

$\text{fact}(\text{fact}(n))$

利用函数替换

等价替换

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外提

规约参数

这就是Y-Combinator

const $Y \Rightarrow \lambda e \Rightarrow (f \Rightarrow f(f)) (g \Rightarrow \lambda e \Rightarrow g(g)(x))$;


```
const Y = le => (f => f(f))(g => le(x => g(g)(x)));  
const fact = Y(fact => n => n < 2 ? 1 : n * fact(n - 1));  
fact(5);
```

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$$= \left(f = f \right) \left(\text{fact} \right) \left(n \right)$$

$\Rightarrow (f \Rightarrow f(f)) ((\neg \Rightarrow f \Rightarrow \neg (x \Rightarrow f(f(x))) (P)) (n) ;$

$$\Rightarrow (p \Rightarrow (f \Rightarrow f)) (\neg \Rightarrow f \Rightarrow \neg (x \Rightarrow f) (x)) (p) (P) (n);$$

$$= \lambda (p \Rightarrow (f \Rightarrow f) (f \Rightarrow f) (x \Rightarrow f) (f) (x)) (P) (n) ;$$

fact(fact)(n)

利用函数替换

=> (f => f(f))(fact)(n)

等价替换

=> (f => f(f))((l => f => l(x => f(f)(x)))(P))(n);

外提

=> (p => (f => f(f))((l => f => l(x => f(f)(x)))(p)))(P)(n);

规约参数

=> (p => (f => f(f))(f => p(x => f(f)(x))))(P)(n);

这就是**Y-Combinator**

const Y = le => (f => f(f))(g => le(x => g(g)(x)));

```
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函数式编程的数学理论——λ演算

