

**Department of Computer Science,  
Data Structures (CSC212),  
Tutorial 9  
Autumn Semester 1427-28**

**Question 1.**

Use the hash function  $H(\text{key}) = \text{key} \bmod 11$  to store the sequence of integers: 82, 31, 28, 4, 45, 27, 59, 79, 35 in the hash table of TableSize = 11. (a) Use linear rehashing (b) Use external chaining (c) Use coalesced chaining with a cell size of four and the hash function  $H(\text{key}) = \text{key} \bmod 7$ .

For each of the collision resolution strategies determine (after the values have been inserted into the table) the following:

(d) The load factor (e) The average number of probes needed to find a value that is in the table (f) The average number of probes needed to find a value that is not in the table.

**Question 2.**

Develop a hashing function to store student's records, with ID # as their key, into a hash table of a suitable size. Assume that the number of students is about 1000. Use a suitable collision resolution strategy.

**Question 3.**

Develop a hashing function to convert a character key of 15 characters into integers in the range of 0 to 999.

**Question 4.**

Assuming the keys are integers, denoted by  $d_n d_{n-1} \dots d_k \dots d_2 d_1$  where  $d_i$  is the  $i$ -th decimal digit in the key,  $d_n$  being the leftmost decimal digit. The hash function  $H(\text{key})$  is given by:

$$H(\text{key}) = (d_1 d_2 + d_{n-1} d_n + d_k) \bmod 11$$

where  $d_1 d_2$  is a two digit number (composed by swapping the rightmost two digits),  $d_{n-1} d_n$  is also a two digit number (composed by swapping the leftmost two digits), and  $k = \lceil n/2 \rceil$ . For example:

$$H(70934) = (43 + 07 + 9) \bmod 11 = 59 \bmod 11 = 4.$$

Assume the keys are: 1234, 519, 911, 7346, 0, 999, 99834, 54 and 40015.

- (a) Compute  $H(\text{key})$  for each of the above keys.
- (b) Insert the above keys (in exactly the same order) in a hash table with open addressing (linear rehashing).
- (c) Find the number of probes required to search for keys 54 and 11 in the above hash table.
- (d) Repeat part (b) using an external chaining hash table.

Q1

$$H(\text{key}) = \text{key} \bmod 11$$

①  $H(82) = 82 \bmod 11 = 3$

LF  $1/11$

e	e	e	e	e	82	e	e	c	c	e
0	1	2	3	4	5	6	7	8	9	10

1 prob

②  $H(31) = 31 \bmod 11 = 9$

LF  $2/11$

e	e	e	e	e	82	e	e	c	31	e
0	1	2	3	4	5	6	7	8	9	10

1 prob

③  $H(28) = 28 \bmod 11 = 6$

LF  $3/11$

					82	28			31	
0	1	2	3	4	5	6	7	8	9	10

1 prob

④  $H(4) = 4 \bmod 11 = 4$

LF  $4/11$

				4	82	28			31	
0	1	2	3	4	5	6	7	8	9	10

1 prob

⑤  $H(45) = 45 \bmod 11 = 1$

LF  $5/11$

	45			4	82	28			31	
0	1	2	3	4	5	6	7	8	9	10

1 prob

⑥  $H(27) = 27 \bmod 11 = 5$

LF  $6/11$

	45			4	82	28	27		31	
0	1	2	3	4	5	6	7	8	9	10

~~rehash = 5 mod 7 = 5~~  
~~6 mod 7 = 6~~

3 probs

rehash =  $5 + 1 \bmod 11 = 6$

=  $6 + 1 \bmod 11 = 7$

⑦  $H(59) = 59 \bmod 11 = 4$

5 probs LF  $7/11$

rehash =  $4 + 1 \bmod 11 = 5$

$5 + 1 \bmod 11 = 6$

$6 + 1 \bmod 11 = 7$

$7 + 1 \bmod 11 = 8$

	45			4	82	28	27	59	31	
0	1	2	3	4	5	6	7	8	9	10

T9/1

$$H(79) = 79 \bmod 11 = 2$$

	45	79		4	82	28	27	59	31	
0	1	2	3	4	5	6	7	8	9	10

LF  $\frac{8}{11}$

$$H(35) = 35 \bmod 11 = 2$$

	45	79	35	4	82	28	27	59	31	
0	1	2	3	4	5	6	7	8	9	10

LF  $\frac{9}{11}$

$$\text{rehash} = 2 + 1 \bmod 11 = 3$$

2 probs

⑥ external chaining all 1 prob.

0		
1	45	
2	79	→ 35
3		
4	4	→ 59
5	82	→ 38 → 27
6		
7		
8		
9	31	
10		

LF  $\frac{1}{11}$

$\frac{2}{11}$

$\frac{3}{11}$

$\frac{4}{11}$

$\frac{5}{11}$

③ Coalesced  
 $H(\text{key}) = \text{key mod } 7$

28		29	<del>31</del>	4	82	27		35	59	45
0	1	2	3	4	5	6	7	8	9	10

82 1 prob. LF  $1/11$

31 1 =  $2/11$

28 1 =  $3/11$

4 1 =  $4/11$

45 2 =  $5/11$

27 1 =

59 3 =

79 1 =

35 2 =

①

load factor =  $n/s$  when  $n$  is the stored entry.  
 $s$  is the Array size.

- linear rehashing =  $7/11$   
 - External =  $5/11$   
 - Coalesced =  $9/11$  } Final

② avg probs:

- open :  $17/9$

- External :  $9/9$

- Coalesced :  $13/9$ .

③

avg probs not found:  $+1$

$T_9/2$

Q2

Key  $\Rightarrow$  ID No.

no of student 1000.

Digit selection.

$$H(\text{key}) = \text{key} \bmod 1000.$$

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Collision: External or open.

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Q3

Key 15 character  $\Rightarrow$  Int range 0-999.

Q4

$$H(\text{key}) = (d_1 d_2 + d_{n-1} d_n + d_k) \bmod 11.$$

Example

$$\begin{array}{ccccccc} H(70934) & = & 43 & + & 07 & + & 9 \\ \begin{array}{cc} // & // \\ d_n & d_{n-1} \end{array} & & \begin{array}{cc} / & | \\ d_2 & d_1 \end{array} & & \begin{array}{cc} / & | \\ d_2 & d_1 \end{array} & & \begin{array}{cc} / & | \\ n-1 & n \end{array} & & \begin{array}{c} / \\ n/2 \\ 5/2 = 3 \end{array} \\ & = & 59 & \bmod 11 & = & 4 \end{array}$$

$$H(1234) = 43 + 21 + 3 = 67 \bmod 11 = 1$$

$$H(519) = 91 + 15 + 1 = 107 \bmod 11 = 8$$

$$H(911) = 11 + 19 + 1 = 31 \bmod 11 = 9$$

⋮

$$H(40015) = 51 + 04 + 0 = 55 \bmod 11 = 0.$$

T9  
/3