

# KING SAUD UNIVERSITY

COLLEGE OF COMPUTER & INFORMATION SCIENCES

DEPT OF COMPUTER SCIENCE

CSC281 Discrete Mathematics for CS Students

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## Practice Questions (Final)

1. The car plate board in Saudi Arabia has the form: A #, where # is any number 1 to 9999, and A is a three letter in the range A-Z. How many car plate boards can you have?
2. Find the coefficient of the smallest and largest power of  $x$  in the expansion of  $(3x + 2x^2 + 4/x)^{100}$ .
3. How many base 3 strings of length 10 that starts with 000, or 222?
4. How many positive integers between 25 and 134 that are divisible by 4 and by 6 at the same time?
5. English alphabet has 21 consonants and 5 vowels. How many strings of length 6 of lowercase letters that has no vowels? Exactly 2 vowels? At least 2 vowels?
6. Solve the recurrence relation:  $a_n = 3a_{n-1} + 2a_{n-2}$  with initial conditions  $a_0 = 0$ ,  $a_1 = 5$ .
7. Convert the number 123 (in base 6) to a number in base 9.
8. Write the sequence generated by the GF  $\frac{1+x+x^2}{(1-x)^2}$ .
9. Derive the recurrence relation to count the number of bit strings of length  $n$  that has the pattern 101.
10. Prove using induction that for all  $n \geq 1$ ,

$$\sum_{k=1}^n \frac{1}{k(k+1)} = \frac{n}{n+1}.$$