

Question 1: Find the total number of primitive operations and the Big Oh notation of the following methods:

	Statements	S/E	Freq.	Total
1	for (int i = 0; i < n-5; i++)	1	n-4	n-4
2	for (int j = n; j >= 2; j--)	1	n(n-5)	n ² -5n
3	S.O.P(i);	1	(n-5)(n-1)	n ² -6n+5
	Total Operations		$n^2 - 10n + 1$	
	Big Oh		$O(n^2)$	

	Statements	S/E	Freq.	Total
1	for (int i = 0; i < n; i++)	1	n+1	n+1
2	for (int j = 0; j <= i; j++)	1	$\frac{n^2}{2} + \frac{3n}{2}$	$\frac{n^2}{2} + \frac{3n}{2}$
3	S.O.P(i);	1	$\frac{n^2}{2} + \frac{n}{2}$	$\frac{n^2}{2} + \frac{n}{2}$
	Total Operations		$n^2 + 3n + 1$	
	Big Oh		$O(n^2)$	

Line 2:

$$\begin{aligned}
 \sum_{i=0}^{n-1} i + 2 &= \sum_{i=0}^{n-1} i + \sum_{i=0}^{n-1} 2 \\
 &= \frac{n-1(n-1+1)}{2} + 2n \\
 &= \frac{n^2-n}{2} + \frac{4n}{2} \\
 &= \frac{n^2}{2} + \frac{3n}{2}
 \end{aligned}$$

Line 3:

$$\begin{aligned}
 \sum_{i=0}^{n-1} i + 1 &= \sum_{i=0}^{n-1} i + \sum_{i=0}^{n-1} 1 \\
 &= \frac{n-1(n-1+1)}{2} + n \\
 &= \frac{n^2-n}{2} + \frac{2n}{2} \\
 &= \frac{n^2}{2} + \frac{n}{2}
 \end{aligned}$$

Question 2: Find the simplest $g(n)$, c and n_0 for the following $f(n)$ s.t: $f(n) \leq cg(n)$, $\forall n \geq n_0$.

$$\begin{aligned}
 5n^3 \log n + 20n^2 - 4n + 3 &\leq 5n^3 \log n + 20n^3 \log n + 3n^3 \log n \\
 &\leq 28n^3 \log n
 \end{aligned}$$

$$C = 28$$

$$g(n) = n^3 \log n$$

$$n_0 = 2$$

Question 3: Find the Big Oh notation for the following functions:

$$\begin{aligned}
 &2^{4\log n + 2} + n^3 \log n \\
 &= 2^{4\log n} * 2^2 + n^3 \log n \\
 &= n^4 * 4 + n^3 \log n \\
 &= 4n^4 + n^3 \log n \\
 &O(n^4)
 \end{aligned}$$