

MATLAB/Simulink Session 2

Part 2

Symbolic Laplace Calculation

```
% laplace with syms
```

```
syms t s
```

```
laplace(cos(t))
```

```
ans =
```

$$\frac{s}{s^2 + 1}$$

```
laplace(sin(t))
```

```
ans =
```

$$\frac{1}{s^2 + 1}$$

```
y = t*exp(-t)
```

$$y = t e^{-t}$$

```
laplace(y)
```

```
ans =
```

$$\frac{1}{(s + 1)^2}$$

```
syms y(t) a
```

```
eqn = diff(y,t) == a*y;
```

```
y = dsolve(eqn)
```

$$y = C_1 e^{at}$$

```
laplace(y)
```

```
ans =
```

$$-\frac{C_1}{a - s}$$

Laplace Inverse Calculation

```
% inverse laplace
```

```
ilaplace(ans)
```

$$ans = C_1 e^{at}$$

```
syms t s
G = 1/(s + 1)
```

```
G =
    1
  ---
 s + 1
```

```
ilaplace(G)
```

```
ans = e-t
```

Define Laplace: Second Method

Note: To plot the step response or calculate DC gain, poles and zeros, use methods below.

```
% another method
s = tf('s')
```

```
s =
```

```
s
```

Continuous-time transfer function.

```
G = 1/(s + 1)
```

```
G =
```

```
    1
  ----
 s + 1
```

Continuous-time transfer function.

```
clc;
clear

% 1st method
N = [1 1]
```

```
N = 1×2
    1    1
```

```
D = [1 2 1]
```

```
D = 1×3
    1    2    1
```

```
G1 = tf(N, D)
```

```
G1 =
    s + 1
  -----
```

$$s^2 + 2s + 1$$

Continuous-time transfer function.

```
% 2nd method
s = tf('s')
```

s =

s

Continuous-time transfer function.

$$G2 = (s+1)/(s^2 + 2s + 1)$$

G2 =

$$\frac{s + 1}{s^2 + 2s + 1}$$

Continuous-time transfer function.

Poles, Zeros and DC gain of Transfer Functions

```
% poles, zeros, dc gain
zero(G2)
```

ans = -1

```
pole(G2)
```

```
ans = 2x1
     -1
     -1
```

```
dcgain(G2)
```

ans = 1

Step Response

```
% step response
s = tf('s')
```

s =

s

Continuous-time transfer function.

$$G1 = 1/(s+1)$$

G1 =

$$\frac{1}{s+1}$$

$$s + 1$$

Continuous-time transfer function.

$$G2 = 1/(s+1)^2$$

G2 =

$$\frac{1}{s^2 + 2s + 1}$$

Continuous-time transfer function.

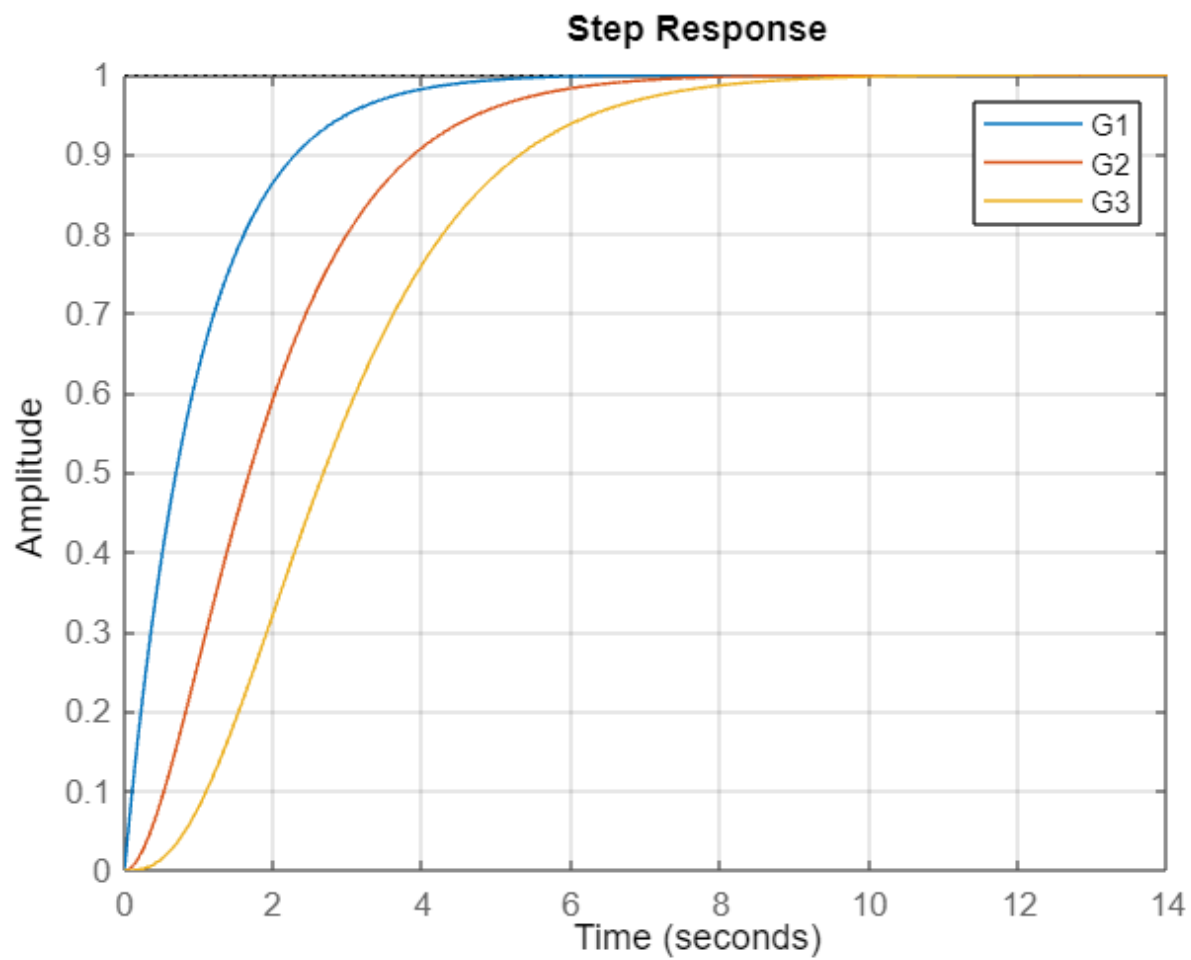
$$G3 = 1/(s+1)^3$$

G3 =

$$\frac{1}{s^3 + 3s^2 + 3s + 1}$$

Continuous-time transfer function.

```
step(G1)
hold on
step(G2)
step(G3)
grid on
legend
```



```
clc
close all
clear
s = tf('s')
```

s =

s

Continuous-time transfer function.

```
H1 = (s+1)/(s+2)
```

H1 =

$$\frac{s + 1}{s + 2}$$

Continuous-time transfer function.

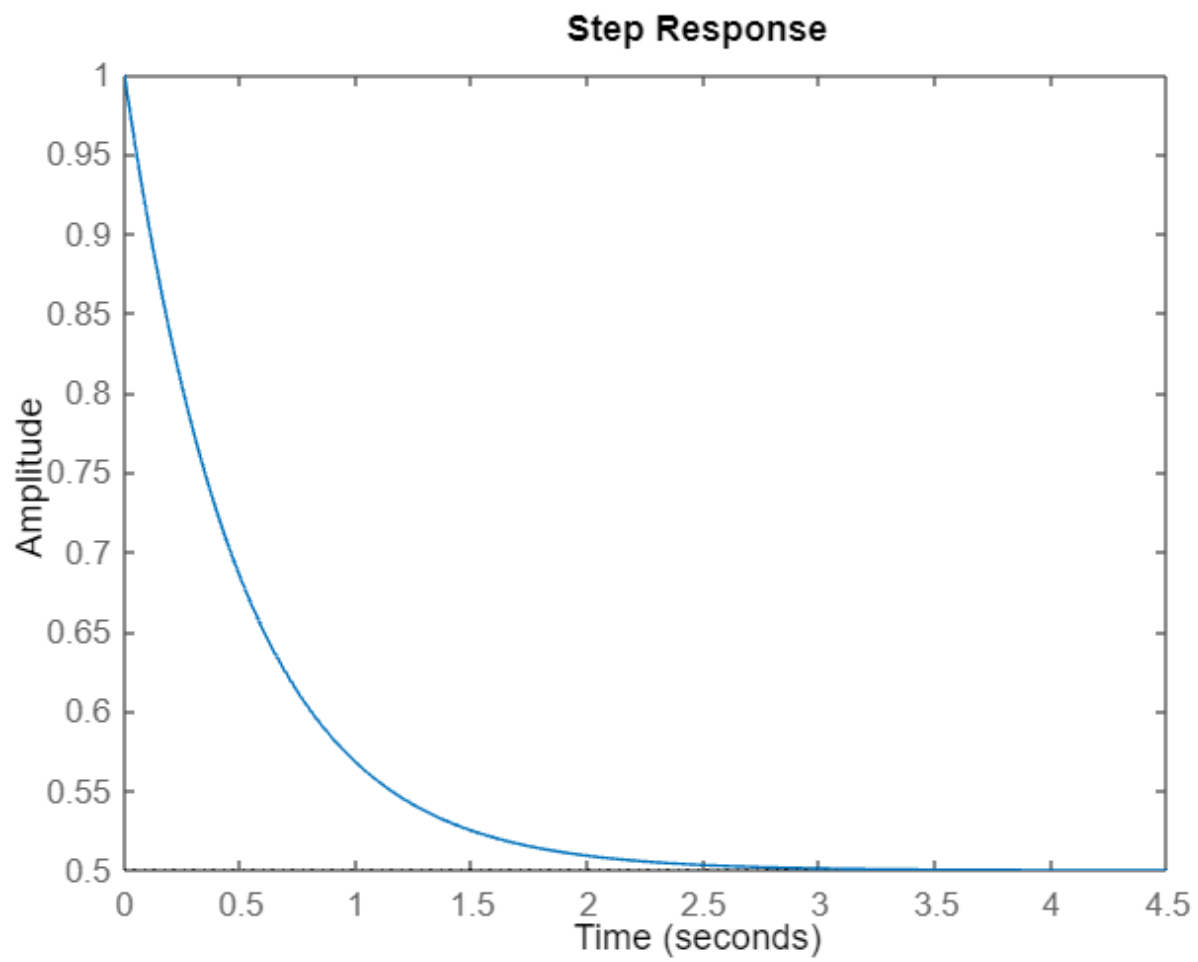
```
H2 = 2/(s+2)
```

H2 =

$$\frac{2}{s + 2}$$

Continuous-time transfer function.

step(H1)



step(H2)

