

General Trees & Binary Trees

CSC212: Data Structures

Trees

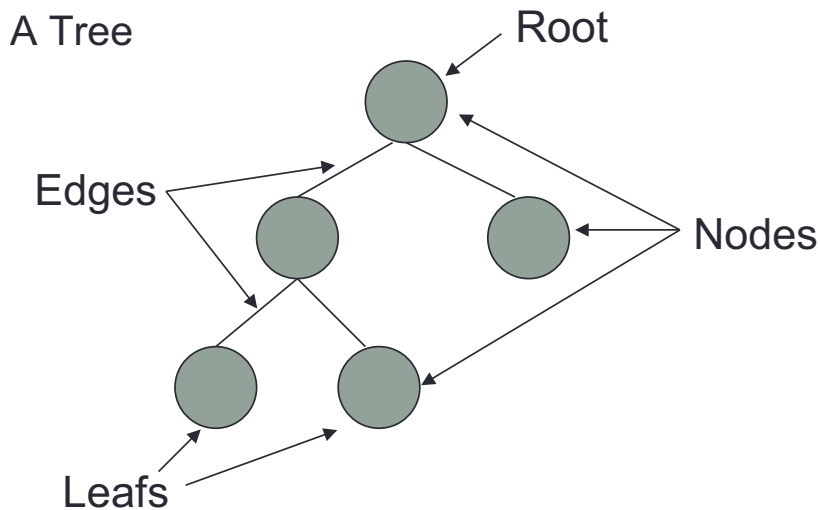
- Previous data structures (e.g. lists, stacks, queues) have a linear structure.
- Linear structures represent one-to-one relation between data elements.
- Trees have a nested or a hierarchical structure.
- Hierarchical structures represent one-to-many relation between data elements.

Trees

- Examples of situations where one-to-many relations exist... these can be represented as trees.
 - Relation between a parent and his children.
 - Relation between a person and books he owns.
 - Relation between a football team and the players on the team.
 - Card catalog in a library.

Trees: Some Terminology

- A tree is represented as a set of nodes connected by edges.



Trees: Comparison with Lists

A List

- ▶ Unique first element.
- ▶ Unique last element.
- ▶ Each element, other than the first and the last, has a unique predecessor and a unique successor.

A Tree

- ▶ Unique first node called root.
- ▶ Each node has successors, called its children.
- ▶ Each node has one predecessor, called parent.
- ▶ Leafs have no children.
- ▶ Root has no parent.

Trees: More Terminology

- Simple path: a sequence of distinct nodes in the tree.
- Path length: number of nodes in a path.
- Siblings: two nodes that have the same parent.
- Ancestors: given a node A in a tree, the parent of the node A and the ancestors of the parent of A, are ancestors of A.

Trees: More Terminology

Parent: a parent of a node is its predecessor.

Child: a child of a node is its successor.

Root: a unique node without any predecessor.

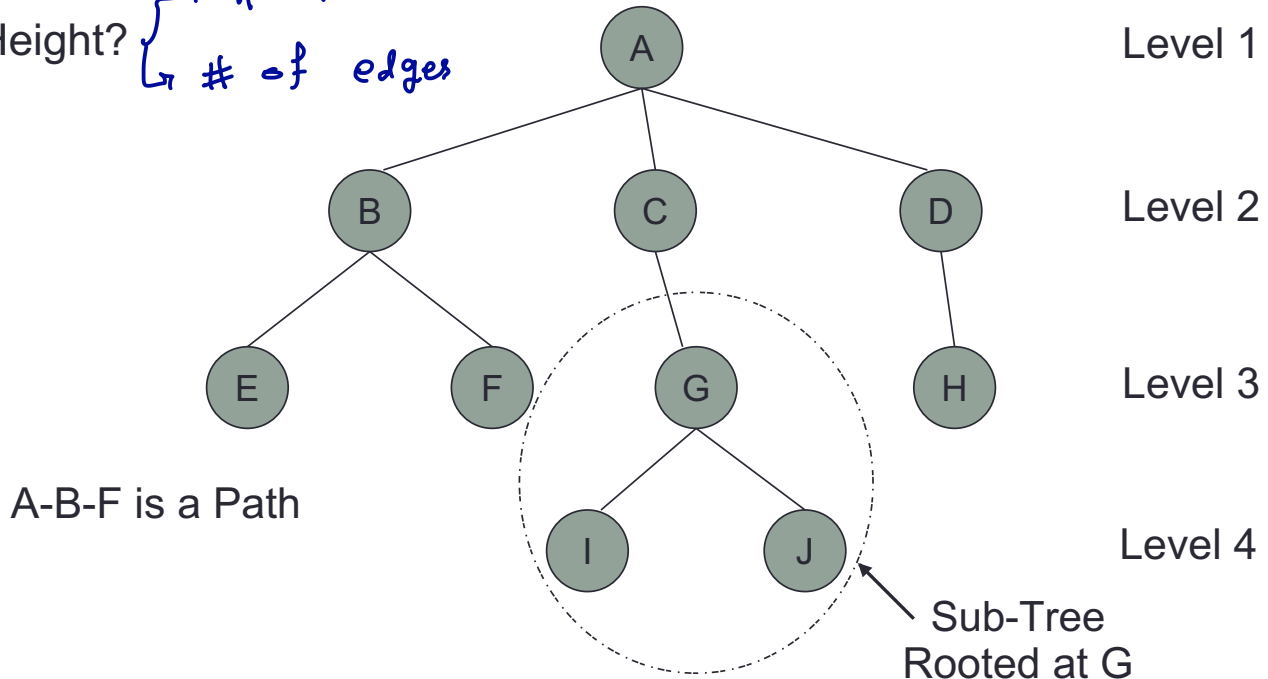
Leafs: nodes without any children.

Descendents: given a node A in a tree, the children of A and all descendents of the children of A are descendents of A.

Trees: More Terminology

two different schools:

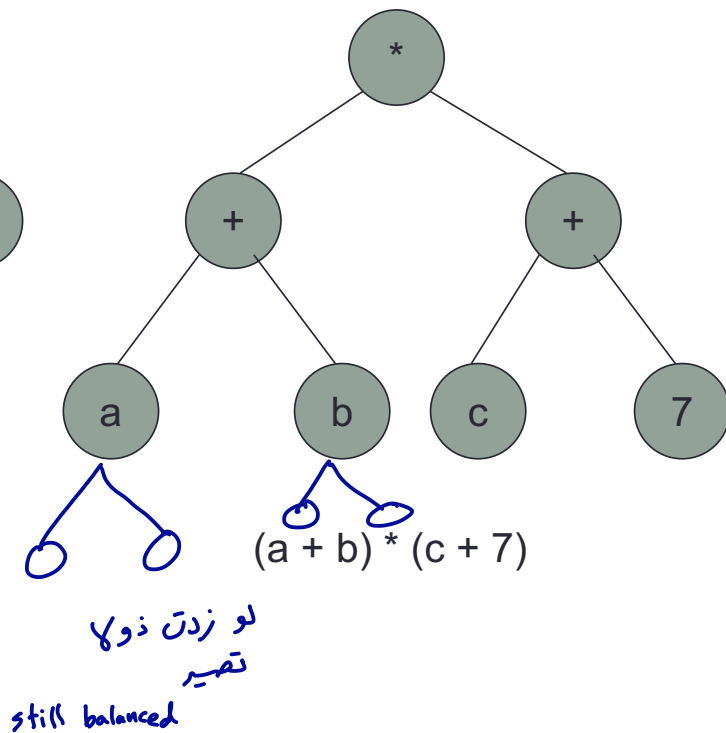
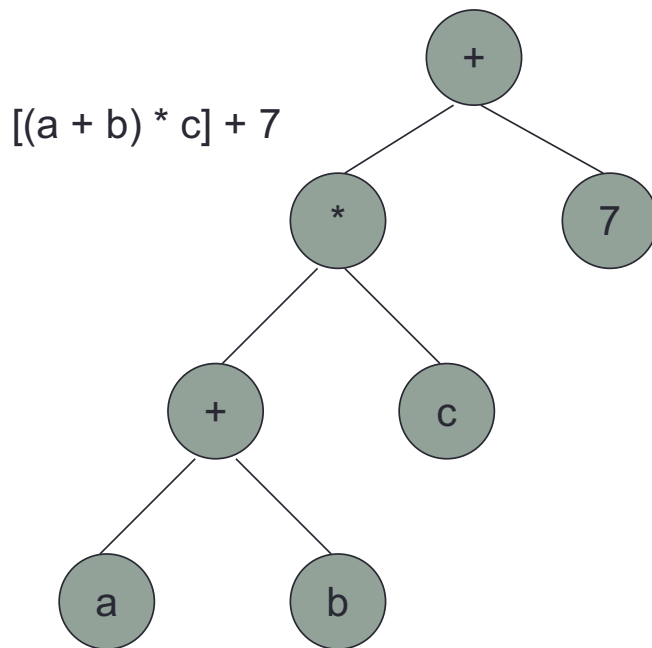
Height? $\left\{ \begin{array}{l} \rightarrow \# \text{ of nodes} \\ \rightarrow \# \text{ of edges} \end{array} \right.$



Binary Trees

- A binary tree is a tree with the following:
 1. Each node can have at most two subtrees and therefore at most two children.
 2. Each subtree is identified as being either the left subtree or the right subtree of the parent.
 3. It may be empty.
- Nodes in a binary tree may be composite e.g. of variable type 'Type'.

Binary Trees



ADT Binary Tree

Elements: The elements are nodes, each node contains the following data type: Type and has LeftChild and RightChild references.

Structure: hierarchical structure; each node can have two children: left or right child; there is a root node and a current node.

Domain: the number of nodes in a binary tree is bounded; domain contains empty tree, trees with one element, two elements, ...

ADT Binary Tree

Operations:

1. Method Traverse (Order ord)

requires: Binary Tree (BT) is not empty.

input: ord. *order*

results: Each element in the tree is processed exactly once by a user supplied procedure. The order in which nodes are processed depends on the value of ord (Order = {preorder, postorder, inorder})

preorder: each node processed **before** any node in either of its subtrees. *Parent → Left child → right child*

inorder: each node is processed **after** all its nodes in its **left** subtree and **before** any node in its **right** subtree. *Left child → Parent → right child*

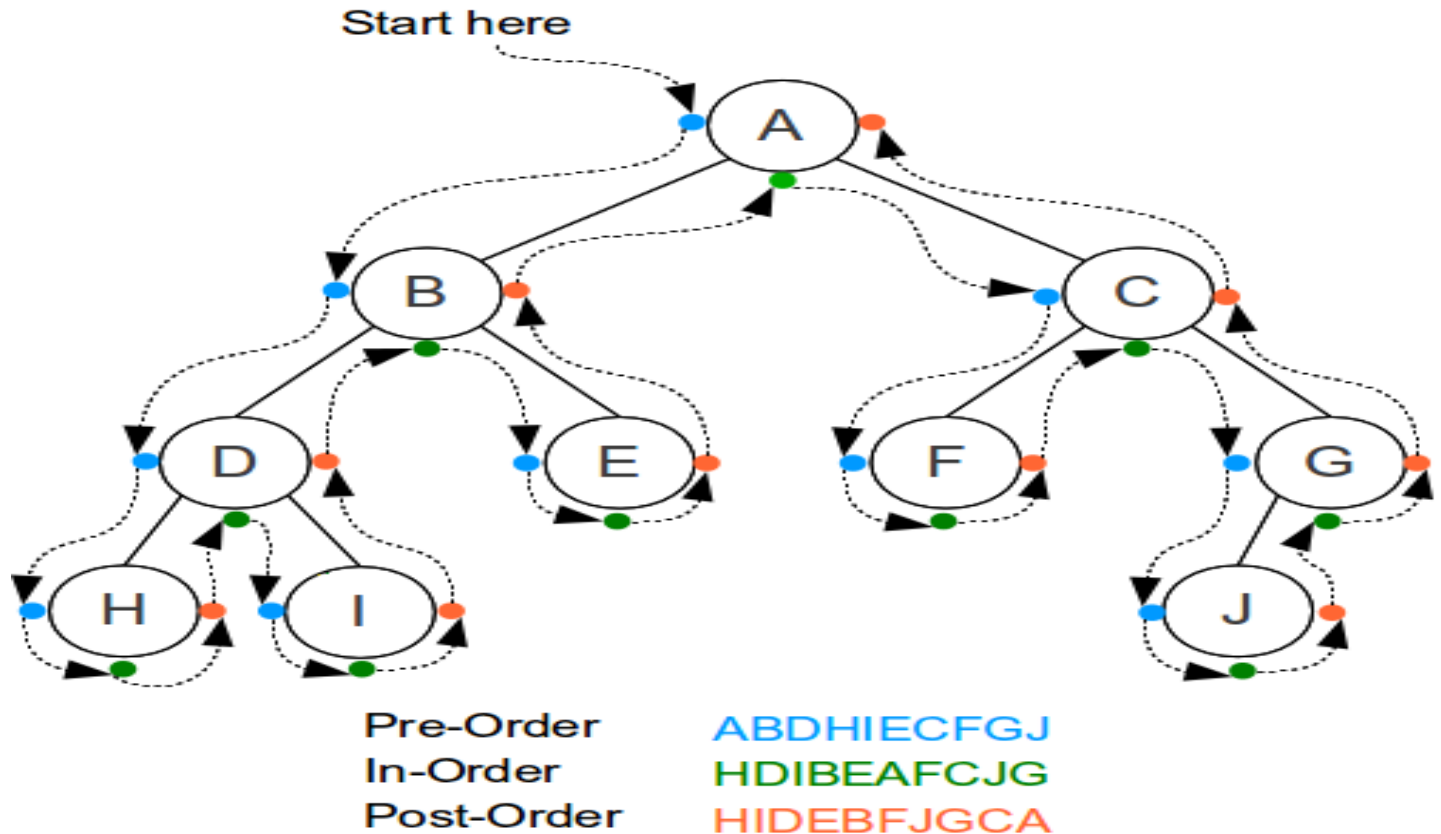
postorder: each node is processed **after** all its nodes in both of its subtrees. *Left child → right child → Parent*

output: none.

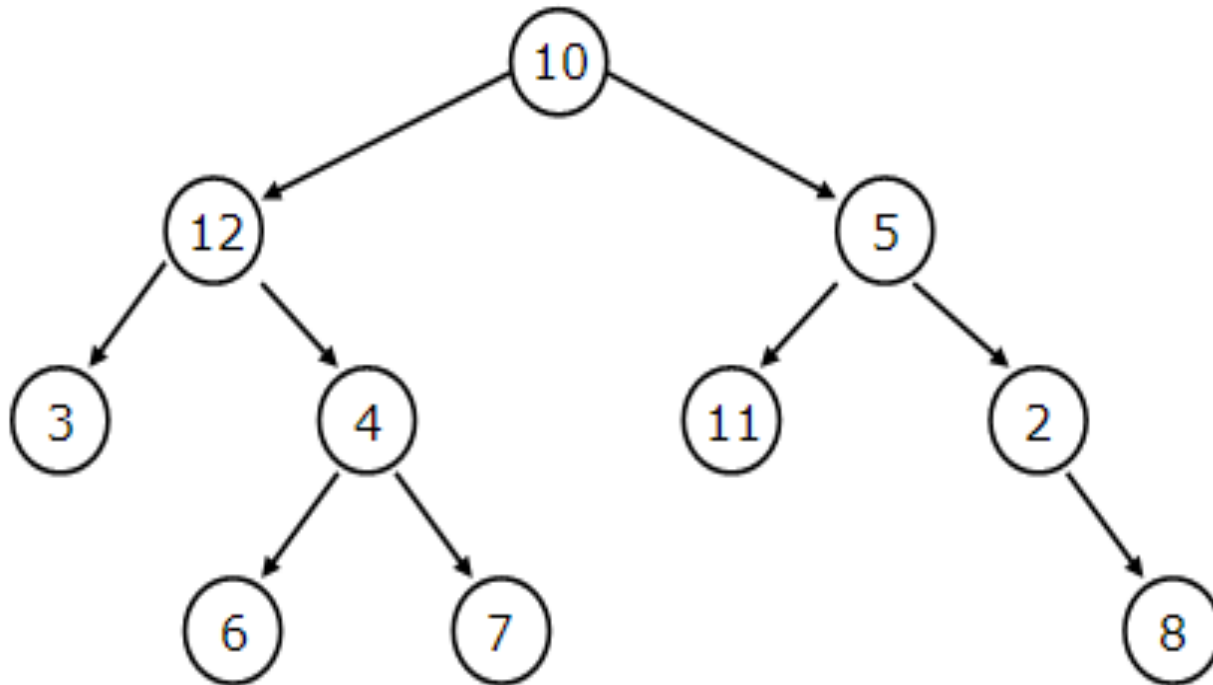
Tree Traversals

- To traverse a tree means to process (e.g. printing it) each element in the tree.
- Tree traversals
 - $n!$ ways of traversing a tree of n nodes.
 - pre-order, in-order, post-order [?] three natural traversals orders.
- List traversals
 - $n!$ ways of traversing a list of n nodes.
 - front-to-back, or back-to-front. [?] two natural traversals orders.

Tree Traversals Example



Tree Traversals Example



ADT Binary Tree

Operations:

2. Method Insert (Type e, Relative rel, boolean inserted)

(Relative = {leftchild, rightchild, root, parent})

requires: (1) Full () is false and (2) either (a) rel = root and Empty() is true or (b) rel \neq root and rel \neq parent and Empty() is false.

input: e, rel.

results: if case (1) rel = leftChild, current node has a left child, or (2) rel = rightChild, current node has a right child, then inserted is false. Else a node containing e is added as rel of the current node in the tree and becomes the current node and inserted is true.

output: inserted.

ADT Binary Tree

3. Procedure DeleteSub ()

requires: Binary tree is not empty.

input: none

results: The subtree whose root node was the current node is deleted from the tree. If the resulting tree is not empty, then the root node is the current node.

output: none.

4. Procedure Update (Type e).

requires: Binary tree is not empty.

input: e.

results: the element in e is copied into the current node.

output: none.

ADT Binary Tree

5. Procedure Retrieve (Type e)
 - requires: Binary tree is not empty.
 - input: none
 - results: element in the current node is copied into e.
 - output: e.

ADT Binary Tree

6. Procedure Find (Relative rel, boolean found)
requires: Binary tree is not empty.
input: rel.
results: The current node of the tree is determined by the value of rel and previous current node..
output: found.
7. Procedure Empty (boolean empty).
requires: None.
input: none
results: If Binary tree is empty then empty is true; otherwise empty is false.
output: empty.

ADT Binary Tree

8. Procedure Full (boolean full)
requires: None.
input: None.
results: if the binary tree is full then full is true
otherwise false.
output: full.

ADT Binary Tree: Element

```
public class BTNode <T> {  
    public T data;  
    public BTNode<T> left, right;  
  
    /** Creates a new instance of BTNode */  
    public BTNode(T val) {  
        data = val;  
        left = right = null;  
    }  
  
    public BTNode(T val, BTNode<T> l, BTNode<T> r){  
        data = val;  
        left = l;  
        right = r;  
    }  
}
```

ADT Binary Tree: Order & Relative Classes

- These definitions are in separate files and define:
 - The Order class.

```
public enum Order {preOrder, inOrder, postOrder};
```

- The Relative class.

```
public enum Relative {Root, Parent, LeftChild, RightChild};
```

ADT Binary Tree: Implementation

```
public class BT<T> {  
    BTNode<T> root, current;  
  
    /** Creates a new instance of BT */  
    public BT() {  
        root = current = null;  
    }  
  
    public boolean empty(){  
        return root == null;  
    }  
}
```

ADT Binary Tree: Implementation

```
public class BT<T> {  
    BTreeNode<T> root, current;  
  
    /** Creates a new instance of BT */  
    public BT() {  
        root = current = null;  
    }  
  
    public boolean empty(){  
        return root == null;  
    }  
}
```

R C
↓ ↓
null

ADT Binary Tree: Implementation

```

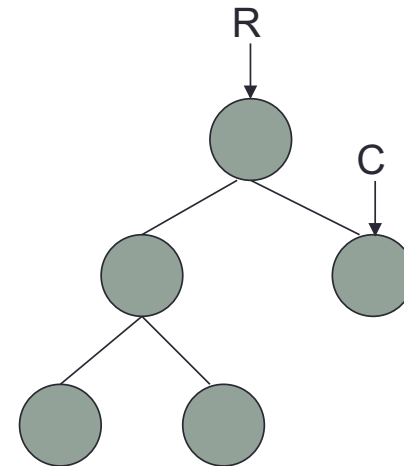
public class BT<T> {
    BTreeNode<T> root, current;

    /** Creates a new instance of BT */
    public BT() {
        root = current = null;
    }

    public boolean empty(){
        return root == null;
    }
}

```

R C
↓ ↓
null
true



false

ADT Binary Tree: Implementation

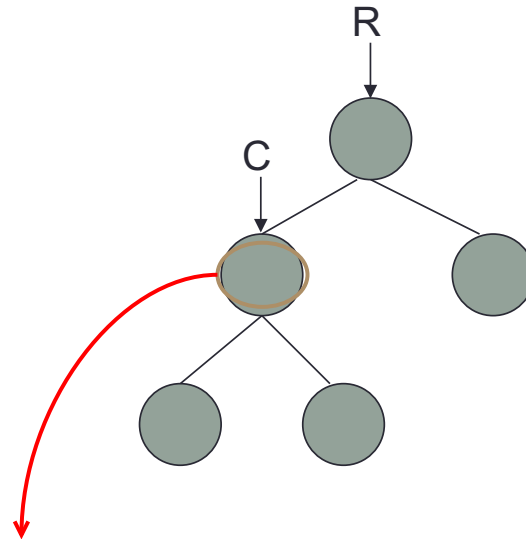
```
public T retrieve() {  
    return current.data;  
}
```

```
public void update(T val) {  
    current.data = val;  
}
```

ADT Binary Tree: Implementation

```
public T retrieve() {  
    return current.data;  
}
```

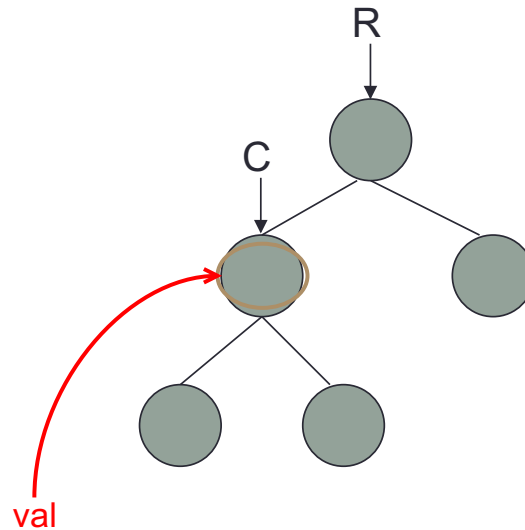
```
public void update(T val) {  
    current.data = val;  
}
```



ADT Binary Tree: Implementation

```
public T retrieve() {  
    return current.data;  
}
```

```
public void update(T val) {  
    current.data = val;  
}
```



ADT Binary Tree: Implementation

```
switch(rel) {  
    case Root:  
        if(.empty()) return false;  
        current = root = new BTreeNode<T>(val);  
        return true;  
    case Parent:    //This is an impossible case.  
        return false;  
    case LeftChild:  
        if(current.left != null) return false;  
        current.left = new BTreeNode<T>(val);  
        current = current.left;  
        return true;  
    case RightChild:  
        if(current.right != null) return false;  
        current.right = new BTreeNode<T>(val);  
        current = current.right;  
        return true;  
    default:  
        return false;  
}
```

ADT Binary Tree: Implementation

```
switch(rel) {
```

```
case Root:
```

```
if(.empty()) return false;
```

```
current = root = new BTreeNode<T>(val);
```

```
return true;
```

```
case Parent: //This is an impossible case.
```

```
return false;
```

```
case LeftChild:
```

```
if(current.left != null) return false;
```

```
current.left = new BTreeNode<T>(val);
```

```
current = current.left;
```

```
return true;
```

```
case RightChild:
```

```
if(current.right != null) return false;
```

```
current.right = new BTreeNode<T> (val);
```

```
current = current.right;
```

```
return true;
```

```
default:
```

```
return false;
```

```
}
```

Example #1

rel = Root

```

R C
↓ ↓
null

```

switch(rel) {

case Root:

if(!empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent: //This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T>(val);

current = current.right;

return true;

default:

return false;

}

ADT Binary Tree: Implementation

Example #1

rel = Root

R C



null

switch(rel) {

case Root:

if(!empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent:

//This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T>(val);

current = current.right;

return true;

default:

return false;

}

ADT Binary Tree: Implementation

Example #1

rel = Root



ADT Binary Tree: Implementation

```
switch(rel) {
```

```
case Root:
```

```
if(.empty()) return false;
```

```
current = root = new BTreeNode<T>(val);
```

```
return true;
```

```
case Parent: //This is an impossible case.
```

```
return false;
```

```
case LeftChild:
```

```
if(current.left != null) return false;
```

```
current.left = new BTreeNode<T>(val);
```

```
current = current.left;
```

```
return true;
```

```
case RightChild:
```

```
if(current.right != null) return false;
```

```
current.right = new BTreeNode<T> (val);
```

```
current = current.right;
```

```
return true;
```

```
default:
```

```
return false;
```

```
}
```

Example #2

rel = LeftChild



switch(rel) {

case Root:

if(.empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent:

//This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T> (val);

current = current.right;

return true;

default:

return false;

}

ADT Binary Tree: Implementation

Example #2

rel = LeftChild



switch(rel) {

case Root:

if(.empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent: //This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T> (val);

current = current.right;

return true;

default:

return false;

}

ADT Binary Tree: Implementation

Example #2

rel = LeftChild



switch(rel) {

case Root:

if(!empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent:

//This is an impossible case

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T>(val);

current = current.right;

return true;

default:

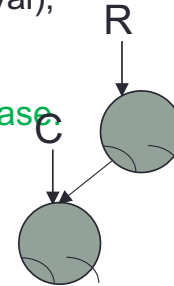
return false;

}

ADT Binary Tree: Implementation

Example #2

rel = LeftChild



switch(rel) {

case Root:

if(.empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent:

//This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T> (val);

current = current.right;

return true;

default:

return false;

}

ADT Binary Tree: Implementation

Example #3

rel = RightChild



switch(rel) {

case Root:

if(.empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent:

//This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T> (val);

current = current.right;

return true;

default:

return false;

}

ADT Binary Tree: Implementation

Example #3

rel = RightChild



switch(rel) {

case Root:

if(.empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent:

//This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T>(val);

current = current.right;

return true;

default:

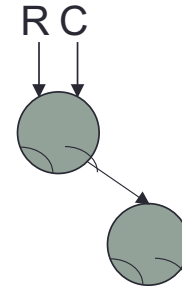
return false;

}

ADT Binary Tree: Implementation

Example #3

rel = RightChild



switch(rel) {

case Root:

if(.empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent:

//This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T> (val);

current = current.right;

return true;

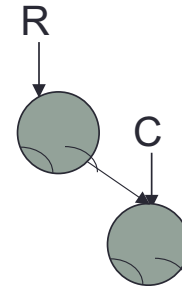
default:

return false;

}

ADT Binary Tree: Implementation

Example #3
rel = RightChild



switch(rel) {

case Root:

if(.empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent:

//This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T> (val);

current = current.right;

return true;

default:

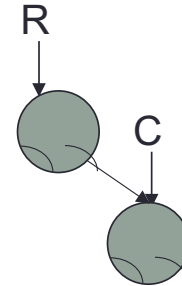
return false;

}

ADT Binary Tree: Implementation

Example #4

rel = Parent



switch(rel) {

case Root:

if(.empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent: //This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T>(val);

current = current.right;

return true;

default:

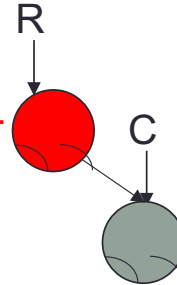
return false;

}

ADT Binary Tree: Implementation

Example #4

rel = Parent



switch(rel) {

case Root:

if(!empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent: //This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T>(val);

current = current.right;

return true;

default:

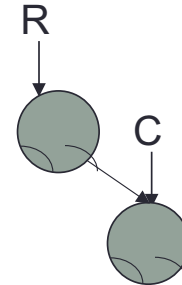
return false;

}

ADT Binary Tree: Implementation

Example #5

rel = LeftChild



switch(rel) {

case Root:

if(!empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent: //This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T>(val);

current = current.right;

return true;

default:

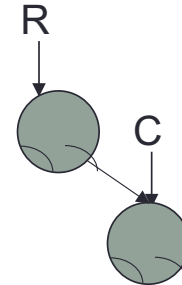
return false;

}

ADT Binary Tree: Implementation

Example #5

rel = LeftChild



switch(rel) {

case Root:

if(.empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent: //This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T>(val);

current = current.right;

return true;

default:

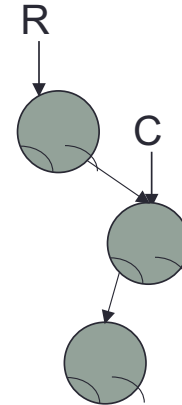
return false;

}

ADT Binary Tree: Implementation

Example #5

rel = LeftChild



switch(rel) {

case Root:

if(!empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent: //This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T>(val);

current = current.right;

return true;

default:

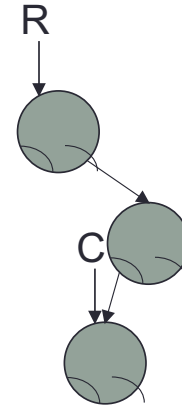
return false;

}

ADT Binary Tree: Implementation

Example #5

rel = LeftChild



switch(rel) {

case Root:

if(.empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent: //This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T>(val);

current = current.right;

return true;

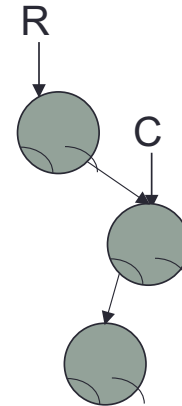
default:

return false;

}

ADT Binary Tree: Implementation

Find Parent



switch(rel) {

case Root:

if(.empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent: //This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T> (val);

current = current.right;

return true;

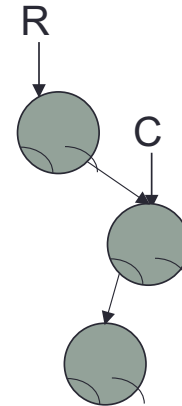
default:

return false;

}

ADT Binary Tree: Implementation

Example #6
rel = RightChild



ADT Binary Tree: Implementation

```
switch(rel) {
```

```
case Root:
```

```
if(.empty()) return false;
```

```
current = root = new BTreeNode<T>(val);
```

```
return true;
```

```
case Parent: //This is an impossible case.
```

```
return false;
```

```
case LeftChild:
```

```
if(current.left != null) return false;
```

```
current.left = new BTreeNode<T>(val);
```

```
current = current.left;
```

```
return true;
```

```
case RightChild:
```

```
if(current.right != null) return false;
```

```
current.right = new BTreeNode<T> (val);
```

```
current = current.right;
```

```
return true;
```

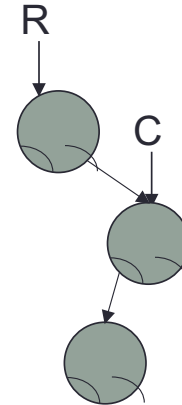
```
default:
```

```
return false;
```

```
}
```

Example #6

rel = RightChild



switch(rel) {

case Root:

if(!empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent: //This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T>(val);

current = current.right;

return true;

default:

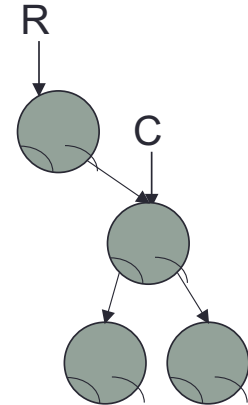
return false;

}

ADT Binary Tree: Implementation

Example #6

rel = RightChild



switch(rel) {

case Root:

if(.empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent: //This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T> (val);

current = current.right;

return true;

default:

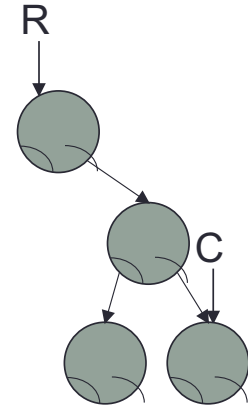
return false;

}

ADT Binary Tree: Implementation

Example #6

rel = RightChild



switch(rel) {

case Root:

if(.empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent: //This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T> (val);

current = current.right;

return true;

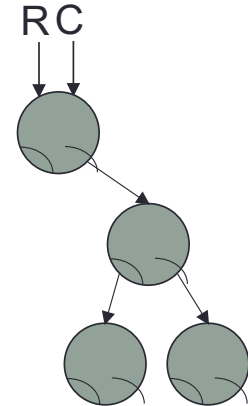
default:

return false;

}

ADT Binary Tree: Implementation

Find Root



switch(rel) {

case Root:

if(.empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent: //This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T> (val);

current = current.right;

return true;

default:

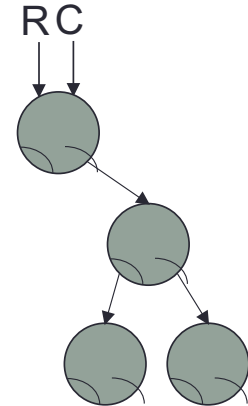
return false;

}

ADT Binary Tree: Implementation

Example #7

rel = LeftChild



switch(rel) {

case Root:

if(.empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent: //This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T> (val);

current = current.right;

return true;

default:

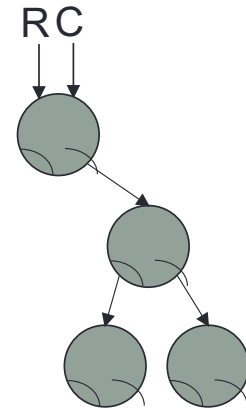
return false;

}

ADT Binary Tree: Implementation

Example #7

rel = LeftChild



switch(rel) {

case Root:

if(.empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent: //This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T>(val);

current = current.right;

return true;

default:

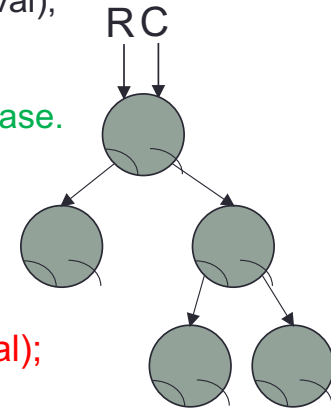
return false;

}

ADT Binary Tree: Implementation

Example #7

rel = LeftChild



switch(rel) {

case Root:

if(!empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent:

//This is an impossible case

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T>(val);

current = current.right;

return true;

default:

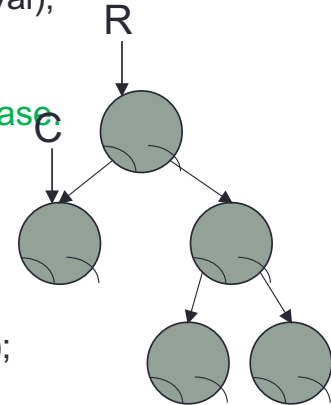
return false;

}

ADT Binary Tree: Implementation

Example #7

rel = LeftChild



switch(rel) {

case Root:

if(.empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent: //This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T>(val);

current = current.right;

return true;

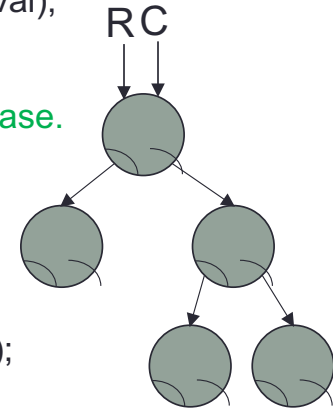
default:

return false;

}

ADT Binary Tree: Implementation

Find Root



switch(rel) {

case Root:

if(.empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent: //This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T> (val);

current = current.right;

return true;

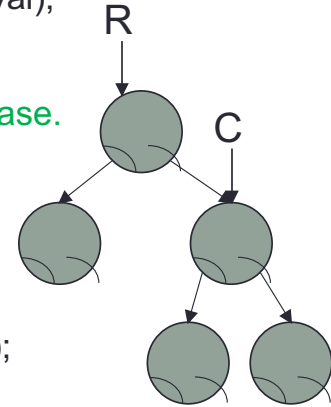
default:

return false;

}

ADT Binary Tree: Implementation

Find RightChild



switch(rel) {

case Root:

if(.empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent: //This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T>(val);

current = current.right;

return true;

default:

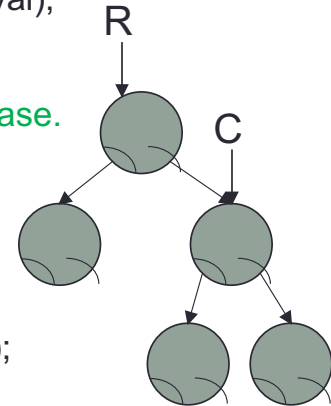
return false;

}

ADT Binary Tree: Implementation

Example #8

rel = LeftChild



switch(rel) {

case Root:

if(.empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent:

//This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T> (val);

current = current.right;

return true;

default:

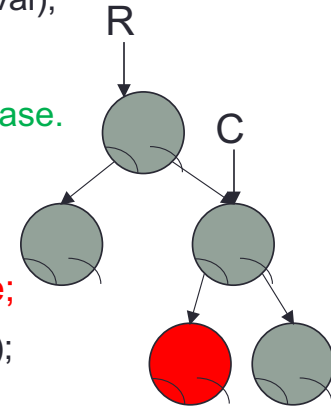
return false;

}

ADT Binary Tree: Implementation

Example #8

rel = LeftChild



switch(rel) {

case Root:

if(.empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent:

//This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T> (val);

current = current.right;

return true;

default:

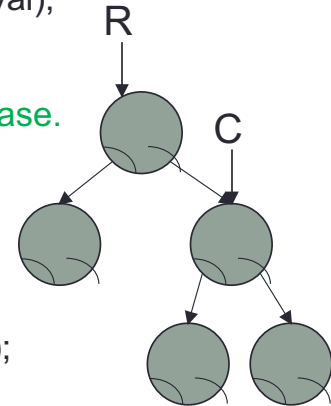
return false;

}

ADT Binary Tree: Implementation

Example #9

rel = RightChild



switch(rel) {

case Root:

if(.empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent:

//This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T> (val);

current = current.right;

return true;

default:

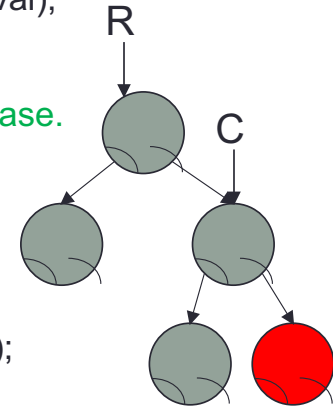
return false;

}

ADT Binary Tree: Implementation

Example #9

rel = RightChild



switch(rel) {

case Root:

if(.empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent:

//This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T> (val);

current = current.right;

return true;

default:

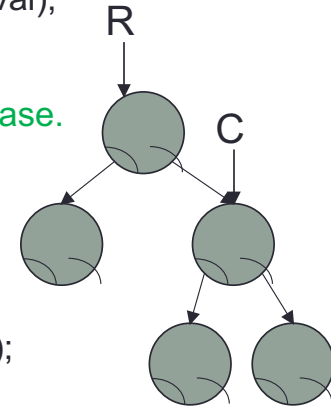
return false;

}

ADT Binary Tree: Implementation

Example #10

rel = Parent



switch(rel) {

case Root:

if(.empty()) return false;

current = root = new BTreeNode<T>(val);

return true;

case Parent: //This is an impossible case.

return false;

case LeftChild:

if(current.left != null) return false;

current.left = new BTreeNode<T>(val);

current = current.left;

return true;

case RightChild:

if(current.right != null) return false;

current.right = new BTreeNode<T>(val);

current = current.right;

return true;

default:

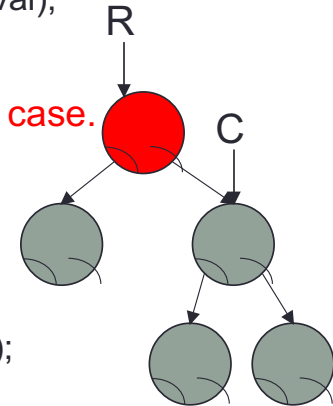
return false;

}

ADT Binary Tree: Implementation

Example #10

rel = Parent



ADT Binary Tree: Implementation

```
public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTNode<T> p = current;
        find(Relative.Parent);// current = findparent(current, root);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}
```

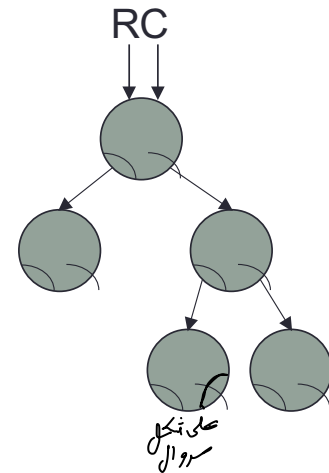
ADT Binary Tree: Implementation

Example #1

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTreeNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```



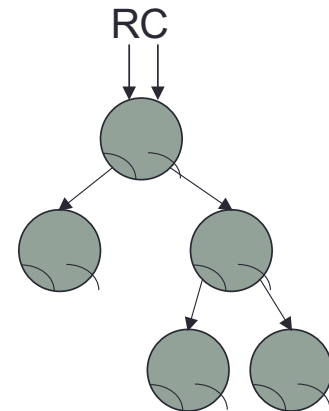
ADT Binary Tree: Implementation

Example #1

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTreeNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```



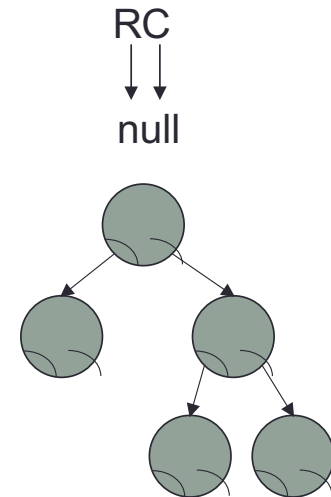
ADT Binary Tree: Implementation

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTreeNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```

Example #1



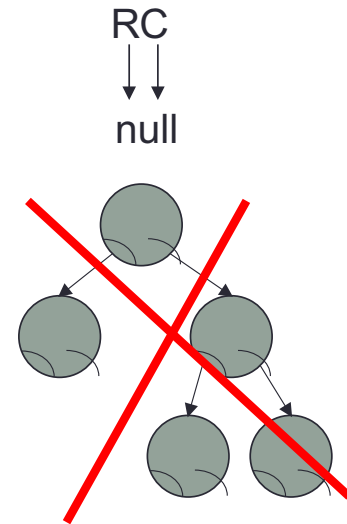
ADT Binary Tree: Implementation

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```

Example #1



ADT Binary Tree: Implementation

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTreeNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

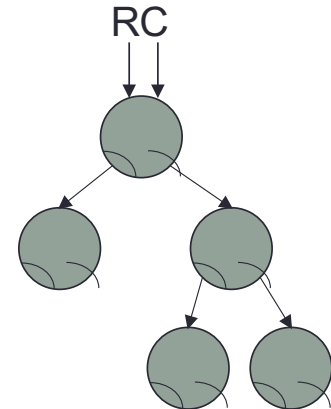
```

Example #1

RC
 ↓ ↓
 null

ADT Binary Tree: Implementation

```
public void deleteSubtree(){  
    if(current == root){  
        current = root = null;  
    }  
    else {  
        BTreeNode<T> p = current;  
        find(Relative.Parent);  
        if(current.left == p)  
            current.left = null;  
        else  
            current.right = null;  
        current = root;  
    }  
}
```



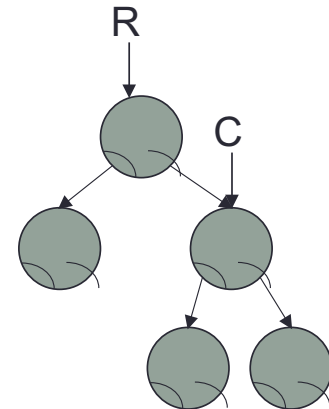
ADT Binary Tree: Implementation

Find RightChild

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTreeNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```



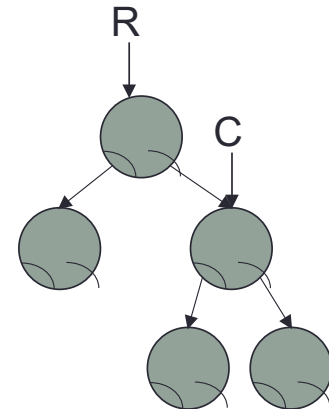
ADT Binary Tree: Implementation

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTreeNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```

Example #2



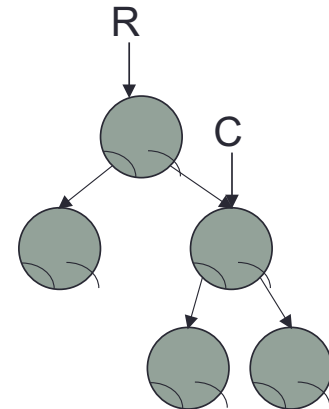
ADT Binary Tree: Implementation

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTreeNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```

Example #2



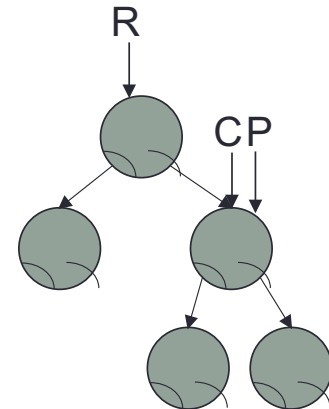
ADT Binary Tree: Implementation

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```

Example #2



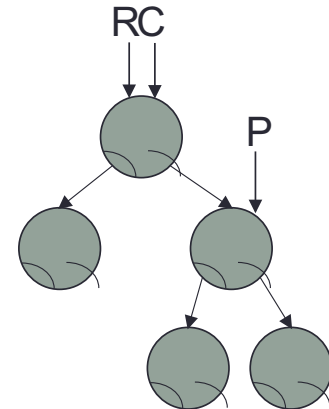
ADT Binary Tree: Implementation

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```

Example #2



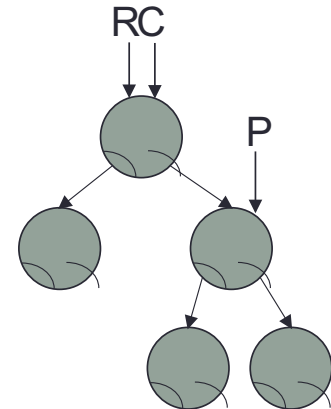
ADT Binary Tree: Implementation

Example #2

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTreeNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```



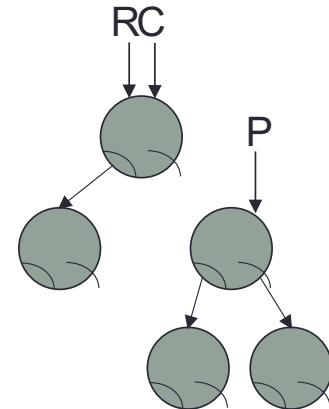
ADT Binary Tree: Implementation

Example #2

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTreeNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```



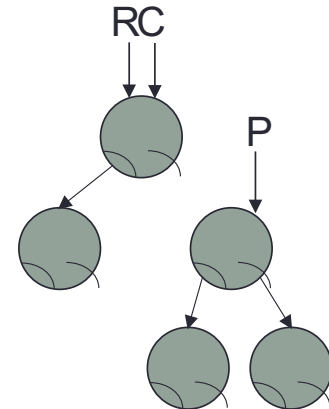
ADT Binary Tree: Implementation

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTreeNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```

Example #2



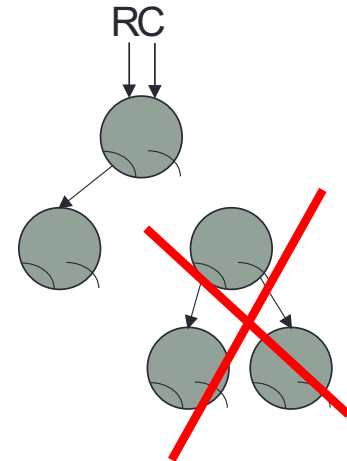
ADT Binary Tree: Implementation

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTreeNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```

Example #2

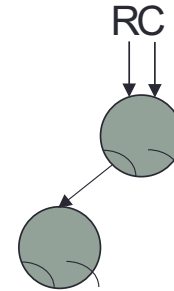


ADT Binary Tree: Implementation

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```



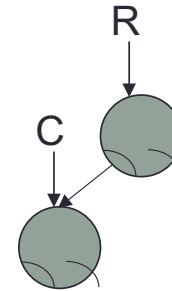
ADT Binary Tree: Implementation

Find LeftChild

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTreeNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```



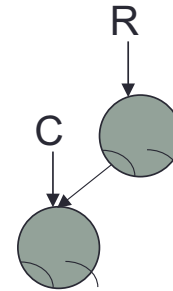
ADT Binary Tree: Implementation

Example #3

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```



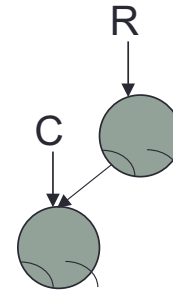
ADT Binary Tree: Implementation

Example #3

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```



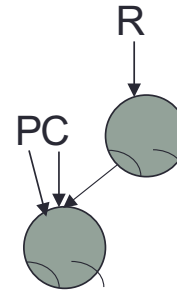
ADT Binary Tree: Implementation

Example #3

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```



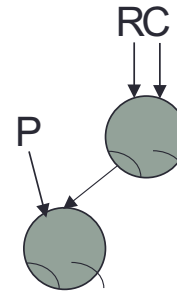
ADT Binary Tree: Implementation

Example #3

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```



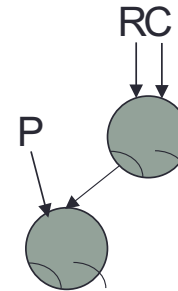
ADT Binary Tree: Implementation

Example #3

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```



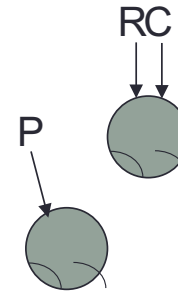
ADT Binary Tree: Implementation

Example #3

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```



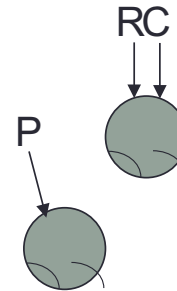
ADT Binary Tree: Implementation

Example #3

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTreeNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```



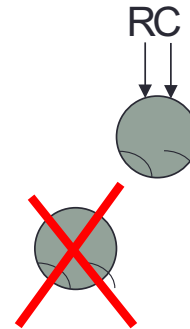
ADT Binary Tree: Implementation

Example #3

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTreeNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```



ADT Binary Tree: Implementation

Example #4

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTreeNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```



ADT Binary Tree: Implementation

Example #4

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTreeNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```



ADT Binary Tree: Implementation

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTreeNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```

Example #4



ADT Binary Tree: Implementation

```

public void deleteSubtree(){
    if(current == root){
        current = root = null;
    }
    else {
        BTreeNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
            current.left = null;
        else
            current.right = null;
        current = root;
    }
}

```

Example #4

RC
 ↓ ↓
 null

ADT Binary Tree: Implementation

```
switch (rel) {  
    case Root: // Easy case  
        current = root;  
        return true;  
    case Parent:  
        if(current == root) return false;  
        current = findparent(current, root);  
        return true;  
    case LeftChild:  
        if(current.left == null) return false;  
        current = current.left;  
        return true;  
    case RightChild:  
        if(current.right == null) return false;  
        current = current.right;  
        return true;  
    default:  
        return false;  
}
```

switch (rel) {

case Root: // Easy case

current = root;

return true;

case Parent:

if(current == root) return false;

current = findparent(current, root);

return true;

case LeftChild:

if(current.left == null) return false;

current = current.left;

return true;

case RightChild:

if(current.right == null) return false;

current = current.right;

return true;

default:

return false;

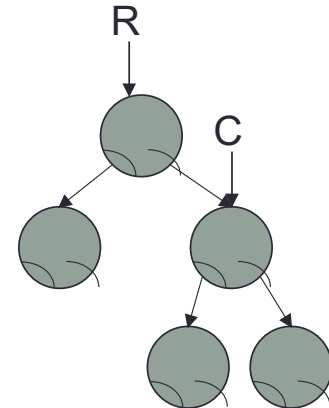
}

}

ADT Binary Tree: Implementation

Example #1

rel = Root



switch (rel) {

case Root: // Easy case

current = root;

return true;

case Parent:

if(current == root) return false;

current = findparent(current, root);

return true;

case LeftChild:

if(current.left == null) return false;

current = current.left;

return true;

case RightChild:

if(current.right == null) return false;

current = current.right;

return true;

default:

return false;

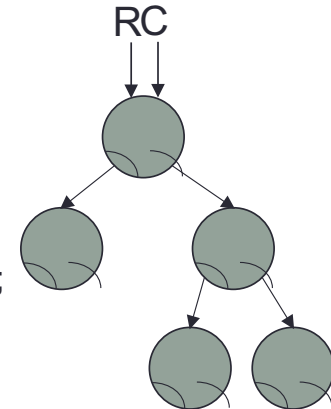
}

}

ADT Binary Tree: Implementation

Example #1

rel = Root



switch (rel) {

case Root: // Easy case

current = root;

return true;

case Parent:

if(current == root) return false;

current = findparent(current, root);

return true;

case LeftChild:

if(current.left == null) return false;

current = current.left;

return true;

case RightChild:

if(current.right == null) return false;

current = current.right;

return true;

default:

return false;

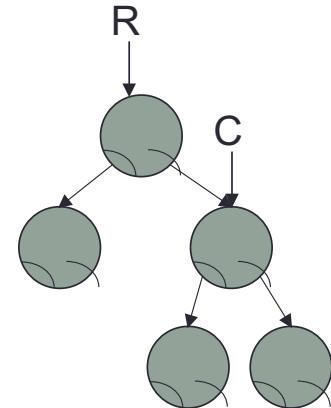
}

}

ADT Binary Tree: Implementation

Example #2

rel = LeftChild



switch (rel) {

case Root: // Easy case

current = root;

return true;

case Parent:

if(current == root) return false;

current = findparent(current, root);

return true;

case LeftChild:

if(current.left == null) return false;

current = current.left;

return true;

case RightChild:

if(current.right == null) return false;

current = current.right;

return true;

default:

return false;

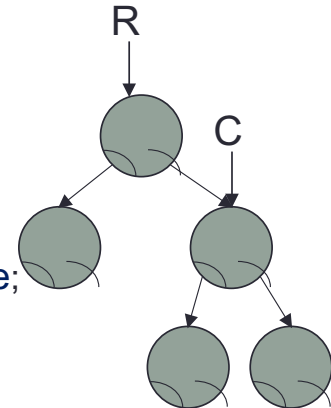
}

}

ADT Binary Tree: Implementation

Example #2

rel = LeftChild



```
switch (rel) {
```

```
case Root:           // Easy case
```

```
    current = root;
```

```
    return true;
```

```
case Parent:
```

```
    if(current == root) return false;
```

```
    current = findparent(current, root);
```

```
    return true;
```

```
case LeftChild:
```

```
    if(current.left == null) return false;
```

```
    current = current.left;
```

```
    return true;
```

```
case RightChild:
```

```
    if(current.right == null) return false;
```

```
    current = current.right;
```

```
    return true;
```

```
default:
```

```
    return false;
```

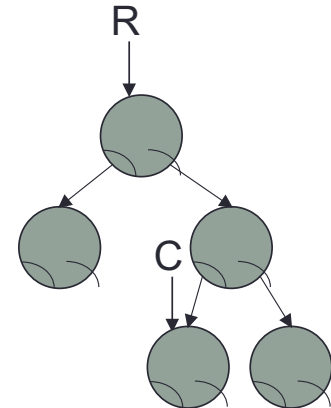
```
}
```

```
}
```

ADT Binary Tree: Implementation

Example #2

rel = LeftChild



switch (rel) {

case Root: // Easy case

current = root;

return true;

case Parent:

if(current == root) return false;

current = findparent(current, root);

return true;

case LeftChild:

if(current.left == null) return false;

current = current.left;

return true;

case RightChild:

if(current.right == null) return false;

current = current.right;

return true;

default:

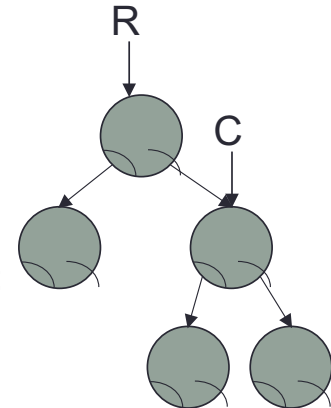
return false;

}

}

ADT Binary Tree: Implementation

Example #3
rel = RightChild



switch (rel) {

case Root: // Easy case

current = root;

return true;

case Parent:

if(current == root) return false;

current = findparent(current, root);

return true;

case LeftChild:

if(current.left == null) return false;

current = current.left;

return true;

case RightChild:

if(current.right == null) return false;

current = current.right;

return true;

default:

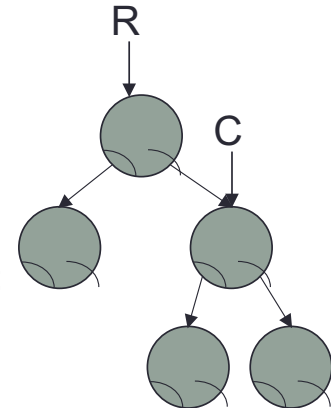
return false;

}

}

ADT Binary Tree: Implementation

Example #3
rel = RightChild



```
switch (rel) {
```

```
case Root: // Easy case
```

```
current = root;
```

```
return true;
```

```
case Parent:
```

```
if(current == root) return false;
```

```
current = findparent(current, root);
```

```
return true;
```

```
case LeftChild:
```

```
if(current.left == null) return false;
```

```
current = current.left;
```

```
return true;
```

```
case RightChild:
```

```
if(current.right == null) return false;
```

```
current = current.right;
```

```
return true;
```

```
default:
```

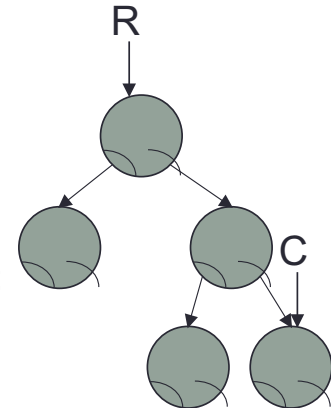
```
return false;
```

```
}
```

```
}
```

ADT Binary Tree: Implementation

Example #3
rel = RightChild



switch (rel) {

case Root: // Easy case

current = root;

return true;

case Parent:

if(current == root) return false;

current = findparent(current, root);

return true;

case LeftChild:

if(current.left == null) return false;

current = current.left;

return true;

case RightChild:

if(current.right == null) return false;

current = current.right;

return true;

default:

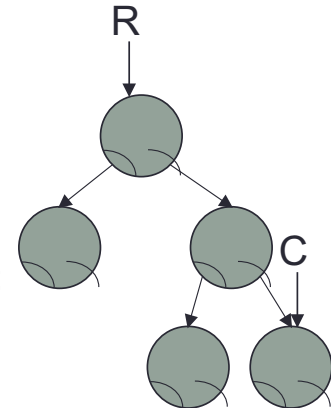
return false;

}

}

ADT Binary Tree: Implementation

Example #4
rel = RightChild



switch (rel) {

case Root:

// Easy case

current = root;

return true;

case Parent:

if(current == root) return false;

current = findparent(current, root);

return true;

case LeftChild:

if(current.left == null) return false;

current = current.left;

return true;

case RightChild:

if(current.right == null) return false;

current = current.right;

return true;

default:

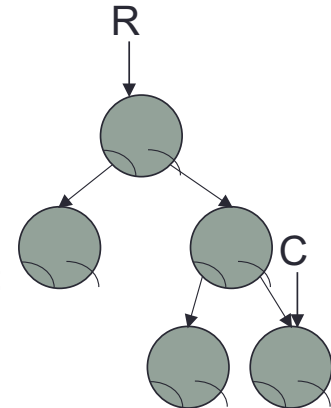
return false;

}

}

ADT Binary Tree: Implementation

Example #4
rel = RightChild



```
switch (rel) {
```

```
case Root:           // Easy case
```

```
    current = root;
```

```
    return true;
```

```
case Parent:
```

```
    if(current == root) return false;
```

```
    current = findparent(current, root);
```

```
    return true;
```

```
case LeftChild:
```

```
    if(current.left == null) return false;
```

```
    current = current.left;
```

```
    return true;
```

```
case RightChild:
```

```
    if(current.right == null) return false;
```

```
    current = current.right;
```

```
    return true;
```

```
default:
```

```
    return false;
```

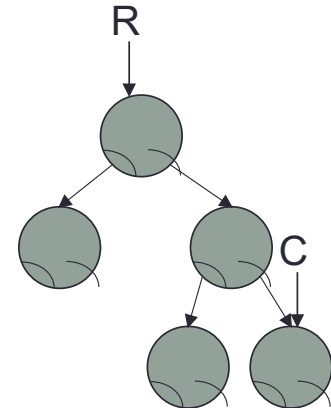
```
}
```

```
}
```

ADT Binary Tree: Implementation

Example #5

rel = LeftChild



switch (rel) {

case Root: // Easy case

current = root;

return true;

case Parent:

if(current == root) return false;

current = findparent(current, root);

return true;

case LeftChild:

if(current.left == null) return false;

current = current.left;

return true;

case RightChild:

if(current.right == null) return false;

current = current.right;

return true;

default:

return false;

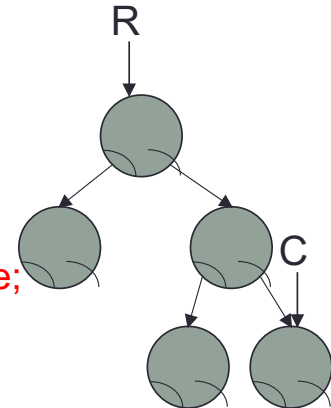
}

}

ADT Binary Tree: Implementation

Example #5

rel = LeftChild



```
switch (rel) {
```

```
case Root: // Easy case
```

```
current = root;
```

```
return true;
```

```
case Parent:
```

```
if(current == root) return false;
```

```
current = findparent(current, root);
```

```
return true;
```

```
case LeftChild:
```

```
if(current.left == null) return false;
```

```
current = current.left;
```

```
return true;
```

```
case RightChild:
```

```
if(current.right == null) return false;
```

```
current = current.right;
```

```
return true;
```

```
default:
```

```
return false;
```

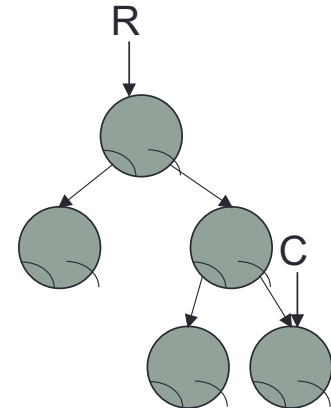
```
}
```

```
}
```

ADT Binary Tree: Implementation

Example #6

rel = Parent



```
switch (rel) {
```

```
case Root:           // Easy case
```

```
    current = root;
```

```
    return true;
```

```
case Parent:
```

```
    if(current == root) return false;
```

```
    current = findparent(current, root);
```

```
    return true;
```

```
case LeftChild:
```

```
    if(current.left == null) return false;
```

```
    current = current.left;
```

```
    return true;
```

```
case RightChild:
```

```
    if(current.right == null) return false;
```

```
    current = current.right;
```

```
    return true;
```

```
default:
```

```
    return false;
```

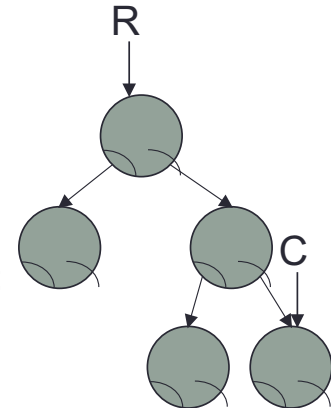
```
}
```

```
}
```

ADT Binary Tree: Implementation

Example #6

rel = Parent



switch (rel) {

case Root: // Easy case

current = root;

return true;

case Parent:

if(current == root) return false;

current = findparent(current, root);

return true;

case LeftChild:

if(current.left == null) return false;

current = current.left;

return true;

case RightChild:

if(current.right == null) return false;

current = current.right;

return true;

default:

return false;

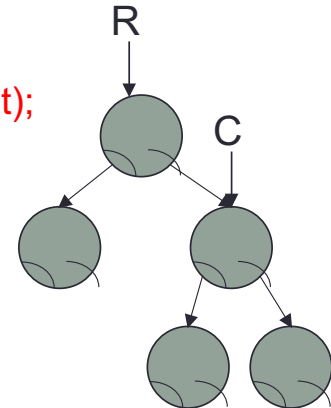
}

}

ADT Binary Tree: Implementation

Example #6

rel = Parent



```
switch (rel) {
```

```
case Root:           // Easy case
```

```
    current = root;
```

```
    return true;
```

```
case Parent:
```

```
    if(current == root) return false;
```

```
    current = findparent(current, root);
```

```
    return true;
```

```
case LeftChild:
```

```
    if(current.left == null) return false;
```

```
    current = current.left;
```

```
    return true;
```

```
case RightChild:
```

```
    if(current.right == null) return false;
```

```
    current = current.right;
```

```
    return true;
```

```
default:
```

```
    return false;
```

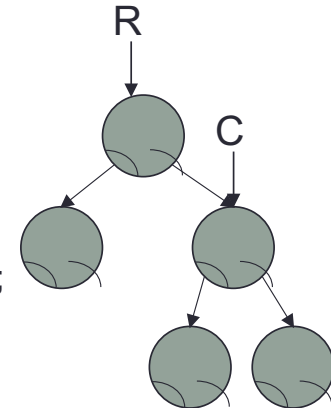
```
}
```

```
}
```

ADT Binary Tree: Implementation

Example #7

rel = Parent



switch (rel) {

case Root: // Easy case

current = root;

return true;

case Parent:

if(current == root) return false;

current = findparent(current, root);

return true;

case LeftChild:

if(current.left == null) return false;

current = current.left;

return true;

case RightChild:

if(current.right == null) return false;

current = current.right;

return true;

default:

return false;

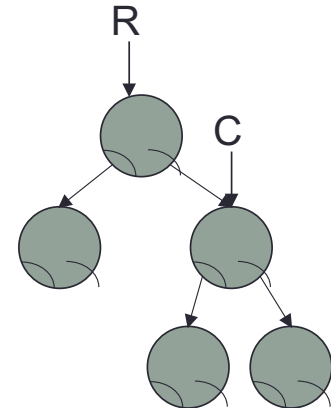
}

}

ADT Binary Tree: Implementation

Example #7

rel = Parent



switch (rel) {

case Root:

// Easy case

current = root;

return true;

case Parent:

if(current == root) return false;

current = findparent(current, root);

return true;

case LeftChild:

if(current.left == null) return false;

current = current.left;

return true;

case RightChild:

if(current.right == null) return false;

current = current.right;

return true;

default:

return false;

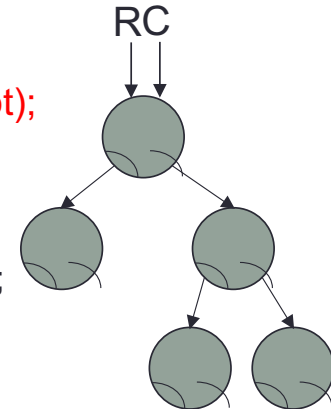
}

}

ADT Binary Tree: Implementation

Example #7

rel = Parent



```
switch (rel) {
```

```
case Root:           // Easy case
```

```
    current = root;
```

```
    return true;
```

```
case Parent:
```

```
    if(current == root) return false;
```

```
    current = findparent(current, root);
```

```
    return true;
```

```
case LeftChild:
```

```
    if(current.left == null) return false;
```

```
    current = current.left;
```

```
    return true;
```

```
case RightChild:
```

```
    if(current.right == null) return false;
```

```
    current = current.right;
```

```
    return true;
```

```
default:
```

```
    return false;
```

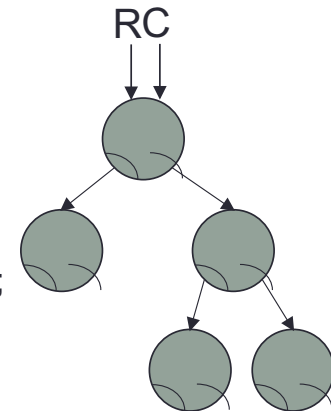
```
}
```

```
}
```

ADT Binary Tree: Implementation

Example #8

rel = Parent



switch (rel) {

case Root:

// Easy case

current = root;

return true;

case Parent:

if(current == root) return false;

current = findparent(current, root);

return true;

case LeftChild:

if(current.left == null) return false;

current = current.left;

return true;

case RightChild:

if(current.right == null) return false;

current = current.right;

return true;

default:

return false;

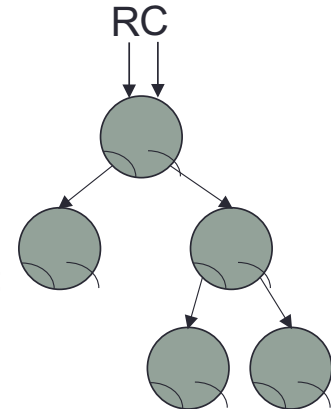
}

}

ADT Binary Tree: Implementation

Example #8

rel = Parent



ADT Binary Tree: Implementation

// Non-recursive version of findparent – uses pre-order traversal

```
private BTreeNode<T> findparent(BTreeNode<T> p, BTreeNode<T> t) {
```

// Stack is used to store the right pointers of nodes

```
    LinkStack<BTreeNode<T>> stack = new LinkStack<BTreeNode<T>>();
```

```
    BTreeNode<T> q = t;
```

```
    while(q.right != p && q.left != p) {
```

```
        if(q.right != null)
```

```
            stack.push(q.right);
```

```
        if(q.left != null)
```

```
            q = q.left;
```

```
        else
```

```
            q = stack.pop(); // Go right here
```

```
    }
```

```
    return q;
```

```
}
```

ADT Binary Tree: Implementation

// Non-recursive version of findparent – uses pre-order traversal

private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {

كانها متحمل
essentials
"مخوضها قاعه"

// Stack is used to store the right pointers of nodes

LinkStack<BTNode<T>> stack = new LinkStack<BTNode<T>>();

BTNode<T> q = t;

while(q.right != p && q.left != p) {

if(q.right != null)

 stack.push(q.right);

if(q.left != null)

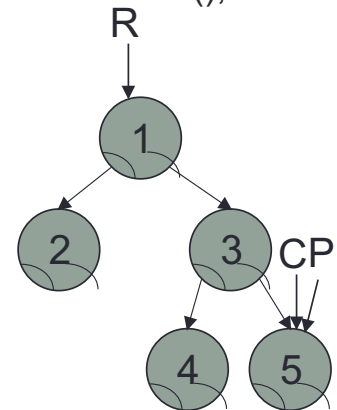
 q = q.left;

else

 q = stack.pop(); // Go right here

}

return q;



Example #1

p = current, t = root

ADT Binary Tree: Implementation

// Non-recursive version of findparent – uses pre-order traversal

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

// Stack is used to store the right pointers of nodes

```
    LinkStack<BTNode<T>> stack = new LinkStack<BTNode<T>>();
```

```
    BTNode<T> q = t;
```

```
    while(q.right != p && q.left != p) {
```

```
        if(q.right != null)
```

```
            stack.push(q.right);
```

```
        if(q.left != null)
```

```
            q = q.left;
```

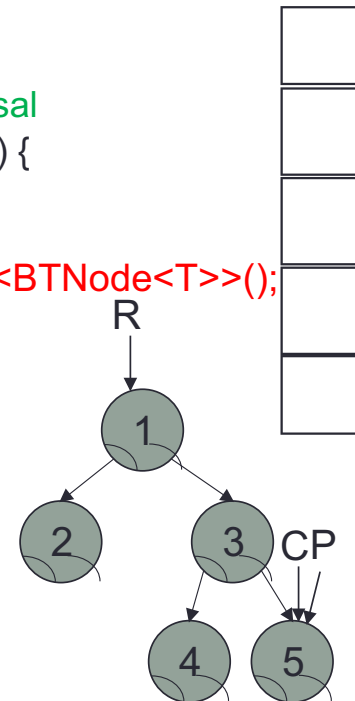
```
        else
```

```
            q = stack.pop(); // Go right here
```

```
    }
```

```
    return q;
```

```
}
```



Example #1

p = current, t = root

ADT Binary Tree: Implementation

// Non-recursive version of findparent – uses pre-order traversal

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

// Stack is used to store the right pointers of nodes

```
    LinkStack<BTNode<T>> stack = new LinkStack<BTNode<T>>();
```

```
    BTNode<T> q = t;
```

```
    while(q.right != p && q.left != p) {
```

```
        if(q.right != null)
```

```
            stack.push(q.right);
```

```
        if(q.left != null)
```

```
            q = q.left;
```

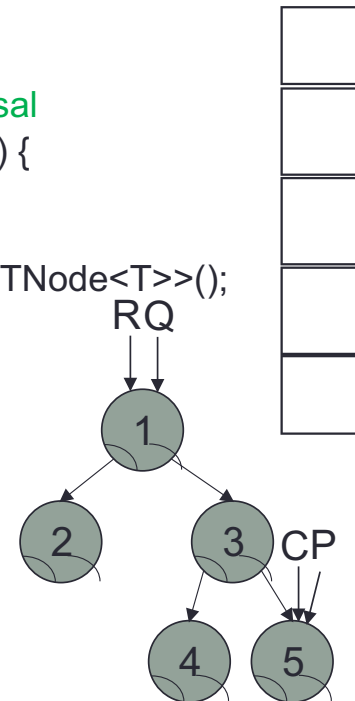
```
        else
```

```
            q = stack.pop(); // Go right here
```

```
    }
```

```
    return q;
```

```
}
```



Example #1

p = current, t = root

ADT Binary Tree: Implementation

// Non-recursive version of findparent – uses pre-order traversal

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

// Stack is used to store the right pointers of nodes

```
    LinkStack<BTNode<T>> stack = new LinkStack<BTNode<T>>();
```

```
    BTNode<T> q = t;
```

```
    while(q.right != p && q.left != p) {
```

```
        if(q.right != null)
```

```
            stack.push(q.right);
```

```
        if(q.left != null)
```

```
            q = q.left;
```

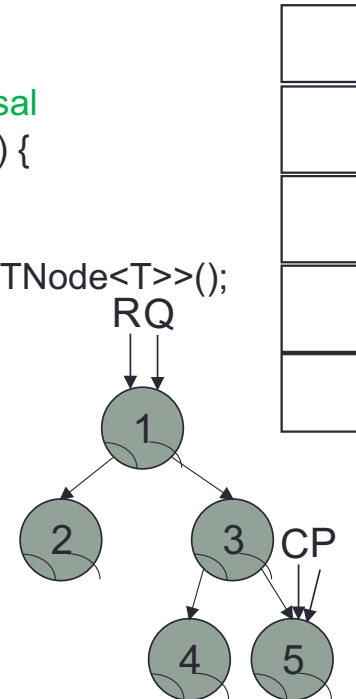
```
        else
```

```
            q = stack.pop(); // Go right here
```

```
    }
```

```
    return q;
```

```
}
```



Example #1

p = current, t = root

ADT Binary Tree: Implementation

// Non-recursive version of findparent – uses pre-order traversal

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

// Stack is used to store the right pointers of nodes

```
    LinkStack<BTNode<T>> stack = new LinkStack<BTNode<T>>();
```

```
    BTNode<T> q = t;
```

```
    while(q.right != p && q.left != p) {
```

```
        if(q.right != null)
```

```
            stack.push(q.right);
```

```
        if(q.left != null)
```

```
            q = q.left;
```

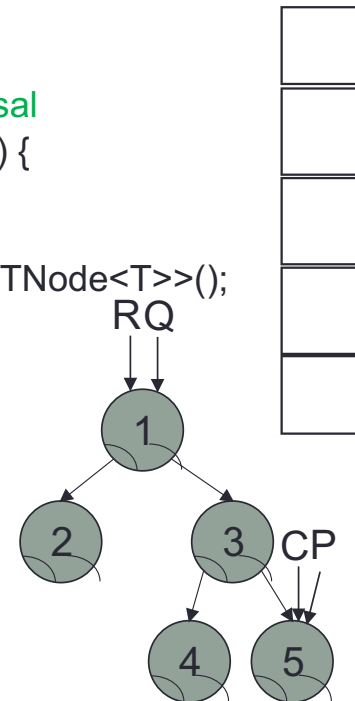
```
        else
```

```
            q = stack.pop(); // Go right here
```

```
    }
```

```
    return q;
```

```
}
```



Example #1

p = current, t = root

ADT Binary Tree: Implementation

// Non-recursive version of findparent – uses pre-order traversal

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

// Stack is used to store the right pointers of nodes

```
    LinkStack<BTNode<T>> stack = new LinkStack<BTNode<T>>();
```

```
    BTNode<T> q = t;
```

```
    while(q.right != p && q.left != p) {
```

```
        if(q.right != null)
```

```
            stack.push(q.right);
```

```
        if(q.left != null)
```

```
            q = q.left;
```

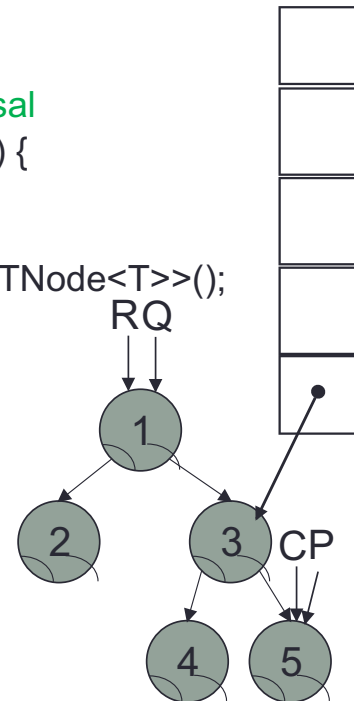
```
        else
```

```
            q = stack.pop(); // Go right here
```

```
    }
```

```
    return q;
```

```
}
```



Example #1

p = current, t = root

ADT Binary Tree: Implementation

// Non-recursive version of findparent – uses pre-order traversal

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

// Stack is used to store the right pointers of nodes

```
    LinkStack<BTNode<T>> stack = new LinkStack<BTNode<T>>();
```

```
    BTNode<T> q = t;
```

```
    while(q.right != p && q.left != p) {
```

```
        if(q.right != null)
```

```
            stack.push(q.right);
```

```
        if(q.left != null)
```

```
            q = q.left;
```

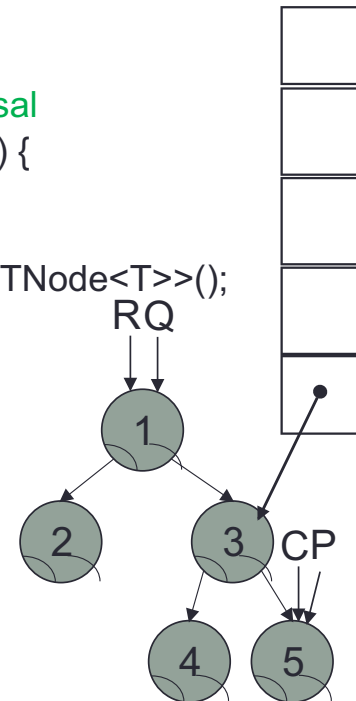
```
        else
```

```
            q = stack.pop(); // Go right here
```

```
    }
```

```
    return q;
```

```
}
```



Example #1

p = current, t = root

ADT Binary Tree: Implementation

// Non-recursive version of findparent – uses pre-order traversal

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

// Stack is used to store the right pointers of nodes

```
    LinkStack<BTNode<T>> stack = new LinkStack<BTNode<T>>();
```

```
    BTNode<T> q = t;
```

```
    while(q.right != p && q.left != p) {
```

```
        if(q.right != null)
```

```
            stack.push(q.right);
```

```
        if(q.left != null)
```

```
            q = q.left;
```

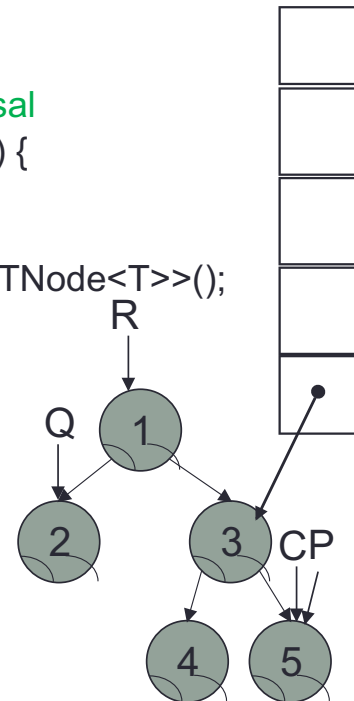
```
        else
```

```
            q = stack.pop(); // Go right here
```

```
    }
```

```
    return q;
```

```
}
```



Example #1

p = current, t = root

ADT Binary Tree: Implementation

// Non-recursive version of findparent – uses pre-order traversal

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

// Stack is used to store the right pointers of nodes

```
LinkStack<BTNode<T>> stack = new LinkStack<BTNode<T>>();
```

```
BTNode<T> q = t;
```

```
while(q.right != p && q.left != p) {
```

```
    if(q.right != null)
```

```
        stack.push(q.right);
```

```
    if(q.left != null)
```

```
        q = q.left;
```

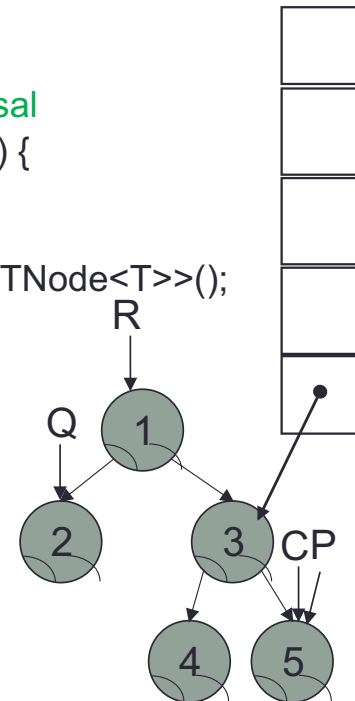
```
    else
```

```
        q = stack.pop(); // Go right here
```

```
}
```

```
return q;
```

```
}
```



Example #1

p = current, t = root

ADT Binary Tree: Implementation

// Non-recursive version of findparent – uses pre-order traversal

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

// Stack is used to store the right pointers of nodes

```
    LinkStack<BTNode<T>> stack = new LinkStack<BTNode<T>>();
```

```
    BTNode<T> q = t;
```

```
    while(q.right != p && q.left != p) {
```

```
        if(q.right != null)
```

```
            stack.push(q.right);
```

```
        if(q.left != null)
```

```
            q = q.left;
```

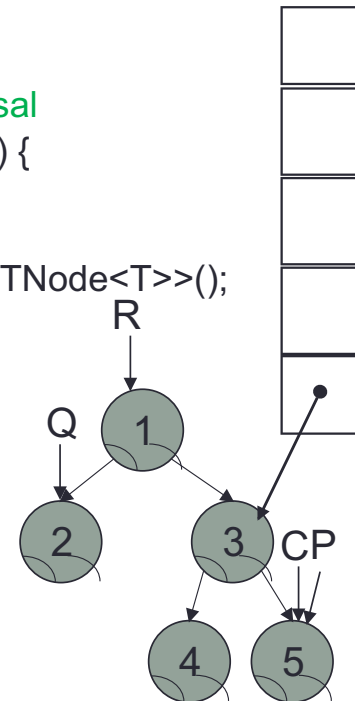
```
        else
```

```
            q = stack.pop(); // Go right here
```

```
    }
```

```
    return q;
```

```
}
```



Example #1

p = current, t = root

ADT Binary Tree: Implementation

// Non-recursive version of findparent – uses pre-order traversal

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

// Stack is used to store the right pointers of nodes

```
    LinkStack<BTNode<T>> stack = new LinkStack<BTNode<T>>();
```

```
    BTNode<T> q = t;
```

```
    while(q.right != p && q.left != p) {
```

```
        if(q.right != null)
```

```
            stack.push(q.right);
```

```
        if(q.left != null)
```

```
            q = q.left;
```

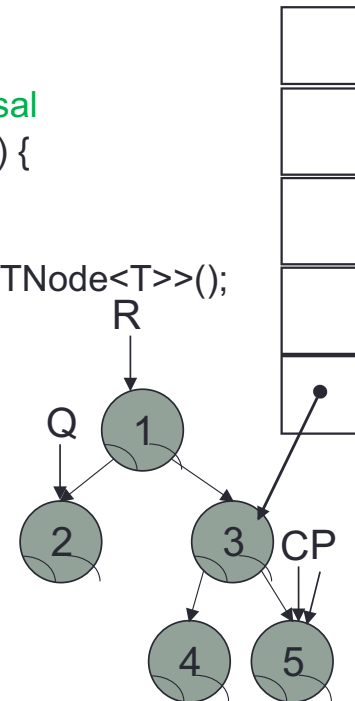
```
        else
```

```
            q = stack.pop(); // Go right here
```

```
    }
```

```
    return q;
```

```
}
```



Example #1

p = current, t = root

ADT Binary Tree: Implementation

// Non-recursive version of findparent – uses pre-order traversal

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

// Stack is used to store the right pointers of nodes

```
    LinkStack<BTNode<T>> stack = new LinkStack<BTNode<T>>();
```

```
    BTNode<T> q = t;
```

```
    while(q.right != p && q.left != p) {
```

```
        if(q.right != null)
```

```
            stack.push(q.right);
```

```
        if(q.left != null)
```

```
            q = q.left;
```

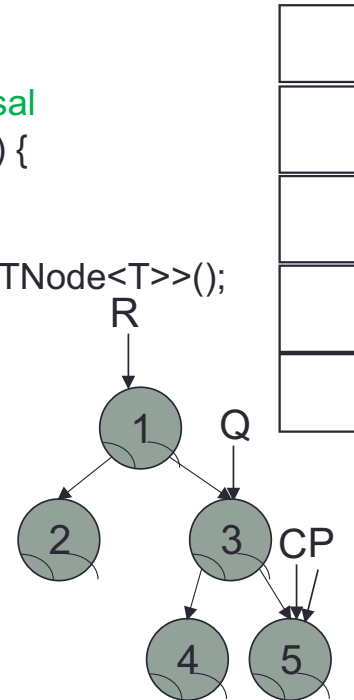
```
        else
```

```
            q = stack.pop(); // Go right here
```

```
    }
```

```
    return q;
```

```
}
```



Example #1

p = current, t = root

ADT Binary Tree: Implementation

// Non-recursive version of findparent – uses pre-order traversal

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

// Stack is used to store the right pointers of nodes

```
    LinkStack<BTNode<T>> stack = new LinkStack<BTNode<T>>();
```

```
    BTNode<T> q = t;
```

```
    while(q.right != p && q.left != p) {
```

```
        if(q.right != null)
```

```
            stack.push(q.right);
```

```
        if(q.left != null)
```

```
            q = q.left;
```

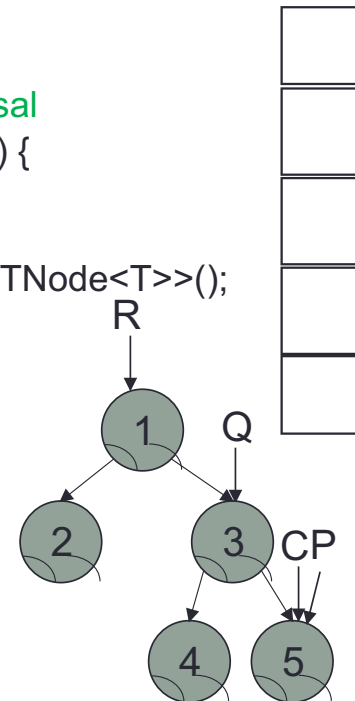
```
        else
```

```
            q = stack.pop(); // Go right here
```

```
    }
```

```
    return q;
```

```
}
```



Example #1

p = current, t = root

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
// Stack is used to store the right pointers of nodes
```

```
LinkStack<BTNode<T>> stack = new LinkStack<BTNode<T>>();
```

```
BTNode<T> q = t;
```

```
while(q.right != p && q.left != p) {
```

```
if(q.right != null)
```

```
stack.push(q.right);
```

```
if(q.left != null)
```

```
q = q.left;
```

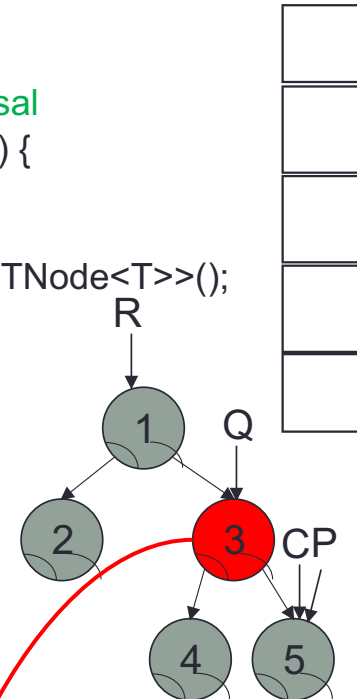
else

```
q = stack.pop(); // Go right here
```

}

```
return q;
```

}



Example #1

p = current, t = root

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal used

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null;           // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t; // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal used

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null;           // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t; // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

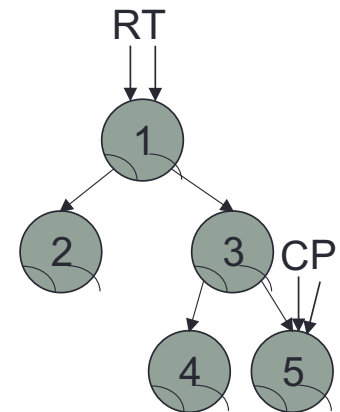
```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```



Example #1

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal used

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null;           // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t; // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

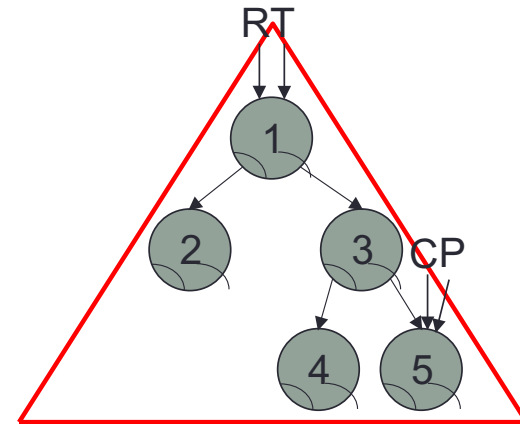
```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```



Example #1

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal used

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null;        // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t;    // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

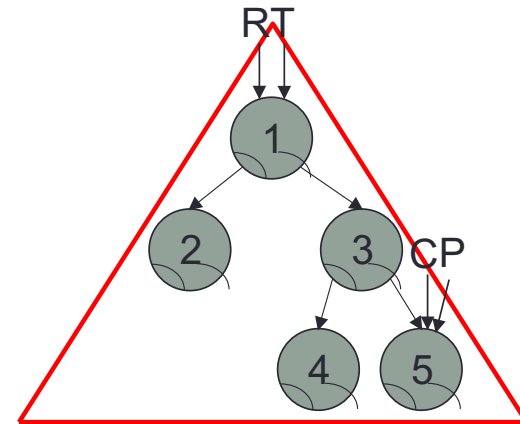
```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```



Example #1

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal used

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null;           // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t;           // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

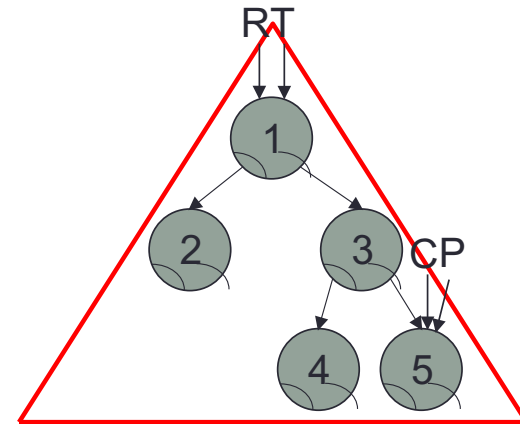
```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```



Example #1

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal used

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null;           // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t; // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

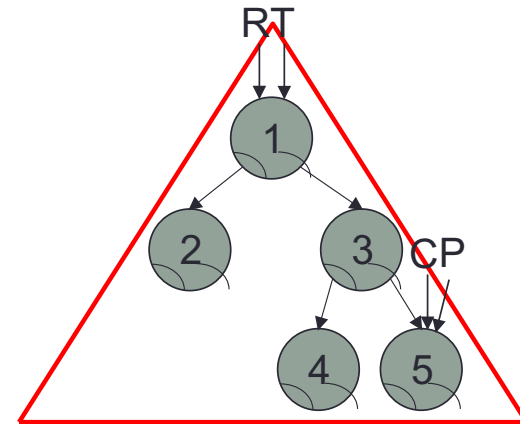
```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```



Example #1

ADT Binary Tree: Implementation

findparent(P,T.Left)

// Recursive version of findparent – preorder traversal

private BTNode<T> findparent(BTNode<T> p, BTNode<T> t){

if(t == null)

return null; // empty tree

if(t.right == null && t.left == null)

return null;

else if(t.right == p || t.left == p)

return t; // parent is t

else {

BTNode q = findparent(p, t.left);

if (q != null)

return q;

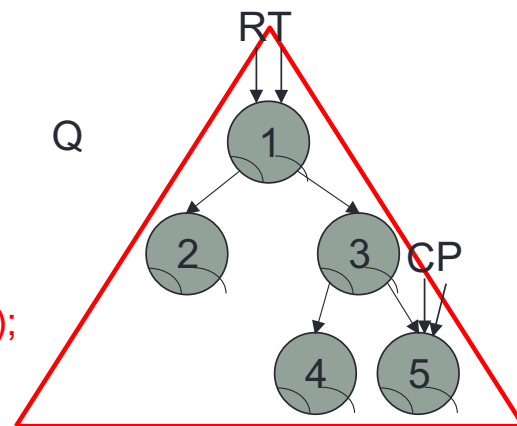
else

return findparent(p, t.right);

}

}

}



Example #1

findparent(C,R)

findparent(P,T.Left)

ADT Binary Tree: Implementation

```
// Recursive version of findparent – preorder traversal
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t){
```

```
    if(t == null)
```

```
        return null;        // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t;    // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

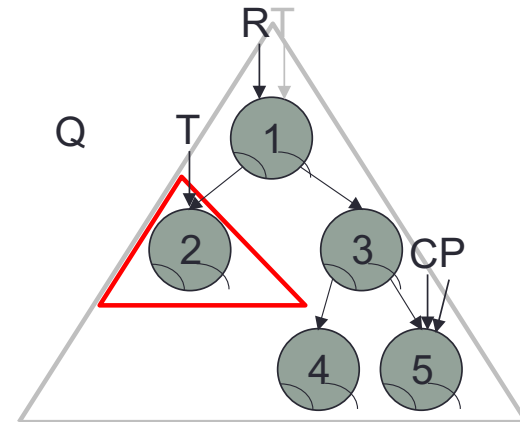
```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```



Example #1

findparent(C,R)

findparent(P,T.Left)

ADT Binary Tree: Implementation

```
// Recursive version of findparent – preorder traversal
private BTNode<T> findparent(BTNode<T> t, BTNode<T> p) {
```

```
    if(t == null)
```

```
        return null;           // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t; // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

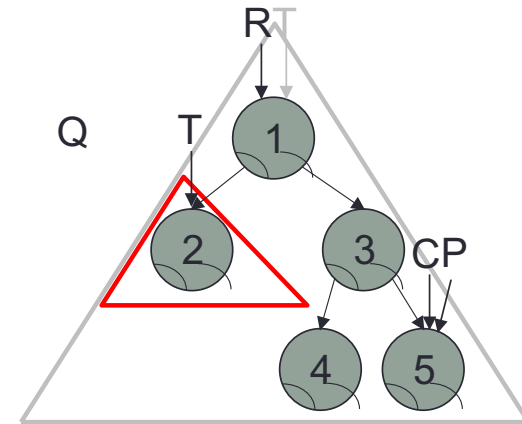
```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```



Example #1

findparent(C,R)

findparent(P,T.Left)

ADT Binary Tree: Implementation

```
// Recursive version of findparent – preorder traversal
private BTNode<T> findparent(BTNode<T> t, BTNode<T> p) {
```

```
    if(t == null)
```

```
        return null;           // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t;           // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

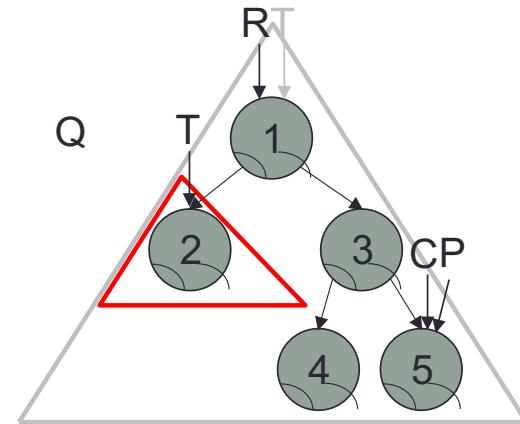
```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```



Example #1

findparent(C,R)

findparent(P,T.Left)

ADT Binary Tree: Implementation

```
// Recursive version of findparent – preorder traversal
private BTNode<T> findparent(BTNode<T> t, BTNode<T> p) {
```

```
    if(t == null)
```

```
        return null;           // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t;           // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

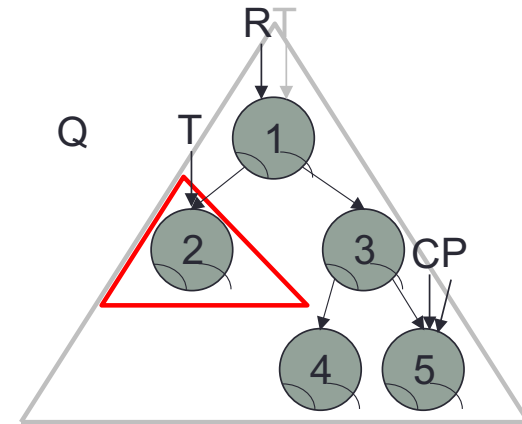
```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```



Example #1

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal used

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null;           // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t; // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

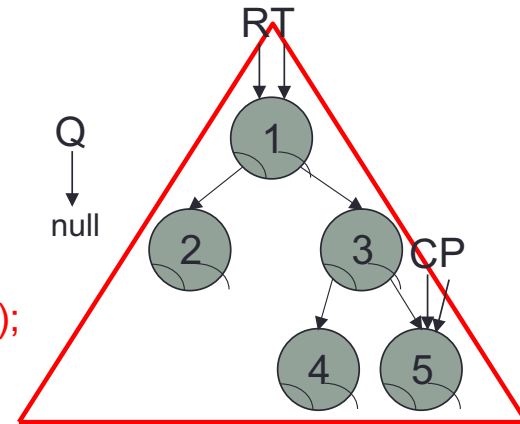
```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```



Example #1

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal used

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null;           // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t;           // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

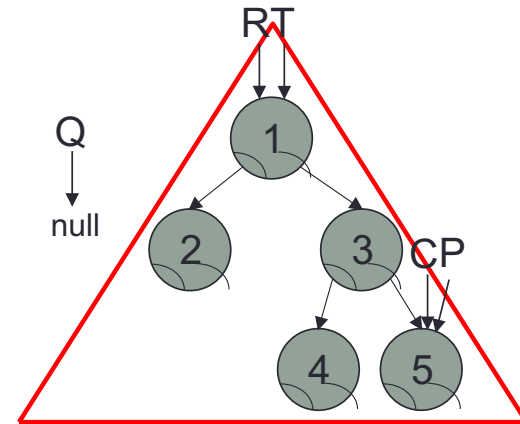
```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```



Example #1

findparent(C,R)

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal use

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null;        // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t;    // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

```
        else
```

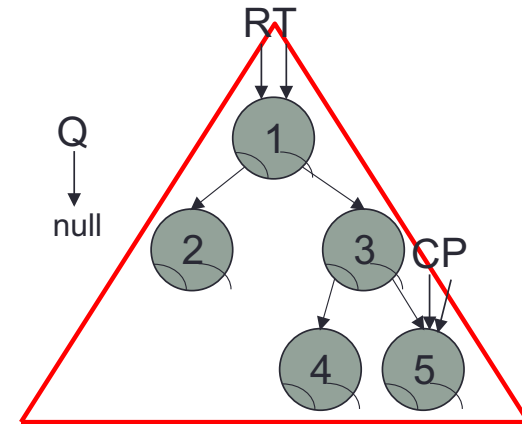
```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```

findparent(P,T.Right)



Example #1

findparent(C,R)

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal use

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null;        // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t;    // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

```
        else
```

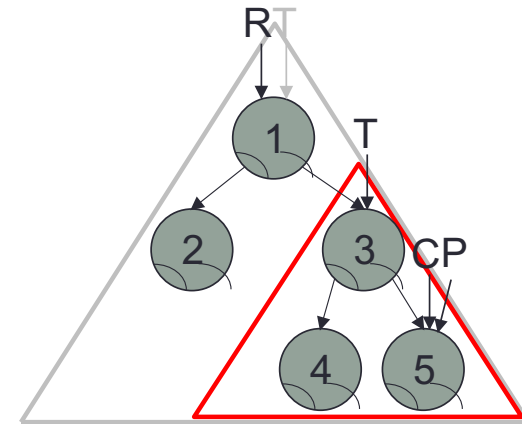
```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```

findparent(P,T.Right)



Example #1

findparent(C,R)

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal use

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null;        // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t;    // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

```
        else
```

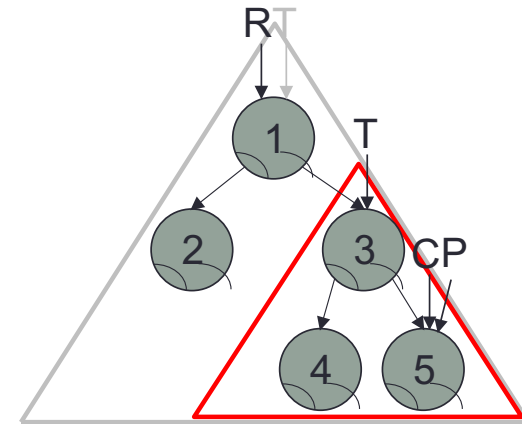
```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```

```
findparent(P,T.Right)
```



Example #1

findparent(C,R)

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal use

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null;        // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t; // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

```
        else
```

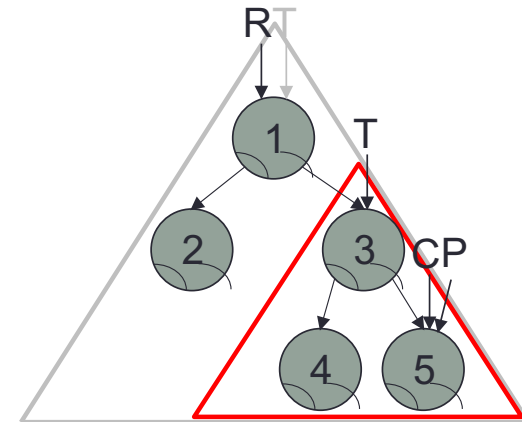
```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```

findparent(P,T.Right)



Example #1

findparent(C,R)

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal use

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null;        // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t;    // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

```
        else
```

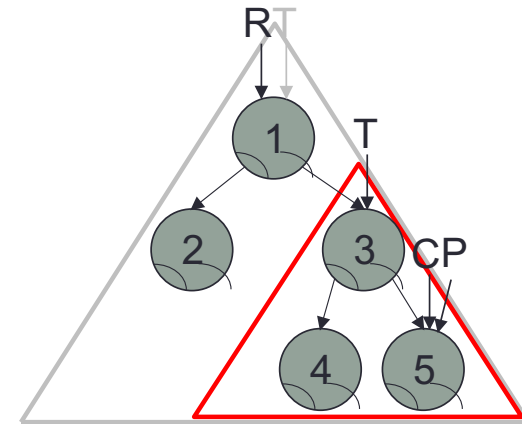
```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```

findparent(P,T.Right)



Example #1

findparent(C,R)

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal use

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null;        // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t; // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

```
        else
```

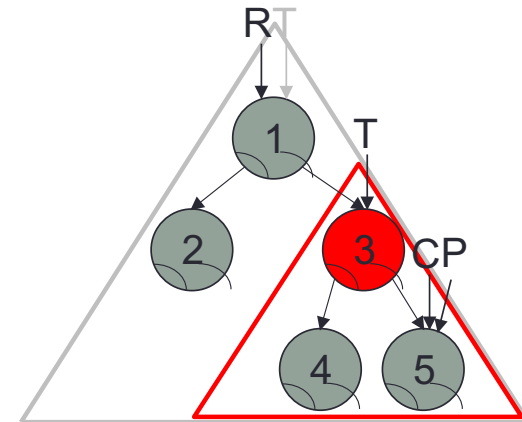
```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```

findparent(P,T.Right)



Example #1

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal used

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null;           // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t; // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

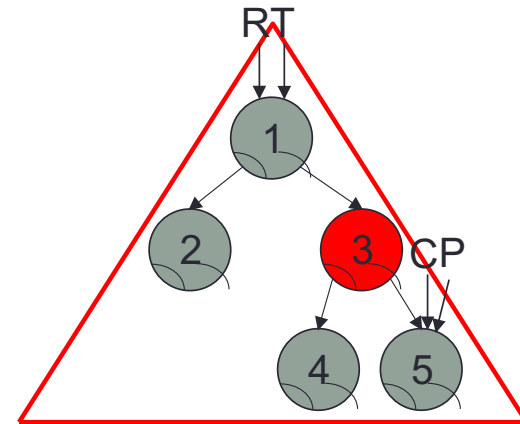
```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```



Example #1

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal used

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null;           // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t; // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

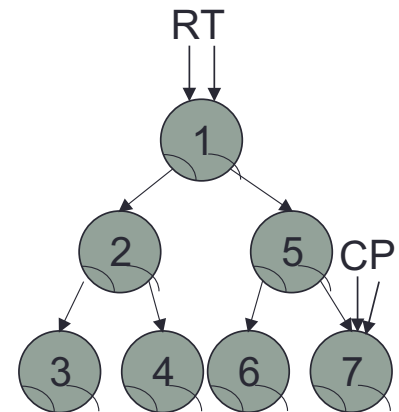
```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```



Example #2

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal used

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null;           // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t; // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

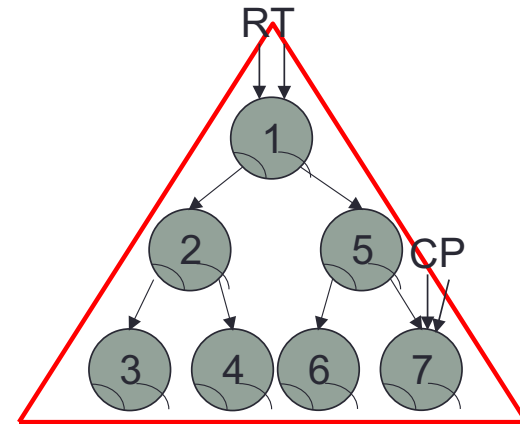
```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```



Example #2

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal used

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null;        // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t;    // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

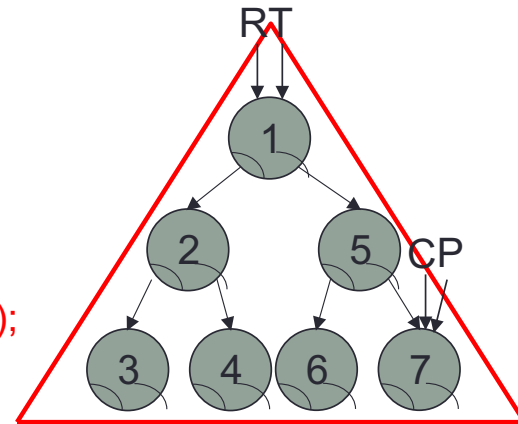
```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```



Example #2

findparent(C,R)

findparent(P,T.Left)

ADT Binary Tree: Implementation

```
// Recursive version of findparent – preorder traversal
private BTNode<T> findparent(BTNode<T> t, BTNode<T> p) {
```

```
    if(t == null)
```

```
        return null;           // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t; // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

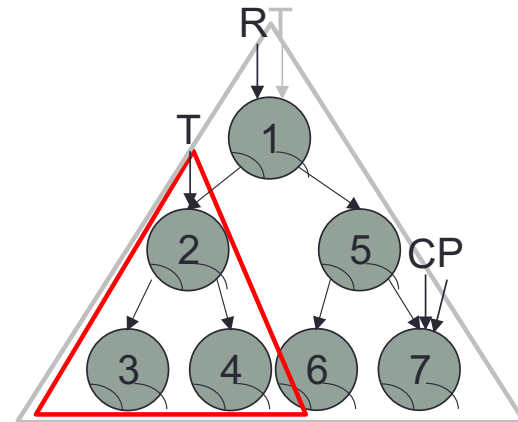
```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```



Example #2

findparent(C,R)

findparent(P,T.Left)

ADT Binary Tree: Implementation

```
// Recursive version of findparent – preorder traversal
private BTNode<T> findparent(BTNode<T> t, BTNode<T> p) {
```

```
    if(t == null)
```

```
        return null;           // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t; // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

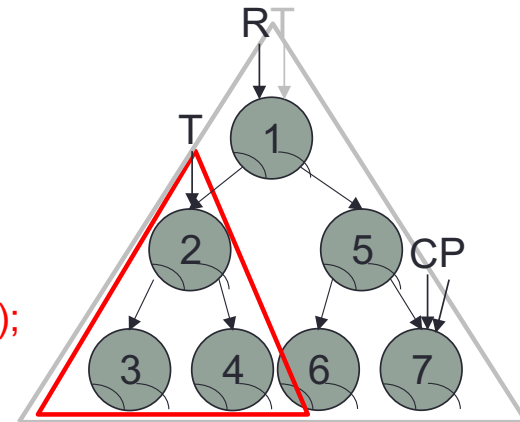
```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```



Example #2

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null;    // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t;    // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

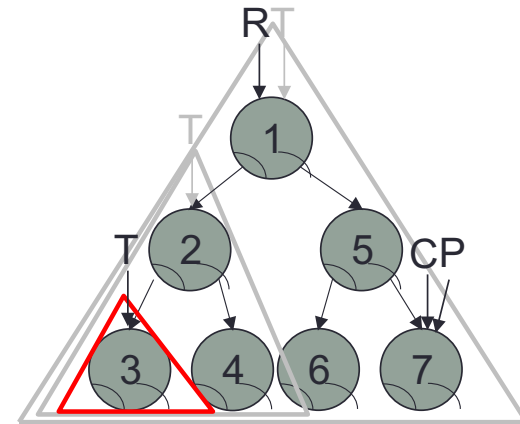
```
}
```

```
}
```

findparent(C,R)

findparent(P,T.Left)

findparent(P,T.Left)



Example #2

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null; // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t; // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

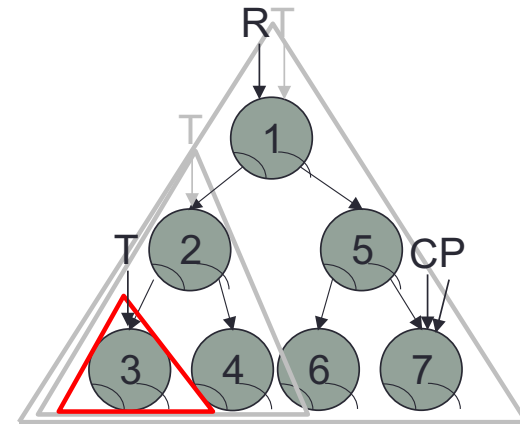
```
}
```

```
}
```

findparent(C,R)

findparent(P,T.Left)

findparent(P,T.Left)



Example #2

findparent(C,R)

findparent(P,T.Left)

ADT Binary Tree: Implementation

```
// Recursive version of findparent – preorder traversal
private BTNode<T> findparent(BTNode<T> t, BTNode<T> p) {
```

```
    if(t == null)
```

```
        return null;           // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t;           // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

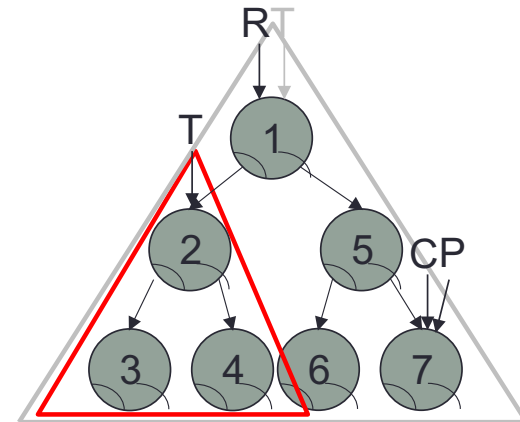
```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```



Example #2

findparent(C,R)

findparent(P,T.Left)

ADT Binary Tree: Implementation

```
// Recursive version of findparent – preorder traversal
private BTNode<T> findparent(BTNode<T> t, BTNode<T> p) {
```

```
    if(t == null)
```

```
        return null;           // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t; // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

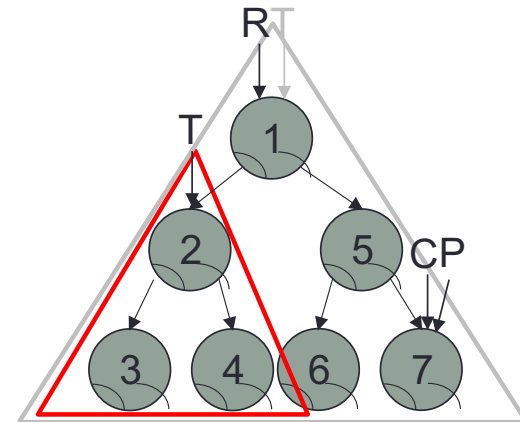
```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```



Example #2

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null; // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t; // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

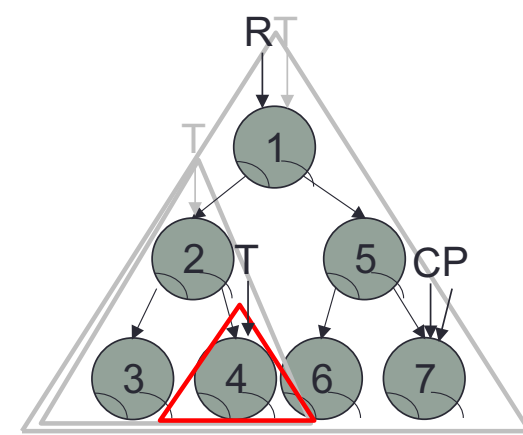
```
}
```

```
}
```

findparent(C,R)

findparent(P,T.Left)

findparent(P,T.Right)



Example #2

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null;        // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t;    // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

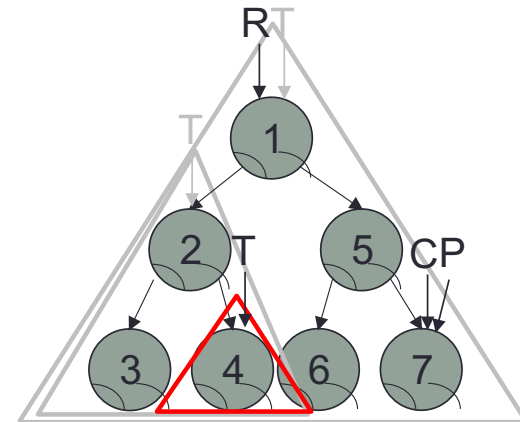
```
}
```

```
}
```

findparent(C,R)

findparent(P,T.Left)

findparent(P,T.Right)



Example #2

findparent(C,R)

findparent(P,T.Left)

ADT Binary Tree: Implementation

```
// Recursive version of findparent – preorder traversal
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null;           // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t;           // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

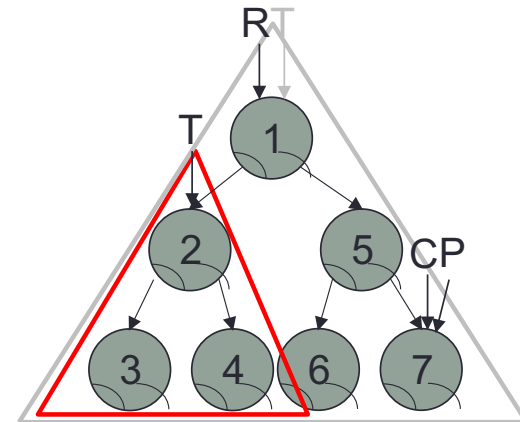
```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```



Example #2

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal used

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null;           // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t; // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

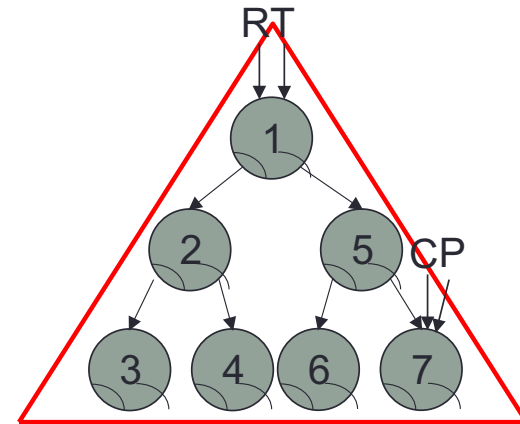
```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```



Example #2

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal used

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null;           // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t; // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

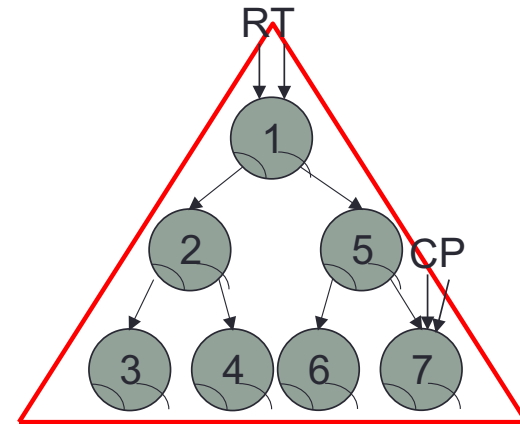
```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```



Example #2

findparent(C,R)

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal use

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null;        // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t;    // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

```
        else
```

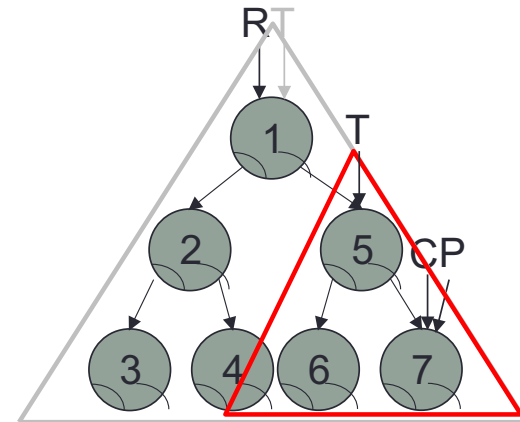
```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```

findparent(P,T.Right)



Example #2

findparent(C,R)

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal use

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null;        // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t; // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

```
        else
```

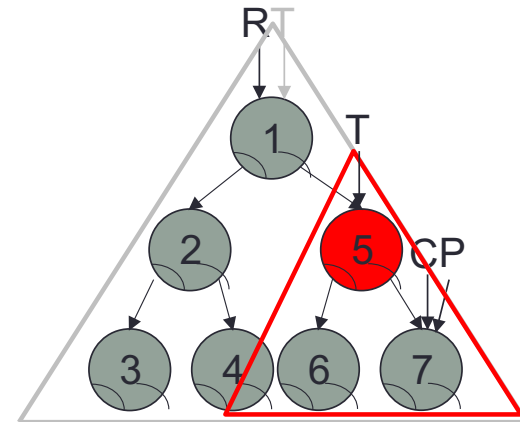
```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```

```
findparent(P,T.Right)
```



Example #2

ADT Binary Tree: Implementation

// Recursive version of findparent – preorder traversal used

```
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
```

```
    if(t == null)
```

```
        return null;           // empty tree
```

```
    if(t.right == null && t.left == null)
```

```
        return null;
```

```
    else if(t.right == p || t.left == p)
```

```
        return t;           // parent is t
```

```
    else {
```

```
        BTNode q = findparent(p, t.left);
```

```
        if (q != null)
```

```
            return q;
```

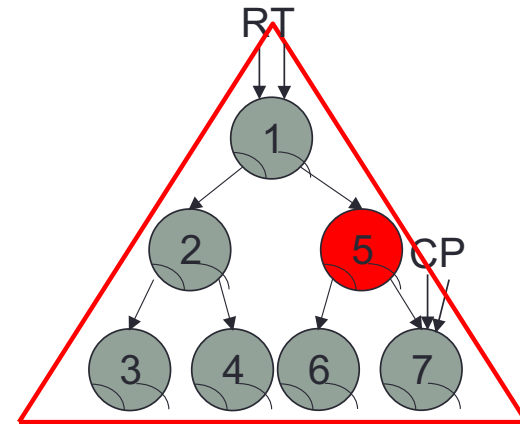
```
        else
```

```
            return findparent(p, t.right);
```

```
    }
```

```
}
```

```
}
```



Example #2