CS 577 – Introduction to Algorithms

Solving Recurrences Review

Q1) Solve the following recurrences -

1.
$$T(n) = T(n-1) + O(1)$$

2.
$$T(n) = T(n-1) + O(n)$$

3.
$$T(n) = T(n/2) + O(1)$$

4.
$$T(n) = T(n/2) + O(n)$$

5.
$$T(n) = 2T(n/2) + O(n)$$

6.
$$T(n) = T(n-1) + T(n-2) + O(1)$$

7.
$$T(n) = T(n-1) + 2^n$$
 and $T(0) = 1$

8.
$$T(n) = 4T(n/2) + n^2$$

9.
$$T(n) = T(n/3) + T(2n/3) + O(n)$$

10.
$$T(n) = 2T(n/3) + 2T(2n/3) + O(n)$$

11.
$$T(n) = T(n/2) + T(n/4) + T(n/8) + n$$

12.
$$T(n) = 3T(n/2) + n$$

13.
$$T(n) = 3T(n/4) + n^2$$

14.
$$T(n) = 3T(n/3) + n^3$$
 and $T(1) = 0$

Q2) Come up with your own recurrences and try to solve them!