

Chiplet Placement for 2.5D IC with Sequence Pair Based Tree and Thermal Consideration

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ABSTRACT

This work develops an efficient chiplet placer with thermal consideration for 2.5D ICs. Combining the sequence-pair based tree, branch-and-bound method, and advanced placement/pruning techniques, the developed placer can find the solution fast with the optimized total wirelength (TWL) on half-perimeter wirelength (HPWL). Additionally, with the post placement procedure, the placer reduces maximum temperatures with slight increase of wirelength. Experimental results show that the placer can not only find better optimized TWL (reducing 1.035% HPWL) but also speed up at most two orders of magnitude than the prior art. With thermal consideration, the placer can reduce the maximum temperature up to 8.214 °C with an average 5.376% increase of TWL.

KEYWORDS

2.5D IC, chiplet placement, sequence pair, thermal

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1 INTRODUCTION

As technology nodes scale down, chips can achieve higher performance. As the transistor size has approached to its physical limit, recently, 2.5D ICs (also called interposer-based 3D ICs) have been developed by the IC foundry [1] to alleviate the issues of technology node scaling. 2.5D ICs can provide better performance and yield than 2D ICs [2] and have been realized as commercial products [3, 4]. Fig. 1 illustrates the structure of a 2.5D IC [5]. It contains a silicon interposer as an interface between chiplets and the package substrate. The nets between chiplets are routed in the redistribution layer (RDL) of the silicon interposer, and μ -bumps and C4 bumps are for the connections between chiplets, interposer, and package substrate.

Several approaches have been proposed to minimize wirelength of interconnects between chiplets. Ho and Chang [6] utilized the simulated annealing (SA) method to place multiple chiplets, macros, and I/O buffers. Liu *et al.* [7] introduced an enumeration-based algorithm with acceleration techniques for solving the multi-die floorplanning problems, which can obtain the optimal placement with minimizing total wirelength (TWL) on HPWL. Recently, Osmolovskiy *et al.* [8] modeled the chiplet placement as the constraint-satisfaction problem (CSP) and applied advanced pruning techniques to an advanced branch-and-bound (B&B) method for saving runtimes and obtaining

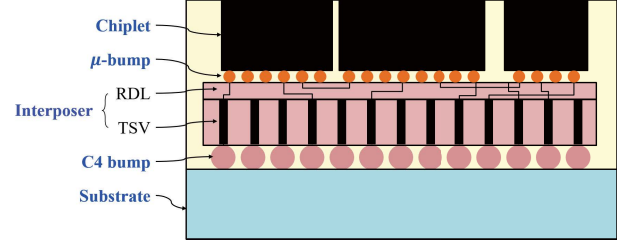


Figure 1: The architecture of 2.5D IC.

the optimal placement while minimizing TWL. For thermal consideration on chiplet placement, [9, 10] presented a thermal-aware chiplet placement by using the SA technique with thermal-aware cost function and inserting spaces between chiplets while finding a routing solution simultaneously. However, the SA based chiplet placement methods might obtain a sub-optimal solution.

To our best knowledge, there is no chiplet placer considering thermal effects while seeking the optimal placement. This work develops an efficient chiplet placer via the sequence pair based tree and we name it SP-CP that can obtain the optimal TWL. Moreover, to alleviate thermal issues, we build a post placement procedure to find a better thermal solution from the optimal and near-optimal placements of SP-CP. The main contributions are

- We develop an efficient chiplet placer, SP-CP. We build a sequence pair (SP) based tree (SP-Tree), which contains both rotation and partial/complete SP representation, and apply the B&B method on SP-Tree to find the optimal solution. Moreover, we advance placement/pruning techniques for the optimal solution and faster runtime in SP-CP.
- For thermal consideration, we build a post placement procedure to reduce the operating temperatures of 2.5D ICs on the optimal and near-optimal placements of SP-CP. It seeks for placement solution considering thermal effects but slightly increasing TWL.

We organize this paper as follows. First, Section 2 introduces the floorplanning and chiplet placement techniques of the prior art and Section 3 states the problem formulation. Next, Section 4 overviews the proposed framework for chiplet placement with SP-Tree and thermal consideration. Section 5 details SP-CP containing SP-Tree and advanced placement/pruning techniques for optimizing TWL. Then, Section 6 presents the post placement procedure of SP-CP to reduce the maximum temperature. Finally, Section 7 shows experimental results and Section 8 concludes this work.

2 PRELIMINARY

2.1 The B&B method for chiplet placement [8]

2.1.1 Chiplet ordering. [8] considers the interconnect of chiplets and constructs a complete graph with weights $e_{ij} = n_{ij} \cdot (w_i + h_i + w_j + h_j) / 2$. w_i/w_j and h_i/h_j are the width and the height of chiplet i/j (c_i/c_j), respectively. n_{ij} is the number of nets connected by c_i and c_j . Then, it determines a node that has the maximum cut from sorted nodes iteratively.

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2.1.2 Placement optimization with whitespace. The default packed chiplets in [8] are set in the left-bottom corner of interposer. As a chiplet has terminal nets, this packing may not be optimal. Hence, first, it treats all chiplets as a “virtual chiplet” and moves this virtual chiplet to minimize terminal connections. Then, it moves one chiplet for minimizing HPWL. It iteratively performs these two steps until there is no further improvement of TWL.

2.1.3 Terminal handling (TH). When a chiplet is added to a partial placement, [8] looks forward to predicting WL augmentation from its terminal nets. For a chiplet, [8] calculates the optimized HPWL by using the method in Section 2.1.2 with its terminal nets. Since a chiplet can have four rotations, each chiplet has four values in TH.

2.1.4 Forward wirelength checking (FC). [8] calculates the minimum WL for each chiplet pair with the nets only connected between them by using Section 2.1.2 in 4^3 possible cases, which includes rotations (4×4 , rotations of c_i and c_j) and topologies (4 topologies between c_i and c_j).

2.2 Sequence pair (SP) representation [11]

The sequence pair uses two sequences to express the topological relations between blocks (chiplets) as

$$(\cdot \cdot i \cdot j \cdot \cdot \cdot i \cdot j \cdot \cdot) \Rightarrow c_i \text{ is on the left of } c_j, \quad (1a)$$

$$(\cdot \cdot i \cdot j \cdot \cdot \cdot j \cdot i \cdot \cdot) \Rightarrow c_j \text{ is below } c_i. \quad (1b)$$

The placement of SP can be packed with horizontal/vertical constraint graph and its time complexity is $O(n^2)$, where n is the number of chiplets.

3 PROBLEM FORMULATIONS

The problem for chiplet placement with thermal consideration is to find a suitable placement while reducing the maximum temperature of chiplets. Firstly, we optimize the chiplet placement while minimizing TWL and it is formulated as

$$\min \sum_k^{\#nets} HPWL_k \quad (2)$$

subject to

$$0 \leq x_{l,i}, x_{r,i} \leq W; 0 \leq y_{b,i}, y_{t,i} \leq H. \quad (3a)$$

$$w_s \leq \min\{|x_{l,i} - x_{r,j}|, |x_{l,j} - x_{r,i}|, |y_{b,i} - y_{t,j}|, |y_{b,j} - y_{t,i}|\}, \quad (3b)$$

where W/H is the width/height of the interposer, $x_{l,i}/x_{r,i}$ is the left/right position of c_i along the x -axis, and $y_{b,i}/y_{t,i}$ is the bottom/top position of c_i along the y -axis.

Here, we utilize the metric of HPWL to estimate the wirelength of a net k and our goal is to minimize TWL. The placement constraints include the fixed-outline constraint in (3a), and the minimum distance between chiplets [5] in (3b).

Then, with the optimal and near-optimal placements by solving (2), the problem is to reduce the maximum temperature from these placements. And we find a near-optimal placement satisfying thermal constraint T_{cstr} , with an acceptable TWL increase in percentage $\eta\%$ compared to the optimized TWL (TWL^{opt}). If the maximum temperature T_{max} of chiplets is still larger than T_{cstr} , we choose the placement with the minimal cost from the placements with increased TWL $< \eta\%$ and the cost function is formulated as

$$cost = \phi \times \frac{TWL - TWL^{opt}}{TWL^{max} - TWL^{opt}} + (1 - \phi) \times \frac{T_{max} - T_{max}^{min}}{T_{max}^{max} - T_{max}^{min}}, \quad (4)$$

where TWL^{max} is the maximum TWL, and $T_{max}^{max}/T_{max}^{min}$ is the maximum/minimum of maximum temperatures of the placements with increased TWL $< \eta\%$.

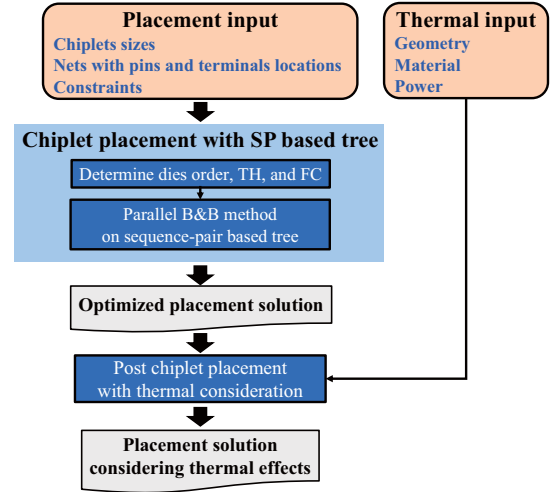


Figure 2: The proposed framework.

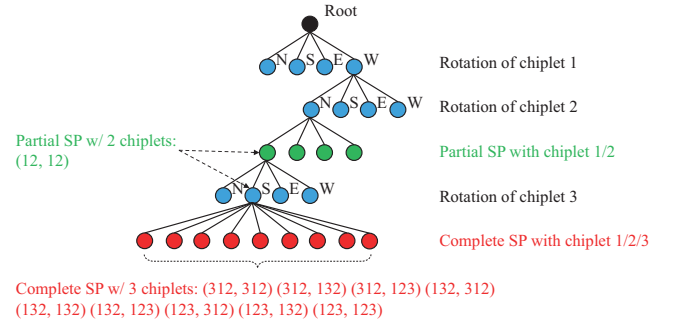


Figure 3: Sequence pair based tree.

4 THE PROPOSED FRAMEWORK

Fig. 2 shows the framework for minimizing TWL in (2) and reducing the maximum temperature under placement constraints. Given sizes of chiplets, nets with pins, net weights, terminal locations, placement constraints, geometries of 2.5D IC components, material, and power consumption of each chiplet, firstly, we perform the placer preprocessing for die ordering and estimated HPWL (TH and FC) as Sections 2.1.1, 2.1.3, and 2.1.4. Then, we apply the parallel B&B method on sequence-pair based tree for obtaining a set of optimal and sub-optimal placements with minimizing TWL. Finally, we perform post placement by considering the thermal effect to reduce T_{max} and find a near-optimal placement with lower T_{max} .

5 CHIPLET PLACEMENT WITH SP BASED TREE

5.1 SP based tree (SP-Tree)

SP-CP builds SP-Tree to represent all possible solutions. SP-Tree consists of three kinds of nodes: (i) rotation node with the direction of chiplet, north (0°), west (90°), south (180°) and east (270°) (blue nodes in Fig. 3), (ii) partial SP for topological relation between chiplets (green nodes in Fig. 3), and (iii) complete SP (red leaf nodes in Fig. 3). We add one chiplet while traversing to a rotation node. And a new index of chiplet is inserted into the SP with partial SP of the parent node. For example, when we insert chiplet 3 into the parent node with SP (12, 12), we can get nine child nodes (312, 312), (312, 132), (312, 123), (132, 312), (132, 132), (132, 123), (123, 312), (123, 132), and (123, 123).

CSP-Tree (a tree with a constraint-satisfaction problem) in [8] represents the rotation of chiplets and topology (left, right, bottom, and top) of each chiplet pair. Compared with CSP-Tree, all the nodes of

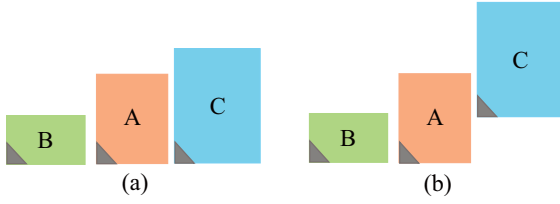


Figure 4: An example of two topology nodes in CSP-Tree having the same SP representation (BAC, BAC).

partial SP and complete SP in SP-Tree can be packed into a placement, but some of topology nodes in CSP-Tree might not be packed into a placement. For example, if chiplet B (c_B) is at the left of chiplet A (c_A), chiplet C (c_C) is at the right of c_A , and c_C is at the left of c_B . It forms a cyclic horizontal constraint graph. Thus, it cannot be packed into a placement.

In addition, one SP representation might cover multiple topology nodes in CSP-Tree. For example, Fig. 4.(a) shows one node in CSP-Tree (c_B is at the left of c_A , c_C is at the right of c_A , and c_C is at the right of c_B). And Fig. 4.(b) shows the other node in CSP-Tree (c_B is at the left of c_A , c_C is at the right of c_A , c_C is above of c_B). Both nodes in Fig. 4 can be represented as a SP (BAC, BAC).

The solution spaces of CSP-Tree and SP-Tree for n chiplets are $4^n \times 4^{n(n-1)/2}$ and $4^n \times (n!)^2$, respectively, and $\forall n > 2, 4^{n(n-1)/2} > (n!)^2$. For instance, as the chiplet number n is 11, the solution spaces of CSP-Tree are about 5.44×10^{39} which is much larger than the solution spaces of SP-Tree which are 6.68×10^{21} .

5.2 Advanced placement/pruning techniques

5.2.1 Analytical whitespace optimization. Besides the two steps presented in Section 2.1.2 [8] for optimizing TWL within whitespace, SP-CP introduces two extra moves to optimize TWL within whitespace. One move is that SP-CP fixes one chiplet and moves other chiplets as a “virtual chiplet” while minimizing TWL with terminal nets. Then, it iteratively fixes each chiplet and optimizes the “virtual chiplet” until no further improvement on TWL. The other move is that SP-CP fixes two chiplets and moves other chiplets as a “virtual chiplet” while minimizing TWL with terminal nets. Then, it fixes two chiplets among all chiplets iteratively and optimizes the “virtual chiplet” until no further improvement on TWL.

5.2.2 Remaining distance for SP-Tree. [8] uses “remaining distances (RD)” to estimate the HPWL of chiplets that are unplaced in the partial placement. In SP-Tree, this methodology can be applied as well. SP-CP utilizes the TH and the FC from Section 2.1.3 and 2.1.4 to calculate the RD for a partial SP node. If there are k placed chiplets (c_k, \dots, c_1) at a partial SP node, the RD of this node can be calculated by $(n - k)$ rotations for the TH and $(n \times (n - 1)/2 - k \times (k - 1)/2)$ topologies for the FC. Moreover, if there are k placed chiplets (c_k, \dots, c_1) at a rotation node, the RD of this node can be calculated by $(n - k - 1)$ rotations for the TH and $(n \times (n - 1)/2 - (k - 1) \times (k - 2)/2)$ topologies for the FC. SP-CP chooses the minimum value of TH (with four values) and the minimum value of FC (with sixty-four values) while calculating the RD at a rotation node and a partial SP node in SP-Tree, respectively. Note that sixty-four values are needed for calculating the minimum FC in a topology for the RD. The number of values for calculating the minimum FC can be reduced to sixteen values (if the rotation of one chiplet in FC is known) or four values (if the rotation of both chiplets in FC are known).

At the partial SP node, SP-CP defines the optimized partial TWL of a partial SP as TWL_{par, c_k} which can be obtained by using the method in Section 5.2.1. Fig. 5 illustrates one example for estimating the HPWL lower bound. There are two cases, the rotation node and the partial SP

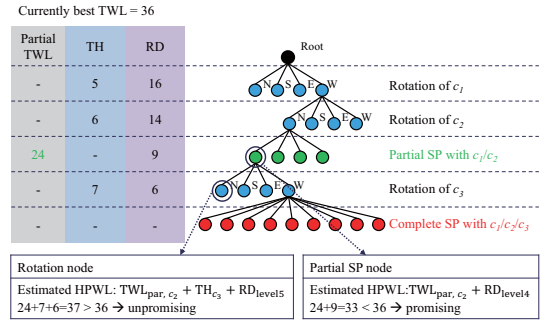


Figure 5: An example for estimating HPWL.

node. For the rotation node, the estimated HPWL is the summation of TWL_{par, c_2} (from the parent node), TH of the current node, and RD (the minimum value of FC for c_2 and c_3). For the partial SP node, the estimated HPWL is the summation of TWL_{par, c_2} and RD (the minimum value of TH for c_3 and the minimum value of FC for c_2 and c_3). If the estimated HPWL is larger than the current best TWL, this node is pruned in the B&B method.

5.2.3 Pruning dominated nodes of rotation and partial SP. [8] proposed the pruning dominated configuration to address the non-linear nature of HPWL metric for partial configurations on CSP-Tree. For B&B on SP-Tree, we might similarly discard a rotation/topology node when its estimated TWL is larger than the estimated minimum TWL, *bestTWL*, with the amount of *bestTWL* / $(n_k + 1)$, and we call this procedure the PDSP. Here, n_k is the number of placed chiplets at the level.

However, a topology node in CSP-Tree represents one topology while a partial SP node in SP-Tree represents multiple topology relationships. Hence, we calculate a modification coefficient $\gamma[i]$ by Algorithm 1 (A1) for each node i to reduce the amount to be $\gamma[i] \times \text{bestTWL} / (n_k + 1)$ for pruning more topology nodes. We call this procedure the PDSP & A1. First, we define $\alpha[i]$ to be the number of topology differences between the partial SP at node i and the partial SP having the best estimated HPWL at the same level. For example, after inserting c_3 into partial SP (12, 12), we analyze the contribution to $\alpha[i]$. Here, we assume (312, 312) have the minimum estimated HPWL at the same level. For (312, 312) and (312, 132) at node 1 at the same level, we compare the topology of c_3 with c_1 , and the topology of c_3 with c_2 .

- 1) $(\cdot \cdot 3 \cdot 1 \cdot \cdot, \cdot \cdot 3 \cdot 1 \cdot \cdot)(\cdot \cdot 3 \cdot 1 \cdot \cdot, \cdot \cdot 1 \cdot 3 \cdot \cdot)$ the topology of c_3 and c_1 is different. \Rightarrow this case contributes 1 to $\alpha[1]$.
- 2) $(\cdot \cdot 3 \cdot 2 \cdot \cdot, \cdot \cdot 3 \cdot 2 \cdot \cdot)(\cdot \cdot 3 \cdot 2 \cdot \cdot, \cdot \cdot 3 \cdot 2 \cdot \cdot)$ the topology of c_3 and c_2 is the same. \Rightarrow this case contributes 0 to $\alpha[1]$.

Here, $\alpha[1] = 1 + 0 = 1$.

Algorithm 1 (A1) calculates $\gamma[i]$ with $\alpha[i]$. First, we record the positions of the chiplet inserted by two sequences, called insertion position 1 (IP_1) and insertion position 2 (IP_2), and record the gap between the insertion positions of these two sequences (IP_{gap}). Then, using the insertion position of the node with the minimum estimated HPWL ($IP_1 \min, IP_2 \min, IP_{gap} \min$), we calculate the difference between IP and IP_{min} to get $\Delta IP_1, \Delta IP_2$, and ΔIP_{gap} . Finally, α is half of the sum of $\Delta IP_1, \Delta IP_2$, and ΔIP_{gap} . The time complexity for $\gamma[i]$ is $O(1)$ for each node i at the same level.

5.3 Parallel B&B on SP-Tree

The B&B method consists of two parts. In the branching part, we traverse SP-Tree using depth-first search. First, we insert a chiplet into SP-Tree at a time. For each node, we generate four new nodes of the partial SP node and n_k^2 nodes for the rotation node. In the bounding (pruning) part, we prune the nodes which do not meet

Algorithm 1 Modified coefficient γ on the same level of partial SP

```

Input: integer array  $[1, 2, \dots, n^2]$   $IP_1, IP_2$ 
        float array  $[1, 2, \dots, n^2]$   $TWL$ 
Output: float array  $[1, 2, \dots, n^2]$   $\gamma$ 
1: integer array  $[1, 2, \dots, n^2]$   $\alpha$ 
2:  $IP_{1min} = \min(IP_1)$ ;
3:  $IP_{2min} = \min(IP_2)$ ;
4:  $n = n_k$ ;
5: for each  $i \in [1, n^2]$  do
6:    $IP_{gap}[i] = IP_1[i] - IP_2[i]$ 
7:    $IP_{gapmin} = IP_{1min} - IP_{2min}$ 
8:    $\alpha[i] = (|IP_1[i] - IP_{1min}| + |IP_2[i] - IP_{2min}| + |IP_{gap}[i] - IP_{gapmin}|) / 2$ ;
9: end for
10: for each  $i \in [1, n^2]$  do
11:    $\gamma[i] = 1 - \frac{\alpha[i]}{n_k}$ ;
12: end for
    
```

placement constraints, the nodes with estimated HPWL larger than the current best TWL, and the nodes which do not satisfy the method in Section 5.2.3.

Moreover, we implement the B&B algorithm with parallel processing by using OpenMP [12]. We assign stacks to different threads for processing. When updating the currently best TWL, we suspend other threads (by setting the barrier in OpenMP) to ensure efficiency on the B&B method.

6 POST CHIPLET PLACEMENT (POST-CP) WITH THERMAL CONSIDERATION

6.1 Chiplet thermal simulation

To calculate the thermal profile of 2.5D IC efficiently and accurately, based on the duality between thermal and electrical quantities [13] and the finite difference method [14], we solve temperatures by building the equation

$$GT = P, \quad (5)$$

where G is the thermal conductance matrix, T is the temperature vector, and P is the power source vector.

To model the heat transfer, as shown in Fig. 1, five layers, substrate, C4 bump, interposer, μ -bump and chiplet, are included. The mesh is $64 \times 64 \times 5$. The heat transfer coefficients for the top and bottom sides of the 2.5D IC are 8700 and 2017 W/(m²K) for modeling the primary heat flow to the heat sink and secondary heat flow to PCB [15], and it is adiabatic for lateral sides of the 2.5D IC. We solve T of chiplets by using a sparse matrix solver, SuperLU 5.3.0 [16]. The errors of maximum temperature for the experiments are less than 1% compared to the commercial tool Icepak [17]. Since it is time-consuming (taking hours) while the proposed framework integrates with Icepak, we solve the thermal profile of 2.5D IC as mentioned above.

6.2 Placement refinement with thermal effects

After completing SP-CP, some placements might have shorter wirelength but violate T_{cstr} . To trade off their wirelength and operating temperatures, we perform the refinement procedure to satisfy T_{cstr} by slightly modifying the placements with increasing $TWL < \eta\%$ compared to TWL_{opt} . Then, we select the placement that has the minimum wirelength and also satisfies T_{cstr} . If none of them satisfies T_{cstr} , we choose the minimum cost from (4) of the placements with increasing $TWL < \eta\%$.

The refinement of a placement consists of two types of movement. One is moving one chiplet at a time without alternating other chiplets as illustrated in Fig. 6(a). The other is moving all chiplets together

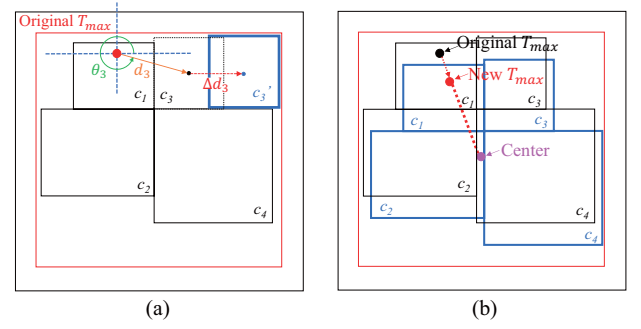


Figure 6: Placement refinement. (a) Move one chiplet (c_3); (b) Move all chiplets (c_1 - c_4).

toward the center but sticking to their same relative positions shown in Fig. 6(b). Generally, the rising temperature is highly related to the distance of power sources and their values. Hence, we plan to move away some chiplets which influence temperatures and have less impact on wirelength.

Given a placement result violating the thermal constraint and having its maximum temperature value (T_{max}) and position, we calculate the contribution to T_{max} by each c_i ($T_{max,i}$) via superposition and calculate the wirelength increase because of moving c_i by a certain distance (Δd_i). We also simply assume that the temperature influence between two chiplets is proportional to the reciprocal of their distance. Then, the value $(\delta T_i / \delta W_i)$ is calculated by dividing the temperature variations and the increasing wirelength per unit moving length of each c_i to measure its effectiveness. And we choose the c_m that has the lowest value $(\delta T_m / \delta W_m)$ to be the moving candidate because it is the most effective chiplet for trading off temperatures and wirelength. Then, we choose a suitable moving length that is less than the estimated required length for satisfying the thermal constraint.

After moving one chiplet, we renew the value and position of T_{max} . Finally, to increase the heat dissipation region of T_{max} , we move all chiplets together in the direction from the position of T_{max} to the center of the interposer by a certain distance. We iteratively perform the above steps until the maximum temperature meets the threshold temperature or the chiplets cannot be moved such as encountering the boundaries or other chiplets.

We summarize the steps of the refinement procedure as follows.

- 1) Calculate T_{max} and its position of a given placement by using the simulation in Section 6.1.
- 2) Define and calculate the thermal gain of each c_i , $g_i = T_{max,i} / P_i$, $i=1 \sim n$. P_i is the power of c_i and $T_{max} = \sum_{i=1}^n g_i P_i$.
- 3) Partially differentiate $T_{max,d} = \sum_{i=1}^n d_i g_i P_i / (d_i + \Delta d_i)$ on each Δd_i and have $\delta T_i = -g_i P_i / d_i$. Here, d_i is the distance between c_i and the position of T_{max} .
- 4) Calculate the increasing HPWL per unit moving length of c_i to be $\delta W_i = (|\cos \theta_i| + |\sin \theta_i|) * (\#net_i)$.
- 5) Calculate $\delta T_i / \delta W_i$ for each c_i and choose c_m having the lowest value.
- 6) Calculate $\Delta d_{m,max}$ to be $(T_{max} - T_{cstr}) \div (g_m P_m / d_m)$.
- 7) Move c_m away from the point of T_{max} with a suitable distance $\Delta d_m \leq \Delta d_{m,max}$.
- 8) Renew the position and value of T_{max} .
- 9) Move all chiplets simultaneously along the direction of interposer center from the position of T_{max} , and the displacement is $r\%$ of the distance between the position of T_{max} and the interposer center (the default value of r is 1).
- 10) Repeat the above steps iteratively until the temperature meets the thermal threshold, or the chiplet cannot be moved.

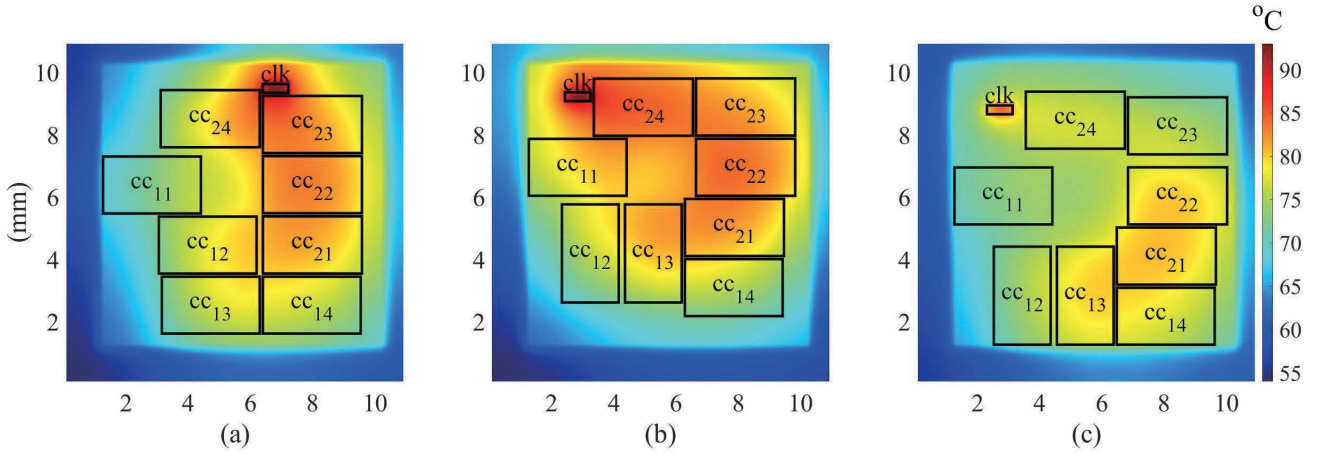


Figure 7: Thermal maps on apte_scaled30. (a) The optimal placement before Post-CP with TWL = 0.40872 m (+0.00%) and maxT = 92.669 °C; (b) The sub-optimal placement before Post-CP with TWL = 0.41076 m (+0.49%) and maxT = 90.308 °C; (c) The sub-optimal placement after Post-CP with TWL = 0.42707 m (+4.48%) and maxT = 84.455 °C.

- 11) If none of placements with increasing TWL $< \eta\%$ is satisfied T_{cstr} , then choose the minimum cost from (4) of those placements.

7 EXPERIMENTAL RESULTS

We implement the proposed framework in C++ language with compiler gcc 8.3.1, and execute it on a Linux workstation with Intel CPU Xeon E5-2620 v4 with eight cores at 2.10 GHz (disabled hyper-threading). Three benchmarks are used from [8, 18] for the experiments. One is interposer-based chiplets cases [7] with four, six, and eight chiplets (t4/t6/t8). Another is from the MCNC benchmark [19] with nine, ten, and eleven chiplets (apte/xerox/hp). The other is the modified MCNC benchmark scaled by [8] for practical 2.5D IC design with scaled interposer size and terminals within whitespace from 5% to 20%.

7.1 Wirelength-driven placement compared to [8]

To demonstrate the performance of SP-CP, we set the minimum gap $w_{space} = 0$ mm which is the same setting as [7, 8]. [7, 8] performed chiplet placement for the optimal TWL, and its B&B with the advanced pruning technique [8] is $10^4\times$ faster than the enumeration-based placer [7] at most. To compare SP-CP with [8], we run its released tool from [18]. In Table 1, for SP-CP with PDSP, the optimized TWL of SP-CP is at most 1.035% better than that of [8]. The better optimized TWL in SP-CP with PDSP results from applying the method in Section 5.2.1. Compared to [8], the speed-up of SP-CP with PDSP can be up to 103.824 \times . Moreover, in the xerox case, we stop searching for the optimal solution after 12 hours for [8], and SP-CP with PDSP obtains the optimal solution by taking 9.72 hours and finds a better placement (−0.430 % in reducing TWL). One reason why we can achieve the speed-up is that partial SP nodes in SP-Tree can be placed while some topology nodes in CSP-Tree [8] can not be packed into a placement. The other reason is that one partial/complete SP in SP-Tree might cover multiple topology nodes in CSP-Tree [8] described in Section 5.1.

For SP-CP with PDSP & A1 presented in Section 5.2.3, it obtains the same optimized TWL of SP-CP with PDSP. Compared with [8], the runtime is accelerated up to 156 \times (in the xerox case, 6.16 hours to obtain the best TWL). It shows that PDSP & A1 can help prune more nodes while obtaining the optimized TWL for all cases.

7.2 Placement with thermal consideration

Since [7, 8] did not handle the constraint of minimum gap w_{space} , we compare placement results with thermal consideration between

“SP-CP” (the framework in Fig. 2 without thermal consideration) and “SP-CP & Post-CP” (the framework in Fig. 2). w_{space} , η , and ϕ are set to 0.1 mm [5], 10, and 0.5, respectively. Because SP-CP cannot obtain the solution for cases (apte_scaled10, apte_scaled5, xerox_scaled10, xerox_scaled5, and all scaled hp cases in Table 1 with $w_{space} = 0.1$ mm) due to the constraint of w_{space} with less whitespace, we build scaled cases for the MCNC benchmark within whitespace 25% and 30%. The power density is assigned randomly from 10^5 to 10^7 W/m² [20] for each chiplet, and T_{cstr} is set to 85 °C [10]. As illustrated in Table 2, with Post-CP in Section 6, the maximum temperature reduction can be up to 8.214 °C. Even two cases (apte_scaled20 and apte_scaled15) cannot meet T_{cstr} , with the minimum cost in (4) of the searched placements in Post-CP, our framework can reduce 3 to 5 °C with increasing wirelength less than 6.7%. Moreover, the average runtime overhead is about 50 seconds, and most of the runtime overhead is to solve the temperatures of chiplets while applying thermal simulation in Section 6.1. Fig. 7 plots the case apte_scaled30 which has the maximum reduced temperature among all the cases. Fig. 7.(a) shows its optimal wirelength solution. Fig. 7.(b) and Fig. 7.(c) are its sub-optimal wirelength placements before and after Post-CP, respectively. It shows different topologies between the optimal placement and sub-optimal placements. And the maximum temperatures of sub-optimal placements are lower. During Post-CP, the chiplet “clk” is moved away from other chiplets, and the whole chiplets move together toward the middle slightly for better thermal performance.

8 CONCLUSION

We have developed an efficient chiplet placer, SP-CP, with sequence pair based tree, advanced placement/pruning techniques, and parallel B&B method for the optimal placement. Moreover, with thermal consideration, we have built Post-CP to reduce the maximum temperatures with maximum allowable increasing wirelength. The results show that SP-CP can speed up at most two orders of magnitude with better TWL (reducing 1.035% HPWL) compared to the prior-art. With Post-CP, the maximum temperature can be reduced to 8.214 °C with an average increase of 5.376% TWL.

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Table 1: Results on wirelength driven placement with $w_{space} = 0$ mm

| Case | Chiplets | Pins | Nets | Terminals | [8] | | SP-CP | | | Comparison | | |
|----------------|----------|--------|-------|-----------|----------|-----------|----------|------------------|-----------------------|---------------|---------------------|--------------------------|
| | | | | | TWL (m) | Time (s) | TWL (m) | w/ PDSP Time (s) | w/ PDSP & A1 Time (s) | TWL Diff. (%) | w/ PDSP Speedup (×) | w/ PDSP & A1 Speedup (×) |
| t4_s | 4 | 15611 | 1808 | 789 | 10.87000 | 0.263 | 10.87000 | 0.127 | 0.123 | 0.000 | 2.071 | 2.138 |
| t4_m | 4 | 91005 | 5326 | 1174 | 38.14000 | 0.577 | 38.14000 | 0.226 | 0.214 | 0.000 | 2.553 | 2.696 |
| t4_b | 4 | 223781 | 12265 | 1033 | 58.92000 | 1.180 | 58.92000 | 0.411 | 0.396 | 0.000 | 2.871 | 2.980 |
| t6_s | 6 | 20138 | 1720 | 639 | 9.01000 | 0.366 | 9.01000 | 0.122 | 0.098 | 0.000 | 3.000 | 4.572 |
| t6_m | 6 | 121935 | 7123 | 1162 | 33.77000 | 1.791 | 33.77000 | 0.439 | 0.392 | 0.000 | 4.080 | 4.572 |
| t6_b | 6 | 229228 | 14264 | 1192 | 62.71000 | 2.470 | 62.71000 | 0.945 | 0.886 | 0.000 | 2.614 | 2.788 |
| t8_s | 8 | 18689 | 1918 | 882 | 23.51000 | 1.341 | 23.51000 | 0.192 | 0.165 | 0.000 | 6.984 | 8.127 |
| t8_m | 8 | 159149 | 8391 | 1391 | 36.39000 | 2.058 | 36.39000 | 0.711 | 0.683 | 0.000 | 2.895 | 3.013 |
| t8_b | 8 | 306057 | 12593 | 1049 | 66.61000 | 12.116 | 66.61000 | 1.094 | 0.933 | 0.000 | 11.075 | 12.986 |
| apte_scaled20 | 9 | 287 | 97 | 73 | 0.37701 | 17.620 | 0.37704 | 9.782 | 8.501 | 0.008 | 1.801 | 2.073 |
| apte_scaled15 | 9 | 287 | 97 | 73 | 0.37320 | 14.087 | 0.37265 | 9.559 | 8.457 | -0.147 | 1.474 | 1.666 |
| apte_scaled10 | 9 | 287 | 97 | 73 | 0.36630 | 12.192 | 0.36551 | 9.430 | 6.963 | -0.216 | 1.293 | 1.751 |
| apte_scaled5 | 9 | 287 | 97 | 73 | 0.37526 | 31.774 | 0.37526 | 6.299 | 5.270 | 0.000 | 5.044 | 6.029 |
| xerox_scaled20 | 10 | 698 | 203 | 2 | 0.36399 | 22881.822 | 0.36398 | 220.391 | 146.051 | -0.003 | 103.824 | 156.670 |
| xerox_scaled15 | 10 | 698 | 203 | 2 | 0.37876 | 4634.995 | 0.37861 | 111.165 | 88.330 | -0.040 | 41.695 | 52.474 |
| xerox_scaled10 | 10 | 698 | 203 | 2 | 0.41998 | 3685.743 | 0.41830 | 101.963 | 65.245 | -0.400 | 36.148 | 56.491 |
| xerox_scaled5 | 10 | 698 | 203 | 2 | 0.43747 | 1853.318 | 0.43747 | 64.173 | 50.623 | 0.000 | 28.880 | 36.610 |
| hp_scaled20 | 11 | 309 | 83 | 45 | 0.14002 | 17.315 | 0.13992 | 10.044 | 9.524 | -0.071 | 1.724 | 1.818 |
| hp_scaled15 | 11 | 309 | 83 | 45 | 0.14342 | 9.649 | 0.14194 | 2.851 | 2.580 | -1.035 | 3.384 | 3.740 |
| hp_scaled10 | 11 | 309 | 83 | 45 | 0.14377 | 5.140 | 0.14295 | 1.729 | 1.641 | -0.570 | 2.974 | 3.132 |
| hp_scaled5 | 11 | 309 | 83 | 45 | 0.16401 | 4718.180 | 0.16401 | 930.729 | 836.377 | 0.000 | 5.069 | 5.641 |
| apte | 9 | 287 | 97 | 73 | 0.43751 | 1397.697 | 0.43751 | 323.930 | 186.660 | 0.000 | 4.315 | 7.488 |
| xerox | 10 | 698 | 203 | 2 | 0.36587 | >12hr | 0.36430 | 34994.700 | 22187.000 | -0.430 | NA | NA |
| hp | 11 | 309 | 83 | 45 | 0.15026 | 14281.288 | 0.15014 | 438.440 | 348.699 | -0.080 | 32.573 | 40.956 |
| Avg. | | | | | | | | | | -0.124 | 13.406 | 18.242 |

Table 2: Results on placement with thermal consideration and $w_{space} = 0.1$ mm

| Case | SP-CP | | | SP-CP & Post-CP | | | | | | |
|----------------|---------|-----------------|----------|-----------------|-----------------|----------|--------------------|---------------------------|----------------------|--|
| | TWL (m) | Max. Temp. (°C) | Time (s) | TWL (m) | Max. Temp. (°C) | Time (s) | Increasing TWL (%) | Max. Temp. Reduction (°C) | Runtime Overhead (s) | |
| apte_scaled30 | 0.40872 | 92.669 | 17.504 | 0.42707 | 84.455 | 75.605 | 4.490 | 8.214 | 58.101 | |
| apte_scaled25 | 0.40213 | 91.889 | 15.803 | 0.43193 | 84.979 | 87.846 | 7.411 | 6.910 | 72.043 | |
| apte_scaled20 | 0.39267 | 99.579 | 9.782 | 0.41887 | 94.562 | 83.610 | 6.672 | 5.017 | 73.828 | |
| apte_scaled15 | 0.41692 | 95.123 | 43.177 | 0.43818 | 91.556 | 88.489 | 5.099 | 3.567 | 45.312 | |
| xerox_scaled30 | 0.40664 | 88.631 | 149.792 | 0.42894 | 83.603 | 184.882 | 5.484 | 5.028 | 35.090 | |
| xerox_scaled25 | 0.42087 | 89.632 | 71.292 | 0.45233 | 84.673 | 187.037 | 7.475 | 4.959 | 115.745 | |
| xerox_scaled20 | 0.48135 | 87.810 | 192.405 | 0.50846 | 84.091 | 220.035 | 5.632 | 3.719 | 27.630 | |
| xerox_scaled15 | 0.51508 | 86.778 | 334.773 | 0.56097 | 84.918 | 344.944 | 8.909 | 1.860 | 10.171 | |
| hp_scaled30 | 0.16144 | 86.284 | 10.252 | 0.16362 | 84.773 | 23.564 | 1.350 | 1.511 | 13.312 | |
| hp_scaled25 | 0.19377 | 85.050 | 265.859 | 0.19617 | 84.584 | 320.769 | 1.239 | 0.466 | 54.910 | |
| Avg. | | | | | | | 5.376 | 4.125 | 50.614 | |

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