

1. True or False? (5 Marks)

- a) Every regular language is context-free ✓
- b) The language $\{0^n 1^n \mid n \geq 0\}$ is not context free ✓
- c) The class of context free languages is not closed under intersection
- d) A language is recursively enumerable iff some Turing machine recognizes it. ✓
- e) A language is recursive iff some Turing machine decides it ✓
- f) Turing machines with multiple tapes are more powerful in their ability to compute than Turing Machines with just one tape. ✓
- g) A Multitape Turing machine is a 7-tuple. ✓
- h) An enumerator does not need to halt ✓
- i) Any computable problem could be solved with a single tape Turing machine.
- j) All computational models give the same notion of an algorithm

Question	a	b	c	d	e	f	g	h	i	j
Answer : (T/F)	F	F	T	T	T	F	T	T	T	T

2. Give a context free grammar that generates the language $A = \{ww^R \mid w \in \{a, b\}^*\}$. (3 marks)

$S \rightarrow w B w^R \mid B$ $B \rightarrow a \mid b$

3. Prove that if a language A and its complement $\neg A$ are recursively enumerable, then A is decidable

(7 marks)

A and $\neg A$ are recursively enumerable

I assume the A is non recursively enumerable

if A non-recur that meaning

A is non-decidable if this then

then $\neg A$ is recur but A non recur

this is a contradiction because I assume A non-recur and I get $\neg A$ is recur enumerable then I now A and $\neg A$ are same

4. Prove using the pumping lemma that the language $L = \{a^n b^n c^n, n \geq 0\}$ is not regular (8 marks)

* 5 Steps *

1) $L = \{a^n b^n c^n, n \geq 0\}$

2) $\nexists p \in L$ AND $|xy| \leq p$ AND $|y| \geq 1$

3) $\exists S \in L$ s.t. $|S| \geq p$

4) ~~Pike~~ ^{Pick} $S = xyz$ where $xy^i z \in L, i \geq 1$

5) now we can write

$xy^0 z$ is a contradiction

for $S = xy^i z, i \geq 1$

we have 2 possibilities:

for \nexists assume L is non-regular

i) y only a 's OR b 's OR c 's

but this

~~but~~ false because y never
can c 's only; this is ~~cond~~ ^{contradiction}

ii) ^{contain} y more from a 's ~~or~~ and b 's and c 's

but this false because bac false for example
order important this is contradiction