

$$(1.55)^{\frac{1}{2}} = \sum_{k=0}^{\infty} \binom{\frac{1}{2}}{k} 0.55^k$$

$$\begin{aligned} \left(\frac{1}{2}\right) 0.55^0 &+ \left(\frac{1}{2}\right) 0.55^1 + \left(\frac{1}{2}\right) 0.55^2 \\ \downarrow &+ 0.275 \quad \frac{\left(\frac{1}{2}\right)\left(-\frac{1}{2}\right)}{2} \times 0.55^2 \\ & \quad \quad \quad \times 0.3025 \\ & \quad \quad \quad -0.0378 \end{aligned}$$

$$\begin{aligned} \left(\frac{1}{2}\right) 0.55^3 \\ \downarrow \\ \frac{\left(\frac{1}{2}\right)\left(-\frac{1}{2}\right)\left(-\frac{3}{2}\right)}{6} \times 0.55^3 \\ 0.003466146 \end{aligned}$$

$$\begin{aligned} \left(\frac{1}{2}\right) 0.55^4 \\ \downarrow \\ \frac{\left(\frac{1}{2}\right)\left(-\frac{1}{2}\right)\left(-\frac{3}{2}\right)\left(-\frac{5}{2}\right)}{24} \times 0.55^4 \\ -0.002859570 \end{aligned}$$

$$\begin{aligned} \left(\frac{1}{2}\right) 0.55^5 \\ \downarrow \\ \frac{\left(\frac{1}{2}\right)\left(-\frac{1}{2}\right)\left(-\frac{3}{2}\right)\left(-\frac{5}{2}\right)\left(-\frac{7}{2}\right)}{120} \times 0.55^5 \\ 0.003931909 \end{aligned}$$

$$\begin{aligned} &0.003931909 \\ &= 1.241738485 \end{aligned}$$

$$\sqrt{3} = \frac{p}{q}$$

$$p = \sqrt{3} q$$

$$p^2 = 3q^2 \rightarrow \textcircled{1}$$

$$\frac{p^2}{3} = q^2$$

3 is a factor of p

$$p = 3c$$

c is constant

~~$$p = 3c$$~~

$$3c^2 = 3q^2$$

$$9c^2 = 3q^2$$

$$3c^2 = q^2 \rightarrow c^2 = \frac{q^2}{3}$$

\therefore 3 is also a factor of q.

contradiction

then $\sqrt{3}$ is irrational

$$\frac{15}{10} = 1.5$$

$$\frac{21}{15} = 1.4$$

$$\frac{29}{21} = 1.38$$

k	1	2	3
1	1	1	1

~~$$a_{50} = 10 + 5(4) + 1(2) + 1(3)$$~~

~~$$a_{50} = 28$$~~

~~$$10 + 15 + 21 + 29 + 40$$~~

~~$$5 + 6 + 8 + 11$$~~

~~$$1 + 2 + 3$$~~

~~$$1 + 1$$~~

$$a_{50} = 10 \binom{50}{0} + 5 \binom{50}{1} + 1 \binom{50}{2} + 1 \binom{50}{3}$$

$$a_{50} = 10 \binom{50}{0} + 5 \binom{50}{1} + 1 \binom{50}{2} + 1 \binom{50}{3}$$

$$= 21085$$

Second Principle
 $P(1), P(2), \dots, P(n)$
 that one number ≥ 8 can be divided
 by 7 only
 Case (n=2)
 $7+5=12$
 for all numbers ≥ 8 to be
 for 7 only

3 (never = 14) mod 19

$$4x^2 = 3 \pmod{19}$$

$$19 = 4 \times 4 + 3$$

$$4 = 1 \times 3 + \boxed{1} \quad g=d$$

$$3 = 3 \times 1 + 0$$

$$1 = 4 - 1 \times 3$$

~~$$2 \times 4 - 1 \times 3$$~~

~~$$2 \times 4 - 1 \times 3$$~~

$$= 4(19 - 4 \times 4)$$

$$4 \times 19 - 16 \times 4$$

$$x^2 = 3(-16) \pmod{19}$$

$$= -48 \pmod{19}$$

$$\equiv 9 \pmod{19}$$

$$x = 3 \quad x = 16$$

x	x^2	$x^2 \pmod{19}$
1	1	1
2	4	4
3	9	$\boxed{9}$
4	16	16
5	25	6
6	36	17
7	49	11
8	64	
9	81	
10	100	
11	121	
12	144	
13	169	
14	196	
15	225	
16	256	
17	289	
18	324	