

STACK OPERATIONS

CS212: Data Structure

Applications of Stacks

- Direct applications

- Page-visited history in a Web browser
- Undo sequence in a text editor
- Chain of method calls in the Java Virtual Machine

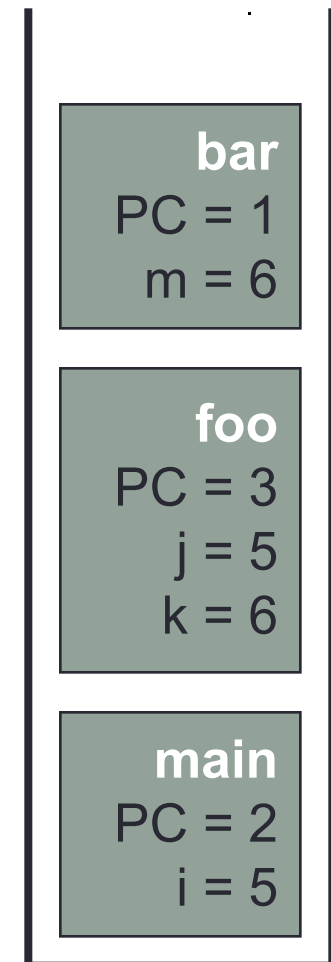
- Indirect applications

- Auxiliary data structure for algorithms
- Component of other data structures → ^{Ex.} "Implement a stack of queue"

Method Stack in the JVM

- The Java Virtual Machine (JVM) keeps track of the chain of active methods with a stack
- When a method is called, the JVM pushes on the stack a frame containing
 - Local variables and return value
 - Program counter, keeping track of the statement being executed
- When a method ends, its frame is popped from the stack and control is passed to the method on top of the stack
- Allows for **recursion**

```
main() {  
    int i = 5;  
    foo(i);  
}  
  
foo(int j) {  
    int k;  
    k = j+1;  
    bar(k);  
}  
  
bar(int m) {  
    ...  
}
```



Reverse a List using Stack

```
public class Tester {
```

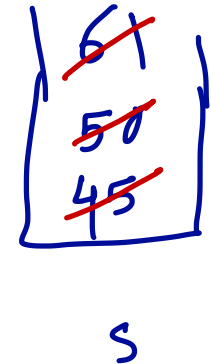
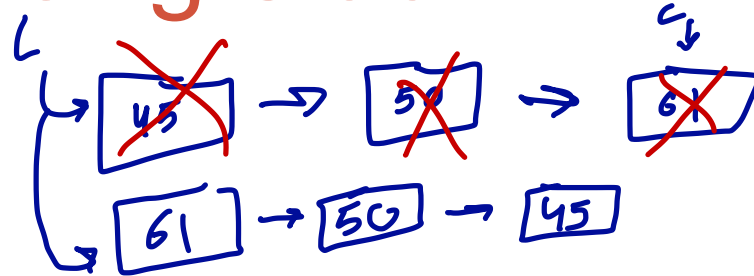
```
// ... other methods here
```

```
public void intReverse(List<Integer> l) {
    Stack<Integer> s = new Stack<Integer>();
```

```
    l.findFirst();
    while(!l.empty()) {
        s.push(l.retrieve());
        l.remove();
    }
```

```
    while(!s.empty())
        l.insert(s.pop());
```

```
}
```



Parentheses Matching

- Each “(”, “{”, or “[” must be paired with a matching “)”, “}”, or “]”
 - correct: ()(()){([())}
 - correct: ((()(()))}{([())}
 - incorrect:)(()){([())}
 - incorrect: ({ []})
 - incorrect: (

Parentheses Matching Algorithm

Algorithm ParenMatch(X, n):

Input: An array X of n tokens, each of which is either a grouping symbol, a variable, an arithmetic operator, or a number

Output: **true** if and only if all the grouping symbols in X match

Let S be an empty stack

for $i=0$ to $n-1$ **do**

if $X[i]$ is an opening grouping symbol **then**

$S.push(X[i])$

else if $X[i]$ is a closing grouping symbol **then**

if $S.isEmpty()$ **then**

return false {nothing to match with}

if $S.pop()$ does not match the type of $X[i]$ **then**

return false {wrong type}

if $S.isEmpty()$ **then**

return true {every symbol matched}

else

return false {some symbols were never matched}

HTML Tag Matching

For fully-correct HTML, each `<name>` should pair with a matching `</name>`

```
<body>
  <center>
    <h1> The Little Boat </h1>
  </center>
  <p> The storm tossed the little
boat like a cheap sneaker in an
old washing machine. The three
drunken fishermen were used to
such treatment, of course, but
not the tree salesman, who even as
a stowaway now felt that he
had overpaid for the voyage.</p>
  <ol>
    <li> Will the salesman die? </li>
    <li> What color is the boat? </li>
    <li> And what about Naomi? </li>
  </ol>
</body>
```

The Little Boat

The storm tossed the little boat like a cheap sneaker in an old washing machine. The three drunken fishermen were used to such treatment, of course, but not the tree salesman, who even as a stowaway now felt that he had overpaid for the voyage.

1. Will the salesman die?
2. What color is the boat?
3. And what about Naomi?

Evaluating Arithmetic Expressions

$$14 - 3 * 2 + 7 = (14 - (3 * 2)) + 7$$

Operator precedence

* has precedence over +/−

Associativity

operators of the same precedence group
evaluated from left to right

Example: $(x - y) + z$ rather than $x - (y + z)$

Idea: push each operator on the stack, but first pop and perform higher and *equal* precedence operations.

Algorithm for Evaluating Expressions

Two stacks:

- opStk holds operators
- valStk holds values
- Use \$ as special “end of input” token with lowest precedence

Algorithm doOp()

```
x ← valStk.pop();
y ← valStk.pop();
op ← opStk.pop();
valStk.push( y op x )
```

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Algorithm repeatOps(refOp):

```
while ( valStk.size() > 1 ^ )
    prec(refOp) ≤ prec(opStk.top() )
    doOp()
```

Algorithm EvalExp()

Input: a stream of tokens representing an arithmetic expression (with numbers)

Output: the value of the expression

while there's another token z

if isNumber(z) **then**

valStk.push(z)

else

repeatOps(z);

opStk.push(z)

repeatOps(\$);

return valStk.top()

Algorithm on an Example Expression

14 ≤ 4 - 3 * 2 + 7

Operator ≤ has lower precedence than +/−

