

S 17

Q1

" Palindrome

w

int minCut (string S){

int len = S.length();

vector &lt;vector&lt;bool&gt;&gt; isPal (len, vector &lt;bool&gt; (len),

for (int i = 0; i &lt; len; ++i)

{ for (int j = 0; j &lt; i; ++j)

{ char ch1 = S[i], ch2 = S[j];

if (ch1 == ch2 &amp;&amp; (i &lt; j+1 || isPal (j+1, i-1)))

{ isPal [j][i] = true;

}

}

cut X

b) for a string with length n

construct a nxn diagonal matrix

the elements in it is more than the first element are set to be 1, others are 0

for example

S = "acaddgeg"

S[1] = 1

S[2] = [0, 0]

S[3] = [1, 1, 1]

S[4] = [1, 1, 1, 0]

S[5] = [1, 1, 1, 1, 1]

S[6] = [1, 1, 1, 1, 1, 0]

S[7] = [1, 1, 1, 1, 1, 0, 1]

	a	c	a	d	d	g	e	g
a	0							
c	1	0						
a	0	0	0					
d	1	1	1	0				
d	1	1	1	0	0			
g	1	1	1	1	1	1	0	
e	1	1	1	1	1	1	0	0
g	1	1	1	1	1	1	0	1

 $O(n^2)$ (4) Precision =  $\frac{TP}{TP+FP}$

IS 17. Q4. (a) step 1: classify in  $C_1 = 1100$ ,  $C_2 = 1600$

$$C_1 = \{0, 200, 300, 900, 1100\} \quad C_2 = \{1600\}$$

step 2: update  $C_1 = 500$ ,  $C_2 = 1600$

step 3: classify in  $C_1 = 500$ ,  $C_2 = 1600$

$$C_1 = \{0, 200, 300, 900\} \quad C_2 = \{1100, 1600\}$$

step 4: update  $C_1 = 350$ ,  $C_2 = 1350$

step 5: classify in  $C_1 = 350$ ,  $C_2 = 1350$

$$C_1 = \{0, 200, 300\} \quad C_2 = \{900, 1100, 1600\}$$

step 6: update  $C_1 = \frac{300}{3}$ ,  $C_2 = 1200$

$$\begin{aligned} \text{(b)} \quad SSE &= (0 - \frac{500}{3})^2 + (200 - \frac{500}{3})^2 + (300 - \frac{500}{3})^2 + (900 - 1200)^2 + (1100 - 1200)^2 + (1600 - 1200)^2 \\ &= 100^2 \times (\frac{25}{9} + \frac{1}{9} + \frac{16}{9} + 9 + 1 + 16) \\ &= \frac{920000}{3} \end{aligned}$$

$$BSS = 3 \times (\frac{500}{3} - \frac{2050}{3})^2 + 3 \times (1200 - \frac{2050}{3})^2 = 3 \times (\frac{1550}{3})^2 \times 2 = \frac{4205000}{3}$$

$$\text{(c)} \quad \text{for } 200: a = \frac{1}{2} \times [\sqrt{(200-0)^2} + \sqrt{(200-300)^2}] = 150$$

$$b = \frac{1}{3} \times [\sqrt{(200-900)^2} + \sqrt{(200-1100)^2} + \sqrt{(200-1600)^2}] = 1000$$

$$S = \frac{b-a}{\max(a,b)} = 1 - \frac{a}{b} = 0.35$$

$$\text{for } 1100: b = \frac{1}{3} \times [\sqrt{(1100-0)^2} + \sqrt{(1100-200)^2} + \sqrt{(1100-300)^2}] = \frac{2600}{3}$$

$$a = \frac{1}{2} \times [\sqrt{(1100-900)^2} + \sqrt{(1100-1600)^2}] = 350$$

$$S = 1 - \frac{a}{b} = 1 - \frac{350}{\frac{2600}{3}} = 0.625$$

(d) step 1: d 0 200 300 900 1100 1600 step 2 0 200 300 900 1100 1600

0	0	200	300	900	1100	1600
200	200	0				
300	300	100	0			
900	900	700	600	0		
1100	1100	900	800	200	0	
1600	1600	1400	1300	700	500	0

0	0					
200	300	300	0			
900	900	700	0			
1100	1100	900	200	0		
1600	1600	1400	700	500	0	

step 3: d 0 200 300 900 1100 1600

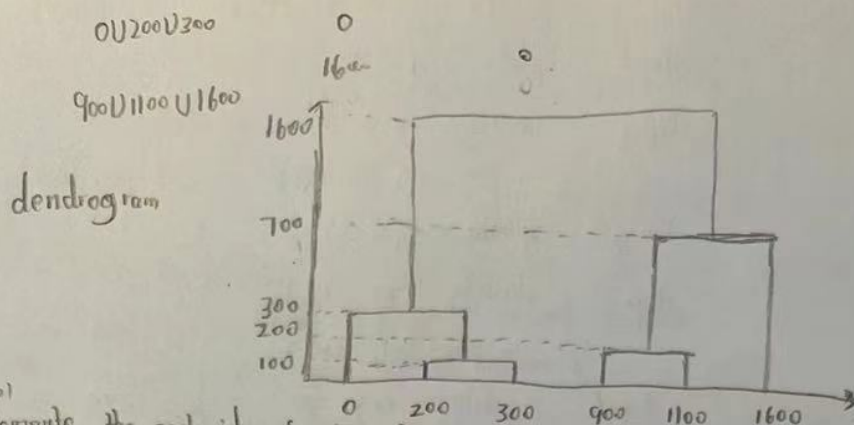
0	0				
200	300	300	0		
900	1100	1100	700	0	
1600	1600	1400	700	0	

step 4: 0 200 300 900 1100 1600

0	200	300			
900	1100	1100	0		
1600	1600	700	0		



step 5: d 0-200 U 300 900 U 1100 U 1600



Q 5. (a) (i) Step 1 Compute the centroids for two classes

$$\mu_1 = \frac{1}{2}(d_1 + d_2) = (0, 0.4975, 0.4975, 0.707, 0)$$

$$\mu_2 = \frac{1}{2}(d_3 + d_4) = (0.5635, 0, 0.7085, 0.274, 0)$$

(2) The boundary between two classes in Rocchio classification is the set of points with equal distance from the two centroids.

The classification of  $d_i$  is determined by the minimum distance between  $d_i$  and all the centroids.

(3) For the multimodal classification problem, Rocchio classification cannot classify properly as the following example.



For class 1 with the label "o", it is grouped by two clusters, the test data should be classified in "o", but the centroid of two clusters is far from "o" and "o" will be mis-classified in cluster "x".

- (b) (i) true positive (TP): a sample with actual label "1" is classified in "1"  
 false positive (FP): a sample with actual label "0" is classified in "1"  
 false negative (FN): a sample with actual label "1" is classified in "0"  
 true negative (TN): a sample with actual label "0" is classified in "0"

(2) Accuracy =  $\frac{TP + TN}{TP + TN + FN + FP}$

(3)

sample	$x_1$	$x_2$	$x_3$	$x_4$	$x_5$	$x_6$	$x_7$	$x_8$	$x_9$	$x_{10}$
label	1	1	1	1	1	0	0	1	1	1
prediction	1	1	1	1	1	1	1	1	1	1

Accuracy = 80%, but such a classifier may predict all the samples to be "1", while FPR is 100%. If we have many samples with label "0", the performance will be bad.

(4) Precision =  $\frac{TP}{TP + FP}$  Recall =  $\frac{TP}{TP + FN}$

Using concepts in IR  
 Retrieved!!!

15)	Relevant	Non-relevant
Retrieved	1	9
Not Retrieved	0	990

the number of true relevant is 1

$$Acc = \frac{1+990}{1000} = 0.991 \quad Recall = 100\%$$

$$Precision = 10\%$$

in such a system, to improve the performance,  
we prefer the precision to recall

Q.2: (a) a) "mutex": ensure that the producer can't add data into full buffer and consumer can't remove data from an empty buffer (enforce mutual exclusion)

"empty" is used to keep track of the number of empty space

"full" is used to keep track of the number of items in the buffer

(2) "Producer Process" line 8  $\xrightarrow{\text{signal (mutex)}}$   $\rightarrow \text{signal (empty)} \times \rightarrow \text{signal (full)}$

1b) The system spends most of its time swapping pieces rather than executing instructions

Stop the process, Increase the memory

(c)	1	2	3	4	5	3	4	1	6	7	8	7	8	9	7	8	9	5	4	5	4	2
	1	1	1	4	4	4	4	4	4	7	7	7	7	7	7	7	7	5	5	5	5	5
		2	2	2	5	5	5	1	1	1	8	8	8	8	8	8	8	8	4	4	4	4
			3	3	3	3	3	3	6	6	6	6	9	9	9	9	9	9	9	9	2	
	F	F	F	F	F			F	F	F	F			F				F	F		F	

# page faults = 13

Q3: (a) # CUSTOMER  $\bowtie$  RENTAL = 20000

# CUSTOMER  $\bowtie$  VEHICLE =  $5000 \times 1000$   
= 5000000

(b)  $B_c = \frac{5000}{100} = 50$

$b_R = \frac{20000}{50} = 400$

CUSTOMER as outer relation cost =  $\lceil \frac{50}{4-2} \rceil \times 400 + 50$  block transfers  
+  $2 \times \lceil \frac{50}{4-2} \rceil$  seeks

= 10050 block transfers + 50 seeks

RENTAL cost =  $\lceil \frac{400}{4-2} \rceil \times 50 + 400$  block transfers +  $2 \times \lceil \frac{400}{4-2} \rceil$  seeks

= 40050 block transfers + 400 seeks

(c) cost =  $b_r + n_r(h_r) = 50 + 5000 \times (13 \text{ ti}) = 20050$