



King Saud University

College of Computer and Information Sciences

Department of Computer Science

Data Structures CSC 212

Final Exam - Fall 2017

Date: 30/12/2017

Duration: 3 hours

Guidelines

- No calculators or any other electronic devices are allowed in this exam.
- Use a pencil in choice questions.

Student ID:

Name:

Section:

Instructor:

1	2.1	2.2	3.1	3.2	4	5	6	7	8	Total

Question 1 16 points

(a) Choose the correct frequency for every line as well as the total O of the following code:

```
1 sum = 1;
2 for (i = 1; i <= n; i++) {
3     sum+= i;
4     for (j = i; j >= 2; j--)
5         sum--;}

```

- Line 1: (A) 1 (B) 2 (C) 3 (D) n (E) $2n$
- Line 2: (A) n (B) $n + 1$ (C) $n - 1$ (D) $n + 2$ (E) $n - 2$
- Line 3: (A) n (B) $n + 1$ (C) $n - 1$ (D) $n + 2$ (E) $n - 2$
- Line 4: (A) n^2 (B) $n(n - 1)/2$ (C) $(2n + 1)/2$ (D) $(2n - 1)/2$ (E) $n(n + 1)/2$
- Line 5: (A) n^2 (B) $n(n - 1)/2$ (C) $(2n + 1)/2$ (D) $(2n - 1)/2$ (E) $n(n + 1)/2$
- Total O : (A) 1 (B) n (C) n^2 (D) $n \log(n)$ (E) n^3

(b) Choose the correct frequency for every line as well as the total O of the following code:

```
1 count = 0;
2 for (i = 1; i < n+1; i++)
3     count ++;
4 for (j = 0; j <= count; j++)
5     k = j+1;

```

- Line 1: (A) 0 (B) 1 (C) 2 (D) n (E) n^2
- Line 2: (A) n (B) $n + 1$ (C) $n - 1$ (D) $n + 2$ (E) $n - 2$
- Line 3: (A) n (B) $n + 1$ (C) $n - 1$ (D) $n + 2$ (E) $n - 2$
- Line 4: (A) $count + 2$ (B) $n + 1$ (C) $n - 1$ (D) $n + 2$ (E) $n(n + 1)/2$
- Line 5: (A) $count + 1$ (B) $n + 1$ (C) $n - 1$ (D) $n + 2$ (E) $n(n - 1)/2$
- Total O : (A) 1 (B) n (C) n^2 (D) $n \log(n)$ (E) n^3

(b) Consider a stack of decreasing time intervals, that is, starting from the top, each interval contains the next. Write the method `public static Pair<Integer, Integer> smallest(Stack<Pair<Integer, Integer>> st, int t)`, which returns the smallest interval containing `t` if it exists, `null` otherwise. Assume that all intervals in `st` are valid (that is `first <= second`).

Example 0.1. If $st : \{[0, 8], [1, 6], [1, 5], [2, 4]\}$, then $smallest(st, 1)$ returns $[1, 5]$, $smallest(st, 3)$ returns $[2, 4]$, $smallest(st, 9)$ returns `null`.

Complete the code below by choosing the correct answer:

1 public static Pair<Integer, Integer>smallest(Stack<Pair<Integer, Integer>> st, int t){
2 ...
3 Pair<Integer, Integer> itm = null;
4 while (!st.empty()) {
5 Pair<Integer, Integer> it = st.pop();
6 ...
7 if (...)
8 itm = it;
9 else
10 ...
11 }
12 while (...) {
13 ...
14 }
15 return itm; }

1. Line 2:

(A) Queue<Pair<Integer, Integer>> r = new
LinkedQueue<Pair<Integer, Integer>>();

(B) Stack<Integer> r = new LinkedStack<
Integer>();

(C) List<Pair<Integer, Integer>> r = new
LinkedList<Pair<Integer, Integer>>();

(D) Stack<Pair<Integer, Integer>> r = new
LinkedStack<Pair<Integer, Integer>>();

(E) None

2. Line 6:

(A) r.push(it.first);

(B) r.insert(it);

(C) r.enqueue(it);

(D) r.push(it);

(E) None

3. Line 7:

(A) if (it.first < t && t <= it.second)

(B) if (it.first <= t && t <= it.second)

(C) if (it.first < t || it.second > t)

(D) if (it.first <= t && it.second <= t)

(E) None

4. Line 10:

(A) r.serve();

(B) break;

(C) r.pop();

(D) r.findNext();

(E) None

5. Line 12:

(A) while (r.empty()){

(B) while (!r.empty()){

(C) while (r.pop() != null){

(D) while (r.length() != 0){

(E) None

6. Line 13:

(A) st.push(r.pop());

(B) st.push(r.serve());

(C) st.push(r.retrieve()); r.findNext();

(D) st.push(r.push());

(E) None

Question 3..... 10 points

- (a) The method `private BTNode<T> mirrorCopy(BTNode<T> t)` creates **recursively** a mirror copy of the subtree `t`. Choose the correct option to complete the code of this method:

```
1 private BTNode<T> mirrorCopy(BTNode<T> t) {
2     ...
3     ...
4     ...
5     ...
6     ...
7     ...
8 }
```

- | | |
|--|---|
| <p>1. Line 2:</p> <ul style="list-style-type: none"><input type="radio"/> (A) if (t.left == null t.right == null)<input type="radio"/> (B) if (t.left == null && t.right == null)<input type="radio"/> (C) if (t == null)<input type="radio"/> (D) if (root != null)<input type="radio"/> (E) None <p>2. Line 3:</p> <ul style="list-style-type: none"><input type="radio"/> (A) return null;<input type="radio"/> (B) return root;<input type="radio"/> (C) return mirrorCopy(root);<input type="radio"/> (D) return mirrorCopy(t);<input type="radio"/> (E) None <p>3. Line 4:</p> <ul style="list-style-type: none"><input type="radio"/> (A) BTNode<T> p = new BTNode<T>(t.data);<input type="radio"/> (B) BTNode<T> p = new BTNode<T>(root);<input type="radio"/> (C) BTNode<T> p = new BTNode<T>(t);<input type="radio"/> (D) BTNode<T> p = new BTNode<T>(root.data);<input type="radio"/> (E) None | <p>4. Line 5:</p> <ul style="list-style-type: none"><input type="radio"/> (A) p.right = mirrorCopy(t.left);<input type="radio"/> (B) t.left = mirrorCopy(t.left);<input type="radio"/> (C) p.right = mirrorCopy(t.right);<input type="radio"/> (D) t.left = mirrorCopy(t.right);<input type="radio"/> (E) None <p>5. Line 6:</p> <ul style="list-style-type: none"><input type="radio"/> (A) t.right = mirrorCopy(t.left);<input type="radio"/> (B) p.left = mirrorCopy(t.left);<input type="radio"/> (C) p.left = mirrorCopy(t.right);<input type="radio"/> (D) t.right = mirrorCopy(t.right);<input type="radio"/> (E) None <p>6. Line 7:</p> <ul style="list-style-type: none"><input type="radio"/> (A) return p;<input type="radio"/> (B) return mirrorCopy(t);<input type="radio"/> (C) mirrorCopy(t.left); mirrorCopy(t.right);<input type="radio"/> (D) return t;<input type="radio"/> (E) None |
|--|---|

- (b) Consider the function `f` below, member of `DoubleLinkedList`:

```
public void f(int n) {
    Node<T> p = head; Node<T> q = null;
    for (int i = 0; i < n; i++) {
        q = p;
        p = p.next;
    }
    if (p != null) {
        p.previous = null;
        while (p.next != null)
            p = p.next;
        p.next = head;
        head = q.next;
        q.next = null;
    }
}
```

Choose the correct result in each of the following cases:

- 1. The list 1: A, B, C, D, E , after calling $1.f(2)$, 1 becomes:
☐ (A) A, B ☐ (B) D, E, A, B, C ☐ (C) C, D, E, A, B ☐ (D) A, D, E, B, C ☐ (E) None
- 2. The list 1: A, B, C, D, E , after calling $1.f(0)$, 1 becomes:
☐ (A) *empty* ☐ (B) A, B, C, D, E ☐ (C) B, C, D, E, A ☐ (D) B, C, D, E ☐ (E) None
- 3. The list 1: A, B, C, D, E , after calling $1.f(5)$, 1 becomes:
☐ (A) *empty* ☐ (B) A, B, C, D, E ☐ (C) E, D, C, B, A ☐ (D) A, D, E, B, C ☐ (E) None
- 4. The list 1: A, B, C, D, E , after calling $1.f(1)$, 1 becomes:
☐ (A) A ☐ (B) E, A, B, C, D ☐ (C) C, D, E, A, B ☐ (D) B, C, D, E, A ☐ (E) None

Question 4..... 14 points

- (a) Consider the following heap represented as an array: 3, 7, 9, 13, 8, 11. Choose the correct answer for every operation (all operations are done on the above heap).
- 1. Heap after inserting 5:
☐ (A) 3,7,9,13,8,11,5 ☐ (B) 3,5,7,13,8,11,9 ☐ (C) 3,7,9,13,8,5,11 ☐ (D) 5,7,3,13,8,11,9 ☐ (E) None
 - 2. Heap after inserting 10:
☐ (A) 3,7,10,13,8,11,9 ☐ (B) 3,7,9,13,8,10,11 ☐ (C) 3,7,9,13,8,11,10 ☐ (D) 3,7,9,10,8,11,13 ☐ (E) None
 - 3. Heap after inserting 2:
☐ (A) 3,7,9,13,8,11,2 ☐ (B) 3,7,2,13,8,11,9 ☐ (C) 2,7,3,13,8,9,11 ☐ (D) 2,7,3,13,8,11,9 ☐ (E) None
 - 4. Heap after deleting one key:
☐ (A) 7,13,9,11,8 ☐ (B) 7,8,9,13,11 ☐ (C) 9,7,11,13,8 ☐ (D) 7,9,8,11,13 ☐ (E) None
 - 5. Heap after deleting two keys:
☐ (A) 7,13,9,11 ☐ (B) 8,11,9,13 ☐ (C) 7,8,9,13 ☐ (D) 13,9,8,11 ☐ (E) None
- (b) What is the result of a bottom-up min-heap construction of the following array: 2,4,6,3,5,1?
- ☐ (A) 1,2,3,5,4,6 ☐ (B) 2,1,3,4,5,6 ☐ (C) 1,3,2,4,5,6 ☐ (D) 1,3,2,5,6,4 ☐ (E) None.
- (c) Choose the correct answer:
- 1. What is the height of a heap of size k ?
☐ (A) $\log \log k$ ☐ (B) $k/2$ ☐ (C) $k \log k$ ☐ (D) $\log k$ ☐ (E) None.
 - 2. Bottom-up heap construction is:
☐ (A) $O(n)$ ☐ (B) $O(\log n)$ ☐ (C) $O(n \log n)$ ☐ (D) $O(n^2)$ ☐ (E) None.
 - 3. The enqueue operation in a heap priority queue is:
☐ (A) $O(1)$ ☐ (B) $O(\log n)$ ☐ (C) $O(n)$ ☐ (D) $O(n \log n)$ ☐ (E) None.

Question 5..... 14 points

Choose the correct result in each of the following cases:

1. After inserting the key 7 in the AVL

5

3

8

6

9

7

6

3

8

5

7

9

6

5

8

3

7

9

8

3

5

6

7

9

None

2. After inserting the key 11 in the AVL

8

4

12

6

10

11

8

4

10

6

11

12

10

6

12

4

8

11

8

4

10

6

11

12

None

3. After inserting the key 7 in the AVL

5

4

6

7

8

9

8

5

9

4

6

7

6

5

8

4

7

9

6

4

8

5

7

9

None

4. After deleting the key 8 from the AVL

6

5

9

4

6

4

9

5

9

5

6

4

5

4

9

6

None

5. After deleting the key 10 from the AVL

4

2

8

3

6

11

6

3

8

2

4

11

6

3

11

2

4

8

4

3

8

2

6

11

None

6. After deleting the key 1 from the AVL

3

1

6

2

5

7

4

3

2

6

1

5

7

4

3

1

6

2

5

7

4

3

2

6

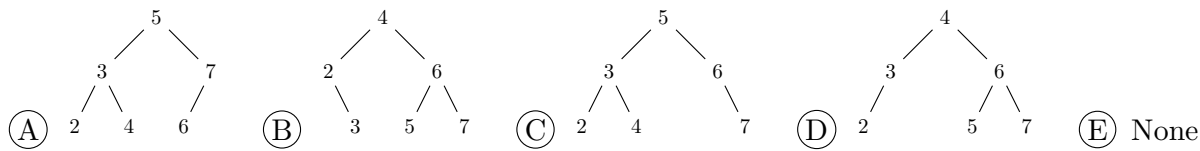
1

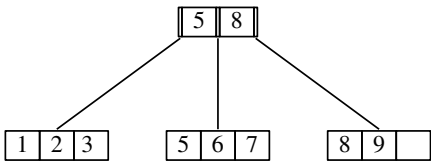
5

7

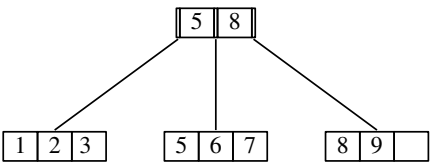
4

None

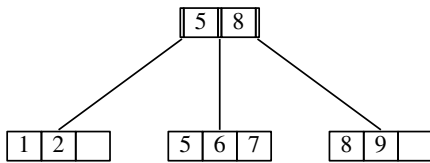




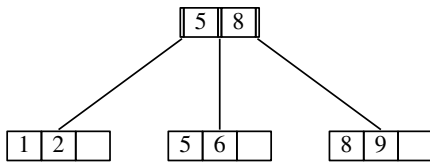
2. After inserting the key 4 in the B+ tree , the **root** of the tree becomes:
- (A) [4, 7] (B) [5, 8] (C) [6,] (D) [8,] (E) None



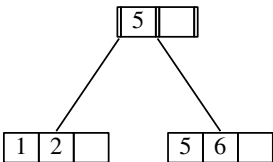
3. After inserting the key 10 in the B+ tree , the **root** of the tree becomes:
- (A) [5, 10] (B) [5, 8] (C) [6,] (D) [6, 10] (E) None



4. After deleting the key 2 from the B+ tree , the **root** of the tree becomes:
- (A) [8,] (B) [5, 8] (C) [6,] (D) [6, 7] (E) None



5. After deleting the key 5 from the B+ tree , the **root** of the tree becomes:
- (A) [8,] (B) [5, 8] (C) [6,] (D) [2,] (E) None

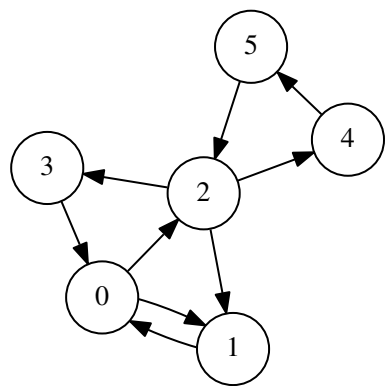


6. After deleting the key 5 from the B+ tree , the **root** of the tree becomes:
- (A) [1, 2,] (B) [1, 2, 6] (C) [6,] (D) [2,] (E) None

7. A B+ tree of order 3 containing n keys has a height that is:
- (A) $O(n)$ (B) $O(n/3)$ (C) $O(n^3)$ (D) $O(\log n)$ (E) None

Question 8 8 points

Consider the following graph.



1. Give the adjacency matrix of the graph.

.....

.....

.....

.....

.....

.....

.....

2. Give the adjacency list representation of the graph.

.....

.....

.....

.....

.....

.....

3. What is the number of edges in the subgraph containing the nodes {1, 2, 3}.

.....

4. What is the maximum number of edges in a directed graph with n nodes (loops, edges from a node to itself, are not allowed)?

.....

ADT Queue Specification

- enqueue (Type e): **requires:** Queue Q is not full. **input:** Type e. **results:** Element e is added to the queue at its tail. **output:** none.
- serve (Type e): **requires:** Queue Q is not empty. **input:** none. **results:** the element at the head of Q is removed and its value assigned to e. **output:** Type e.
- length (int length): **requires:** none. **input:** none. **results:** The number of elements in the Queue Q is returned. **output:** length.
- full (boolean flag): **requires:** none. **input:** none. **results:** If Q is full then flag is set to true, otherwise flag is set to false. **output:** flag.

ADT Stack Specification

- push(Type e): **requires:** Stack S is not full. **input:** Type e. **results:** Element e is added to the stack as its most recently added elements. **output:** none.
- pop(Type e): **requires:** Stack S is not empty. **input:** none. **results:** the most recently arrived element in S is removed and its value assigned to e. **output:** Type e.
- empty(boolean flag): **requires:** none. **input:** none. **results:** If Stack S is empty then flag is true, otherwise false. **output:** flag.
- full(boolean flag): **requires:** none. **input:** none. **results:** If S is full then Full is true, otherwise Full is false. **output:** flag.