

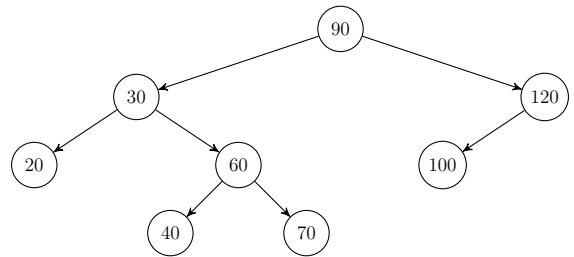
# CSC 212 Extra Example - AVL and B+ Tree

College of Computer and Information Sciences, King Saud University

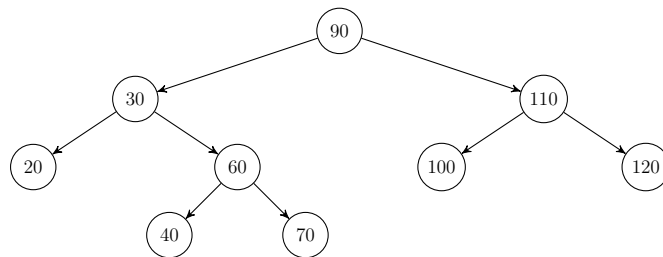
November 24, 2018

## Question 1

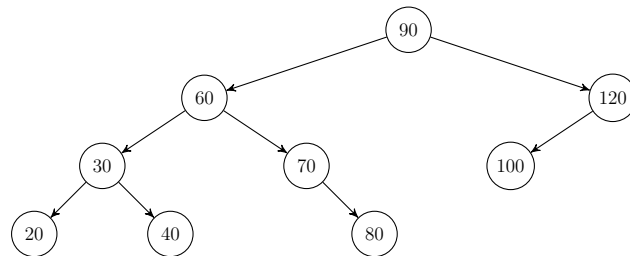
Perform the following operations on this AVL tree: **Insert 110**, **Insert 80**, **Delete 20**, **Delete 60**, **Delete 120**. Mention the rotation type: none, single, or double. **Each operation is independent, and must be performed on the original tree.** **Convention:** When necessary, the key must be replaced by the smallest key in the right subtree.



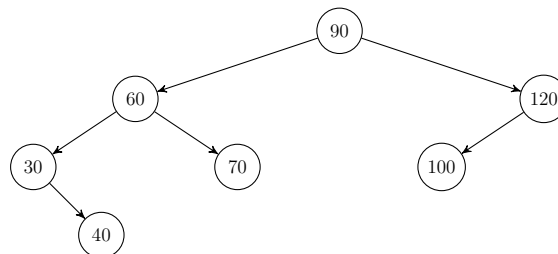
**Insert 110: Double**



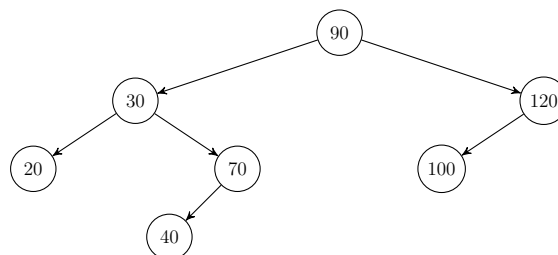
**Insert 80: Single**



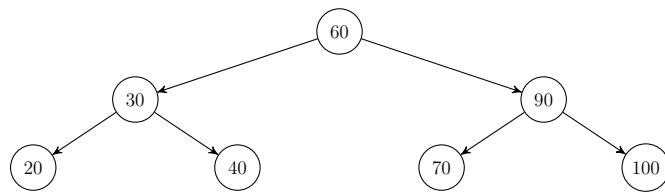
**Delete 20**



**Delete 60: None**

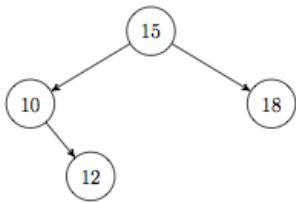


Delete 120: Double

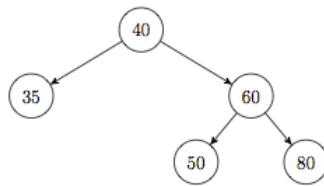


## Question 2

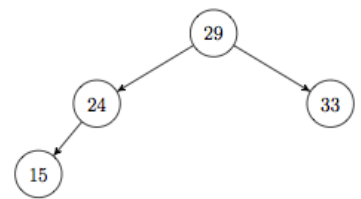
Draw the resulting AVL trees after the following operations:



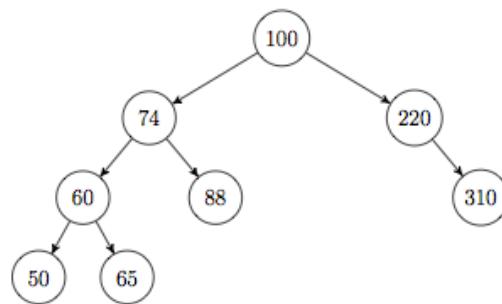
Insert 11



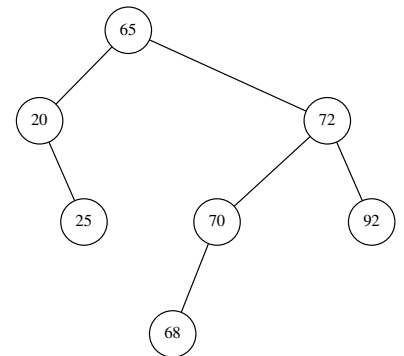
Insert 85



Insert 25

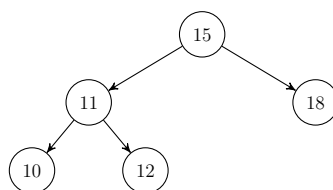


Delete 220

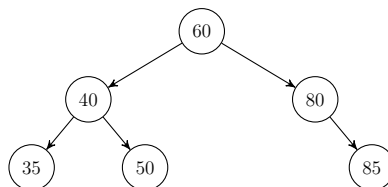


Delete 20

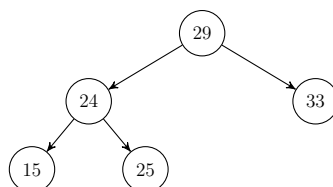
Insert 11



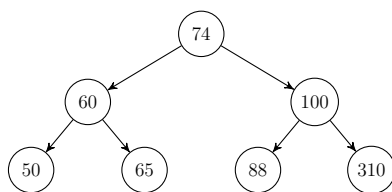
Insert 85



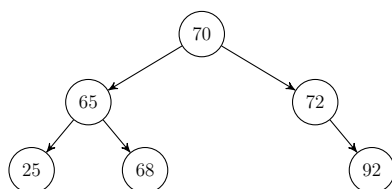
Insert 25



Delete 220



Delete 20



### Question 3

Perform the following operations on this B+ Tree: **Insert 30**, **Insert 27**, **Insert 63**, **Delete 28**, **Delete 65**. Each operation is independent, and must be performed on the original tree.

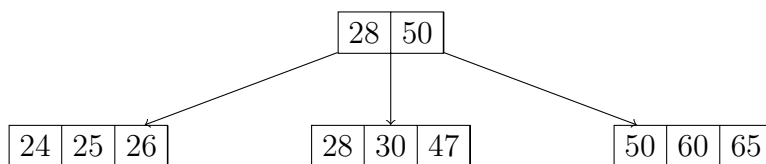
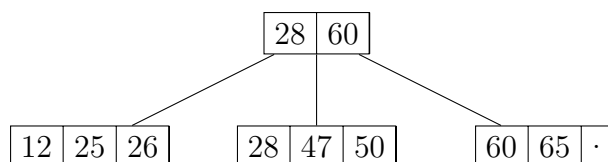


Figure 1: Insert 30 (transfer-update)

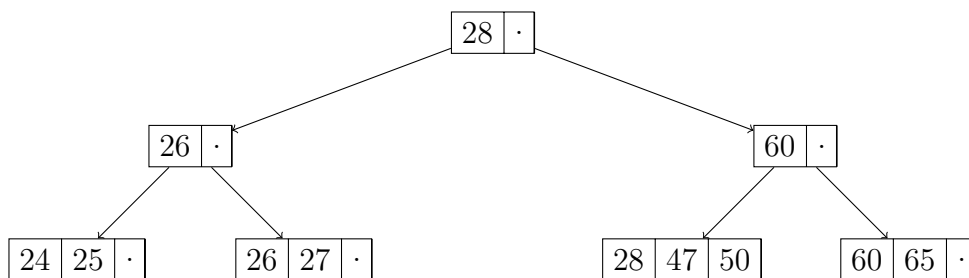


Figure 2: Insert 27 (split-split)

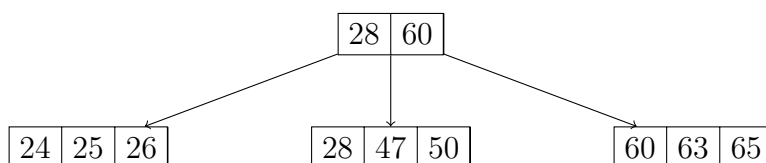


Figure 3: Insert 63 (normal)

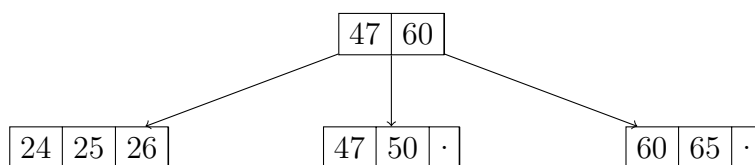


Figure 4: Delete 28 (delete-update)

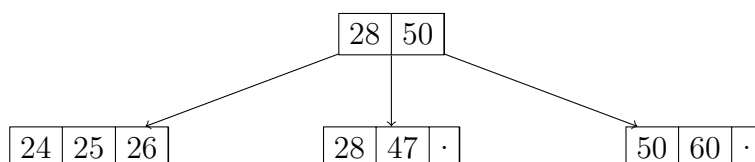


Figure 5: Delete 65 (borrow-update)

### Question 4

Using the following B+ Tree ( $m = 3$ ), perform the following operations: Insert 13, Insert 32, Insert 50, Insert 41, Insert 25 **show the resulting tree after each operation**

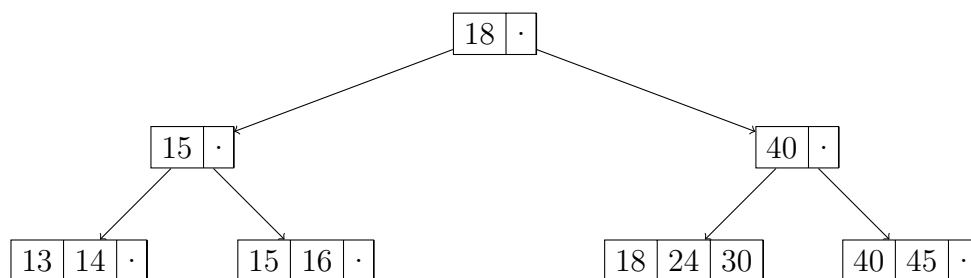
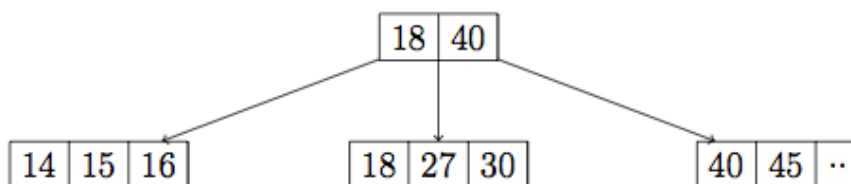


Figure 6: Insert 13

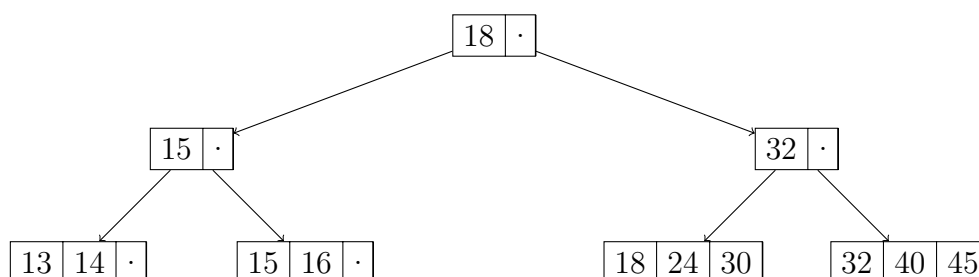


Figure 7: Insert 32

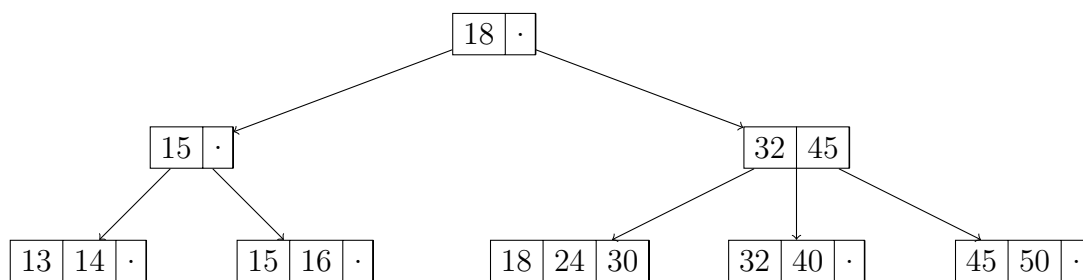


Figure 8: Insert 50

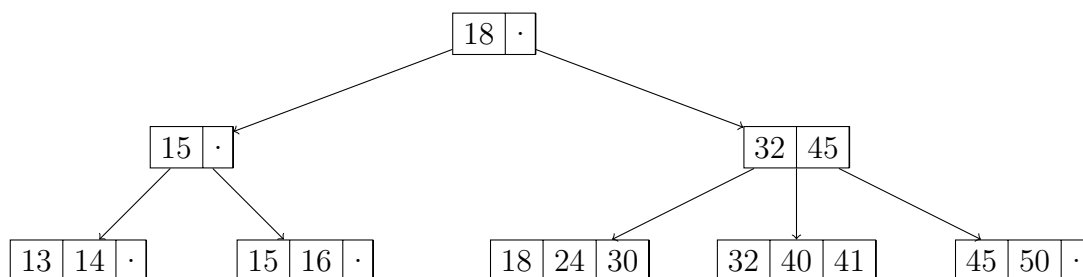


Figure 9: Insert 41

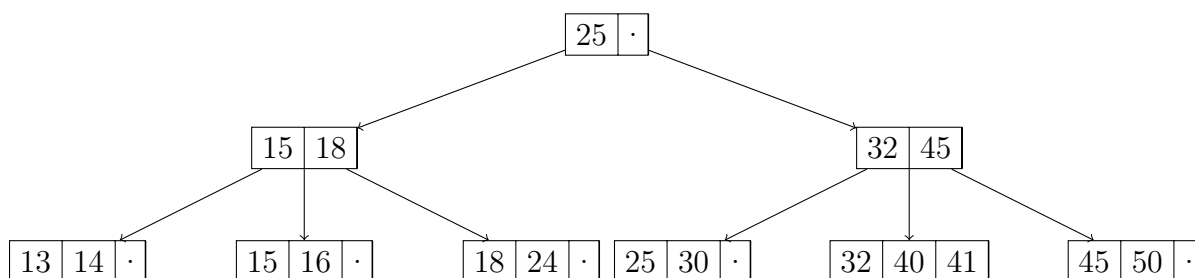


Figure 10: Insert 25 -split-transfer-update

### Question 5

Using the following B+ Tree ( $m = 3$ ), perform the following operations: Delete 45, Delete 15, Delete 30  
**show the resulting tree after each operation**

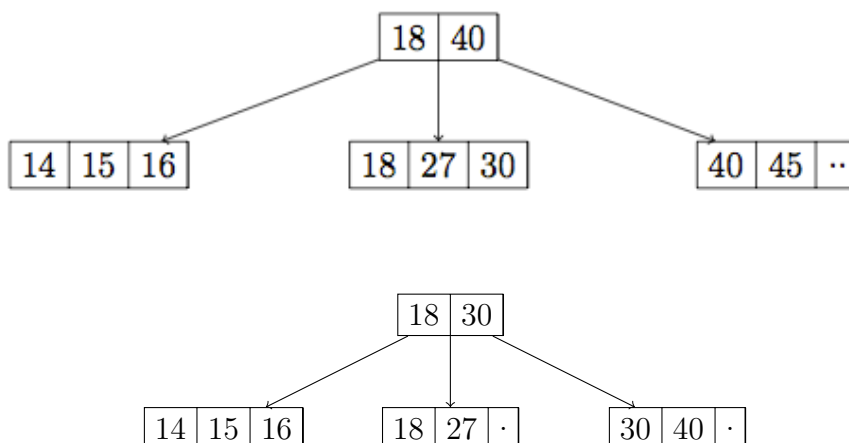


Figure 11: Delete 45

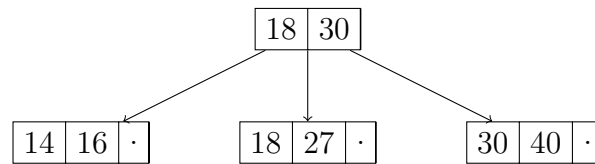


Figure 12: Delete 15

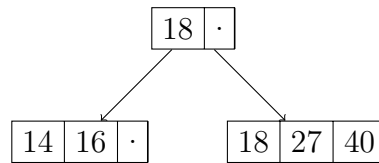


Figure 13: Delete 30