

CSC 212 Homework # 1
Performance Analysis
Due date: 16/10/2016

This is an individual assignment.

Guidelines: The homework must be **submitted electronically through LMS**.

Hard copy submissions are not accepted.

Problem 1

1. Order the following functions by asymptotic growth rate: $4n \log n + 2n$, 2^{10} , $2^{\log n}$, $3n + 100 \log n$, $4n$, 2^n , $n^2 + 10n$, n^3 , $n \log n$. (Question R-4.8 page 182 of the textbook)
2. Show that $\log n^{2n} + n^2$ is $O(n^2)$
3. Show that $\sum_{i=1}^5 i^3$ is $O(1)$
4. Show that $\sum_{i=1}^n \lceil \log i \rceil$ is a $O(n \log n)$
5. Using the definition of the Big-Oh, prove that $f(n) = 10n + 5 \log n$ is a big-oh of $g(n) = n$.

Problem 2

1. Given an n -element array X , Algorithm B chooses $\log n$ elements in X at random and executes an $O(n)$ -time calculation for each. What is the worst-case running time of Algorithm B ? (Question R-4.30 page 184 of the textbook)
2. Given an n -element array X of integers, Algorithm C executes an $O(n)$ -time computation for each even number in X , and an $O(\log n)$ -time computation for each odd number in X . What are the best-case and worst-case running times of Algorithm C ? (Question R-4.31 page 184 of the textbook)

3. Given an n -element array X , Algorithm D calls Algorithm E on each element $X[i]$. Algorithm E runs in $O(i)$ time when it is called on element $X[i]$. What is the worst-case running time of Algorithm D ? (Question R-4.32 page 184 of the textbook)

Problem 3

Analyze the performance of the following algorithms theoretically:

```
public void func1(int n) {
    for (int i = 0; i < n * log(n); i++) {
        System.out.println(i);
        for (int j = 2; j < n; j++) {
            System.out.println(j);
        }
    }
    System.out.println("Goodbye!");
}
```

```
public void func2(int n) {
    for (int i = 0; i < n * n; i++) {
        System.out.println(i);
        for (int j = 2 * n; j > n; j--) {
            System.out.println(j);
        }
    }
    System.out.println("Goodbye!");
}
```

```
public void func3(int n) {
    for (int i = n; i > 0; i--) {
        System.out.println(i);
        for (int j = 0; j < i; j++) {
            System.out.println(j);
        }
    }
    System.out.println("Goodbye!");
}
```

```
void func4(int n) {
    int m = 1;
    while( m <= n ) {
        system.out.println(m);
        i = n;
        while (i > 0 ) {
            system.out.println(i);
            i = i / 2;
        }
        m++;
    }
}
```

Problem 4

The class *Sort* below implements three sorting algorithms: selection sort, bubble sort and Quicksort.

```
import java.util.Arrays;

public class Sort {
    public static void selectionSort(double[] A, int n) {
        for (int i = 0; i < n - 1; i++) {
            int min = i;
            for (int j = i + 1; j < n; j++) {
                if (A[j] < A[min])
                    min = j;
            }
            double tmp = A[i];
            A[i] = A[min];
            A[min] = tmp;
        }
    }

    public static void bubbleSort(double A[], int n) {
        for (int i = 0; i < n - 1; i++) {
            for (int j = 0; j < n - 1 - i; j++) {
                if (A[j] < A[j + 1]) {
                    double tmp = A[j];
                    A[j] = A[j + 1];
                    A[j + 1] = tmp;
                }
            }
        }
    }

    public static void quickSort(double A[], int n) {
        Arrays.sort(A, 0, n - 1);
    }
}
```

Conduct an experimental analysis of these three algorithms as follows:

- Use arrays of sizes ranging from 10000 to 50000 with step size 10000 (so in total you have 5 different sizes).
- Give the same input to all three algorithms.
- Fill the array with random numbers (use `Math.random()`).
- For each input repeat the execution 100 times, measure the execution in nanoseconds (use `System.nanoTime()`), and report the average time in milliseconds.

1. Write the code used for the experimental analysis.
2. Report the results as a table and as a graph.

3. Which of the three algorithms is the fastest?
4. Which of *selection sort* and *bubble sort* is faster? Which one has a larger growth rate?