General Trees & Binary Trees

CSC212: Data Structures

Trees

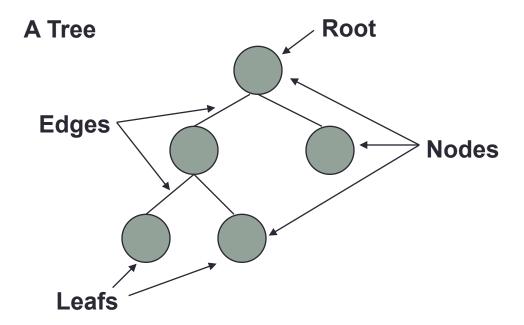
- Previous data structures (e.g. lists, stacks, queues) have a linear structure.
- Linear structures represent one-to-one relation between data elements.
- Trees have a nested or a hierarchical structure.
- Hierarchical structures represent one-tomany relation between data elements.

Trees

- Examples of situations were one-to-many relations exist... these can be represented as trees.
 - Relation between a parent and his children.
 - Relation between a person and books he owns.
 - Relation between a football team and the players on the team.
 - Card catalog in a library.

Trees: Some Terminology

 A tree is represented as a set of <u>nodes</u> connected by <u>edges</u>.



Trees: Comparison with Lists

A List

- Unique <u>first</u> element.
- Unique <u>last</u> element.
- Each element, other than the first and the last, has a unique predecessor and a unique successor.

A Tree

- Unique first node called root.
- Each node has successors, called its children.
- Each node has one predecessor, called parent.
- Leafs have no children.
- Root has no parent.

Trees: More Terminology

Simple path: a sequence of distinct nodes in the tree.

Path length: number of nodes in a path.

Siblings: two nodes that have the same parent.

• Ancestors: given a node A in a tree, the parent of the node A and the ancestors of the parent of A, are ancestors of A.

Trees: More Terminology

Parent: a parent of a node is its predecessor.

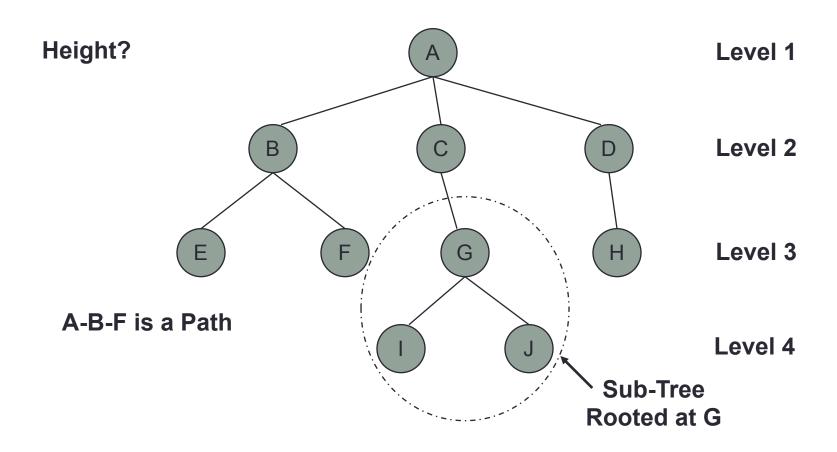
Child: a child of a node is its successor.

Root: a unique node without any predecessor.

Leafs: nodes without any children.

Descendents: given a node A in a tree, the children of A and all descendents of the children of A are descendents of A.

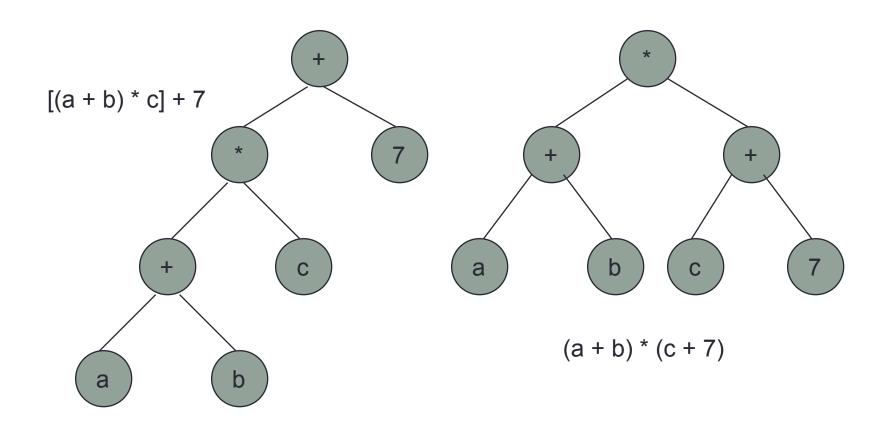
Trees: More Terminology



Binary Trees

- A binary tree is a tree with the following:
 - 1. Each node can have at most two subtrees and therefore at most two children.
 - 2. Each subtree is identified as being either the left subtree or the right subtree of the parent.
 - 3. It may be empty.
- Nodes in a binary tree may be composite e.g. of variable type 'Type'.

Binary Trees



Elements: The elements are nodes, each node contains the following data type: Type and has LeftChild and RightChild references.

Structure: hierarchical structure; each node can have two children: left or right child; there is a root node and a current node.

Domain: the number of nodes in a binary tree is bounded; domain contains empty tree, trees with one element, two elements, ...

Operations:

Method Traverse (Order ord)

requires: Binary Tree (BT) is not empty.

input: ord.

results: Each element in the tree is processed exactly once by a user supplied procedure. The order in which nodes are processed depends on the value of ord (Order = {preorder, postorder, inorder})

preorder: each node processed **before** any node in either of its subtrees.

<u>inorder</u>: each node is processed after all its nodes in its left subtree and before any node in its right subtree.

postorder: each node is processed **after** all its nodes in both of its subtrees.

output: none.

Tree Traversals

 To traverse a tree means to process (e.g. printing it) each element in the tree.

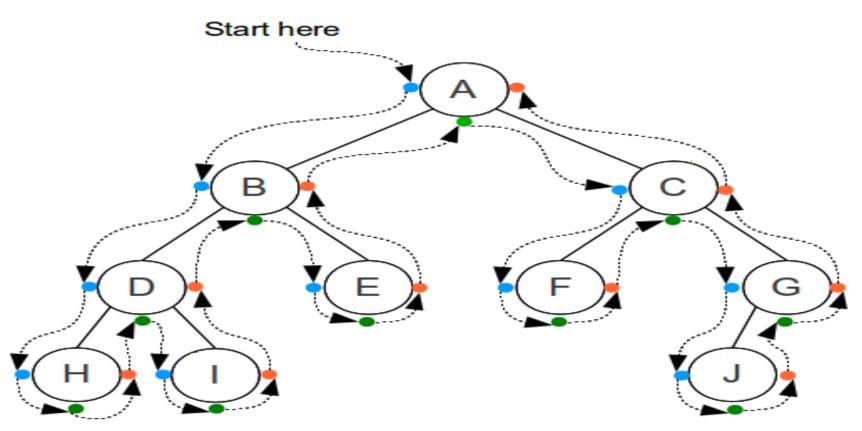
Tree traversals

- n! ways of traversing a tree of n nodes.
- pre-order, in-order, post-order ← three natural traversals orders.

List traversals

- n! ways of traversing a list of n nodes.
- front-to-back, or back-to-front. ← two natural traversals orders.

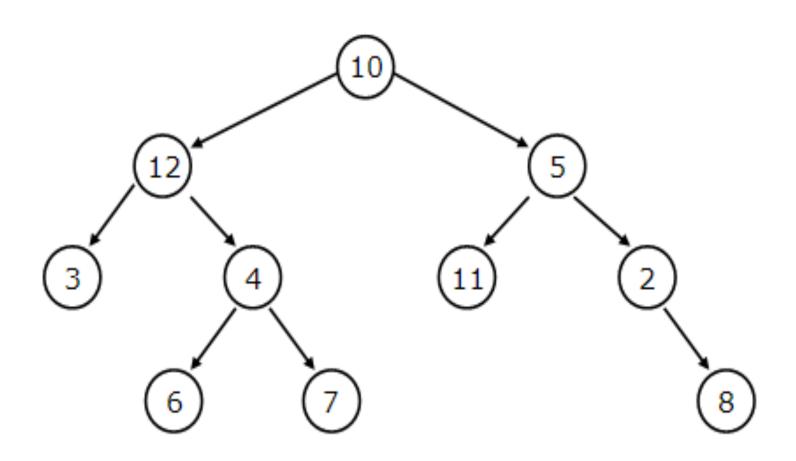
Tree Traversals Example



Pre-Order In-Order Post-Order

ABDHIECFGJ HDIBEAFCJG HIDEBFJGCA

Tree Traversals Example



Operations:

2. **Method** Insert (Type e, Relative rel, boolean inserted)

(Relative = {leftchild, rightchild, root, parent})

requires: (1) Full () is false and (2) either (a) rel = root and Empty() is true or (b) rel <> root and rel <> parent and Empty() is false.

input: e, rel.

results: if case (1) rel = leftChild, current node has a left child, or (2) rel = rightChild, current node has a right child, then inserted is false. Else a node containing e is added as rel of the current node in the tree and becomes the current node and inserted is true.

output: inserted.

3. **Procedure** DeleteSub ()

requires: Binary tree is not empty.

input: none

results: The subtree whose root node was the current node is deleted from the tree. If the resulting tree is not empty, then the root node is the current node.

output: none.

4. **Procedure** Update (Type e).

requires: Binary tree is not empty.

input: e.

results: the element in e is copied into the current

node.

output: none.

5. **Procedure** Retrieve (Type e)

requires: Binary tree is not empty.

input: none

results: element in the current node is copied into e.

output: e.

6. **Procedure** Find (Relative rel, boolean found)

requires: Binary tree is not empty.

input: rel.

results: The current node of the tree is determined by

the value of rel and previous current node..

output: found.

7. Procedure Empty (boolean empty).

requires: None.

input: none

results: If Binary tree is empty then empty is true;

otherwise empty is false.

output: empty.

8. **Procedure** Full (boolean full)

requires: None.

input: None.

results: if the binary tree is full then full is true

otherwise false.

output: full.

ADT Binary Tree: Element

```
public class BTNode <T> {
 public T data;
 public BTNode<T> left, right;
 /** Creates a new instance of BTNode */
 public BTNode(T val) {
        data = val;
        left = right = null;
 public BTNode(T val, BTNode<T> 1, BTNode<T> r) {
        data = val;
        left = 1:
        right = r;
```

ADT Binary Tree: Order & Relative Classes

- These definitions are in separate files and define:
 - The Order class.

```
public enum Order {preOrder, inOrder, postOrder};
```

The Relative class.

```
public enum Relative {Root, Parent, LeftChild, RightChild};
```

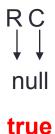
```
public class BT<T> {
 BTNode<T> root, current;
 /** Creates a new instance of BT */
 public BT() {
       root = current = null;
 public boolean empty() {
       return root == null;
```

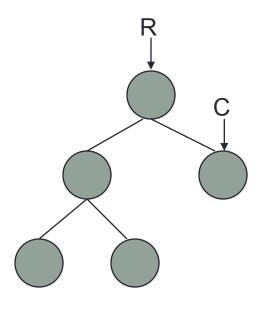
RC

null

```
public class BT<T> {
 BTNode<T> root, current;
 /** Creates a new instance of BT */
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```

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       return root == null;
```





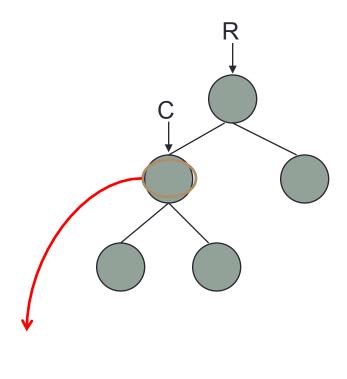
false

```
public T retrieve() {
    return current.data;
}

public void update(T val) {
    current.data = val;
}
```

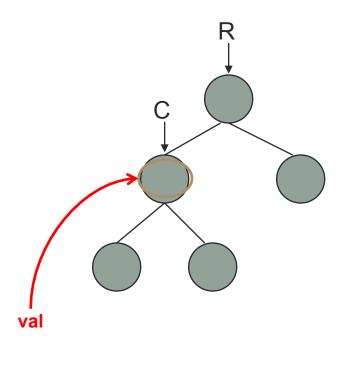
```
public T retrieve() {
    return current.data;
}

public void update(T val) {
    current.data = val;
}
```



```
public T retrieve() {
    return current.data;
}

public void update(T val) {
    current.data = val;
}
```



```
public boolean insert(Relative rel, T val) {
        switch(rel) {
          case Root:
                 if(!empty()) return false;
                 current = root = new BTNode<T>(val);
                 return true:
          case Parent: //This is an impossible case.
                 return false:
          case LeftChild:
                 if(current.left != null) return false;
                 current. left = new BTNode<T>(val);
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right != null) return false;
                 current.right = new BTNode<T> (val);
                 current = current.right;
                 return true:
          default:
                 return false:
```

```
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        switch(rel) {
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                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right != null) return false;
                 current.right = new BTNode<T> (val);
                 current = current.right;
                 return true:
          default:
                 return false:
```

Example #1 rel = Root

R C ↓ ↓ null

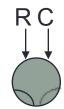
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                 current. left = new BTNode<T>(val);
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right != null) return false;
                 current.right = new BTNode<T> (val);
                 current = current.right;
                 return true:
          default:
                 return false:
```

Example #1 rel = Root



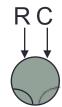
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          case Root:
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                 current. left = new BTNode<T>(val);
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right != null) return false;
                 current.right = new BTNode<T> (val);
                 current = current.right;
                 return true:
          default:
                 return false:
```

Example #1 rel = Root



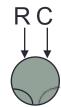
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public boolean insert(Relative rel, T val) {
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          case LeftChild:
                 if(current.left != null) return false;
                 current. left = new BTNode<T>(val);
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right != null) return false;
                 current.right = new BTNode<T> (val);
                 current = current.right;
                 return true:
          default:
                 return false:
```

Example #2 rel = LeftChild



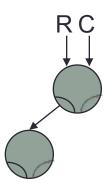
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        switch(rel) {
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           case Parent: //This is an impossible case.
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           case LeftChild:
                  if (current. left != null) return false;
                 current. left = new BTNode<T>(val);
                 current = current.left:
                 return true:
           case RightChild:
                  if(current.right != null) return false;
                  current.right = new BTNode<T> (val);
                 current = current.right;
                 return true:
           default:
                 return false:
```

Example #2 rel = LeftChild



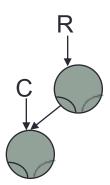
```
Example #2 rel = LeftChild
```

```
public boolean insert(Relative rel, T val) {
       switch(rel) {
          case Root:
                 if(!empty()) return false:
                 current = root = new BTNode<T>(val);
                 return true:
          case Parent: //This is an impossible case.
                 return false:
          case LeftChild:
                 if(current.left != null) return false;
                 current.left = new BTNode<T>(val);
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right != null) return false;
                 current.right = new BTNode<T> (val);
                 current = current.right;
                 return true:
          default:
                 return false:
```



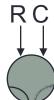
Example #2 rel = LeftChild

```
public boolean insert(Relative rel, T val) {
        switch(rel) {
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                 return true:
          case Parent: //This is an impossible case.
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                 if(current.left != null) return false;
                 current. left = new BTNode<T>(val);
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right != null) return false;
                 current.right = new BTNode<T> (val);
                 current = current.right;
                 return true:
          default:
                 return false:
```



```
Example #3 rel = RightChild
```

```
public boolean insert(Relative rel, T val) {
        switch(rel) {
          case Root:
                 if(!empty()) return false:
                 current = root = new BTNode<T>(val);
                 return true:
          case Parent: //This is an impossible case.
                 return false:
          case LeftChild:
                 if(current.left != null) return false;
                 current. left = new BTNode<T>(val);
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right != null) return false;
                 current.right = new BTNode<T> (val);
                 current = current.right;
                 return true:
          default:
                 return false:
```

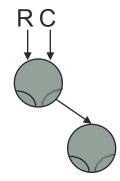


```
Example #3 rel = RightChild
```

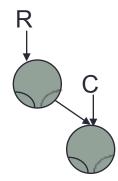
```
RC
```

```
public boolean insert(Relative rel, T val) {
        switch(rel) {
           case Root:
                 if(!empty()) return false:
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                 return true:
           case Parent: //This is an impossible case.
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                 if(current.left != null) return false;
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```

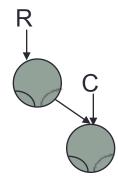


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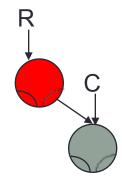
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                 if(current.right != null) return false;
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```

Example #4 rel = Parent

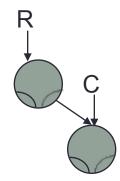


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          case Root:
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                 current = current.right;
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                 return false:
```

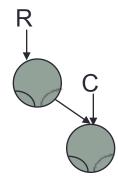
Example #4 rel = Parent



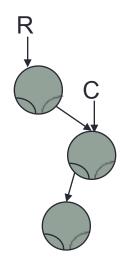
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public boolean insert(Relative rel, T val) {
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                 return false:
```



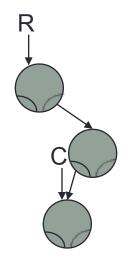
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                 return true:
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```



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          case LeftChild:
                 if(current.left != null) return false;
                 current.left = new BTNode<T>(val);
                 current = current.left:
                 return true:
          case RightChild:
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                 current.right = new BTNode<T> (val);
                 current = current.right;
                 return true:
          default:
                 return false:
```

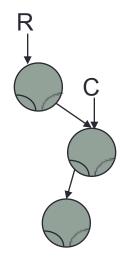


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          case RightChild:
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                 current = current.right;
                 return true:
          default:
                 return false:
```

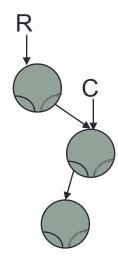


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          case LeftChild:
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                 current = current.left:
                 return true:
          case RightChild:
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                 current.right = new BTNode<T> (val);
                 current = current.right;
                 return true:
          default:
                 return false:
```

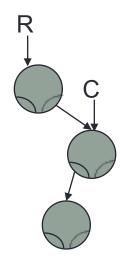
Find Parent



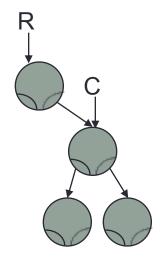
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                 return true:
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```



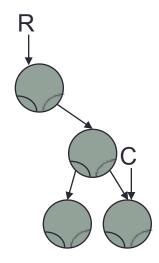
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public boolean insert(Relative rel, T val) {
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          case Root:
                 if(!empty()) return false:
                 current = root = new BTNode<T>(val);
                 return true:
          case Parent: //This is an impossible case.
                 return false:
          case LeftChild:
                 if(current.left != null) return false;
                 current. left = new BTNode<T>(val);
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right != null) return false;
                 current.right = new BTNode<T> (val):
                 current = current.right;
                 return true:
          default:
                 return false:
```



```
public boolean insert(Relative rel, T val) {
        switch(rel) {
          case Root:
                 if(!empty()) return false:
                 current = root = new BTNode<T>(val);
                 return true:
          case Parent: //This is an impossible case.
                 return false:
          case LeftChild:
                 if(current.left != null) return false;
                 current. left = new BTNode<T>(val);
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right != null) return false;
                 current.right = new BTNode<T> (val);
                 current = current.right;
                 return true:
          default:
                 return false:
```

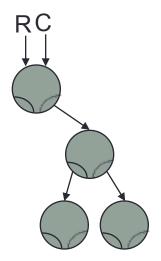


```
public boolean insert(Relative rel, T val) {
        switch(rel) {
          case Root:
                 if(!empty()) return false:
                 current = root = new BTNode<T>(val);
                 return true:
          case Parent: //This is an impossible case.
                 return false:
          case LeftChild:
                 if(current.left != null) return false;
                 current. left = new BTNode<T>(val);
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right != null) return false;
                 current.right = new BTNode<T> (val);
                 current = current.right;
                 return true:
          default:
                 return false:
```

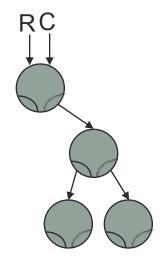


```
public boolean insert(Relative rel, T val) {
        switch(rel) {
          case Root:
                 if(!empty()) return false;
                 current = root = new BTNode<T>(val);
                 return true:
          case Parent: //This is an impossible case.
                 return false:
          case LeftChild:
                 if(current.left != null) return false;
                 current. left = new BTNode<T>(val);
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right != null) return false;
                 current.right = new BTNode<T> (val);
                 current = current.right;
                 return true:
          default:
                 return false:
```

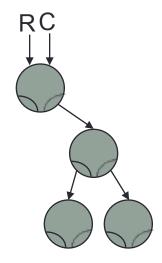
Find Root



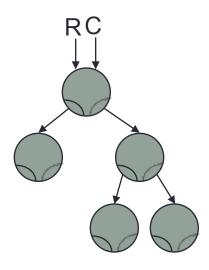
```
public boolean insert(Relative rel, T val) {
        switch(rel) {
          case Root:
                 if(!empty()) return false:
                 current = root = new BTNode<T>(val);
                 return true:
          case Parent: //This is an impossible case.
                 return false:
          case LeftChild:
                 if(current.left != null) return false;
                 current. left = new BTNode<T>(val);
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right != null) return false;
                 current.right = new BTNode<T> (val);
                 current = current.right;
                 return true:
          default:
                 return false:
```



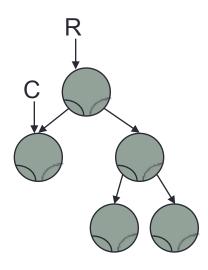
```
public boolean insert(Relative rel, T val) {
        switch(rel) {
          case Root:
                 if(!empty()) return false:
                 current = root = new BTNode<T>(val);
                 return true:
          case Parent: //This is an impossible case.
                 return false:
          case LeftChild:
                 if(current.left != null) return false;
                 current. left = new BTNode<T>(val);
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right != null) return false;
                 current.right = new BTNode<T> (val);
                 current = current.right;
                 return true:
          default:
                 return false:
```



```
public boolean insert(Relative rel, T val) {
        switch(rel) {
          case Root:
                 if(!empty()) return false:
                 current = root = new BTNode<T>(val);
                 return true:
          case Parent: //This is an impossible case.
                 return false:
          case LeftChild:
                 if(current.left != null) return false;
                 current.left = new BTNode<T>(val);
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right != null) return false;
                 current.right = new BTNode<T> (val);
                 current = current.right;
                 return true:
          default:
                 return false:
```

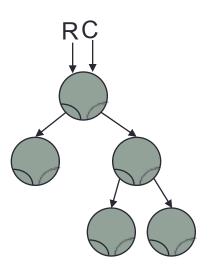


```
public boolean insert(Relative rel, T val) {
        switch(rel) {
          case Root:
                 if(!empty()) return false:
                 current = root = new BTNode<T>(val);
                 return true:
          case Parent: //This is an impossible case.
                 return false:
          case LeftChild:
                 if(current.left != null) return false;
                 current. left = new BTNode<T>(val);
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right != null) return false;
                 current.right = new BTNode<T> (val);
                 current = current.right;
                 return true:
          default:
                 return false:
```



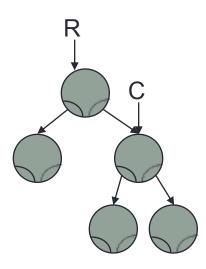
```
public boolean insert(Relative rel, T val) {
        switch(rel) {
          case Root:
                 if(!empty()) return false;
                 current = root = new BTNode<T>(val);
                 return true:
          case Parent: //This is an impossible case.
                 return false:
          case LeftChild:
                 if(current.left != null) return false;
                 current. left = new BTNode<T>(val);
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right != null) return false;
                 current.right = new BTNode<T> (val);
                 current = current.right;
                 return true:
          default:
                 return false:
```

Find Root

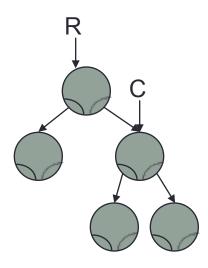


```
public boolean insert(Relative rel, T val) {
        switch(rel) {
          case Root:
                 if(!empty()) return false:
                 current = root = new BTNode<T>(val);
                 return true:
          case Parent: //This is an impossible case.
                 return false:
          case LeftChild:
                 if(current.left != null) return false;
                 current. left = new BTNode<T>(val);
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right != null) return false;
                 current.right = new BTNode<T> (val);
                 current = current.right;
                 return true:
          default:
                 return false:
```

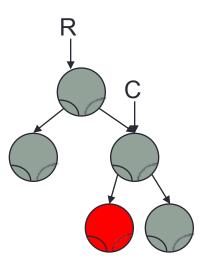
Find RightChild



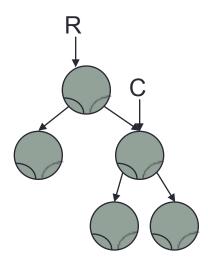
```
public boolean insert(Relative rel, T val) {
        switch(rel) {
          case Root:
                 if(!empty()) return false:
                 current = root = new BTNode<T>(val);
                 return true:
          case Parent: //This is an impossible case.
                 return false:
          case LeftChild:
                 if(current.left != null) return false;
                 current. left = new BTNode<T>(val);
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right != null) return false;
                 current.right = new BTNode<T> (val);
                 current = current.right;
                 return true:
          default:
                 return false:
```



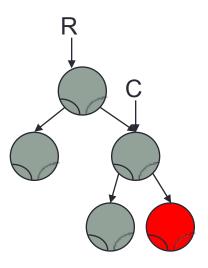
```
public boolean insert(Relative rel, T val) {
        switch(rel) {
           case Root:
                 if(!empty()) return false:
                 current = root = new BTNode<T>(val);
                 return true:
           case Parent: //This is an impossible case.
                 return false:
           case LeftChild:
                 if (current. left != null) return false;
                 current. left = new BTNode<T>(val);
                 current = current.left;
                 return true:
           case RightChild:
                  if(current.right != null) return false;
                 current.right = new BTNode<T> (val):
                 current = current.right;
                 return true:
           default:
                 return false:
```



```
public boolean insert(Relative rel, T val) {
        switch(rel) {
          case Root:
                 if(!empty()) return false:
                 current = root = new BTNode<T>(val);
                 return true:
          case Parent: //This is an impossible case.
                 return false:
          case LeftChild:
                 if(current.left != null) return false;
                 current. left = new BTNode<T>(val);
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right != null) return false;
                 current.right = new BTNode<T> (val):
                 current = current.right;
                 return true:
          default:
                 return false:
```

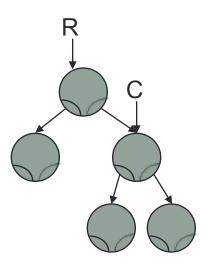


```
public boolean insert(Relative rel, T val) {
        switch(rel) {
           case Root:
                  if(!empty()) return false:
                 current = root = new BTNode<T>(val);
                 return true:
           case Parent: //This is an impossible case.
                 return false:
           case LeftChild:
                 if(current.left != null) return false;
                 current. left = new BTNode<T>(val);
                 current = current.left:
                 return true:
           case RightChild:
                 if (current. right != null) return false;
                 current.right = new BTNode<T> (val):
                 current = current.right;
                 return true:
           default:
                 return false:
```



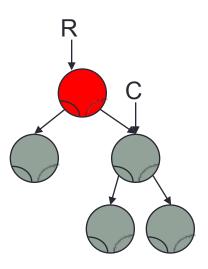
```
public boolean insert(Relative rel, T val) {
        switch(rel) {
          case Root:
                 if(!empty()) return false:
                 current = root = new BTNode<T>(val);
                 return true:
          case Parent: //This is an impossible case.
                 return false:
          case LeftChild:
                 if(current.left != null) return false;
                 current. left = new BTNode<T>(val);
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right != null) return false;
                 current.right = new BTNode<T> (val);
                 current = current.right;
                 return true:
          default:
                 return false:
```

Example #10 rel = Parent



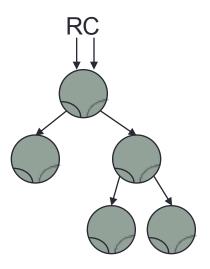
```
public boolean insert(Relative rel, T val) {
        switch(rel) {
          case Root:
                 if(!empty()) return false:
                 current = root = new BTNode<T>(val);
                 return true:
           case Parent: //This is an impossible case.
                 return false:
          case LeftChild:
                 if(current.left != null) return false;
                 current. left = new BTNode<T>(val);
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right != null) return false;
                 current.right = new BTNode<T> (val);
                 current = current.right;
                 return true:
          default:
                 return false:
```

Example #10 rel = Parent

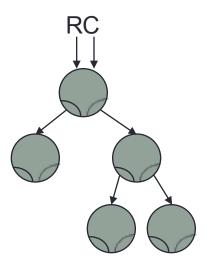


```
public void deleteSubtree() {
       if(current == root) {
                 current = root = null;
                                              كرف الرى الكامل
       else {
                 set مؤلَّ ما اللهِ بنعافه  
BTNode T> p = current;
                 find (Relative. Parent); نعدي الكرنة المبوه
                 current. left = null;
                 else
                          current.right = null;
                 current = root;
                                     مرى كن خلك مسا
```

```
public void deleteSubtree() {
       if(current == root) {
                 current = root = null;
       else {
                 BTNode<T> p = current;
                 find (Relative. Parent);
                 if(current.left == p)
                          current. left = null;
                 else
                          current.right = null;
                 current = root;
```

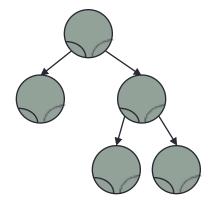


```
public void deleteSubtree() {
       if(current == root) {
                 current = root = null;
       else {
                 BTNode<T> p = current;
                 find (Relative. Parent);
                 if(current.left == p)
                          current. left = null;
                 else
                          current.right = null;
                 current = root;
```



```
public void deleteSubtree() {
       if(current == root) {
                 current = root = null;
       else {
                 BTNode<T> p = current;
                 find (Relative. Parent);
                 if(current.left == p)
                          current. left = null;
                 else
                          current.right = null;
                 current = root;
```





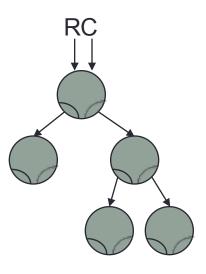
```
public void deleteSubtree() {
       if(current == root) {
                current = root = null;
       else {
                BTNode<T> p = current;
                find(Relative.Parent);
                 if(current.left == p)
                          current. left = null;
                else
                          current.right = null;
                current = root;
```

RC 1 null

```
public void deleteSubtree() {
       if(current == root) {
                 current = root = null;
       else {
                 BTNode<T> p = current;
                 find (Relative. Parent);
                 if(current.left == p)
                          current. left = null;
                 else
                          current.right = null;
                 current = root;
```

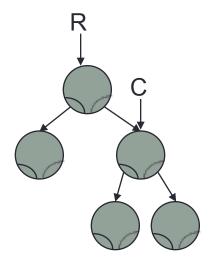


```
public void deleteSubtree() {
       if(current == root) {
                 current = root = null;
       else {
                 BTNode<T> p = current;
                 find (Relative. Parent);
                 if(current.left == p)
                          current. left = null;
                 else
                          current.right = null;
                 current = root;
```

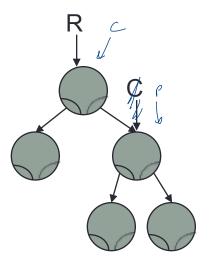


```
public void deleteSubtree() {
       if(current == root) {
                 current = root = null;
       else {
                 BTNode<T> p = current;
                 find (Relative. Parent);
                 if(current.left == p)
                          current. left = null;
                 else
                          current.right = null;
                 current = root;
```

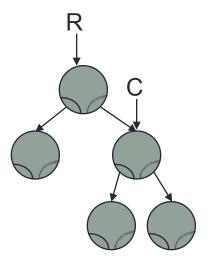
Find RightChild



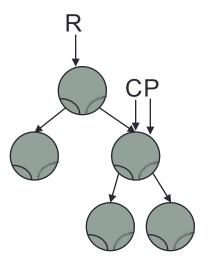
```
public void deleteSubtree() {
       if(current == root) {
                 current = root = null;
       else {
                 BTNode<T> p = current;
                 find (Relative. Parent);
                 if(current.left == p)
                          current. left = null;
                 else
                          current.right = null;
                 current = root;
```



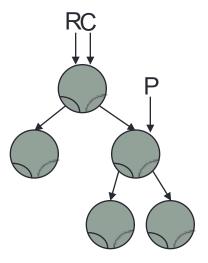
```
public void deleteSubtree() {
       if(current == root) {
                 current = root = null;
       else {
                 BTNode<T> p = current;
                 find (Relative. Parent);
                 if(current.left == p)
                          current. left = null;
                 else
                          current.right = null;
                 current = root;
```



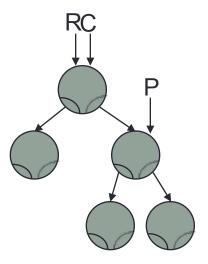
```
public void deleteSubtree() {
       if(current == root) {
                 current = root = null;
       else {
                BTNode<T> p = current;
                 find (Relative. Parent);
                 if(current.left == p)
                          current. left = null;
                 else
                          current.right = null;
                 current = root;
```



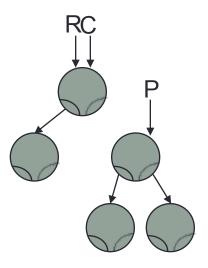
```
public void deleteSubtree() {
       if(current == root) {
                current = root = null;
       else {
                BTNode<T> p = current;
                find(Relative. Parent);
                 if(current.left == p)
                          current. left = null;
                else
                          current.right = null;
                current = root;
```



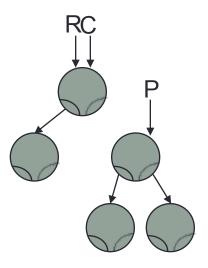
```
public void deleteSubtree() {
       if(current == root) {
                 current = root = null;
       else {
                 BTNode<T> p = current;
                 find (Relative. Parent);
                 if(current.left == p)
                          current. left = null;
                 else
                          current.right = null;
                 current = root;
```



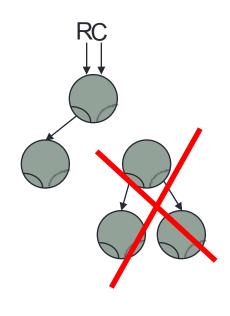
```
public void deleteSubtree() {
       if(current == root) {
                 current = root = null;
       else {
                 BTNode<T> p = current;
                 find (Relative. Parent);
                 if(current.left == p)
                          current. left = null;
                 else
                          current.right = null;
                 current = root;
```



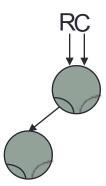
```
public void deleteSubtree() {
       if(current == root) {
                 current = root = null;
       else {
                 BTNode<T> p = current;
                 find (Relative. Parent);
                 if(current.left == p)
                          current. left = null;
                 else
                          current.right = null;
                 current = root;
```



```
public void deleteSubtree() {
       if(current == root) {
                 current = root = null;
       else {
                 BTNode<T> p = current;
                 find (Relative. Parent);
                 if(current.left == p)
                          current. left = null;
                 else
                          current.right = null;
                 current = root;
```

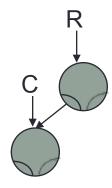


```
public void deleteSubtree() {
       if(current == root) {
                 current = root = null;
       else {
                 BTNode<T> p = current;
                 find(Relative.Parent);
                 if(current.left == p)
                          current. left = null;
                 else
                          current.right = null;
                 current = root;
```

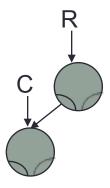


```
public void deleteSubtree() {
       if(current == root) {
                 current = root = null;
       else {
                 BTNode<T> p = current;
                 find (Relative. Parent);
                 if(current.left == p)
                          current. left = null;
                 else
                          current.right = null;
                 current = root;
```

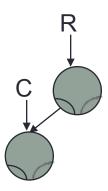
Find LeftChild

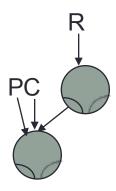


```
public void deleteSubtree() {
       if(current == root) {
                 current = root = null;
       else {
                 BTNode<T> p = current;
                 find (Relative. Parent);
                 if(current.left == p)
                          current. left = null;
                 else
                          current.right = null;
                 current = root;
```

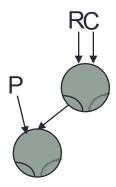


```
public void deleteSubtree() {
       if(current == root) {
                 current = root = null;
       else {
                 BTNode<T> p = current;
                 find (Relative. Parent);
                 if(current.left == p)
                          current. left = null;
                 else
                          current.right = null;
                 current = root;
```

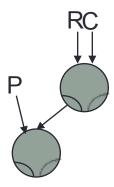




```
public void deleteSubtree() {
       if(current == root) {
                current = root = null;
       else {
                BTNode<T> p = current;
                find(Relative. Parent);
                 if(current.left == p)
                          current. left = null;
                else
                          current.right = null;
                current = root;
```



```
public void deleteSubtree() {
       if(current == root) {
                current = root = null;
       else {
                BTNode<T> p = current;
                find(Relative.Parent);
                if(current.left == p)
                          current. left = null;
                else
                          current.right = null;
                current = root;
```



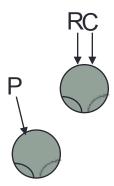
public void deleteSubtree() { if(current == root) { current = root = null; } else { BTNode<T> p = current; find(Relative. Parent); if(current. left == p)

current = root;

else

current.left = null;

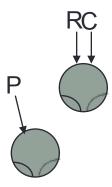
current.right = **null**;



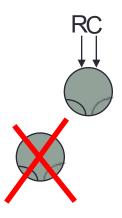
current = root;

current.right = **null**;

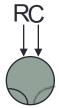
else

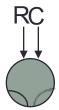


```
public void deleteSubtree() {
       if(current == root) {
                 current = root = null;
       else {
                 BTNode<T> p = current;
                 find (Relative. Parent);
                 if(current.left == p)
                          current. left = null;
                 else
                          current.right = null;
                 current = root;
```



```
public void deleteSubtree() {
       if(current == root) {
                 current = root = null;
       else {
                 BTNode<T> p = current;
                 find (Relative. Parent);
                 if(current.left == p)
                          current. left = null;
                 else
                          current.right = null;
                 current = root;
```





```
public void deleteSubtree() {
       if(current == root) {
                 current = root = null;
       else {
                 BTNode<T> p = current;
                 find (Relative. Parent);
                 if(current.left == p)
                          current. left = null;
                 else
                          current.right = null;
                 current = root;
```





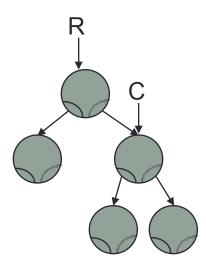
```
public void deleteSubtree() {
       if(current == root) {
                current = root = null;
       else {
                BTNode<T> p = current;
                find(Relative.Parent);
                 if(current.left == p)
                          current. left = null;
                else
                          current.right = null;
                current = root;
```



```
public boolean find(Relative rel) {
        switch (rel) {
           case Root: // Easy case
                  current = root;
                  return true;
           case Parent:
                  if (current == root) return false; الروت الاوت الالا الروت الالا
                  current = findparent(current, root);
                  return true:
           case LeftChild:
                  if(current.left == null) return false:
                  current = current.left:
                  return true:
           case RightChild:
                  if(current.right == null) return false:
                  current = current.right;
                  return true:
           default:
                  return false;
```

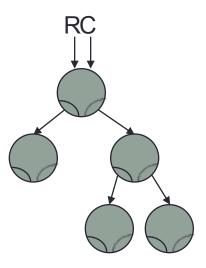
```
public boolean find(Relative rel) {
       switch (rel) {
          case Root: // Easy case
                 current = root;
                 return true:
          case Parent:
                 if(current == root) return false:
                 current = findparent(current, root);
                 return true;
          case LeftChild:
                 if(current.left == null) return false:
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right == null) return false:
                 current = current.right;
                 return true:
          default:
                 return false;
```

Example #1 rel = Root



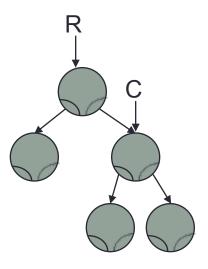
```
public boolean find(Relative rel) {
       switch (rel) {
          case Root: // Easy case
                 current = root:
                 return true;
          case Parent:
                 if(current == root) return false:
                 current = findparent(current, root);
                 return true;
          case LeftChild:
                 if(current.left == null) return false:
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right == null) return false:
                 current = current.right;
                 return true:
          default:
                 return false;
```

Example #1 rel = Root



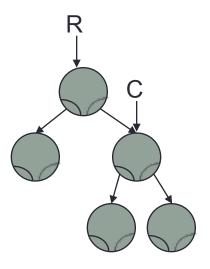
```
public boolean find(Relative rel) {
       switch (rel) {
          case Root: // Easy case
                 current = root;
                 return true:
          case Parent:
                 if(current == root) return false:
                 current = findparent(current, root);
                 return true;
          case LeftChild:
                 if(current.left == null) return false:
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right == null) return false:
                 current = current.right;
                 return true:
          default:
                 return false;
```

Example #2 rel = LeftChild



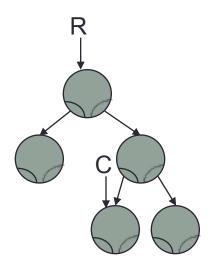
```
public boolean find(Relative rel) {
       switch (rel) {
          case Root:
                     // Easy case
                 current = root;
                 return true:
          case Parent:
                 if(current == root) return false:
                 current = findparent(current, root);
                 return true;
          case LeftChild:
                 if (current. left = null) return false:
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right == null) return false:
                 current = current.right;
                 return true:
          default:
                 return false;
```

Example #2 rel = LeftChild



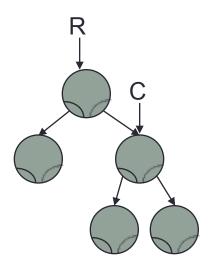
```
public boolean find(Relative rel) {
       switch (rel) {
          case Root: // Easy case
                 current = root;
                 return true:
          case Parent:
                 if(current == root) return false:
                 current = findparent(current, root);
                 return true;
          case LeftChild:
                 if(current.left == null) return false;
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right == null) return false;
                 current = current.right;
                 return true:
          default:
                 return false;
```

Example #2 rel = LeftChild



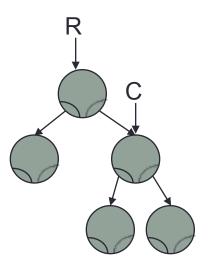
```
public boolean find(Relative rel) {
       switch (rel) {
          case Root: // Easy case
                 current = root;
                 return true:
          case Parent:
                 if(current == root) return false:
                 current = findparent(current, root);
                 return true;
          case LeftChild:
                 if(current.left == null) return false:
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right == null) return false;
                 current = current.right;
                 return true:
          default:
                 return false;
```

Example #3 rel = RightChild



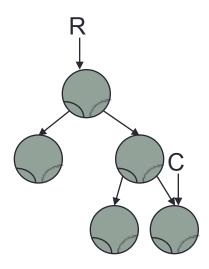
```
public boolean find(Relative rel) {
       switch (rel) {
          case Root: // Easy case
                 current = root;
                 return true:
          case Parent:
                 if(current == root) return false:
                 current = findparent(current, root);
                 return true;
          case LeftChild:
                 if(current.left == null) return false:
                 current = current.left:
                 return true:
          case RightChild:
                 if (current. right = null) return false;
                 current = current.right;
                 return true:
          default:
                 return false;
```

Example #3 rel = RightChild



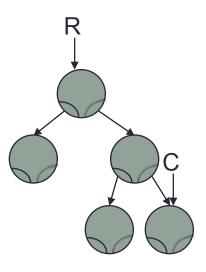
```
public boolean find(Relative rel) {
       switch (rel) {
          case Root: // Easy case
                 current = root;
                 return true:
          case Parent:
                 if(current == root) return false:
                 current = findparent(current, root);
                 return true;
          case LeftChild:
                 if(current.left == null) return false:
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right == null) return false;
                 current = current.right;
                 return true:
          default:
                 return false;
```

Example #3 rel = RightChild



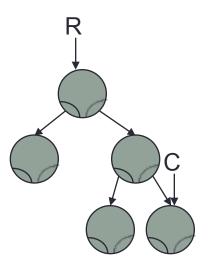
```
public boolean find(Relative rel) {
       switch (rel) {
          case Root: // Easy case
                 current = root;
                 return true:
          case Parent:
                 if(current == root) return false:
                 current = findparent(current, root);
                 return true;
          case LeftChild:
                 if(current.left == null) return false:
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right == null) return false;
                 current = current.right;
                 return true:
          default:
                 return false;
```

Example #4 rel = RightChild



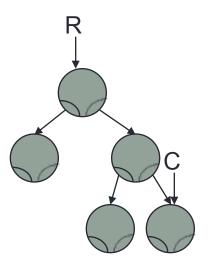
```
public boolean find(Relative rel) {
       switch (rel) {
          case Root: // Easy case
                 current = root;
                 return true:
          case Parent:
                 if(current == root) return false:
                 current = findparent(current, root);
                 return true;
          case LeftChild:
                 if(current.left == null) return false:
                 current = current.left:
                 return true:
          case RightChild:
                 if (current.right = null) return false;
                 current = current.right;
                 return true:
          default:
                 return false;
```

Example #4 rel = RightChild



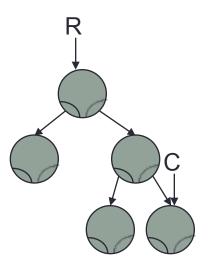
```
public boolean find(Relative rel) {
       switch (rel) {
          case Root: // Easy case
                 current = root;
                 return true:
          case Parent:
                 if(current == root) return false:
                 current = findparent(current, root);
                 return true;
          case LeftChild:
                 if(current.left == null) return false:
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right == null) return false;
                 current = current.right;
                 return true:
          default:
                 return false;
```

Example #5 rel = LeftChild



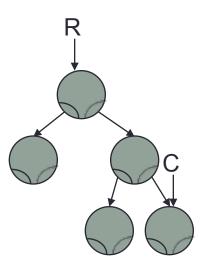
```
public boolean find(Relative rel) {
       switch (rel) {
          case Root:
                     // Easy case
                 current = root;
                 return true:
          case Parent:
                 if(current == root) return false:
                 current = findparent(current, root);
                 return true;
          case LeftChild:
                 if (current. left = null) return false;
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right == null) return false:
                 current = current.right;
                 return true:
          default:
                 return false;
```

Example #5 rel = LeftChild



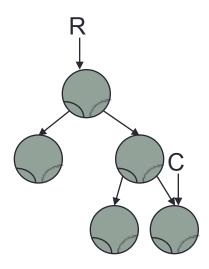
```
public boolean find(Relative rel) {
       switch (rel) {
          case Root: // Easy case
                 current = root;
                 return true:
          case Parent:
                 if(current == root) return false:
                 current = findparent(current, root);
                 return true;
          case LeftChild:
                 if(current.left == null) return false:
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right == null) return false;
                 current = current.right;
                 return true:
          default:
                 return false;
```

Example #6 rel = Parent



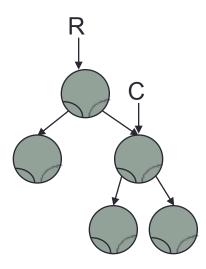
```
public boolean find(Relative rel)
       switch (rel) {
                      // Easy case
          case Root:
                 current = root;
                 return true:
          case Parent:
                 if (current = root) return false:
                 current = findparent(current, root);
                 return true:
          case LeftChild:
                 if(current.left == null) return false:
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right == null) return false:
                 current = current.right;
                 return true:
          default:
                 return false;
```

Example #6 rel = Parent



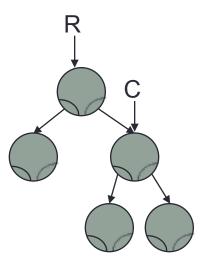
```
public boolean find(Relative rel) {
       switch (rel) {
          case Root: // Easy case
                 current = root;
                 return true:
          case Parent:
                 if(current == root) return false:
                 current = findparent(current, root);
                 return true;
          case LeftChild:
                 if(current.left == null) return false:
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right == null) return false:
                 current = current.right;
                 return true:
          default:
                 return false;
```

Example #6 rel = Parent



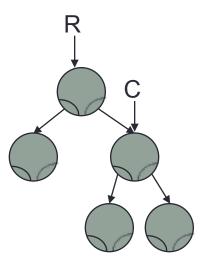
```
public boolean find(Relative rel) {
       switch (rel) {
          case Root: // Easy case
                 current = root;
                 return true:
          case Parent:
                 if(current == root) return false:
                 current = findparent(current, root);
                 return true;
          case LeftChild:
                 if(current.left == null) return false:
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right == null) return false;
                 current = current.right;
                 return true:
          default:
                 return false;
```

Example #7 rel = Parent



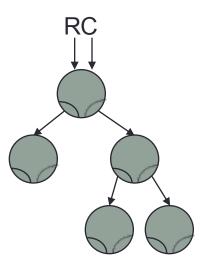
```
public boolean find(Relative rel) {
       switch (rel) {
          case Root:
                     // Easy case
                 current = root;
                 return true:
          case Parent:
                 if (current = root) return false:
                 current = findparent(current, root);
                 return true;
          case LeftChild:
                 if(current.left == null) return false:
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right == null) return false:
                 current = current.right;
                 return true:
          default:
                 return false;
```

Example #7 rel = Parent



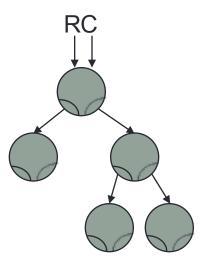
```
public boolean find(Relative rel) {
       switch (rel) {
          case Root:
                     // Easy case
                 current = root;
                 return true:
          case Parent:
                 if(current == root) return false:
                 current = findparent(current, root);
                 return true;
          case LeftChild:
                 if(current.left == null) return false:
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right == null) return false:
                 current = current.right;
                 return true:
          default:
                 return false;
```

Example #7 rel = Parent



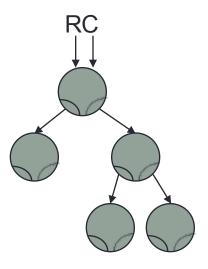
```
public boolean find(Relative rel) {
       switch (rel) {
          case Root: // Easy case
                 current = root;
                 return true:
          case Parent:
                 if(current == root) return false:
                 current = findparent(current, root);
                 return true;
          case LeftChild:
                 if(current.left == null) return false:
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right == null) return false:
                 current = current.right;
                 return true:
          default:
                 return false;
```

Example #8 rel = Parent



```
public boolean find(Relative rel) {
       switch (rel) {
          case Root:
                     // Easy case
                 current = root;
                 return true:
          case Parent:
                 if (current = root) return false:
                 current = findparent(current, root);
                 return true;
          case LeftChild:
                 if(current.left == null) return false:
                 current = current.left:
                 return true:
          case RightChild:
                 if(current.right == null) return false:
                 current = current.right;
                 return true:
          default:
                 return false;
```

Example #8 rel = Parent



```
// Non-recursive version of findparent - uses pre-order traversal
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
       // Stack is used to store the right pointers of nodes
       LinkStack<BTNode<T>> stack = new LinkStack<BTNode<T>>();
       BTNode < T > q = t;
       while(q. right != p && q. left != p) {
                 if (q. right != null)
                          stack. push (q. right);
                 if(q. left != null)
                          q = q. left;
                 else
                          q = stack.pop(); // Go right here
       return q;
```

```
// Non-recursive version of findparent - uses pre-order traversal
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
       // Stack is used to store the right pointers of nodes
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       BTNode < T > q = t;
       while(q. right != p && q. left != p) {
                 if (q. right != null)
                          stack. push (q. right);
                 if(q. left != null)
                          q = q. left;
                 else
                          q = stack.pop(); // Go right here
                                                                   Example #1
                                                                p = current, t = root
       return q;
```

```
// Non-recursive version of findparent - uses pre-order traversal
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                                                                       R
       BTNode < T > q = t;
       while(q. right != p && q. left != p) {
                 if (q. right != null)
                          stack. push (q. right);
                 if(q. left != null)
                          q = q. left;
                 else
                          q = stack.pop(); // Go right here
                                                                   Example #1
                                                                p = current, t = root
       return q;
```

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                                                                      RQ
       BTNode < T > q = t;
       while(q. right != p && q. left != p) {
                 if (q. right != null)
                          stack. push (q. right);
                 if(q. left != null)
                          q = q. left;
                 else
                          q = stack.pop(); // Go right here
                                                                   Example #1
                                                                p = current, t = root
       return q;
```

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       BTNode < T > q = t;
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                 if (q. right != null)
                          stack. push (q. right);
                 if(q. left != null)
                          q = q. left;
                 else
                          q = stack.pop(); // Go right here
                                                                   Example #1
                                                                p = current, t = root
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```

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                                                                      RQ
       BTNode < T > q = t;
       while(q. right != p && q. left != p) {
                 if(q.right != null)
                          stack. push (q. right);
                 if(q. left != null)
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                 else
                          q = stack.pop(); // Go right here
                                                                   Example #1
                                                                p = current, t = root
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                                                                       RQ
       BTNode < T > q = t;
       while(q. right != p && q. left != p) {
                 if (q. right != null)
                          stack. push (q. right);
                 if(q. left != null)
                          q = q. left;
                 else
                          q = stack.pop(); // Go right here
                                                                   Example #1
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                          stack. push (q. right);
                 if (q. left != null)
                          q = q. left;
                 else
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                                                                   Example #1
                                                                p = current, t = root
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                 if (q. right != null)
                          stack. push (q. right);
                 if(q. left != null)
                          q = q. left;
                 else
                          q = stack.pop(); // Go right here
                                                                   Example #1
                                                                p = current, t = root
       return q;
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                 if (q. right != null)
                          stack. push (q. right);
                 if(q. left != null)
                          q = q. left;
                 else
                          q = stack.pop(); // Go right here
                                                                   Example #1
                                                                 p = current, t = root
       return q;
```

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                 if(q.right != null)
                          stack. push (q. right);
                 if(q. left != null)
                          q = q. left;
                 else
                          q = stack.pop(); // Go right here
                                                                   Example #1
                                                                p = current, t = root
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                          stack. push (q. right);
                 if (q. left != null)
                          q = q. left;
                 else
                          q = stack.pop(); // Go right here
                                                                   Example #1
                                                                 p = current, t = root
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```

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// Non-recursive version of findparent - uses pre-order traversal
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
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       LinkStack<BTNode<T>> stack = new LinkStack<BTNode<T>>();
                                                                       R
       BTNode < T > q = t;
       while(q. right != p && q. left != p) {
                 if (q. right != null)
                          stack. push (q. right);
                 if(q. left != null)
                          q = q. left;
                 else
                          q = stack.pop(); // Go right here
                                                                   Example #1
                                                                p = current, t = root
       return q;
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       else {
               BTNode q = findparent(p, t.left);
                if (q != null)
                        return q;
                e1se
                        return findparent(p, t.right);
```

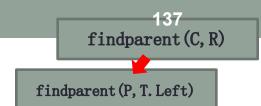
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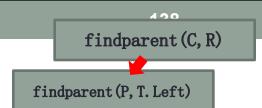
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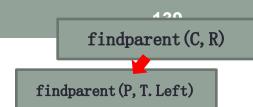
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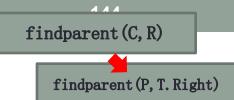
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                                                              Example #2
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                                                              Example #2
```

findparent (C, R) findparent (P, T. Left)

Example #2

findparent (P, T. Left)

ADT Binary Tree: Implementation

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```

return findparent(p, t.right);

findparent (C, R) findparent (P, T. Left)

findparent (P, T. Left)

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Example #2

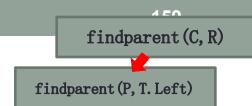
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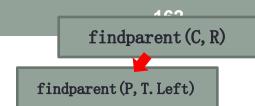
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findparent (C, R) findparent (P, T. Left) findparent (P, T. Right)

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