

Question 3. (8+8+4=20 Marks)

(a) You have to store information about each student in a group of **about 200** students in a hash table. Each student's key is his id. Number, for example, 427102181.

(i) Give a suitable table size and a hash function based on **digit selection**, assuming that **the external chaining** is the collision resolution strategy employed.

(ii) Give a suitable table size and a hash function based on division if the number of students is exactly 200 and **linear rehashing** is the collision resolution strategy employed.

(b) Insert the following keys: 904, 918, 855, 913, 806, 841 and 778, into a hash table with hash function **$H(key) = key \bmod 7$** , using linear rehashing as collision resolution strategy.

(c) How many probes are required to store 913 and 841?

Q3 –a/i)

Table Size = 100 since we are using External chaining for the collision resolution strategy.

$H(key) = key \bmod 100$.

Q3 –a/ii)

Table Size = 200 since we are using linear rehashing is the collision resolution strategy

$H(key) = key \bmod 200$.

Q3 –b and c)

E	E	E	E	E	E	E
0	1	2	3	4	5	6

Insert Key 904: $H(904) = 904 \bmod 7 = 1$ **Props = 1**

E	904	E	E	E	E	E
0	1	2	3	4	5	6

Insert Key 918: $H(918) = 918 \bmod 7 = 1$ **Collision in index 1.**

Rehash = $p + c \bmod \text{tableSize} = 1 + 1 \bmod 7 = 2$ **Props = 2**

E	904	918	E	E	E	E
0	1	2	3	4	5	6

Insert Key 855 : $H(855) = 855 \bmod 7 = 1$ **Collision in index 1.**

Rehash = $p + c \bmod \text{tableSize} = 1 + 1 \bmod 7 = 2$ **Collision in index 2.**

Rehash = $p + c \bmod \text{tableSize} = 2 + 1 \bmod 7 = 3$ **Props = 3**

E	904	918	855	E	E	E
0	1	2	3	4	5	6

Insert Key 913: $H(913) = 913 \bmod 7 = 3$ Collision in index 3.

Rehash = $p + c \bmod \text{tableSize} = 3 + 1 \bmod 7 = 4$ **Props = 2**

E	904	918	855	913	E	E
0	1	2	3	4	5	6

Insert Key 806 : $H(806) = 806 \bmod 7 = 1$ Collision in index 1.

Rehash = $p + c \bmod \text{tableSize} = 1 + 1 \bmod 7 = 2$ Collision in index 2.

Rehash = $p + c \bmod \text{tableSize} = 2 + 1 \bmod 7 = 3$ Collision in index 3.

Rehash = $p + c \bmod \text{tableSize} = 3 + 1 \bmod 7 = 4$ Collision in index 4.

Rehash = $p + c \bmod \text{tableSize} = 4 + 1 \bmod 7 = 5$ **Props = 5**

E	904	918	855	913	806	E
0	1	2	3	4	5	6

Insert Key 841: $H(841) = 841 \bmod 7 = 1$ Collision in index 1.

Rehash = $p + c \bmod \text{tableSize} = 1 + 1 \bmod 7 = 2$ Collision in index 2.

Rehash = $p + c \bmod \text{tableSize} = 2 + 1 \bmod 7 = 3$ Collision in index 3.

Rehash = $p + c \bmod \text{tableSize} = 3 + 1 \bmod 7 = 4$ Collision in index 4.

Rehash = $p + c \bmod \text{tableSize} = 4 + 1 \bmod 7 = 5$ Collision in index 5.

Rehash = $p + c \bmod \text{tableSize} = 5 + 1 \bmod 7 = 6$ **Props = 6**

E	904	918	855	913	806	841
0	1	2	3	4	5	6

Insert Key 778 : $H(778) = 778 \bmod 7 = 1$ Collision in index 1.

Rehash = $p + c \bmod \text{tableSize} = 1 + 1 \bmod 7 = 2$ Collision in index 2.

Rehash = $p + c \bmod \text{tableSize} = 2 + 1 \bmod 7 = 3$ Collision in index 3.

Rehash = $p + c \bmod \text{tableSize} = 3 + 1 \bmod 7 = 4$ Collision in index 4.

Rehash = $p + c \bmod \text{tableSize} = 4 + 1 \bmod 7 = 5$ Collision in index 5.

Rehash = $p + c \bmod \text{tableSize} = 5 + 1 \bmod 7 = 6$ Collision in index 6.

Rehash = $p + c \bmod \text{tableSize} = 6 + 1 \bmod 7 = 0$. **Props = 7**

E	904	918	855	913	806	841
0	1	2	3	4	5	6