

Exam 1 — CSU 390 Theory of Computation — Fall 2007

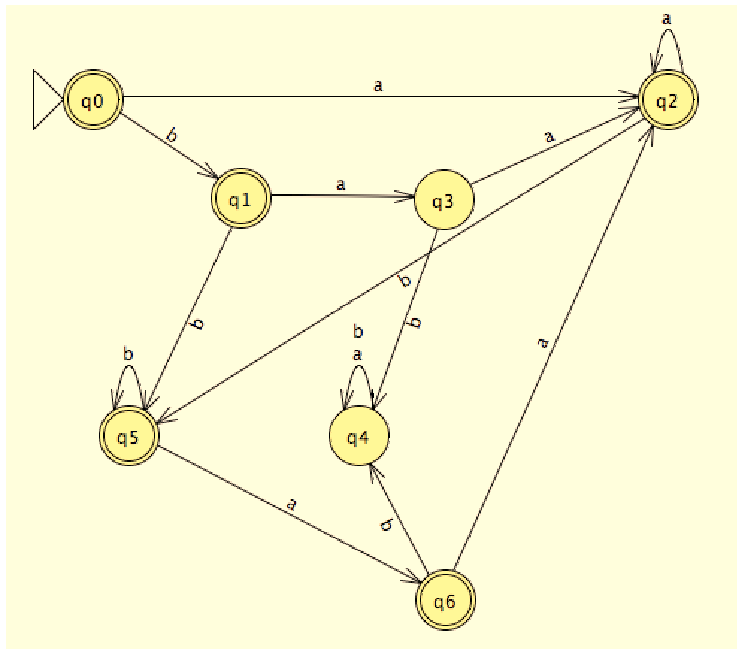
Solutions

Problem 1 [10 points]

Construct a state transition diagram for a DFA that recognizes the following language over the alphabet $\Sigma = \{a, b\}$:

$$L_1 = \{w \mid w \neq ba, \text{ and } w \text{ does not contain } bab\}$$

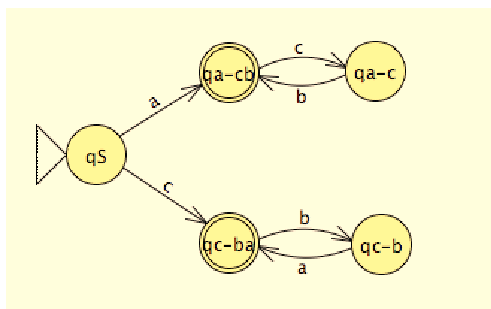
Solution:



Problem 2 [10 points]

Construct a state transition diagram for 5-state NFA that recognizes the language given by the regular expression $a(cb)^* \cup c(ba)^*$.

Solution:



Problem 3 [10 points]

Give a regular expression for the language L_2 over the alphabet $\Sigma = \{0, 1\}$:

$L_2 = \{w \mid w \text{ starts with } 1, \text{ ends with } 0, \text{ contains an even number of substrings } 01\}$

Solution:

$$1(0 + 1 + 0 + 1)^* 0$$

Note: I omitted the word *substrings* on the exam — it was shown on the blackboard. However, a large number of people misread the problem. Therefore, the solution:

$$1(0101)^+ 0$$

was considered *nearly correct* for 9 out of 10 points.