Methods in Psycholinguistics — Mixed effects logistic regression —

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Judith Degen
Stanford University

Logistic regression

- for binary (categorical) instead of continuous outcomes
- instead of predicting the mean of an outcome, we're predicting the log odds of an event occurring
- also called "logit model"

What kind of data?

- grammaticality (binary)
- syntactic variation (e.g., dative alternation)
- phonological variation (e.g., t-deletion)
- experimental forced choice or eye-tracking data

Why not ANOVA?

- ANOVA over proportion has several problems (cf. Jaeger, 2008 for a summary)
 - Hard to interpret output
 - Violated assumption of homogeneity of variances

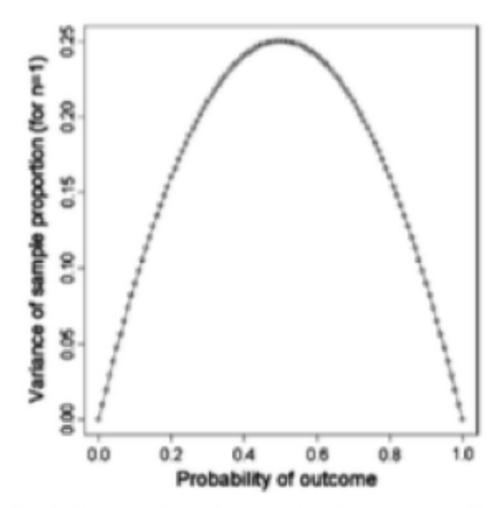


Fig. 1. Variance of sample proportion depending on p (for n = 1).

Why can't we use linear regression for categorical outcomes?

The linear model makes impossible predictions (values of Y > 1 or Y < 0)

The linear model is meaningless if its assumptions are violated

Logistic regression

Recall that **logistic regression** is a kind of **GLM** (with a binomial link function).

• The linear predictor:

$$\eta = \alpha + \beta_1 \mathbf{x_1} + \dots + \beta_n \mathbf{x_n}$$

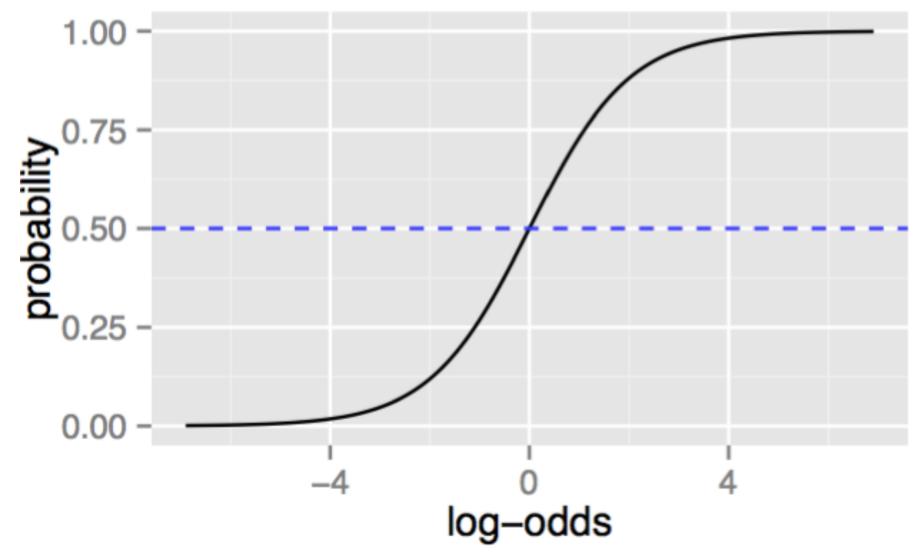
• The link function g is the logit transform:

$$E(\mathbf{y}) = p = g^{-1}(\eta) \Leftrightarrow$$

$$g(p) = \ln \frac{p}{1-p} = \eta = \alpha + \beta_1 \mathbf{x_1} + \dots + \beta_n \mathbf{x_n}$$

The distribution around the mean is taken to be binomial.

Log odds and probability



This relation is particularly clear in the following form of the model:

$$p = \frac{1}{1 + \exp^{-\mathbf{X}\beta}}$$

log odds range from -Inf to +Inf

Mixed effects logistic regression

linear model: mixed linear model::

logit model: mixed logit model

Assumption: individual differences within a grouping factor are normally distributed in log-odds of event

Fixed effects Random effects
$$N(0,\sigma_{b_i})$$

$$\ln(\frac{p}{1-n}) = \mathbf{X}\boldsymbol{\beta} + \mathbf{Z}\boldsymbol{b} , \boldsymbol{b_i}$$

Dative alternation

Realization of recipient:

NP: John gave [the children] [toys]

PP: John gave [toys] [to the children]

What governs the syntactic choice?

Bresnan, J., Cueni, A., Nikitina, T., & Baayen, H. (2007). Predicting the Dative Alternation. In G. Boume, I. Kraemer, & J. Zwarts (Eds.), Cognitive Foundations of Interpretation (pp. 1–33). Amsterdam: Royal Netherlands Academy of Science.

Let's translate it into R!