General Trees & Binary Trees

CSC212: Data Structures

Trees

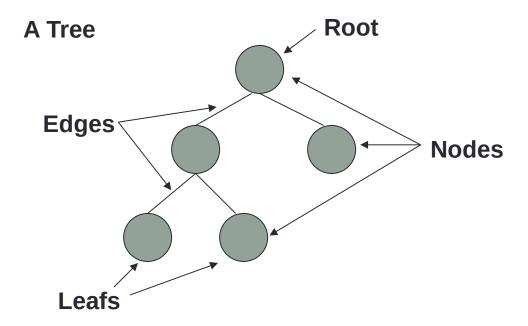
- Previous data structures (e.g. lists, stacks, queues) have a linear structure.
- Linear structures represent one-to-one relation between data elements.
- Trees have a nested or a hierarchical structure.
- Hierarchical structures represent one-to-many relation between data elements.

Trees

- Examples of situations were one-to-many relations exist... these can be represented as trees.
 - Relation between a parent and his children.
 - Relation between a person and books he owns.
 - Relation between a football team and the players on the team.
 - Card catalog in a library.

Trees: Some Terminology

 A tree is represented as a set of <u>nodes</u> connected by <u>edges</u>.



Trees: Comparison with Lists

A List

- Unique <u>first</u> element.
- Unique <u>last</u> element.
- Each element, other than the first and the last, has a unique predecessor and a unique successor.

A Tree

- Unique first node called <u>root</u>.
- Each node has successors, called its children.
- Each node has one predecessor, called parent.
- Leafs have no children.
- Root has no parent.

Trees: More Terminology

• <u>Simple path</u>: a sequence of distinct nodes in the tree.

- Path length: number of nodes in a path.
- Siblings: two nodes that have the same parent.
- Ancestors: given a node A in a tree, the parent of the node A and the ancestors of the parent of A, are ancestors of A.

Trees: More Terminology

Parent: a parent of a node is its predecessor.

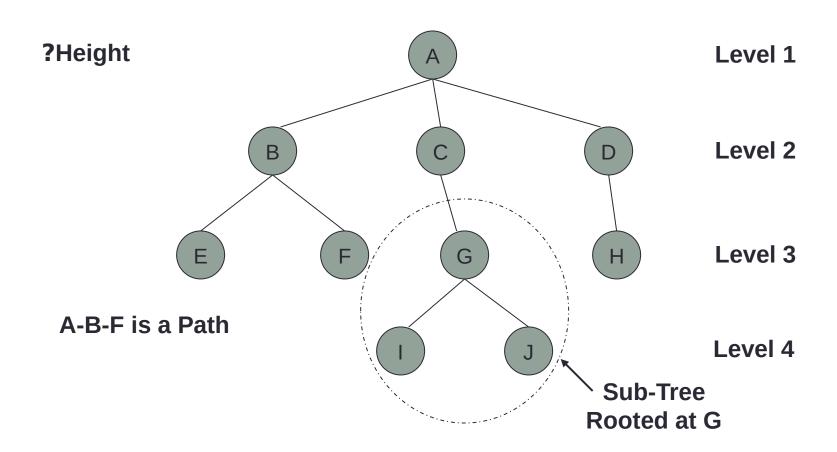
Child: a child of a node is its successor.

Root: a unique node without any predecessor.

Leafs: nodes without any children.

Descendents: given a node A in a tree, the children of A and all descendents of the children of A are descendents of A.

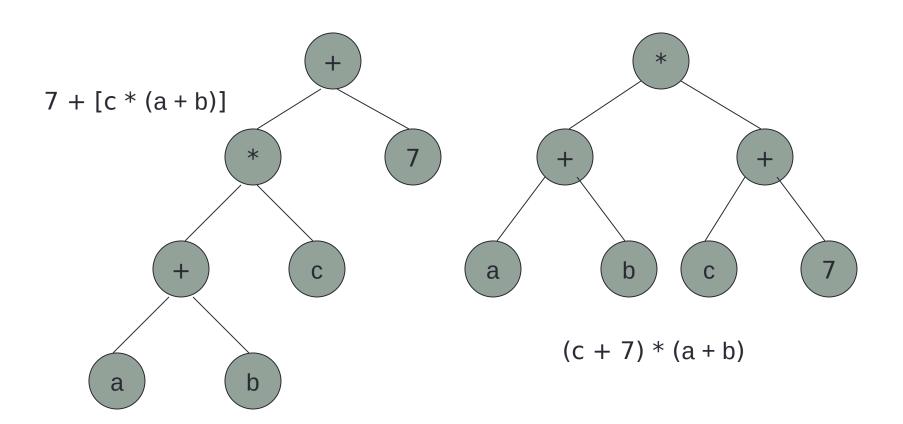
Trees: More Terminology



Binary Trees

- A binary tree is a tree with the following:
 - Each node can have at most two subtrees and therefore at most two children.
 - 2. Each subtree is identified as being either the left subtree or the right subtree of the parent.
 - 3. It may be empty.
- Nodes in a binary tree may be composite e.g. of variable type 'Type'.

Binary Trees



Elements: The elements are nodes, each node contains the following data type: Type and has LeftChild and RightChild references.

Structure: hierarchical structure; each node can have two children: left or right child; there is a root node and a current node.

Domain: the number of nodes in a binary tree is bounded; domain contains empty tree, trees with one element, two elements, ...

Operations:

Method Traverse (Order ord)

requires: Binary Tree (BT) is not empty.

input: ord.

results: Each element in the tree is processed exactly once by a user supplied procedure. The order in which nodes are processed depends on the value of ord (Order = {preorder, postorder, inorder})

<u>preorder</u>: each node processed **before** any node in either of its subtrees.

<u>inorder</u>: each node is processed **after** all its nodes in its **left** subtree and **before** any node in its **right** subtree.

<u>postorder</u>: each node is processed <u>after</u> all its nodes in both of its subtrees.

output: none.

Tree Traversals

 To traverse a tree means to process (e.g. printing it) each element in the tree.

Tree traversals

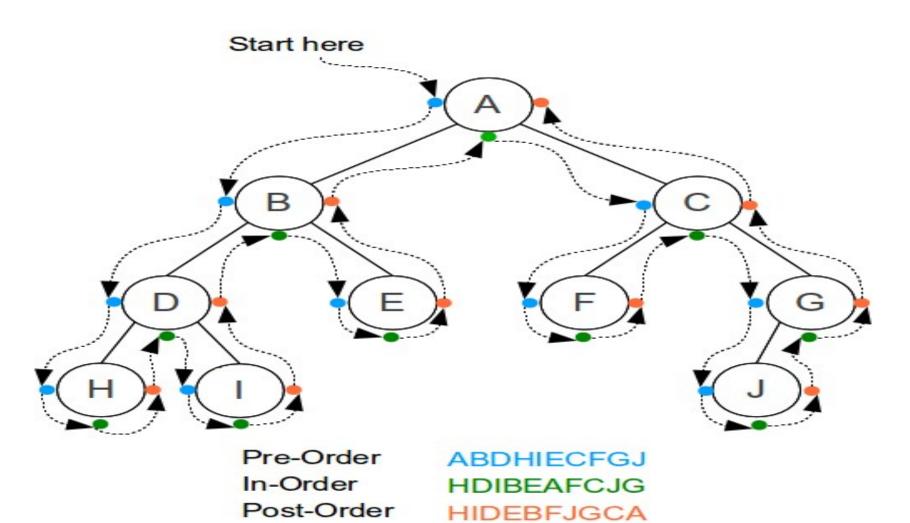
- n! ways of traversing a tree of n nodes.
- pre-order, in-order, post-order

 traversals orders.

List traversals

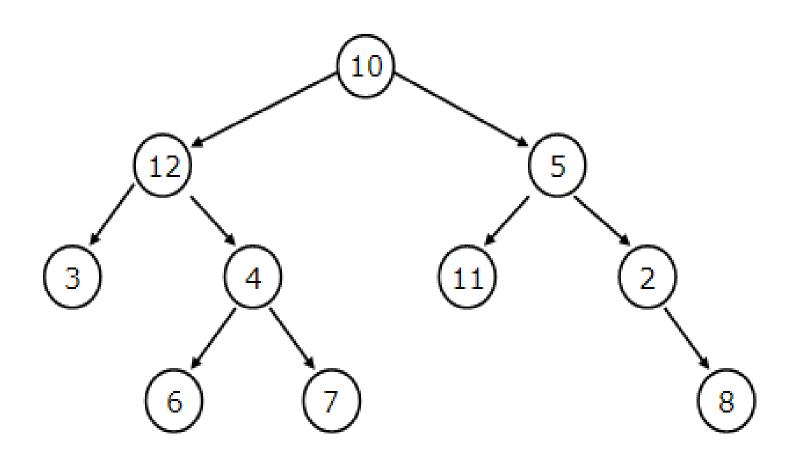
- n! ways of traversing a list of n nodes.
- front-to-back, or back-to-front. [] two natural traversals orders.

Tree Traversals Example



https://en.wikipedia.org/wiki/Tree_traversal

Tree Traversals Example



Operations:

Method Insert (Type e, Relative rel, boolean inserted) (Relative = {leftchild, rightchild, root, parent}) requires: (1) Full () is false and (2) either (a) rel = root and Empty() is true or (b) rel <> root and rel <> parent and Empty() is false.

input: e, rel.

results: **if** case (1) rel = leftChild, current node has a left child, or (2) rel = rightChild, current node has a right child, **then** inserted is false. **Else** a node containing e is added as rel of the current node in the tree and becomes the current node and inserted is true.

output: inserted.

3. **Procedure** DeleteSub ()

requires: Binary tree is not empty.

input: none

results: The subtree whose root node was the current node is deleted from the tree. If the resulting tree is not empty, then the root node is the current node.

output: none.

4. **Procedure** Update (Type e).

requires: Binary tree is not empty.

input: e.

results: the element in e is copied into the current

node.

output: none.

5. Procedure Retrieve (Type e)

requires: Binary tree is not empty.

input: none

results: element in the current node is copied into e.

output: e.

6. **Procedure** Find (Relative rel, boolean found)

requires: Binary tree is not empty.

input: rel.

results: The current node of the tree is determined by

the value of rel and previous current node...

output: found.

7. **Procedure** Empty (boolean empty).

requires: None.

input: none

results: If Binary tree is empty then empty is true;

otherwise empty is false.

output: empty.

8. **Procedure** Full (boolean full)

requires: None.

input: None.

results: if the binary tree is full then full is true

otherwise false.

output: full.

ADT Binary Tree: Element

```
public class BTNode <T> {
 public T data;
 public BTNode<T> left, right;
 /** Creates a new instance of BTNode */
 public BTNode(T val) {
 data = val;
 left = right = null;
 public BTNode(T val, BTNode<T> l, BTNode<T> r){
 data = val;
 left = 1;
 right = r;
```

ADT Binary Tree: Order & Relative Classes

- These definitions are in separate files and define:
 - The Order class.

```
public enum Order {preOrder, inOrder, postOrder};
```

The Relative class.

```
public enum Relative {Root, Parent, LeftChild, RightChild};
```

```
public class BT<T> {
 BTNode<T> root, current;
 /** Creates a new instance of BT */
 public BT() {
    root = current = null;
 public boolean empty(){
    return root == null;
```

RC

null

```
public class BT<T> {
 BTNode<T> root, current;
 /** Creates a new instance of BT */
 public BT() {
    root = current = null;
 public boolean empty(){
    return root == null;
```

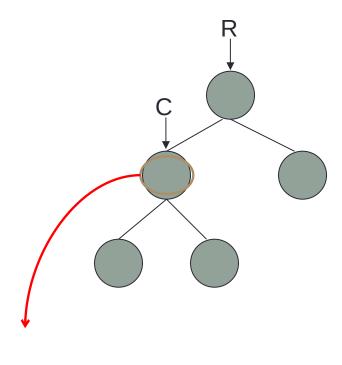
```
RC
public class BT<T> {
 BTNode<T> root, current;
                                               null
                                              true
 /** Creates a new instance of BT */
 public BT() {
    root = current = null;
 public boolean empty(){
    return root == null;
                                              false
```

```
public T retrieve() {
    return current.data;
}

public void update(T val) {
    current.data = val;
}
```

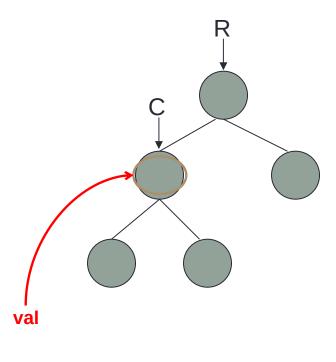
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public T retrieve() {
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    current.data = val;
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public T retrieve() {
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```
public boolean insert(Relative rel, T val) {
    switch(rel) {
     case Root:
   if(!empty()) return false;
    current = root = new BTNode<T>(val);
   return true;
     case Parent: //This is an impossible case.
   return false:
     case LeftChild:
   if(current.left != null) return false;
    current.left = new BTNode<T>(val);
    current = current.left;
   return true;
     case RightChild:
   if(current.right != null) return false;
    current.right = new BTNode<T> (val);
    current = current.right;
   return true:
     default:
   return false;
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   return false;
```

Example #1 rel = Root



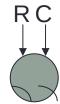
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Example #1 rel = Root

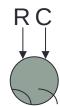


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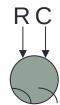
Example #1 rel = Root



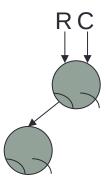
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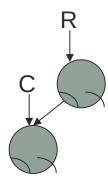
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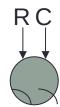
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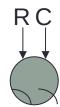
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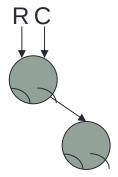
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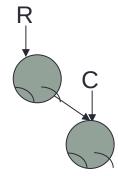
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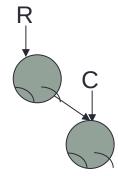


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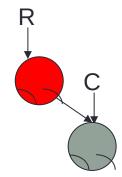
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Example #4 rel = Parent

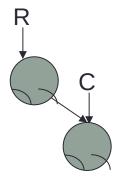


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```

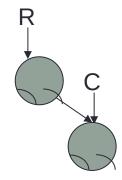
Example #4 rel = Parent



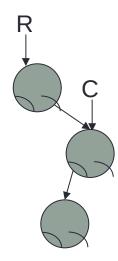
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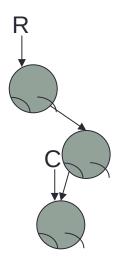
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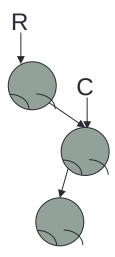


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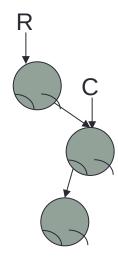


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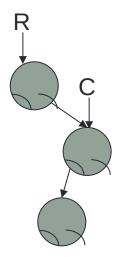
Find Parent



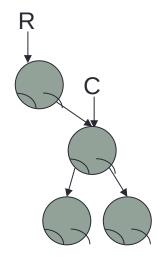
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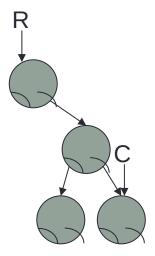
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   if(current.right != null) return false;
    current.right = new BTNode<T> (val);
    current = current.right;
   return true:
     default:
   return false;
```



```
public boolean insert(Relative rel, T val) {
    switch(rel) {
     case Root:
   if(!empty()) return false;
    current = root = new BTNode<T>(val);
   return true:
     case Parent: //This is an impossible case.
   return false:
     case LeftChild:
   if(current.left != null) return false;
    current.left = new BTNode<T>(val);
    current = current.left;
   return true:
     case RightChild:
   if(current.right != null) return false;
    current.right = new BTNode<T> (val);
    current = current.right;
   return true:
     default:
   return false;
```

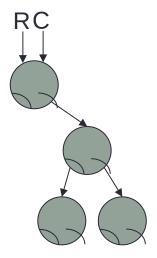


```
public boolean insert(Relative rel, T val) {
    switch(rel) {
     case Root:
   if(!empty()) return false;
    current = root = new BTNode<T>(val);
   return true:
     case Parent: //This is an impossible case.
   return false:
     case LeftChild:
   if(current.left != null) return false;
    current.left = new BTNode<T>(val);
    current = current.left;
   return true;
     case RightChild:
   if(current.right != null) return false;
    current.right = new BTNode<T> (val);
    current = current.right;
   return true;
     default:
   return false;
```

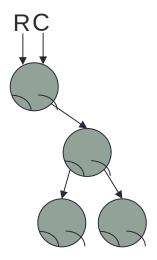


```
public boolean insert(Relative rel, T val) {
    switch(rel) {
     case Root:
   if(!empty()) return false;
    current = root = new BTNode<T>(val);
   return true;
     case Parent: //This is an impossible case.
   return false:
     case LeftChild:
   if(current.left != null) return false;
    current.left = new BTNode<T>(val);
    current = current.left;
   return true;
     case RightChild:
   if(current.right != null) return false;
    current.right = new BTNode<T> (val);
    current = current.right;
   return true:
     default:
   return false;
```

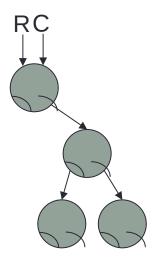
Find Root



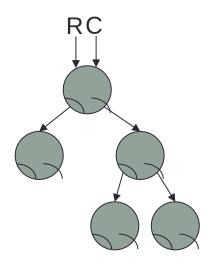
```
public boolean insert(Relative rel, T val) {
    switch(rel) {
     case Root:
   if(!empty()) return false;
    current = root = new BTNode<T>(val);
   return true;
     case Parent: //This is an impossible case.
   return false:
     case LeftChild:
   if(current.left != null) return false;
    current.left = new BTNode<T>(val);
    current = current.left;
   return true;
     case RightChild:
   if(current.right != null) return false;
    current.right = new BTNode<T> (val);
    current = current.right;
   return true:
     default:
   return false;
```



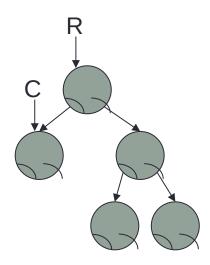
```
public boolean insert(Relative rel, T val) {
    switch(rel) {
     case Root:
   if(!empty()) return false;
    current = root = new BTNode<T>(val);
   return true;
     case Parent: //This is an impossible case.
   return false:
     case LeftChild:
   if(current.left != null) return false;
    current.left = new BTNode<T>(val);
    current = current.left;
   return true;
     case RightChild:
   if(current.right != null) return false;
    current.right = new BTNode<T> (val);
    current = current.right;
   return true:
     default:
   return false;
```



```
public boolean insert(Relative rel, T val) {
    switch(rel) {
     case Root:
   if(!empty()) return false;
    current = root = new BTNode<T>(val);
   return true;
     case Parent: //This is an impossible case.
   return false:
     case LeftChild:
   if(current.left != null) return false;
    current.left = new BTNode<T>(val);
    current = current.left;
   return true;
     case RightChild:
   if(current.right != null) return false;
    current.right = new BTNode<T> (val);
    current = current.right;
   return true:
     default:
   return false;
```

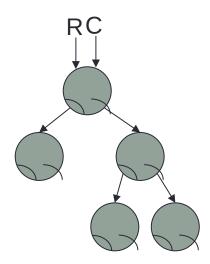


```
public boolean insert(Relative rel, T val) {
    switch(rel) {
     case Root:
   if(!empty()) return false;
    current = root = new BTNode<T>(val);
   return true;
     case Parent: //This is an impossible case.
   return false:
     case LeftChild:
   if(current.left != null) return false;
    current.left = new BTNode<T>(val);
    current = current.left;
   return true;
     case RightChild:
   if(current.right != null) return false;
    current.right = new BTNode<T> (val);
    current = current.right;
   return true:
     default:
   return false;
```



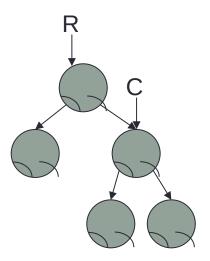
```
public boolean insert(Relative rel, T val) {
    switch(rel) {
     case Root:
   if(!empty()) return false;
    current = root = new BTNode<T>(val);
   return true;
     case Parent: //This is an impossible case.
   return false:
     case LeftChild:
   if(current.left != null) return false;
    current.left = new BTNode<T>(val);
    current = current.left;
   return true;
     case RightChild:
   if(current.right != null) return false;
    current.right = new BTNode<T> (val);
    current = current.right;
   return true:
     default:
   return false;
```

Find Root

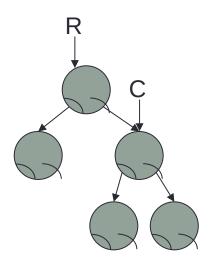


```
public boolean insert(Relative rel, T val) {
    switch(rel) {
     case Root:
   if(!empty()) return false;
    current = root = new BTNode<T>(val);
   return true;
     case Parent: //This is an impossible case.
   return false:
     case LeftChild:
   if(current.left != null) return false;
    current.left = new BTNode<T>(val);
    current = current.left;
   return true;
     case RightChild:
    if(current.right != null) return false;
    current.right = new BTNode<T> (val);
    current = current.right;
   return true:
     default:
   return false;
```

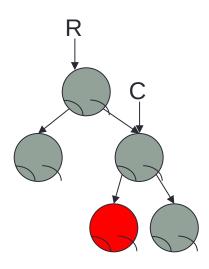
Find RightChild



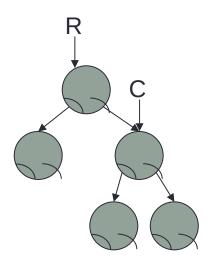
```
public boolean insert(Relative rel, T val) {
    switch(rel) {
     case Root:
   if(!empty()) return false;
    current = root = new BTNode<T>(val);
   return true;
     case Parent: //This is an impossible case.
   return false:
     case LeftChild:
   if(current.left != null) return false;
    current.left = new BTNode<T>(val);
    current = current.left;
   return true;
     case RightChild:
    if(current.right != null) return false;
    current.right = new BTNode<T> (val);
    current = current.right;
   return true:
     default:
   return false;
```



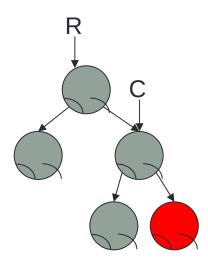
```
public boolean insert(Relative rel, T val) {
    switch(rel) {
     case Root:
   if(!empty()) return false;
    current = root = new BTNode<T>(val);
   return true;
     case Parent: //This is an impossible case.
   return false:
     case LeftChild:
   if(current.left != null) return false;
    current.left = new BTNode<T>(val);
    current = current.left;
   return true;
     case RightChild:
   if(current.right != null) return false;
    current.right = new BTNode<T> (val);
    current = current.right;
   return true:
     default:
   return false;
```



```
public boolean insert(Relative rel, T val) {
    switch(rel) {
     case Root:
   if(!empty()) return false;
    current = root = new BTNode<T>(val);
   return true;
     case Parent: //This is an impossible case.
   return false:
     case LeftChild:
   if(current.left != null) return false;
    current.left = new BTNode<T>(val);
    current = current.left;
   return true;
     case RightChild:
    if(current.right != null) return false;
    current.right = new BTNode<T> (val);
    current = current.right;
   return true:
     default:
   return false;
```

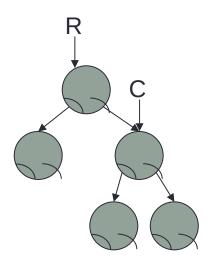


```
public boolean insert(Relative rel, T val) {
    switch(rel) {
     case Root:
   if(!empty()) return false;
    current = root = new BTNode<T>(val);
   return true:
     case Parent: //This is an impossible case.
   return false:
     case LeftChild:
   if(current.left != null) return false;
    current.left = new BTNode<T>(val);
    current = current.left;
   return true;
     case RightChild:
   if(current.right != null) return false;
    current.right = new BTNode<T> (val);
    current = current.right;
   return true:
     default:
   return false;
```



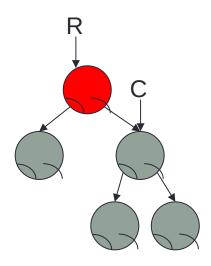
```
public boolean insert(Relative rel, T val) {
    switch(rel) {
     case Root:
   if(!empty()) return false;
    current = root = new BTNode<T>(val);
   return true;
     case Parent: //This is an impossible case.
   return false:
     case LeftChild:
   if(current.left != null) return false;
    current.left = new BTNode<T>(val);
    current = current.left;
   return true;
     case RightChild:
    if(current.right != null) return false;
    current.right = new BTNode<T> (val);
    current = current.right;
   return true:
     default:
   return false;
```

Example #10 rel = Parent



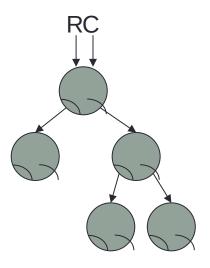
```
public boolean insert(Relative rel, T val) {
    switch(rel) {
     case Root:
   if(!empty()) return false;
    current = root = new BTNode<T>(val);
   return true:
     case Parent: //This is an impossible case.
   return false;
     case LeftChild:
   if(current.left != null) return false:
    current.left = new BTNode<T>(val);
    current = current.left;
   return true;
     case RightChild:
   if(current.right != null) return false;
    current.right = new BTNode<T> (val);
    current = current.right;
   return true:
     default:
   return false;
```

Example #10 rel = Parent

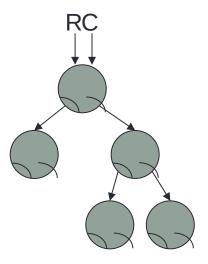


```
public void deleteSubtree(){
    if(current == root){
         current = root = null;
    else {
         BTNode < T > p = current;
         find(Relative.Parent);
         if(current.left == p)
             current.left = null;
         else
             current.right = null;
         current = root;
```

```
public void deleteSubtree(){
    if(current == root){
         current = root = null;
    else {
         BTNode < T > p = current;
         find(Relative.Parent);
         if(current.left == p)
             current.left = null;
         else
             current.right = null;
         current = root;
```

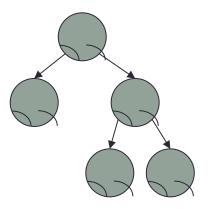


```
public void deleteSubtree(){
    if(current == root){
         current = root = null;
    else {
        BTNode < T > p = current;
        find(Relative.Parent);
        if(current.left == p)
             current.left = null;
        else
             current.right = null;
        current = root;
```



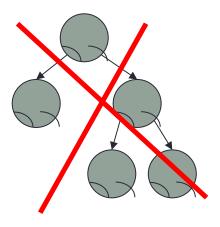
```
public void deleteSubtree(){
    if(current == root){
        current = root = null;
    else {
        BTNode < T > p = current;
        find(Relative.Parent);
        if(current.left == p)
             current.left = null;
        else
             current.right = null;
        current = root;
```





```
public void deleteSubtree(){
    if(current == root){
         current = root = null;
    else {
         BTNode < T > p = current;
         find(Relative.Parent);
         if(current.left == p)
             current.left = null;
         else
             current.right = null;
         current = root;
```

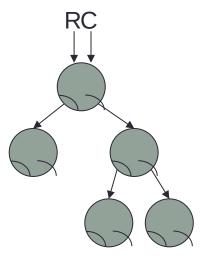




```
public void deleteSubtree(){
    if(current == root){
         current = root = null;
    else {
         BTNode < T > p = current;
         find(Relative.Parent);
         if(current.left == p)
             current.left = null;
         else
             current.right = null;
         current = root;
```

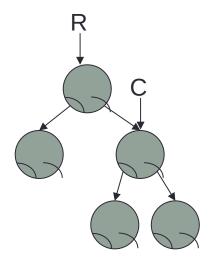


```
public void deleteSubtree(){
    if(current == root){
         current = root = null;
    else {
         BTNode < T > p = current;
         find(Relative.Parent);
         if(current.left == p)
             current.left = null;
         else
             current.right = null;
         current = root;
```

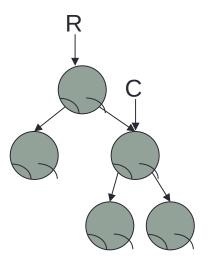


```
public void deleteSubtree(){
    if(current == root){
         current = root = null;
    else {
         BTNode < T > p = current;
         find(Relative.Parent);
         if(current.left == p)
             current.left = null;
         else
             current.right = null;
         current = root;
```

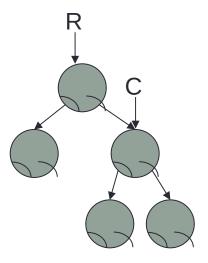
Find RightChild



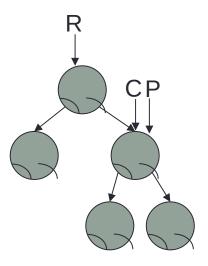
```
public void deleteSubtree(){
    if(current == root){
         current = root = null;
    else {
         BTNode < T > p = current;
         find(Relative.Parent);
         if(current.left == p)
             current.left = null;
         else
             current.right = null;
         current = root;
```



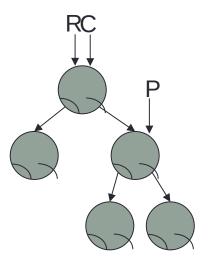
```
public void deleteSubtree(){
    if(current == root){
         current = root = null;
    else {
        BTNode < T > p = current;
        find(Relative.Parent);
        if(current.left == p)
             current.left = null;
        else
             current.right = null;
        current = root;
```



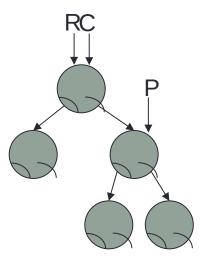
```
public void deleteSubtree(){
    if(current == root){
        current = root = null;
    else {
        BTNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
             current.left = null;
        else
             current.right = null;
        current = root;
```



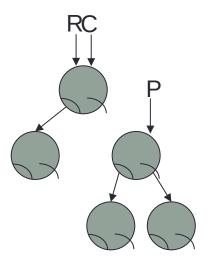
```
public void deleteSubtree(){
    if(current == root){
         current = root = null;
    else {
        BTNode < T > p = current;
        find(Relative.Parent);
        if(current.left == p)
             current.left = null;
        else
             current.right = null;
        current = root;
```



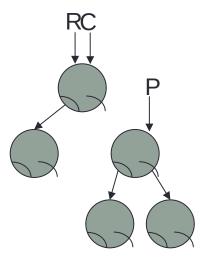
```
public void deleteSubtree(){
    if(current == root){
         current = root = null;
    else {
        BTNode < T > p = current;
        find(Relative.Parent);
        if(current.left == p)
             current.left = null;
        else
             current.right = null;
        current = root;
```



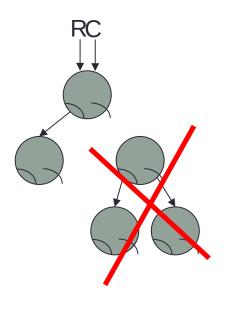
```
public void deleteSubtree(){
    if(current == root){
         current = root = null;
    else {
        BTNode < T > p = current;
        find(Relative.Parent);
        if(current.left == p)
             current.left = null;
        else
             current.right = null;
        current = root;
```



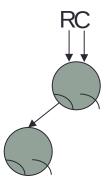
```
public void deleteSubtree(){
    if(current == root){
         current = root = null;
    else {
        BTNode < T > p = current;
        find(Relative.Parent);
        if(current.left == p)
             current.left = null;
        else
             current.right = null;
        current = root;
```



```
public void deleteSubtree(){
    if(current == root){
         current = root = null;
    else {
         BTNode < T > p = current;
         find(Relative.Parent);
         if(current.left == p)
             current.left = null;
         else
             current.right = null;
         current = root;
```

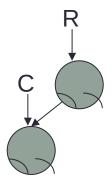


```
public void deleteSubtree(){
    if(current == root){
         current = root = null;
    else {
         BTNode < T > p = current;
         find(Relative.Parent);
         if(current.left == p)
             current.left = null;
         else
             current.right = null;
         current = root;
```

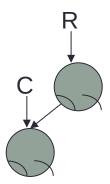


```
public void deleteSubtree(){
    if(current == root){
         current = root = null;
    else {
         BTNode < T > p = current;
         find(Relative.Parent);
         if(current.left == p)
             current.left = null;
         else
             current.right = null;
         current = root;
```

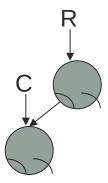
Find LeftChild



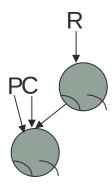
```
public void deleteSubtree(){
    if(current == root){
         current = root = null;
    else {
         BTNode < T > p = current;
         find(Relative.Parent);
         if(current.left == p)
             current.left = null;
         else
             current.right = null;
         current = root;
```



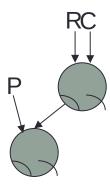
```
public void deleteSubtree(){
    if(current == root){
        current = root = null;
    else {
        BTNode < T > p = current;
        find(Relative.Parent);
        if(current.left == p)
             current.left = null;
        else
             current.right = null;
        current = root;
```



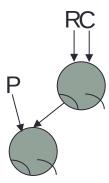
```
public void deleteSubtree(){
    if(current == root){
        current = root = null;
    else {
        BTNode<T> p = current;
        find(Relative.Parent);
        if(current.left == p)
             current.left = null;
        else
             current.right = null;
        current = root;
```



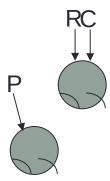
```
public void deleteSubtree(){
    if(current == root){
         current = root = null;
    else {
        BTNode < T > p = current;
        find(Relative.Parent);
        if(current.left == p)
             current.left = null;
        else
             current.right = null;
        current = root;
```



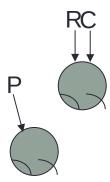
```
public void deleteSubtree(){
    if(current == root){
         current = root = null;
    else {
        BTNode < T > p = current;
        find(Relative.Parent);
        if(current.left == p)
             current.left = null;
        else
             current.right = null;
        current = root;
```



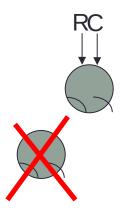
```
public void deleteSubtree(){
    if(current == root){
         current = root = null;
    else {
        BTNode < T > p = current;
        find(Relative.Parent);
        if(current.left == p)
             current.left = null;
        else
             current.right = null;
        current = root;
```



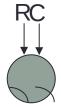
```
public void deleteSubtree(){
    if(current == root){
         current = root = null;
    else {
        BTNode < T > p = current;
        find(Relative.Parent);
        if(current.left == p)
             current.left = null;
        else
             current.right = null;
        current = root;
```



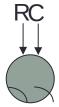
```
public void deleteSubtree(){
    if(current == root){
         current = root = null;
    else {
         BTNode < T > p = current;
         find(Relative.Parent);
         if(current.left == p)
             current.left = null;
         else
             current.right = null;
         current = root;
```



```
public void deleteSubtree(){
    if(current == root){
         current = root = null;
    else {
         BTNode < T > p = current;
         find(Relative.Parent);
         if(current.left == p)
             current.left = null;
         else
             current.right = null;
         current = root;
```



```
public void deleteSubtree(){
    if(current == root){
         current = root = null;
    else {
        BTNode < T > p = current;
        find(Relative.Parent);
        if(current.left == p)
             current.left = null;
        else
             current.right = null;
        current = root;
```



```
public void deleteSubtree(){
    if(current == root){
        current = root = null;
    else {
        BTNode < T > p = current;
        find(Relative.Parent);
        if(current.left == p)
             current.left = null;
        else
             current.right = null;
        current = root;
```





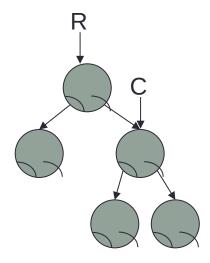
```
public void deleteSubtree(){
    if(current == root){
         current = root = null;
    else {
         BTNode < T > p = current;
         find(Relative.Parent);
         if(current.left == p)
             current.left = null;
         else
             current.right = null;
         current = root;
```



```
public boolean find(Relative rel){
    switch (rel) {
     case Root: // Easy case
    current = root;
   return true;
     case Parent:
   if(current == root) return false;
    current = findparent(current, root);
   return true;
     case LeftChild:
   if(current.left == null) return false;
    current = current.left;
   return true;
     case RightChild:
   if(current.right == null) return false;
    current = current.right;
   return true:
     default:
   return false;
```

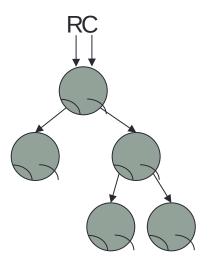
```
public boolean find(Relative rel){
    switch (rel) {
     case Root: // Easy case
    current = root;
   return true;
     case Parent:
   if(current == root) return false;
    current = findparent(current, root);
   return true;
     case LeftChild:
   if(current.left == null) return false;
    current = current.left;
   return true;
     case RightChild:
   if(current.right == null) return false;
    current = current.right;
   return true:
      default:
   return false;
```

Example #1 rel = Root



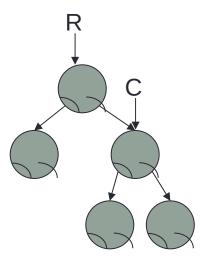
```
public boolean find(Relative rel){
    switch (rel) {
     case Root: // Easy case
    current = root;
   return true;
     case Parent:
   if(current == root) return false;
    current = findparent(current, root);
   return true;
     case LeftChild:
   if(current.left == null) return false;
    current = current.left;
   return true:
     case RightChild:
   if(current.right == null) return false;
    current = current.right;
   return true:
     default:
   return false;
```

Example #1 rel = Root



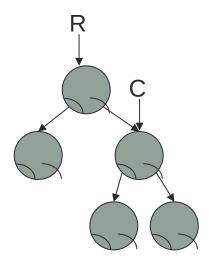
```
public boolean find(Relative rel){
    switch (rel) {
     case Root: // Easy case
    current = root;
   return true;
     case Parent:
   if(current == root) return false;
    current = findparent(current, root);
   return true;
      case LeftChild:
   if(current.left == null) return false;
    current = current.left;
   return true;
     case RightChild:
   if(current.right == null) return false;
    current = current.right;
   return true:
      default:
   return false;
```

Example #2 rel = LeftChild



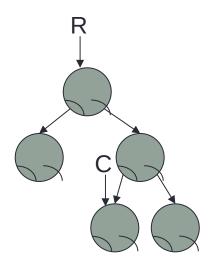
```
public boolean find(Relative rel){
    switch (rel) {
     case Root: // Easy case
    current = root;
   return true:
     case Parent:
   if(current == root) return false;
    current = findparent(current, root);
   return true;
     case LeftChild:
   if(current.left == null) return false;
    current = current.left;
   return true;
     case RightChild:
   if(current.right == null) return false;
    current = current.right;
   return true:
     default:
   return false;
```

Example #2 rel = LeftChild



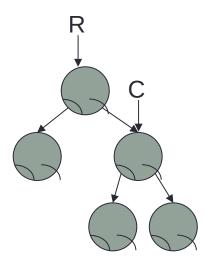
```
public boolean find(Relative rel){
    switch (rel) {
     case Root: // Easy case
    current = root;
   return true:
     case Parent:
   if(current == root) return false;
    current = findparent(current, root);
   return true;
     case LeftChild:
   if(current.left == null) return false;
    current = current.left;
   return true;
     case RightChild:
   if(current.right == null) return false;
    current = current.right;
   return true:
     default:
   return false;
```

Example #2 rel = LeftChild



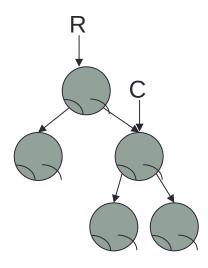
```
public boolean find(Relative rel){
    switch (rel) {
     case Root: // Easy case
    current = root;
   return true:
     case Parent:
   if(current == root) return false;
    current = findparent(current, root);
   return true;
      case LeftChild:
   if(current.left == null) return false;
    current = current.left;
   return true;
     case RightChild:
   if(current.right == null) return false;
    current = current.right;
   return true:
      default:
   return false;
```

Example #3 rel = RightChild



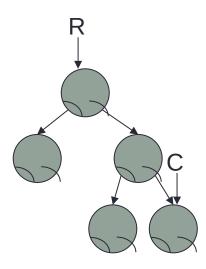
```
public boolean find(Relative rel){
    switch (rel) {
     case Root: // Easy case
    current = root;
   return true:
     case Parent:
   if(current == root) return false;
    current = findparent(current, root);
   return true;
     case LeftChild:
   if(current.left == null) return false;
    current = current.left;
   return true:
     case RightChild:
   if(current.right == null) return false;
    current = current.right;
   return true:
     default:
   return false;
```

Example #3 rel = RightChild



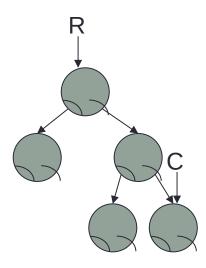
```
public boolean find(Relative rel){
    switch (rel) {
     case Root: // Easy case
    current = root;
   return true:
     case Parent:
   if(current == root) return false;
    current = findparent(current, root);
   return true;
     case LeftChild:
   if(current.left == null) return false;
    current = current.left;
   return true:
     case RightChild:
   if(current.right == null) return false;
    current = current.right;
   return true;
     default:
   return false;
```

Example #3 rel = RightChild



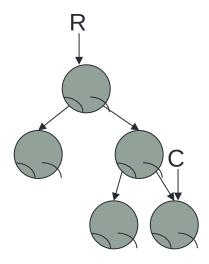
```
public boolean find(Relative rel){
    switch (rel) {
     case Root: // Easy case
    current = root;
   return true:
     case Parent:
   if(current == root) return false;
    current = findparent(current, root);
   return true;
      case LeftChild:
   if(current.left == null) return false;
    current = current.left;
   return true;
     case RightChild:
   if(current.right == null) return false;
    current = current.right;
   return true:
      default:
   return false;
```

Example #4 rel = RightChild



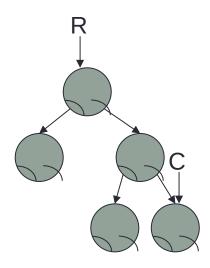
```
public boolean find(Relative rel){
    switch (rel) {
     case Root: // Easy case
    current = root;
   return true:
     case Parent:
   if(current == root) return false;
    current = findparent(current, root);
   return true;
     case LeftChild:
   if(current.left == null) return false;
    current = current.left;
   return true:
     case RightChild:
   if(current.right == null) return false;
    current = current.right;
   return true:
     default:
   return false;
```

Example #4 rel = RightChild



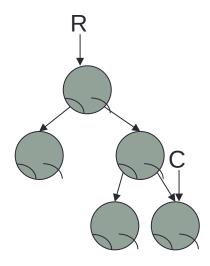
```
public boolean find(Relative rel){
    switch (rel) {
     case Root: // Easy case
    current = root;
   return true;
     case Parent:
   if(current == root) return false;
    current = findparent(current, root);
   return true;
      case LeftChild:
   if(current.left == null) return false;
    current = current.left;
   return true;
     case RightChild:
   if(current.right == null) return false;
    current = current.right;
   return true:
      default:
   return false;
```

Example #5 rel = LeftChild



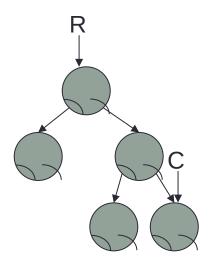
```
public boolean find(Relative rel){
    switch (rel) {
     case Root: // Easy case
    current = root;
   return true:
     case Parent:
   if(current == root) return false;
    current = findparent(current, root);
   return true;
     case LeftChild:
   if(current.left == null) return false;
    current = current.left;
   return true;
     case RightChild:
   if(current.right == null) return false;
    current = current.right;
   return true:
     default:
   return false;
```

Example #5 rel = LeftChild



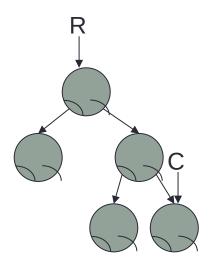
```
public boolean find(Relative rel){
    switch (rel) {
     case Root: // Easy case
    current = root;
   return true;
     case Parent:
   if(current == root) return false;
    current = findparent(current, root);
   return true;
      case LeftChild:
   if(current.left == null) return false;
    current = current.left;
   return true;
     case RightChild:
   if(current.right == null) return false;
    current = current.right;
   return true:
      default:
   return false;
```

Example #6 rel = Parent



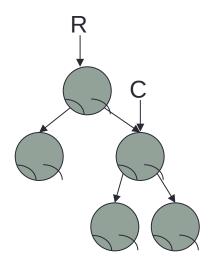
```
public boolean find(Relative rel){
    switch (rel) {
     case Root: // Easy case
    current = root;
   return true;
     case Parent:
   if(current == root) return false;
    current = findparent(current, root);
   return true;
     case LeftChild:
   if(current.left == null) return false;
    current = current.left;
   return true;
     case RightChild:
   if(current.right == null) return false;
    current = current.right;
   return true:
     default:
   return false;
```

Example #6 rel = Parent



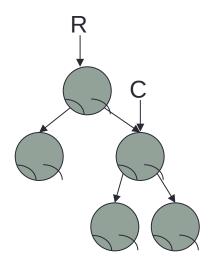
```
public boolean find(Relative rel){
    switch (rel) {
     case Root: // Easy case
    current = root;
   return true:
     case Parent:
   if(current == root) return false;
    current = findparent(current, root);
   return true;
     case LeftChild:
   if(current.left == null) return false;
    current = current.left;
   return true;
     case RightChild:
   if(current.right == null) return false;
    current = current.right;
   return true:
     default:
   return false;
```

Example #6 rel = Parent



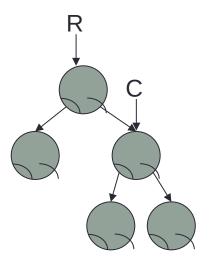
```
public boolean find(Relative rel){
    switch (rel) {
     case Root: // Easy case
    current = root;
   return true;
     case Parent:
   if(current == root) return false;
    current = findparent(current, root);
   return true;
      case LeftChild:
   if(current.left == null) return false;
    current = current.left;
   return true;
     case RightChild:
   if(current.right == null) return false;
    current = current.right;
   return true:
      default:
   return false;
```

Example #7 rel = Parent



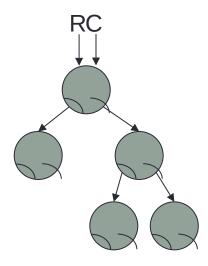
```
public boolean find(Relative rel){
    switch (rel) {
     case Root: // Easy case
    current = root;
   return true;
     case Parent:
   if(current == root) return false;
    current = findparent(current, root);
   return true;
     case LeftChild:
   if(current.left == null) return false;
    current = current.left;
   return true;
     case RightChild:
   if(current.right == null) return false;
    current = current.right;
   return true:
     default:
   return false;
```

Example #7 rel = Parent



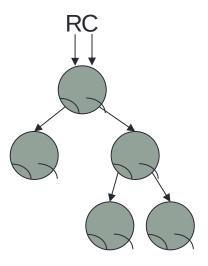
```
public boolean find(Relative rel){
    switch (rel) {
     case Root: // Easy case
    current = root;
   return true:
     case Parent:
   if(current == root) return false;
    current = findparent(current, root);
   return true;
     case LeftChild:
   if(current.left == null) return false;
    current = current.left;
   return true;
     case RightChild:
   if(current.right == null) return false;
    current = current.right;
   return true:
     default:
   return false;
```

Example #7 rel = Parent



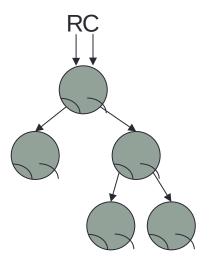
```
public boolean find(Relative rel){
    switch (rel) {
     case Root: // Easy case
    current = root;
   return true;
     case Parent:
   if(current == root) return false;
    current = findparent(current, root);
   return true;
     case LeftChild:
   if(current.left == null) return false;
    current = current.left;
   return true;
     case RightChild:
   if(current.right == null) return false;
    current = current.right;
   return true:
      default:
   return false;
```

Example #8 rel = Parent



```
public boolean find(Relative rel){
    switch (rel) {
     case Root: // Easy case
    current = root;
   return true:
     case Parent:
   if(current == root) return false;
    current = findparent(current, root);
   return true;
     case LeftChild:
   if(current.left == null) return false;
    current = current.left;
   return true;
     case RightChild:
   if(current.right == null) return false;
    current = current.right;
   return true:
     default:
   return false;
```

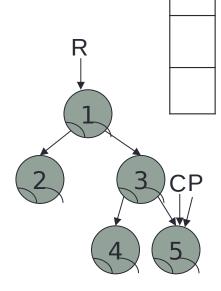
Example #8 rel = Parent



```
// Non-recursive version of findparent – uses pre-order traversal
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    // Stack is used to store the right pointers of nodes
    LinkStack<BTNode<T>> stack = new LinkStack<BTNode<T>>();
    BTNode < T > q = t;
    while(q.right != p && q.left != p) {
        if(q.right != null)
             stack.push(q.right);
        if(q.left != null)
             q = q.left;
        else
             q = stack.pop(); // Go right here
    return q;
}
```

```
// Non-recursive version of findparent – uses pre-order traversal
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    // Stack is used to store the right pointers of nodes
    LinkStack < BTNode < T >> stack = new LinkStack < BTNode < T >> ();
    BTNode < T > q = t;
    while(q.right != p && q.left != p) {
         if(q.right != null)
             stack.push(q.right);
         if(q.left != null)
             q = q.left;
         else
             q = stack.pop(); // Go right here
                                                                Example #1
    return q;
                                                             p = current, t = root
}
```

```
// Non-recursive version of findparent – uses pre-order traversal
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    // Stack is used to store the right pointers of nodes
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LinkStack<BTNode<T>>();
    BTNode < T > q = t;
    while(q.right != p && q.left != p) {
        if(q.right != null)
             stack.push(q.right);
        if(q.left != null)
            q = q.left;
        else
             q = stack.pop(); // Go right here
    return q;
}
```



```
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             stack.push(q.right);
        if(q.left != null)
             q = q.left;
        else
             q = stack.pop(); // Go right here
                                                              Example #1
    return q;
                                                            p = current, t = root
}
```

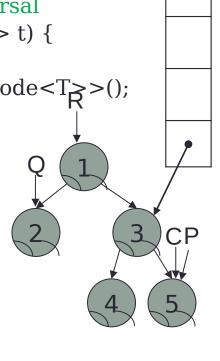
```
// Non-recursive version of findparent – uses pre-order traversal
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    // Stack is used to store the right pointers of nodes
    LinkStack<BTNode<T>> stack = new LinkStack<BTNode<T
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    while (q.right != p && q.left != p) {
        if(q.right != null)
             stack.push(q.right);
        if(q.left != null)
             q = q.left;
        else
             q = stack.pop(); // Go right here
                                                              Example #1
    return q;
                                                            p = current, t = root
}
```

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// Non-recursive version of findparent – uses pre-order traversal
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        if(q.right != null)
             stack.push(q.right);
        if(q.left != null)
             q = q.left;
        else
             q = stack.pop(); // Go right here
                                                              Example #1
    return q;
                                                            p = current, t = root
}
```

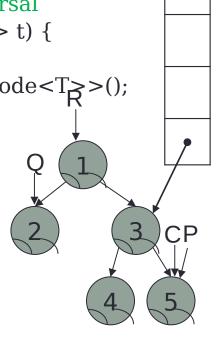
```
// Non-recursive version of findparent – uses pre-order traversal
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    // Stack is used to store the right pointers of nodes
    LinkStack<BTNode<T>> stack = new LinkStack<BTNode<T
    BTNode < T > q = t;
    while(q.right != p && q.left != p) {
        if(q.right != null)
             stack.push(q.right);
        if(q.left != null)
             q = q.left;
        else
             q = stack.pop(); // Go right here
                                                              Example #1
    return q;
                                                            p = current, t = root
}
```

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// Non-recursive version of findparent – uses pre-order traversal
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             stack.push(q.right);
        if(q.left != null)
             q = q.left;
        else
             q = stack.pop(); // Go right here
                                                              Example #1
    return q;
                                                            p = current, t = root
}
```

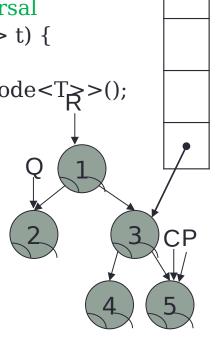
```
// Non-recursive version of findparent – uses pre-order traversal
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    // Stack is used to store the right pointers of nodes
     LinkStack < BTNode < T >> stack = \mathbf{new} \ LinkStack < BTNode < T_{\overrightarrow{P}} > ();
     BTNode < T > q = t;
    while(q.right != p && q.left != p) {
         if(q.right != null)
              stack.push(q.right);
         if(q.left != null)
              q = q.left;
         else
              q = stack.pop(); // Go right here
    return q;
}
```



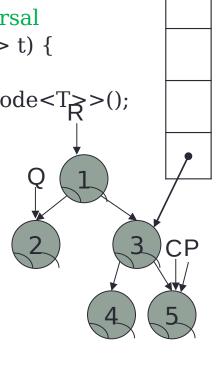
```
// Non-recursive version of findparent – uses pre-order traversal
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    // Stack is used to store the right pointers of nodes
     LinkStack < BTNode < T >> stack = \mathbf{new} \ LinkStack < BTNode < T_{\overrightarrow{P}} > ();
     BTNode < T > q = t;
    while (q.right != p && q.left != p) {
         if(q.right != null)
              stack.push(q.right);
         if(q.left != null)
              q = q.left;
         else
              q = stack.pop(); // Go right here
    return q;
}
```



```
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private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    // Stack is used to store the right pointers of nodes
     LinkStack < BTNode < T >> stack = \mathbf{new} \ LinkStack < BTNode < T_{\overrightarrow{P}} > ();
     BTNode < T > q = t;
    while(q.right != p && q.left != p) {
         if(q.right != null)
              stack.push(q.right);
         if(q.left != null)
              q = q.left;
         else
              q = stack.pop(); // Go right here
    return q;
}
```



```
// Non-recursive version of findparent – uses pre-order traversal
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    // Stack is used to store the right pointers of nodes
     LinkStack < BTNode < T >> stack = \mathbf{new} \ LinkStack < BTNode < T_{\overrightarrow{P}} > ();
     BTNode < T > q = t;
    while(q.right != p && q.left != p) {
         if(q.right != null)
              stack.push(q.right);
         if(q.left != null)
              q = q.left;
         else
              q = stack.pop(); // Go right here
    return q;
}
```



```
// Non-recursive version of findparent – uses pre-order traversal
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    // Stack is used to store the right pointers of nodes
    LinkStack < BTNode < T >> stack = \mathbf{new} \ LinkStack < BTNode < T_{\overrightarrow{P}} > ();
     BTNode < T > q = t;
    while(q.right != p && q.left != p) {
         if(q.right != null)
              stack.push(q.right);
         if(q.left != null)
              q = q.left;
         else
              q = stack.pop(); // Go right here
                                                                    Example #1
    return q;
                                                                 p = current, t = root
}
```

```
// Non-recursive version of findparent – uses pre-order traversal
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    // Stack is used to store the right pointers of nodes
     LinkStack < BTNode < T >> stack = \mathbf{new} \ LinkStack < BTNode < T_{\overrightarrow{P}} > ();
     BTNode < T > q = t;
    while (q.right != p && q.left != p) {
         if(q.right != null)
              stack.push(q.right);
         if(q.left != null)
              q = q.left;
         else
              q = stack.pop(); // Go right here
                                                                    Example #1
    return q;
                                                                  p = current, t = root
}
```

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// Non-recursive version of findparent – uses pre-order traversal
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    // Stack is used to store the right pointers of nodes
     LinkStack < BTNode < T >> stack = \mathbf{new} \ LinkStack < BTNode < T_{\overrightarrow{P}} > ();
     BTNode < T > q = t;
    while(q.right != p && q.left != p) {
         if(q.right != null)
              stack.push(q.right);
         if(q.left != null)
              q = q.left;
         else
              q = stack.pop(); // Go right here
                                                                     Example #1
    return q;
                                                                  p = current, t = root
}
```

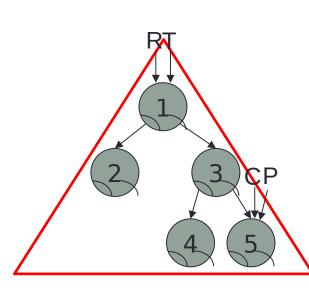
```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
             return findparent(p, t.right);
```

```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
                                                                  RT
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
                                                               Example #1
             return findparent(p, t.right);
```

```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
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        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
                                                              Example #1
             return findparent(p, t.right);
```

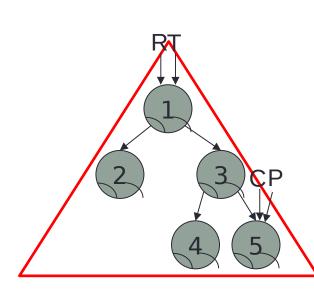
10/

```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
             return findparent(p, t.right);
```



Example #1

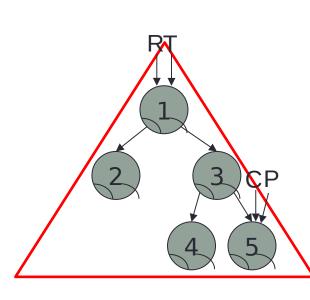
```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
             return findparent(p, t.right);
```



Example #1

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```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p || t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
            return findparent(p, t.right);
```



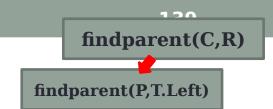
Example #1



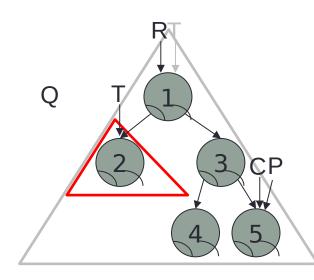
```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
                                                       Q
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
                                                              Example #1
             return findparent(p, t.right);
```



```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
                                                       Q
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
                                                              Example #1
             return findparent(p, t.right);
```



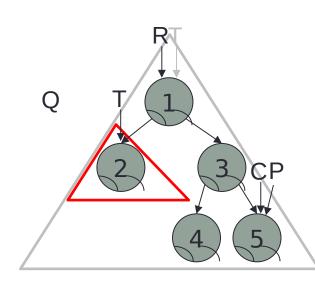
```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
             return findparent(p, t.right);
```



Example #1



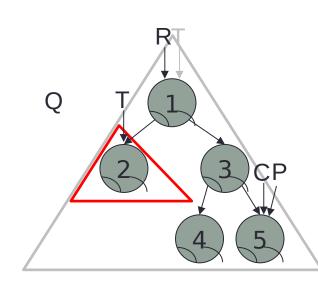
```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
             return findparent(p, t.right);
```



Example #1



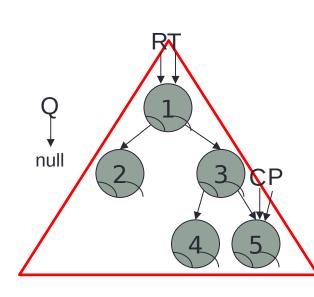
```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
             return findparent(p, t.right);
```



Example #1

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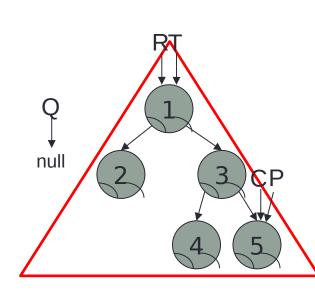
```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
             return findparent(p, t.right);
```



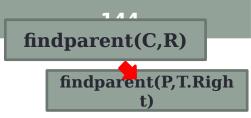
Example #1

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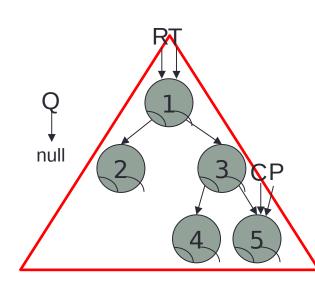
```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q != null)
             return q;
        else
             return findparent(p, t.right);
```



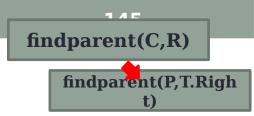
Example #1



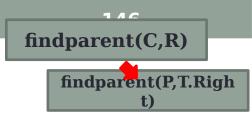
```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
             return findparent(p, t.right);
```



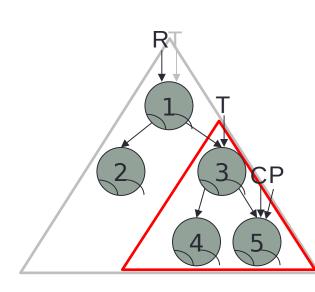
Example #1



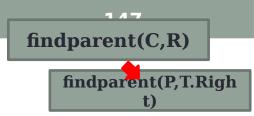
```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
                                                              Example #1
             return findparent(p, t.right);
```



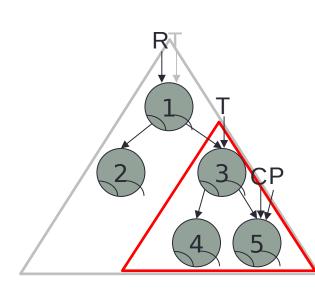
```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
             return findparent(p, t.right);
```



Example #1

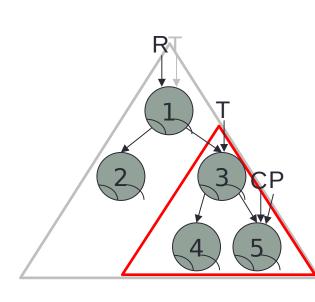


```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
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    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
             return findparent(p, t.right);
```

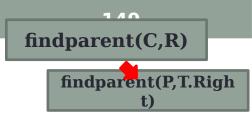


Example #1

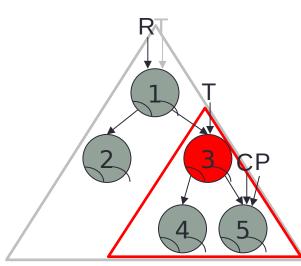
```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p || t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
            return findparent(p, t.right);
```



Example #1

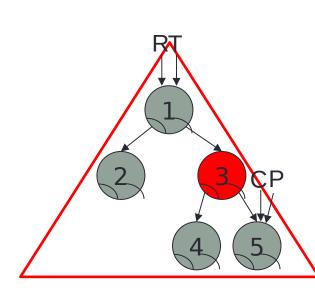


```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
             return findparent(p, t.right);
```



Example #1

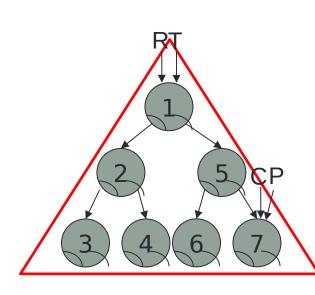
```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
             return findparent(p, t.right);
```



Example #1

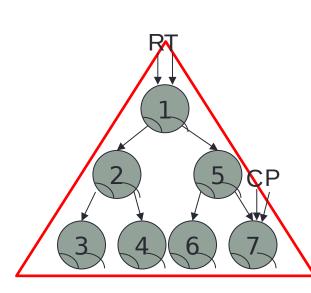
```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
                                                                  RT
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
                                                               Example #2
             return findparent(p, t.right);
```

```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
             return findparent(p, t.right);
```



Example #2

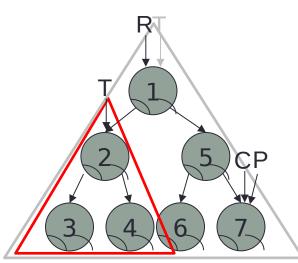
```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
             return findparent(p, t.right);
```



Example #2



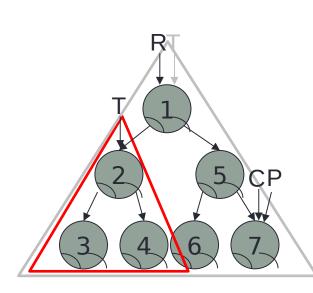
```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
             return findparent(p, t.right);
```



Example #2



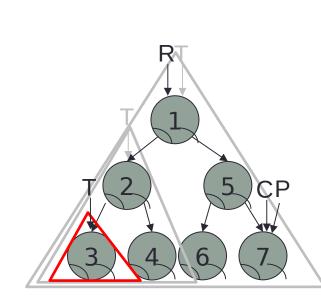
```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
             return findparent(p, t.right);
```



Example #2

156 findparent(C,R) findparent(P,T.Left) findparent(P,T.Left)

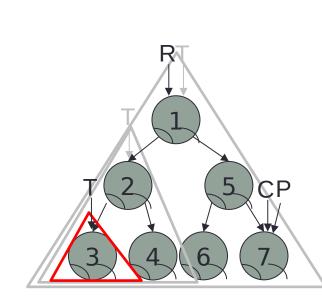
```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
             return findparent(p, t.right);
```



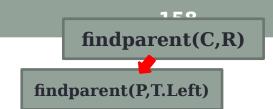
Example #2

1 E 7 findparent(C,R) findparent(P,T.Left) findparent(P,T.Left)

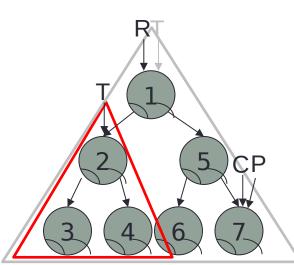
```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
             return findparent(p, t.right);
```



Example #2



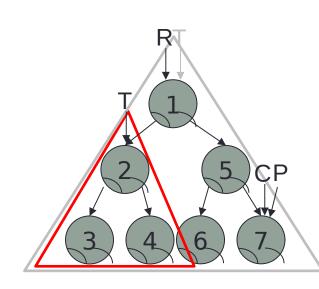
```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
             return findparent(p, t.right);
```



Example #2



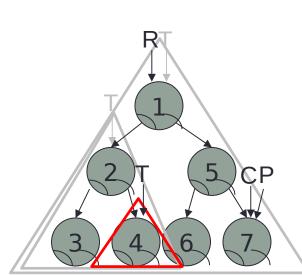
```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
             return findparent(p, t.right);
```



Example #2

findparent(C,R) findparent(P,T.Left) findparent(P,T.Right)

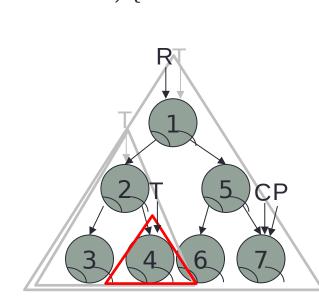
```
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private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
             return findparent(p, t.right);
```



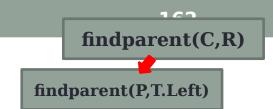
Example #2

161 findparent(C,R) findparent(P,T.Left) findparent(P,T.Righ t)

```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
             return findparent(p, t.right);
```

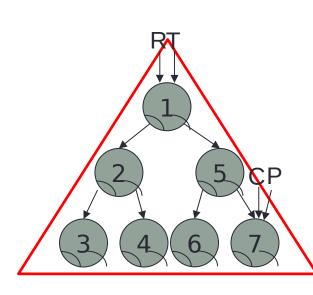


Example #2



```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
                                                               Example #2
             return findparent(p, t.right);
```

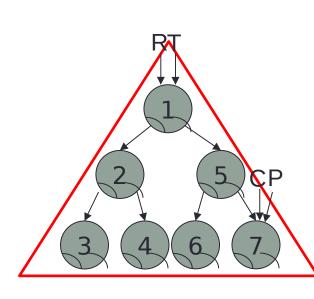
```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
             return findparent(p, t.right);
```



Example #2

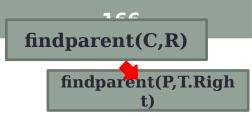
161

```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
             return findparent(p, t.right);
```



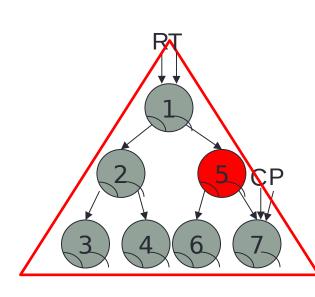
Example #2

```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
                                                               Example #2
             return findparent(p, t.right);
```



```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p || t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
            return q;
        else
                                                             Example #2
            return findparent(p, t.right);
```

```
// Recursive version of findparent – preorder traversal used
private BTNode<T> findparent(BTNode<T> p, BTNode<T> t) {
    if(t == null)
        return null; // empty tree
    if(t.right == null \&\& t.left == null)
        return null;
    else if(t.right == p \mid\mid t.left == p)
        return t; // parent is t
    else {
        BTNode q = findparent(p, t.left);
        if (q!= null)
             return q;
        else
             return findparent(p, t.right);
```



Example #2