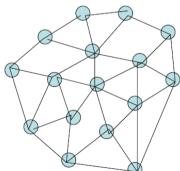
# **GRAPHS**

CSC 212

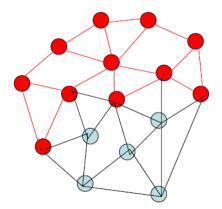
### Graphs

- Many interesting situations can be modeled by a graph.
- is a way of representing connections or relationships between pairs of objects from some set.

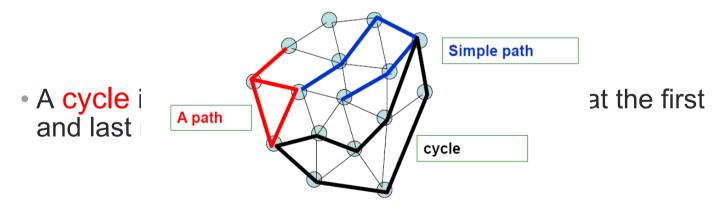


• Ex. Mass transportation system, computer network, electrical engineering

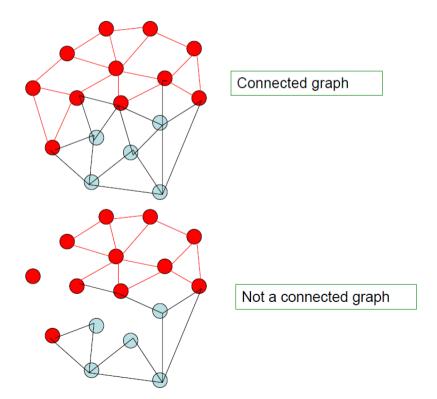
- A graph consists of a set of vertices and a set of edges.
- A vertex v is basic component, which usually contains some information.
- An edge (v,w) connects two distinct vertices v and w.
- A subgraph is graph which consists of a subset of nodes (vertices) and a subset of edges of a graph.



- A path is a sequence of nodes such that each successive pair is connected by an edge.
- A path is a simple path if each of its nodes occurs once in the sequence.

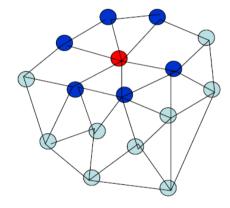


• A graph is a connected graph if there is a path between every pair of its nodes.



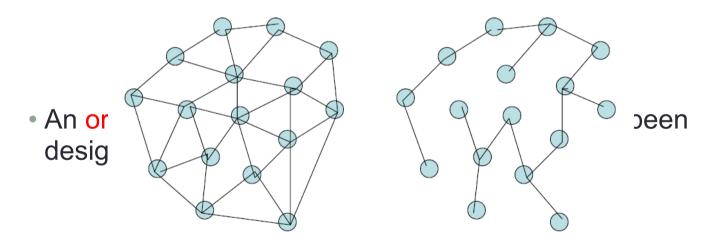
• Two nodes are adjacent nodes if there is an edge that connects them.

- Neighbors of a ne
- A Tree is the spec
  - (i) is connected
  - (ii) has no cycle



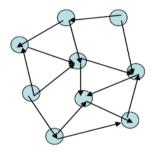
it are adjacent to it.

• If a connected graph has n nodes and n-1 edges, then it is a tree. This tree is called **Spanning Tree**.

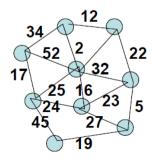


 A directed graph or digraph is a graph in which each edge has an associated direction.

 A weighted grap associated value.



which each edge has an



#### Elements:

A graph consists of nodes and edges

#### Structure:

An edge is a one-to-one relationship between a pair of distinct nodes. A pair of nodes can be connected by at most one edge, but any node can be connected to any collection of other nodes.

### • Domain:

The number of nodes (vertices) in a graph is bounded.

### **Operations:**

InsertNode (Type e)

Requires: G is not full.

Results: If G does not contain an element whose key value

is e.key then e is inserted in G and inserted is true,

otherwise inserted is false.

#### InsertEdge (Key k1, k2)

Requires: G is not full and k1!=k2.

Results: If G contains two nodes whose key values are k1 and k2 then G contains an edge connecting those nodes. If the two nodes were connected by an edge before operation InsertEdge then inserted is false; otherwise inserted is true.

- DeleteNode (Key k)
- Results: G does not contain an element whose key value is k. if G contained a node before this operation with key value k then deleted is true and no edge that connected this node to an other node is in G; otherwise deleted is false.
- DeleteEdge (Key k1, k2)
- Results: G does not contain an edge that connects nodes whose key values are k1 and k2. If G contained such an edge before this operation then deleted is true; otherwise deleted is false.

#### Update (T e)

Results: If G contained a node with key value e.key then the element in the node is e and updated is true. Otherwise updated is false.

#### Retrieve (key k, T e)

Results: If G contains a node whose key value is k before this operation then e is that element and retrieved is true; otherwise retrieved is false.

#### • Full ()

Results: If G is full then Full returns true; otherwise Full returns false.

### Representation of a Graph

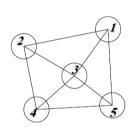
There are two approaches to representing graphs

- (i) Adjacency Matrix
- (ii) Adjacency List

### Adjacency Matrix

 A two dimensional array whose components are of type Boolean and whose index values correspond to the nodes.

		1	2	3	4	5
	1	0	1	1	0	1
Thio ropro	2	1	0	1	1	0
<ul><li>This repres is O(n2) if</li></ul>	3	1	1	0	1	1
` ,	4	0	1	1	0	1
This repres	5	1	0	1	1	0
tile Hullibe						



If A is the adjacency matrix corresponding to a graph G, then A<sub>ij</sub> corresponds to the edge (i, j), and is true if there is an edge between the vertices i, and j.

requirement

dense with er of vertices

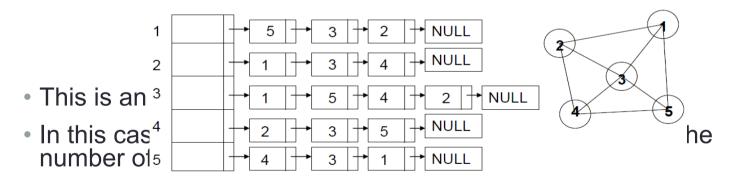
. But in most of the applications this is not true.

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فيد كلام 100 و(1 / إرسة
وفاده إمر مشكلة الـ 20 Army
فاده إمر الله المنظمة على المنظمة المنظمة
```

### Adjacency list

It is an array where each cell corresponds to a vertex of a graph and stores the header of a list of all adjacent vertices.
Ex. The following is an adjacency list corresponding to the graph on the

right.



### Traversal of a Graph

- Process each node of the graph only once
- There are two methods for graph traversal
  - (i) Breadth First Search
  - (ii) Depth First Search The other one uses stack

## Breadth First Search (BFS)

- Breadth First Search (BFS) Start at some source node s and visit all its neighbors, then visit the neighbors of each neighbor of s and so on.
- ALgorithm
  - 1. Assign the status of waiting to all nodes of a graph.
  - 2. Start with source node s, and put it in queue
  - 3.Dequeue one node from the queue, assign it the status of processed, and assign its neighbors the status of ready and put them in the queue.
  - 4. Repeat Step 3 until the queue is empty.

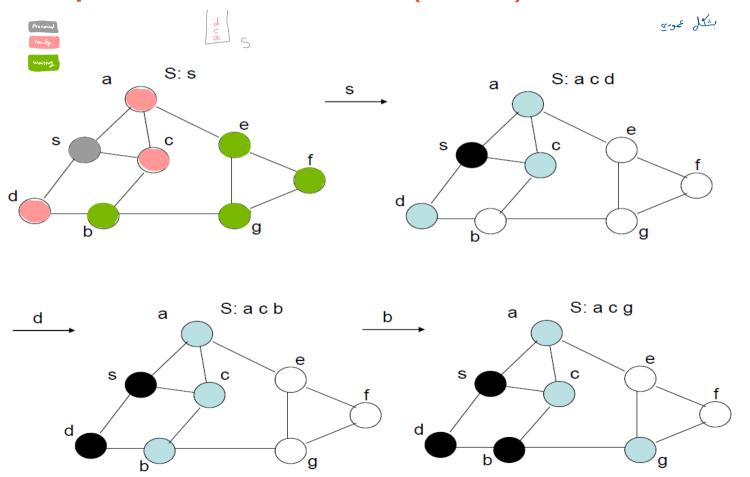
### Breadth First Search (BFS)

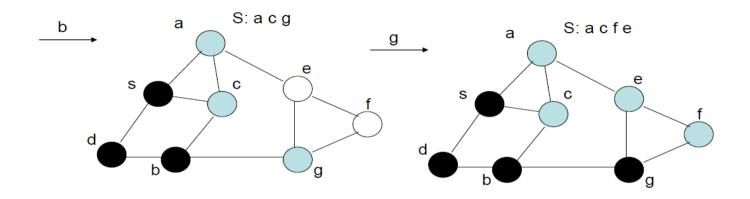
Processed ready Example Waiting Consider a graph with nodes a, b, c, d, e, f, g, s يتك القراف يخكل أخقى cSO Q: a, c, d Q: d, e, b Q: c, d, e b, f, g 0 Q: (empty) Q: b, f, g Q: e, b

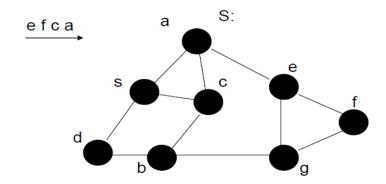
### Breadth First Search (BFS)

```
بن فيه ز شاورد الله
Pseudocode for BFS
BFS(G, s)
    for each node u of G
        set status[u] = waiting; حمير ويتنه كل النودر مهير ويتنه
    status[s] = ready;
    Q = {s}; -> طنا الموس عاكم -
                                         يخلي السورس رميري
    while(!Q.IsEmpty) مطال إم الكيوم، قابق
        u = Q.dequeue(); aka serve
        for each v in Neigh[u]
             if(status[v] = waiting)
                                              رنيك النيورز حقت العنفو اللي طلعناه مم الكيو
                                                  بأذا كانؤا وتتعمد لخطهم ريدي ونخلهم بالكيو
             staus[v] = ready;
                                                 عدى ذلك فيمكم هي أملًا ربدى وموجوديم بالكيو
             Q.enqueue(v);
                                                         أو بعروسيد يعن خلفهنا أشعم
        status[u] = processed;
```

- DFS visits one node and then visits one of its neighbors and puts the rest of its neighbors into a stack and so on.
- Algorithm
  - 1. Assign the status of waiting to all nodes of a graph.
  - 2. For each node of the graph, follow the following steps,
    - a)Change the status of the node to be ready and put in a stack
    - b)Repeat the following steps until the stack is empty:
    - c)Get a node from the stack, process it, change its status to processed and change the status from waiting to ready of its neighbors and put them in the stack
    - d)Go to step b







```
Pseudocode for DFS
 DFS(G)
 for each node u of G
                         status[u] = waiting; مغلیهم وهیم وسیر
 for each node u of G
        if(status[u] == waiting)
                         Visit(u)
  Visit(u)
 stack S; ح
status[u] = ready; جر المود والمالية
  ن خله حوا بنان د الله حوا المال د
 while(|S.IsEmpty) יים טיין צול
                         v = S.pop(); نطلح دنهر
                         for each w in Neigh[v]
                                  if(status[w] = waiting)
                                                                                                                                                                                                       نظلح جيرانه العنهدالل طلعاه
                                     staus[w] = ready;
                                    S.push(w);
                                                                                                                                                                                                                                          وندخله حوا الساك
                         status[v] = processed; المرابع المراب
```

حرکا*ت عجی*بة دس عل*ة*