



King Saud University

College of Computer and Information Sciences

Department of Computer Science

**Theory of computation CSC 339**

**MT2 Exam - Spring 2018**

Date: 5/04/2018

Duration: 1.5 hours

**Guidelines**

- No electronic devices are allowed in this exam.
- Use a pencil in choice questions.

Student ID:

Name:

Section:

Instructor:

1	2	3	4	5	Total

**Question 1: (True/False) ..... 24 points**

For each statement, choose whether it is True or False.

- (a)  $L1 = \{0^p1^q | p, q \in N\}$  cannot be recognized by a push-down automata.  
 (A) True (B) **False**
- (b) Let  $\Sigma = \{a, b\}$ ,  $L = \{xy | x, y \in \Sigma^* \text{ and } |x| = |y|\}$  and  $R = ((a + b).(a + b))^*$ . The language  $L = L(R)$ .  
 (A) **True** (B) False
- (c) Let  $\Sigma = \{a, b\}$  and  $L = \{a^n w a^n | n \geq 1 \text{ and } w \in \Sigma^*\}$ . L is not a context-free language.  
 (A) True (B) **False**
- (d) Some regular expressions cannot be converted to push-down automata.  
 (A) True (B) **False**
- (e) The pumping lemma cannot be used to prove that a language is regular.  
 (A) **True** (B) False
- (f) Some context-free languages are regular languages.  
 (A) **True** (B) False
- (g) Ambiguous grammar is a grammar that produces just one parse tree for every string in the language.  
 (A) True (B) **False**
- (h) Some context-free languages cannot be recognized by Turing machines.  
 (A) True (B) **False**
- (i) If L is a language recognized by a non-deterministic Turing machine, L cannot be recognized by a deterministic turing machine.  
 (A) True (B) **False**
- (j) A Turing machine with multiple track tapes has multiple heads.  
 (A) True (B) **False**

(k) Multidimensional Turing machine can be replaced by a deterministic Turing machine.

☒ **True**   ☐ False

(l) In Turing machines, the accept state is always different from the reject state. ☒ **True**   ☐ False

**Question 2: (Short answers) ..... 12 points**

(a) Which string is generated by the following grammar:

$$S \rightarrow xSy \mid SS \mid \epsilon$$

☐ (A) xxyxxy

☒ (B) **xyxxxyxy**

☐ (C) Both (A) and (B)

☐ (D) None

(b) The context-free grammar that accepts  $L = \{w \mid w \in \Sigma^+ \text{ and } w \text{ starts and ends with the same symbol}\}$  and  $\Sigma = \{a, b\}$  is:

☐ (A)  $S \rightarrow aSa \mid bSb \mid a \mid b$

☒ (B)  **$S \rightarrow aAa \mid bAb$   
 $A \rightarrow aA \mid bA \mid \epsilon$**

☐ (C)  $S \rightarrow aSa \mid A \mid a \mid b$   
 $A \rightarrow bAb \mid a \mid b \mid \epsilon$

☐ (D) None

(c) Let  $L$  be a context-free language. Any production rule of the grammar describing  $L$  has the following form:

$$A \rightarrow BC$$

$$A \rightarrow a$$

where  $A$ ,  $B$ , and  $C$  are non-terminal symbols ( $B$  and  $C$  cannot be the start symbol) and  $a$  is a terminal symbol.

The language  $L^R = \{w^R \mid w \in L\}$  is:

☐ (A) not a regular language and not a context-free language

☒ (B) **a context-free language**

☐ (C) a context-free language for some languages  $L$

☐ (D) None

**Question 3: (Push-down automata) ..... 22 points**

Consider the following formal definition of a push-down automata (PDA):  $P = (Q, \Sigma, \Gamma, \delta, q_0, \$, F)$ , where  $Q = \{q_0, q_1, q_2\}$ ,  $\Sigma = \{a, b\}$ ,  $\Gamma = \{A\}$ ,  $F = \{q_2\}$  and  $\delta$  is given as follows.

$$\delta(q_0, a, \lambda) = (q_0, A)$$

$$\delta(q_0, \lambda, \lambda) = (q_1, \lambda)$$

$$\delta(q_1, b, A) = (q_1, \lambda)$$

$$\delta(q_1, \lambda, A) = (q_2, A)$$

$$\delta(q, x, y) = \phi \text{ in all other cases } (x \in \Sigma \text{ and } y \in \Gamma).$$

- (a) Draw the corresponding push-down automata (assume the stack contains already \$).

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- (b) Is the string **aabb** accepted by P:

☐ (A) Yes    ☒ (B) **No**

- (c) The language recognized by this PDA is:

- ☐ (A)  $L = \{a^n b^n | n \geq 0\}$
- ☒ (B)  $L = \{a^m b^n | m > n \geq 0\}$
- ☐ (C)  $L = \{a^m b^n | n \geq m > 0\}$
- ☐ (D) None

**Question 4: (Context-free grammars) ..... 22 points**

Given the following context-free grammar  $G$ , where  $\Sigma = \{a, b, c\}$ :

$$S \rightarrow AX \mid YC$$

$$A \rightarrow aA \mid \epsilon$$

$$B \rightarrow bB \mid \epsilon$$

$$C \rightarrow cC \mid \epsilon$$

$$X \rightarrow bXc \mid bB \mid cC$$

$$Y \rightarrow aYb \mid aA \mid bB$$

- (a) The grammar  $G$  can derive:

☐ (A) aaba

Ⓑ aabbcc

Ⓒ **aaAbXc**

Ⓓ None

(b) The language described by the grammar is:

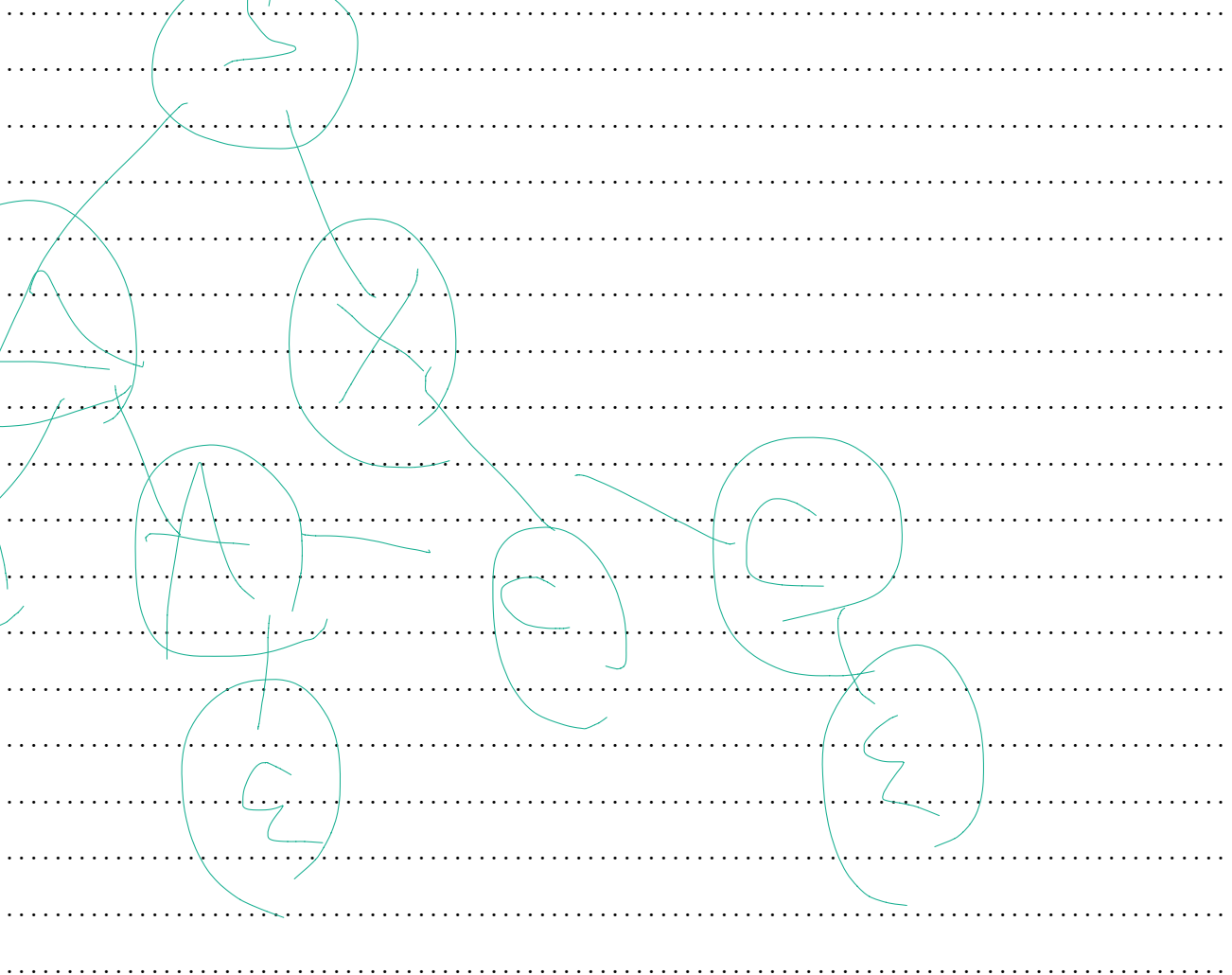
Ⓐ  $L = \{a^n b^n c^n | n \geq 1\}$

Ⓑ  **$L = \{a^i b^j c^k | i \neq j \text{ or } j \neq k\}$**

Ⓒ  $L = \{a^i b^j c^k | i < j \text{ or } j < k\}$

Ⓓ None

(c) Show the derivations for the string *aaabbc* using parse trees:



(d) The grammar is:

Ⓐ ambiguous because S has two possible derivations

Ⓑ **ambiguous because two parse trees can be obtained**

Ⓒ not ambiguous because we can always transform an ambiguous grammar to a non-ambiguous grammar

Ⓓ None

**Question 5: (Turing machine) .....20 points**

Consider the following formal definition of a Turing machine:  $M = (Q, \Sigma, \Gamma, \delta, q_0, q_{acc}, q_{rej})$  where  $Q = \{q_0, q_1, q_2, q_{acc}, q_{rej}\}$ ,  $\Sigma = \{0, 1\}$ ,  $\Gamma = \{0, 1, \sqcup\}$ , and  $\delta$  is given as follows.

$$\delta(q_0, 0) = (q_1, 1, R)$$

$$\delta(q_1, 1) = (q_2, 0, L)$$

$$\delta(q_1, \sqcup) = (q_{acc}, \sqcup, R)$$

$$\delta(q_2, 1) = (q_0, 0, R)$$

(a) Draw the corresponding Turing machine.

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(b) Is the string 0111 accepted by M:

☒ **A Yes**    ☐ B No

(c) Is the string 0110 accepted by M:

☐ A Yes    ☒ **B No**

(d) The language accepted by  $M$  :

- ☐ A cannot be described by a regular expression.
- ☒ **B can be described by the regular expression  $01^*$ .**
- ☐ C can be described by the regular expression  $(0110)^+$ .
- ☐ D None

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