Intorial 4 Use the jumping lemma to show that the following languages are not regular: 1) A1 = { on / u2 u | n > 0} 2) Az = { a2n | n>o}, a2n is a string of 2n a's. 1) A1= { On 1 n2 n | n > 0 } - Assume that As is regular. - Let p be the pumping length given by the pumping Choose & the string OP1P2P, SEA, and |SI>P. The fumping lemma quarantees that s combe the fumping lemma guarantees that s combe Aflit who three farts: S = xyz / Fi)o, xyiz EA1, 141>1, |xy| < P $x = (p-1) \cdot 0/s = 0^{p-1}$ y= 0 (18/2,1) Counter example! 3= (P) 1's and (P) 2's = 1829 s'= x y 28 = 0 P-1 02 182P for i=2: = 0 P+11 P2P & A1 The same result is obtained with any other splitting So, this is a contradiction that means

that A, is not regular.

2) A2= Salla >06

- Assume that A2 is repular.

Let p be the pumping length given by the pumping lemma.

Let S be a2, ISI>P

SEA3 s com be effet vito: 248/) 124/ SP p (2° => 141 < 2° Therefore $|3|=|2y3|+|y|<2^p+2^p=2^{p+1}$ 28 < | 2 y y 3 | < 2 PH => The fength of 2498 cannot be a fower => 5=x yy8. \$ Az. (Contradiction) =) Az is not regular