

Question 1 | /2 Points] [0.5 point for each choice]

Choose the correct value for  $T(n)$  for each segment of algorithm given.

```
int n = 30000  
for (i = 1; i < n; i++)  
    print("****")  
for (i = 1; i < n/5; i++)  
    print("****")
```

A.  $O(1)$

B.  $O(n)$

C.  $O(n^2)$

D.  $O(n \log n)$

```
if x < y  
    for (i = 1; i < n; i++)  
        print("****")  
else if x = y  
    for (j = 1; j < n; j++)
```

```
for (i = 1; i < n; i++)  
    print("****")  
for (j = 1; j < n; j++)  
    for (k = 1; k < n; k*=2)  
        print("****")
```

A.  $O(1)$

B.  $O(n^2)$

C.  $O(n^3)$

D.  $O(n \log n)$

```
for (i = 1; i < n^3; i++)  
    print("****")  
for (j = 1; j < n^2; j++)  
    procedure x(j)
```

☐ Print ☐ Web ☐ Draft ☐ Gridlines ☐ Navigation Pane ☐ One Page ☐ Multiple Pages ☐ Page Width ☐ New Window ☐ Arrange All ☐ Split

View: **A.  $O(1)$**  | B.  $O(n)$  | C.  $O(n^2)$  | D.  $O(n \log n)$

```

if x < y
  for (i = 1; i < n; i++)
    print("****")
else if x = y
  for (j = 1; j < n; j++)
    for (k = 1; k < j; k++)
      print("****")
else
  for (i = 1; i < n; i*=6)
    print("****")
  
```

A.  $O(1)$  | B.  $O(n^2)$  | C.  $O(n^2 \log n)$  | D.  $O(n^3 \log n)$

DESIGN LAYOUT ☐ View Side by Side ☐ Split Screen ☐ Switch Windows ☐ Macro

Window **A.  $O(1)$**  | B.  $O(n^2)$  | C.  $O(n^3)$

```

for (i = 1; i < n3; i++)
  print("****")
for (j = 1; j < n2; j++)
  procedure x(j)

procedure x(int x) {
  for (i = x; i > 1; i--)
    print("****")
}
  
```

**O(n<sup>4</sup>) الجواب**

A.  $O(1)$  | B.  $O(n^n)$  | C.  $O(n^3)$

Question2 [ / 0.75 Point] [0.25 point per correct answer,  $O$  and  $\Omega$  are also acceptable.]

Applying exhaustive search to the three problems listed below, what is the time complexity:  $n^2$

	Problem	Time Complexity
1	The traveling salesman problem	<u><math>\Theta((n-1)!)</math></u>
2	The knapsack problem	$\Theta(2^n)$
3	The assignment problem	<u><math>\Theta(n!)</math></u>

OR  $\Theta(n!)$  OR  $\Theta(\frac{n}{2}!)$  OR  $\Theta(\frac{n-1}{2}!)$



Consider the following recursive definition of a recursive algorithm:

$$F(n) = F(n - 2) * 2 \quad \text{for } n > 1$$

$$F(0) = F(1) = 2$$

- A) What is the basic operation performed? 0.25 Multiplication by 2.
- B) Set up and solve a recurrence relation for the number of times the algorithm's basic operation

For the number of multiplications made by this algorithm

$$M(n) = M(n - 2) + 1 \quad \text{for } n > 1$$

$$M(0) = M(1) = 0$$

0.25 (-0.1 if one of them is not written)

To solving this recurrence, we use the method of backward substitutions:

$$M(n) = M(n - 2) + 1$$

0.25 for using the idea of substituting  
substitute  $M(n - 2) = M(n - 4) + 1$