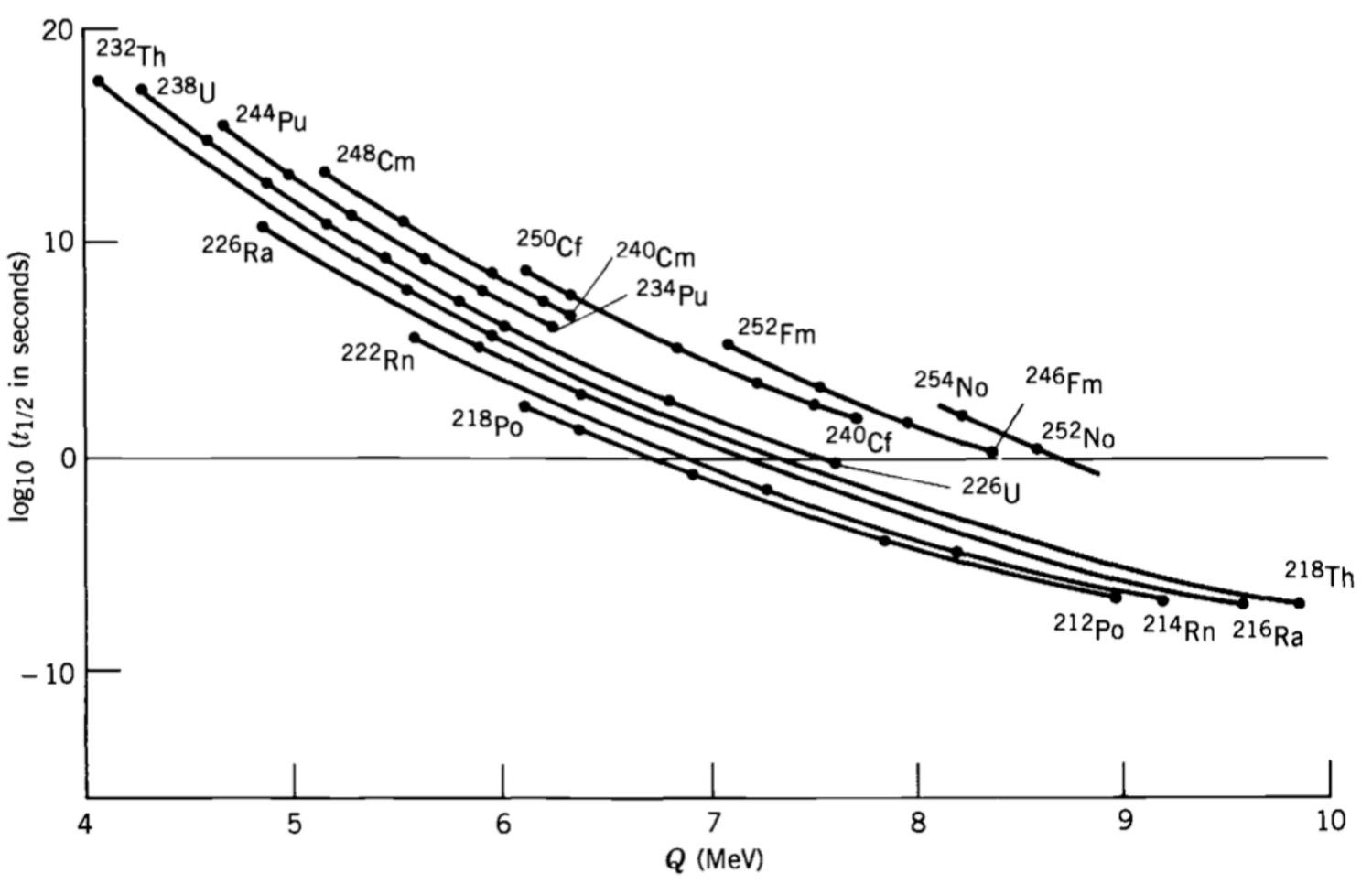


Figure 8.1 The inverse relationship between α -decay half-life and decay energy, called the Geiger-Nuttall rule. Only even-Z, even-N nuclei are shown. The solid lines connect the data points.

A vs. Q

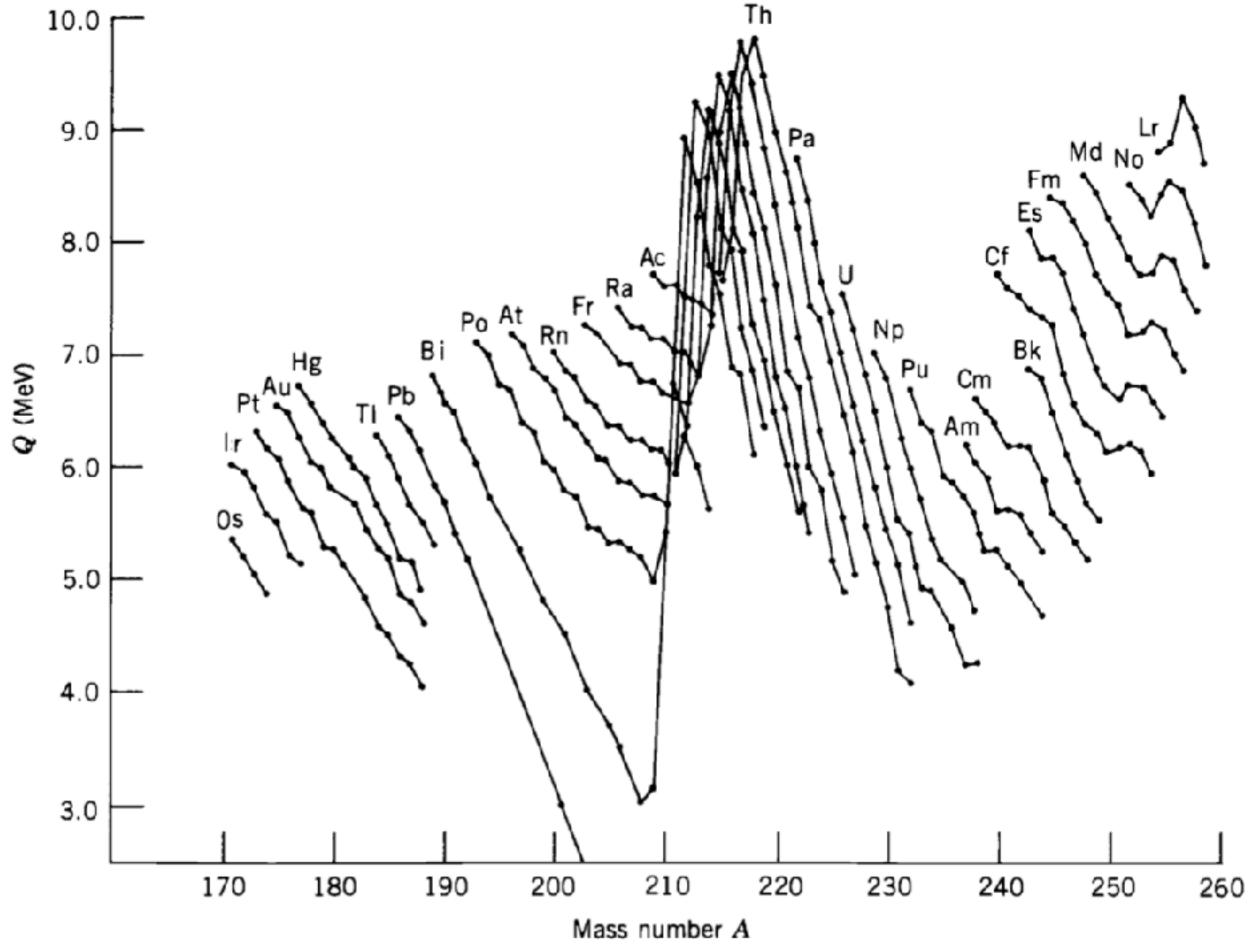


Figure 8.2 Energy released in α decay for various isotopic sequences of heavy nuclei. In contrast to Figure 8.1, both odd-A and even-A isotopes are shown, and a small amount of odd-even staggering can be seen. The effects of the shell closures at N=126 (large dip in data) and Z=82 (larger than average spacing between Po, Bi, and Pb sequences) are apparent.

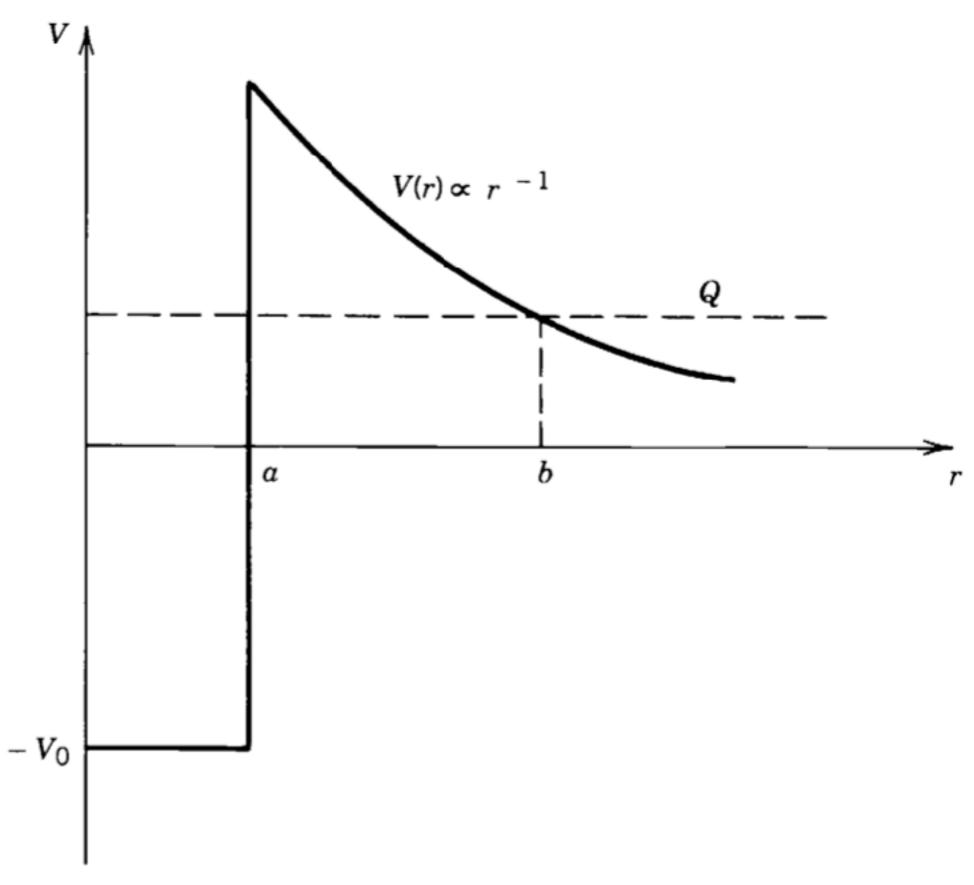


Figure 8.3 Relative potential energy of α -particle, daughter-nucleus system as a function of their separation. Inside the nuclear surface at r=a, the potential is represented as a square well; beyond the surface, only the Coulomb repulsion operates. The α particle tunnels through the Coulomb barrier from a to b.

Table 8.2 Calculated α -Decay Half-lives for Th Isotopes

$m{A}$	Q (MeV)	$t_{1/2}$ (s)	
		Measured	Calculated
220	8.95	10-5	3.3×10^{-7}
222	8.13	2.8×10^{-3}	6.3×10^{-5}
224	7.31	1.04	3.3×10^{-2}
226	6.45	1854	6.0×10^{1}
228	5.52	6.0×10^{7}	2.4×10^{6}
230	4.77	2.5×10^{12}	1.0×10^{11}
232	4.08	4.4×10^{17}	2.6×10^{16}

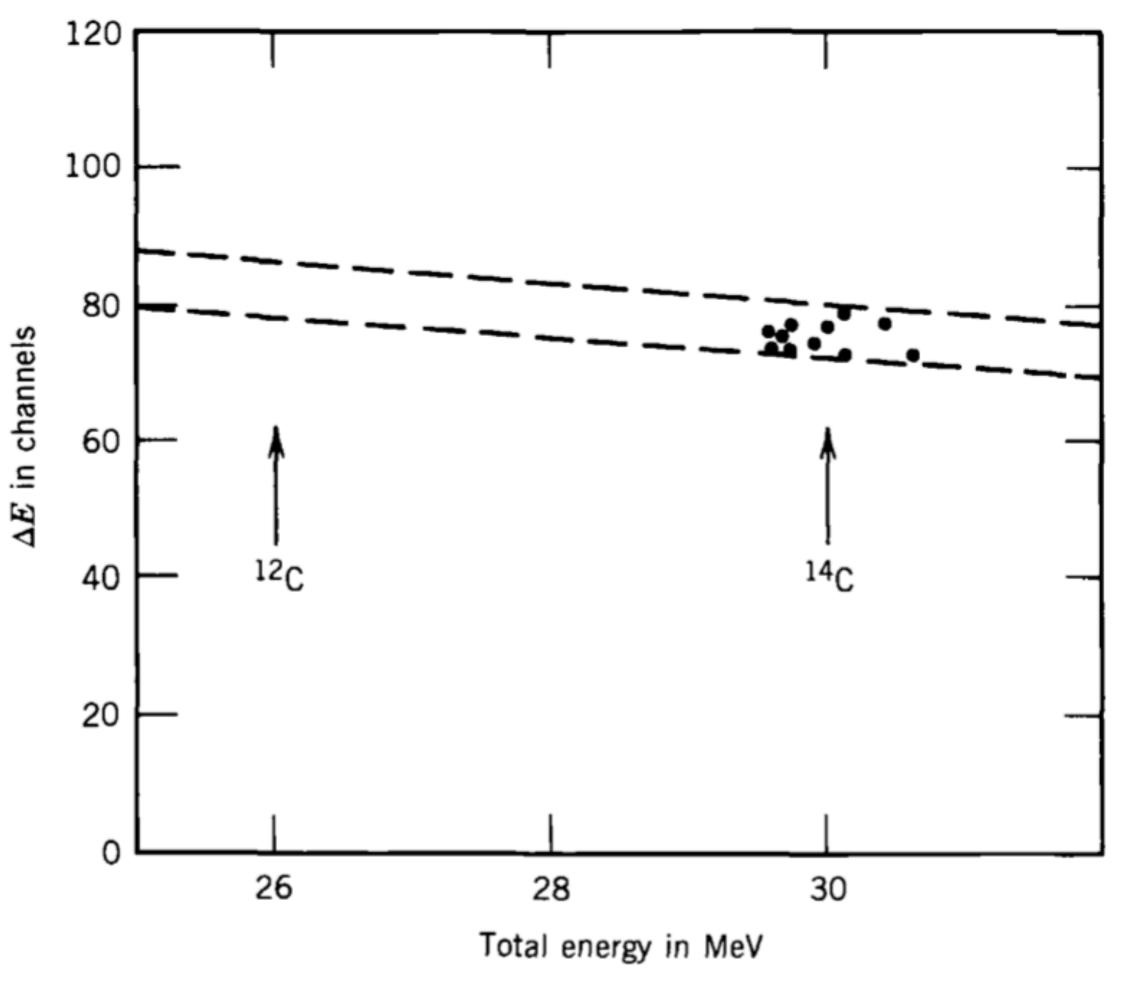


Figure 8.4 A portion of the tail of the $\Delta E \cdot T$ hyperbola showing the observed ¹⁴C events from the decay of ²²³Ra. The dashed lines show the limits expected for carbon. The 11 ¹⁴C events result from 6 months of counting. From H. J. Rose and G. A. Jones, *Nature* **307**, 245 (1984). Reprinted by permission, copyright © Macmillan Journals Limited.

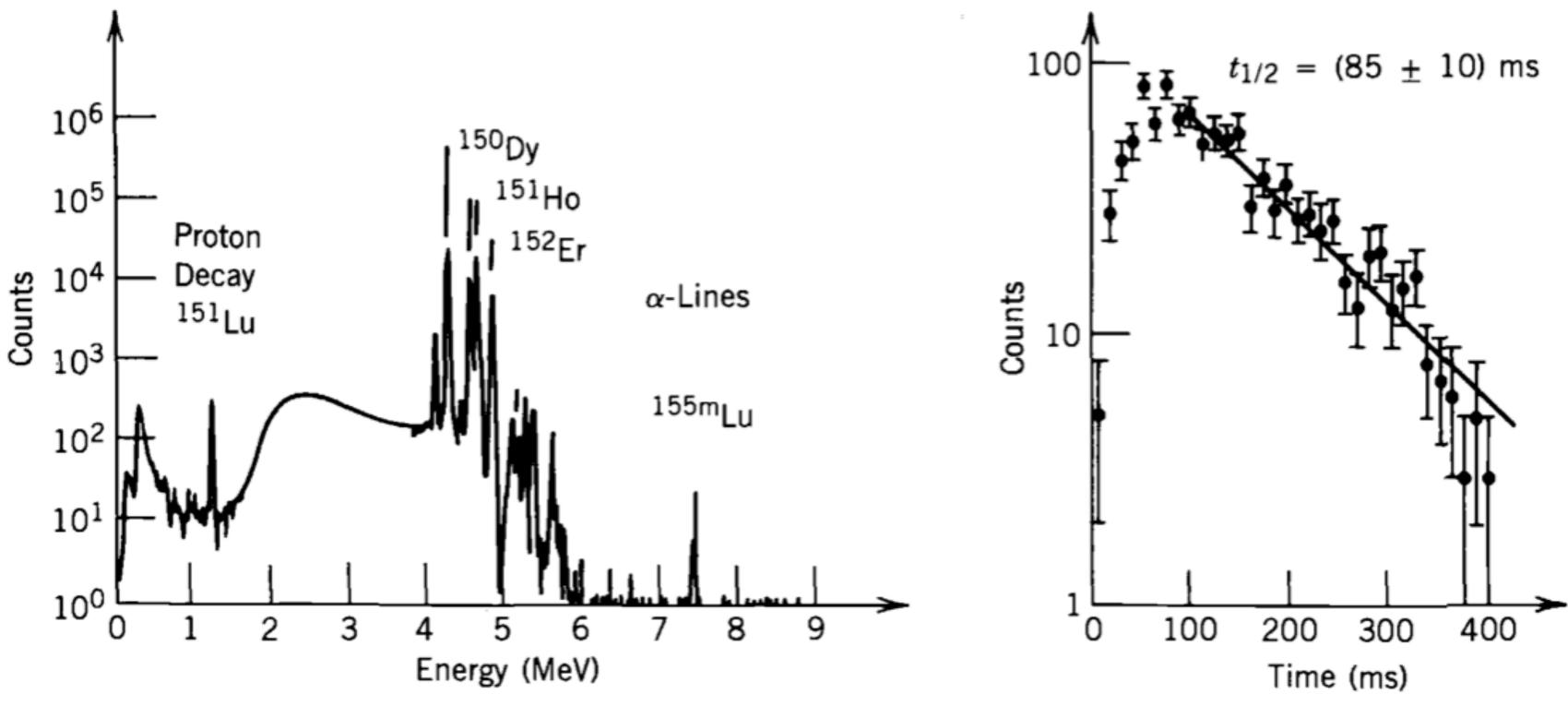


Figure 8.5 (Left) Charged-particle spectrum emitted in the radioactive decays of products of the reaction 96 Ru + 58 Ni. The peaks above 4 MeV represent α decays; the 1.2-MeV peak is from proton emission. (Right) The decay with time of the proton peak gives a half-life of 85 ms. From S. Hofmann et al., *Z. Phys. A* **305**, 111 (1982).

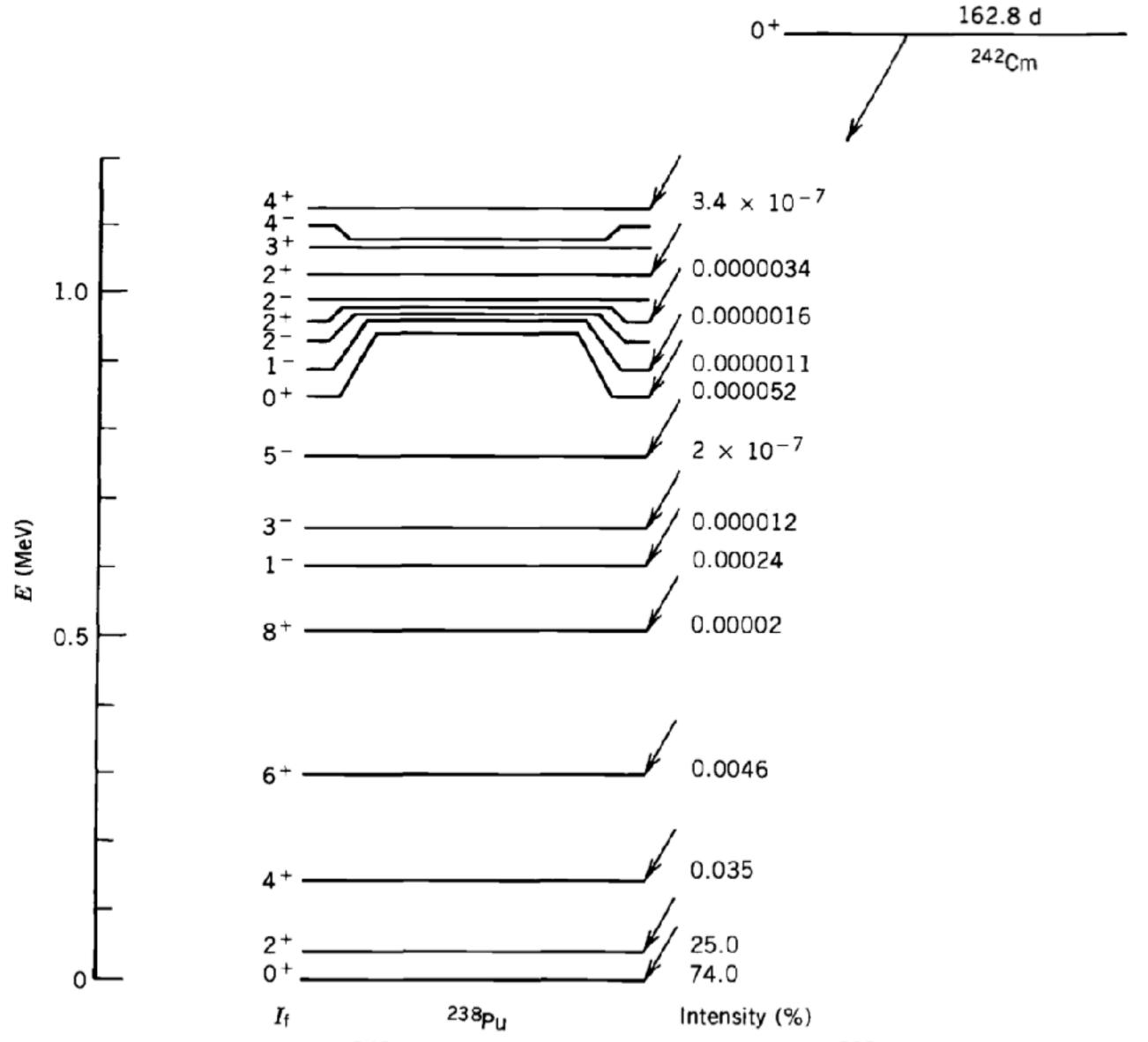


Figure 8.7 α decay of ²⁴²Cm to different excited states of ²³⁸Pu. The intensity of each α -decay branch is given to the right of the level.

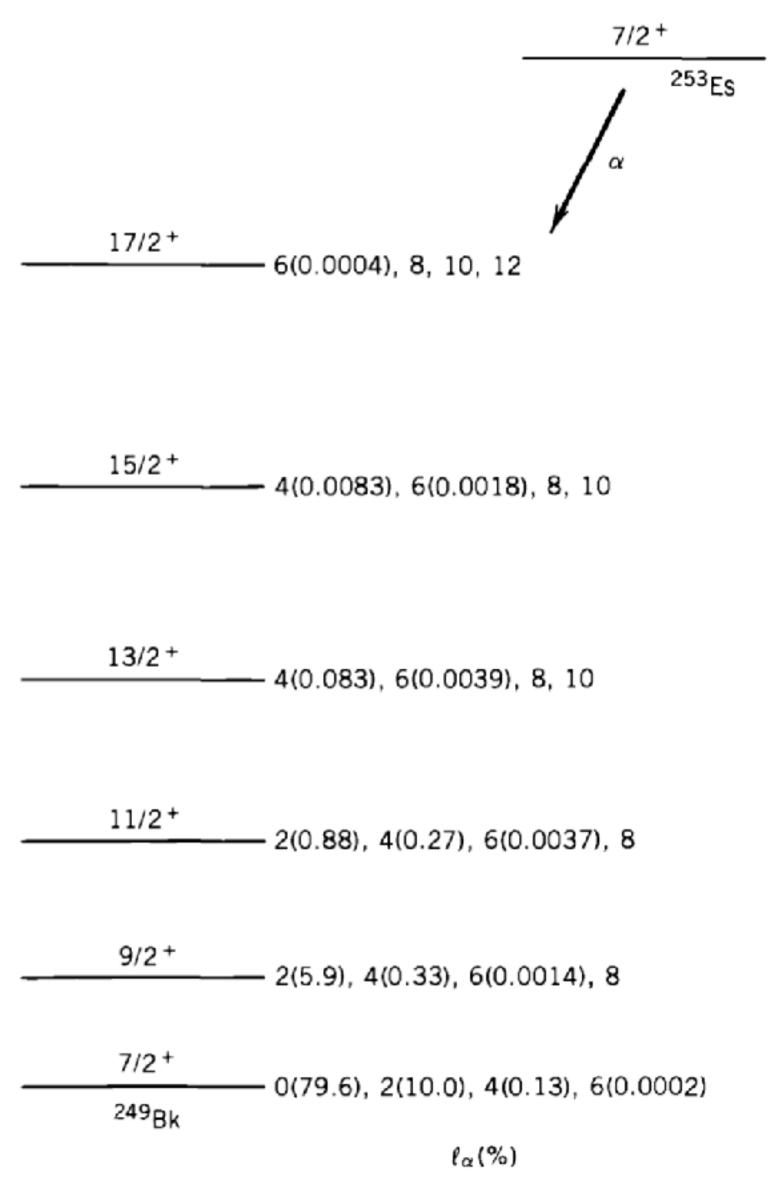


Figure 8.8 Intensities of various α -decay angular momentum components in the decay of 253 Es. For $\ell_{\alpha} = 8$ and higher, the intensities are not known but are presumably negligibly small. From the results of a study of spin-aligned α decays by A. J. Soinski et al., *Phys. Rev. C* 2, 2379 (1970).

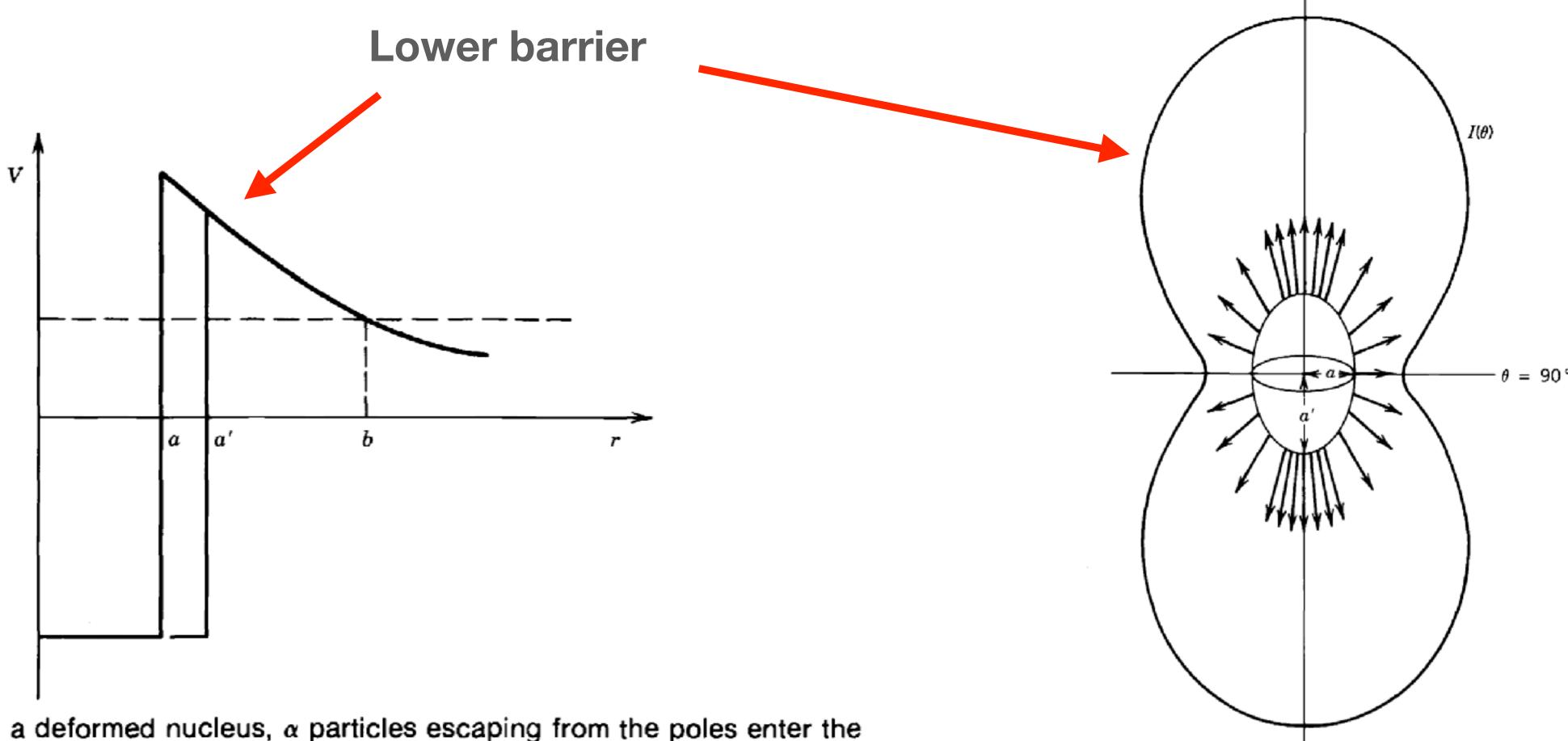


Figure 8.9 In a deformed nucleus, α particles escaping from the poles enter the Coulomb barrier at the larger separation a', and must therefore penetrate a lower, thinner barrier. It is therefore more probable to observe emission from the poles than from the equator.

Figure 8.10 Intensity distribution of α particles emitted from the deformed nucleus at the center of the figure. The polar plot of intensity shows a pronounced angular distribution effect.

 $\theta = 0^{\circ}$

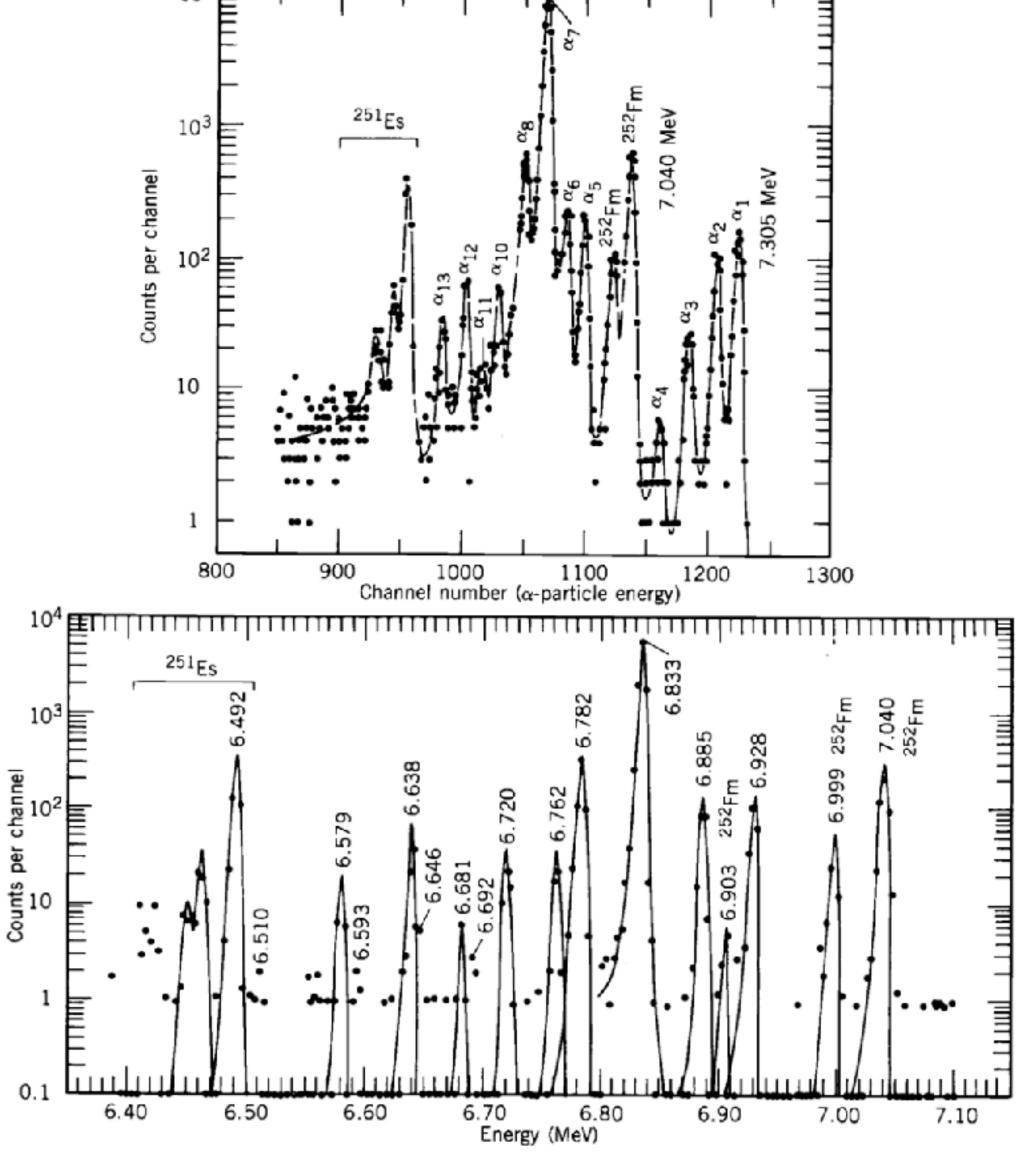


Figure 8.11 α spectrum from the decay of 251 Fm. The top portion shows the spectrum as observed with a Si detector. The bottom shows a portion of the same spectrum observed with a magnetic spectrometer, whose superior energy resolution enables observation of the 6.762-MeV decay, which would be missed in the upper spectrum. From Ahmad et al., *Phys. Rev. C* **8**, 737 (1973).

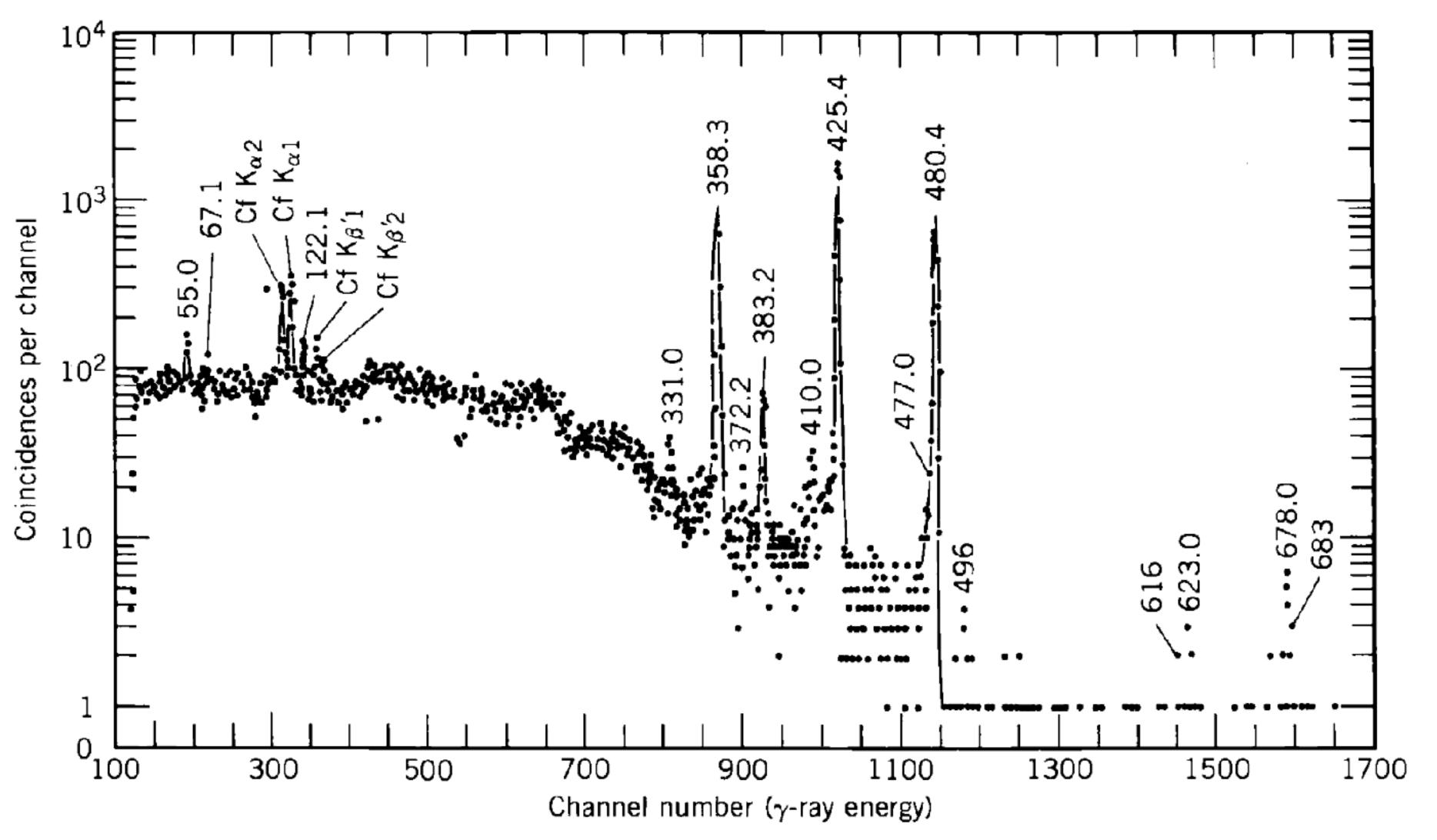


Figure 8.12 γ -ray spectrum of 251 Fm in coincidence with all α decays in the range 6.0 to 7.7 MeV. The spectrum was obtained with a Ge(Li) detector.

Ω is the component of the angular momentum of the odd particle along the symmetry axis

α decay

Excitation energy levels calculated from the α and γ spectra

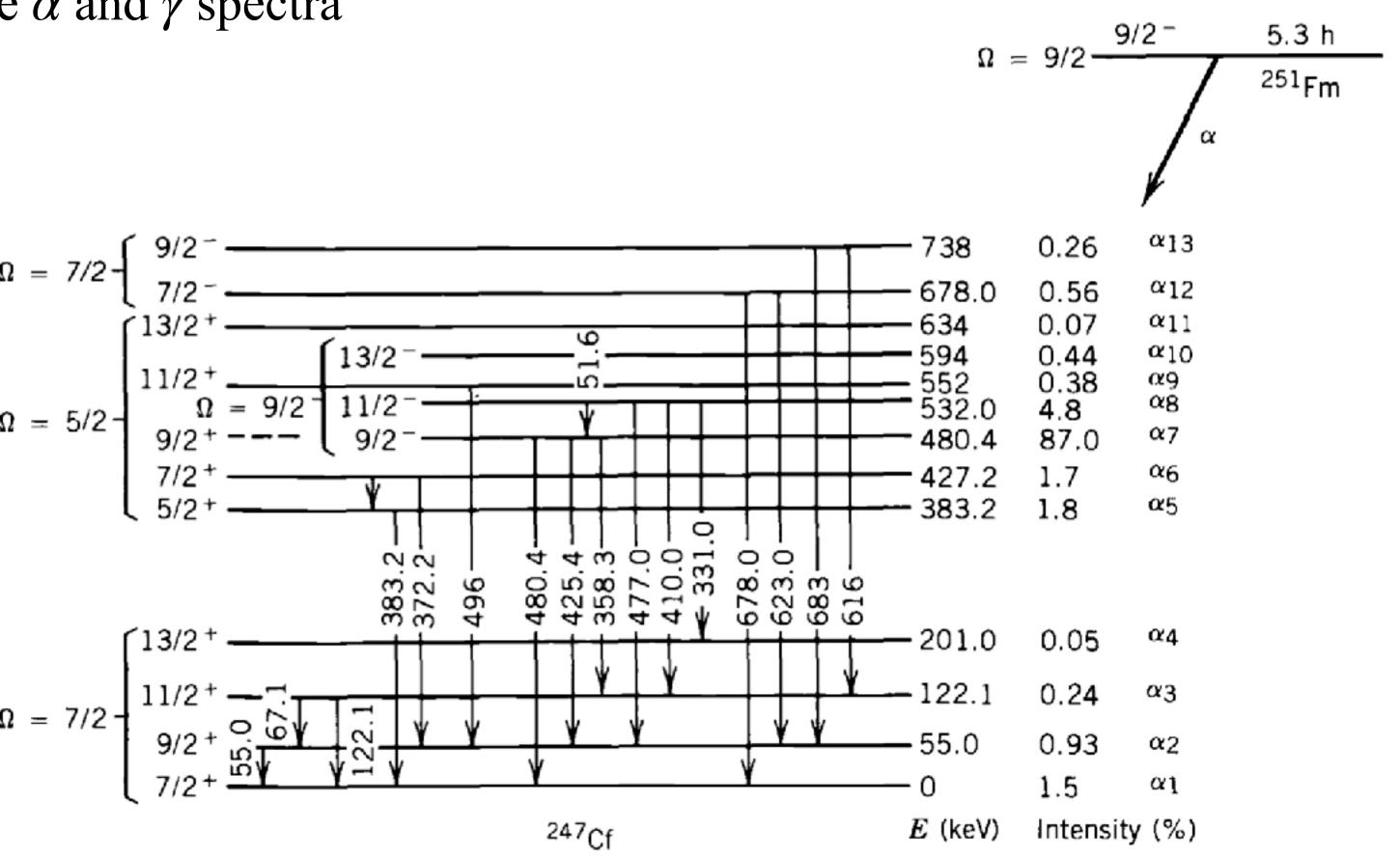


Figure 8.13 The decay scheme of 251 Fm to levels of 247 Cf deduced from α and γ spectroscopy. The spin assignments for the higher levels are deduced using γ -ray and internal conversion techniques described in Chapter 10.

1D spectra

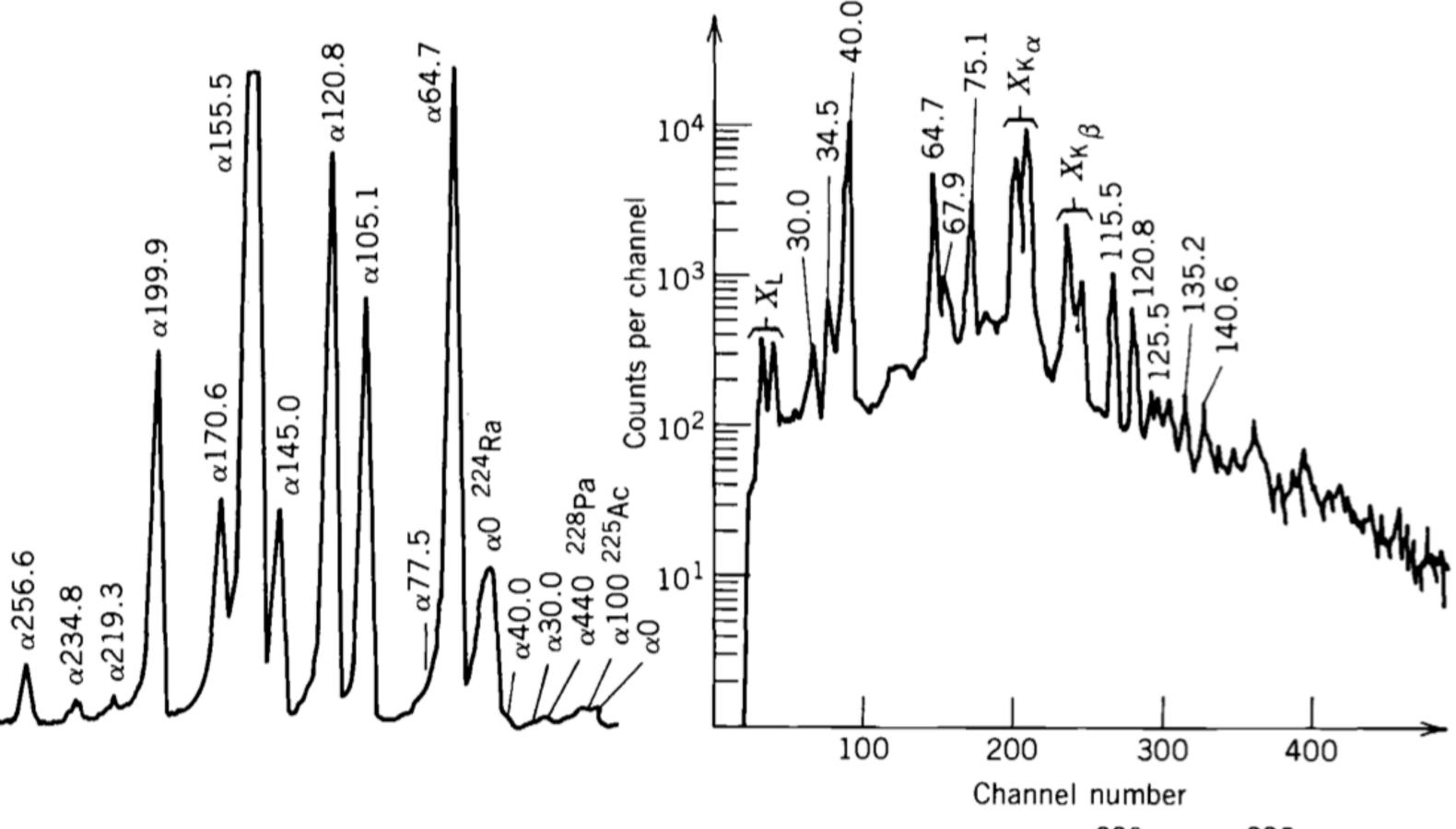


Figure 8.14 α (left) and γ (right) spectra from the decay of ²²⁹Pa to ²²⁵Ac. The α peaks are labeled according to the excited state populated in ²²⁵Ac; thus α 105.1 indicates the decay leading to the excited state at 105.1 keV. Prominent peaks from impurities are also indicated. The γ spectrum is taken in coincidence with all α 's. From P. Aguer et al., *Nucl. Phys. A* **202**, 37 (1973).

2D spectra

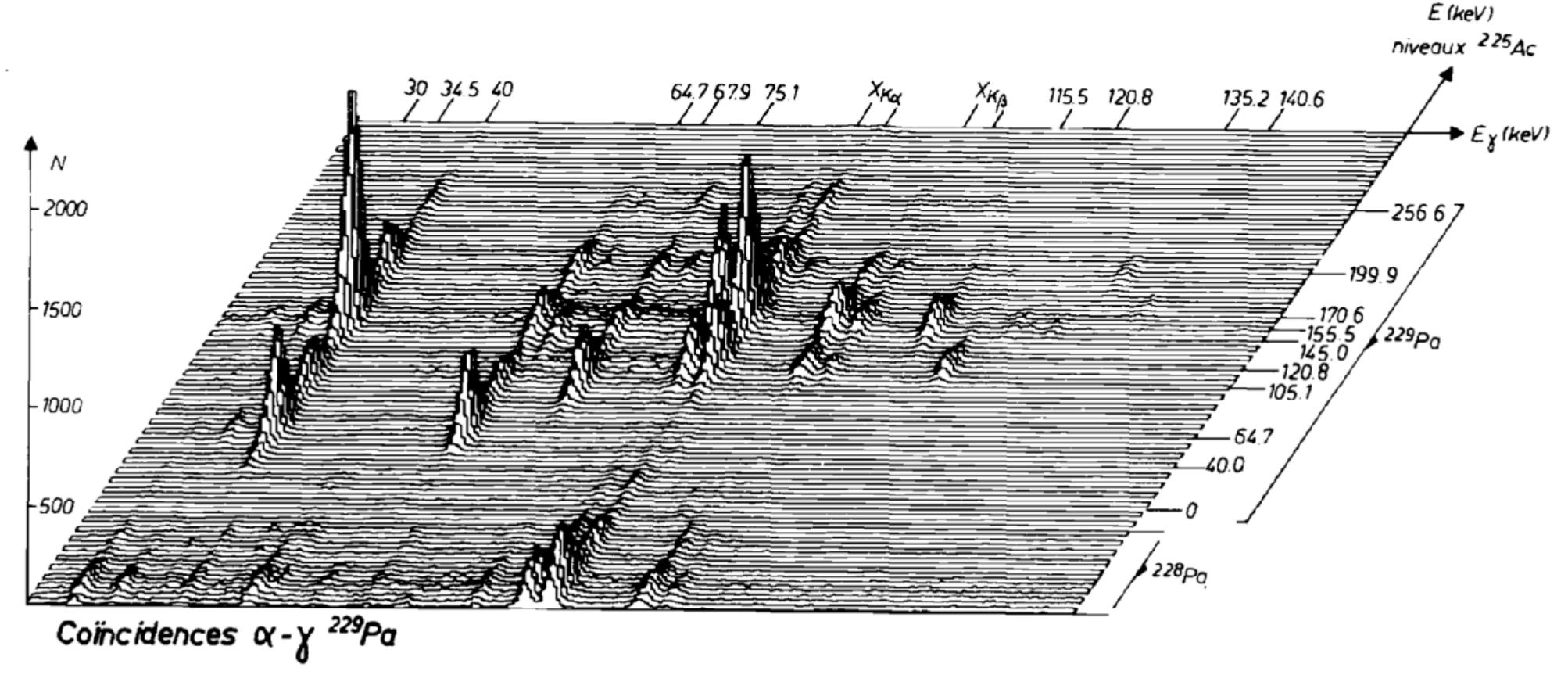
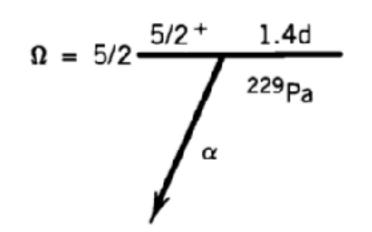


Figure 8.15 Three-dimensional (sometimes called two-parameter) representation of α - γ coincidences in the decay of ²²⁹Pa. The horizontal axis shows γ -ray energies, labeled along the top. The oblique axis gives α -decay energies, labeled to indicate the ²²⁵Ac state populated in the decay. The vertical axis gives the intensity of the coincidence relationship.

Energy levels based on the spectra



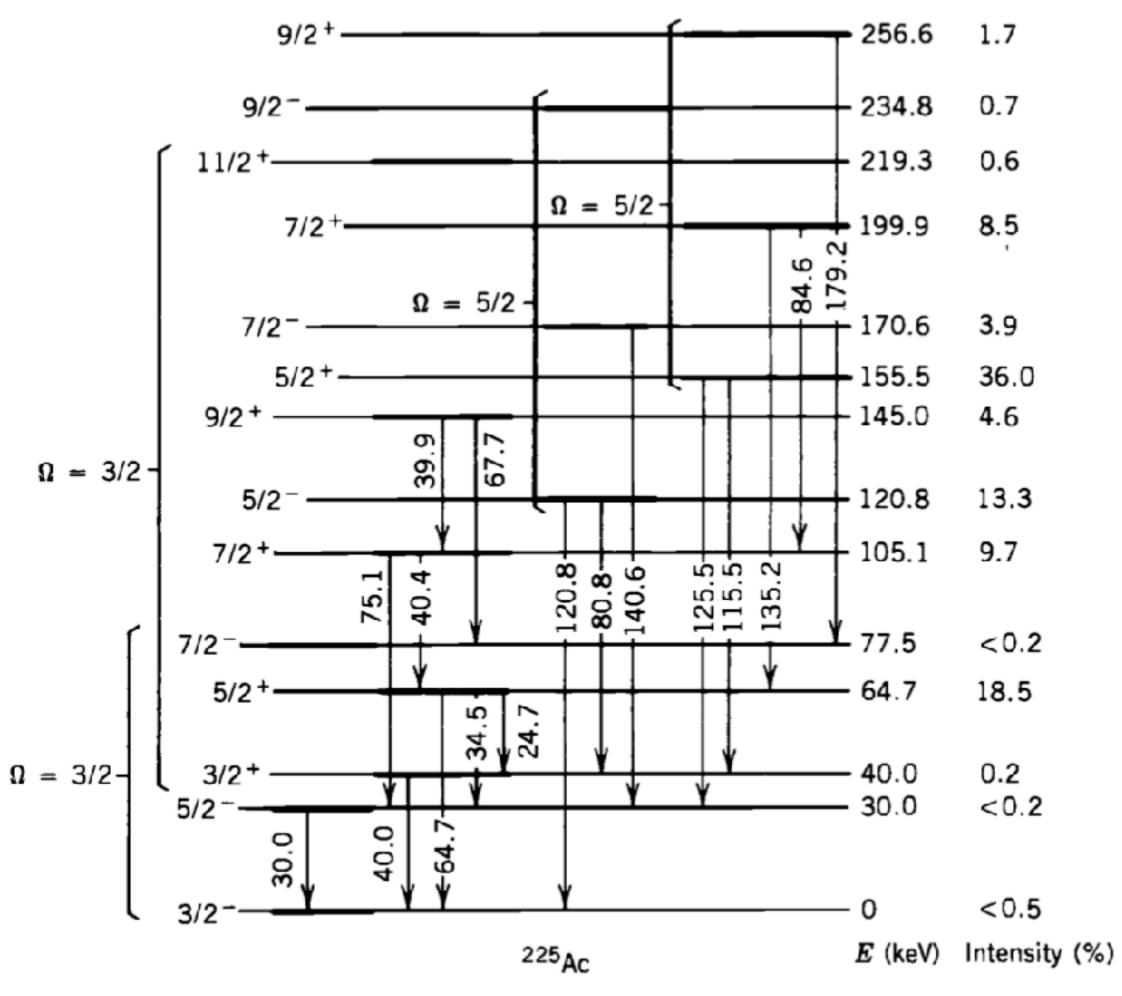


Figure 8.16 Decay scheme of 229 Pa deduced from α and γ spectroscopy.