

Question 4. (15 marks)

Use the hash function $H(\text{key}) = \text{key} \bmod 10$ to store the sequence of integers: 4371, 1323, 6173, 4199, 4344, 9679, 1989 in a hash table of TableSize = 10. Show the resulting hash table when using:

- (a) Linear rehashing
- (b) External chaining
- (c) Coalesced chaining with cellar size of five and hash function $H(\text{key}) = \text{key} \bmod 5$.

(a) Using Linear rehashing:

Insert Key 4371 : $H(4371) = 4371 \bmod 10 = 1$ Probes = 1

E	4371	E	E	E	E	E	E	E	E
0	1	2	3	4	5	6	7	8	9

Insert Key 1323 : $H(1323) = 1323 \bmod 10 = 3$ Probes = 1

E	4371	E	1323	E	E	E	E	E	E
0	1	2	3	4	5	6	7	8	9

Insert Key 6173 : $H(6173) = 6173 \bmod 10 = 3$ Collision in index 3.

Rehash = $p + c \bmod \text{tableSize} = 3 + 1 \bmod 10 = 4$. Probes = 2

E	4371	E	1323	6173	E	E	E	E	E
0	1	2	3	4	5	6	7	8	9

Insert Key 4199 : $H(4199) = 4199 \bmod 10 = 9$. Probes = 1

E	4371	E	1323	6173	E	E	E	E	4199
0	1	2	3	4	5	6	7	8	9

Insert Key 4344 : $H(4344) = 4344 \bmod 10 = 4$ Collision in index 4.

Rehash = $p + c \bmod \text{tableSize} = 4 + 1 \bmod 10 = 5$. Probes = 2

E	4371	E	1323	6173	4344	E	E	E	4199
0	1	2	3	4	5	6	7	8	9

Insert Key 9679 : $H(9679) = 9679 \bmod 10 = 9$ Collision in index 9.

Rehash = $p + c \bmod \text{tableSize} = 9 + 1 \bmod 10 = 0$. Probes = 2

9679	4371	E	1323	6173	4344	E	E	E	4199
0	1	2	3	4	5	6	7	8	9

Insert Key 1989 : $H(1989) = 1989 \bmod 10 = 9$ Collision in index 9.

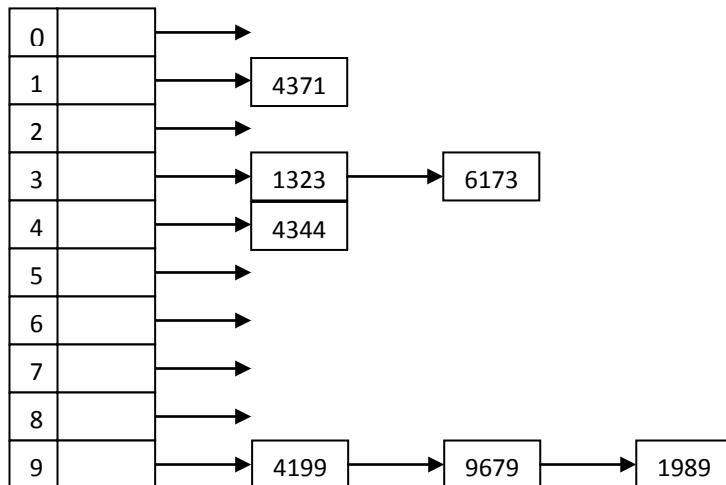
Rehash = $p + c \bmod \text{tableSize} = 9 + 1 \bmod 10 = 0$ Collision in index 0.

Rehash = $p + c \bmod \text{tableSize} = 0 + 1 \bmod 10 = 1$ Collision in index 1.

Rehash = $p + c \bmod \text{tableSize} = 1 + 1 \bmod 10 = 2$. **Probes = 4**

9679	4371	1989	1323	6173	4344	E	E	E	4199
0	1	2	3	4	5	6	7	8	9

(b) Using External chaining rehashing:



(c) Coalesced chaining with cellular size of five and hash function $H(\text{key}) = \text{key} \bmod 5$.

