

# Quiz 1

$$a^2 b^{3(0)} c^0 = aa \checkmark$$

$$a^0 b^{3(0)} c^0 = \epsilon \checkmark$$

$$a^0 b^{3(1)} c^1 = bbb c \checkmark$$

## Question 1:

(2 points)

1. Consider the Language  $L = \{a^m b^{3n} c^n\}$ , where  $n, m \geq 0$ . Which of the following strings are not in the language.

a)  $\lambda$

b)  $bbbc$

c)  $aa$

d)  $aac$  ✓

$$L_1 = \{\lambda, aa, bb, abab\}$$

$$L_2 = \{\lambda, a, b, aa, ab, ba, bb\}$$

2. Let  $\Sigma = \{a, b\}$ . Let  $L_1 = \{x \in \Sigma^* : |x| \leq 2\}$ . Let  $L_2 = \{\lambda, a, b, ab\}$ . List the elements of the following language  $L = L_1 \cap (L_2)^2$ .

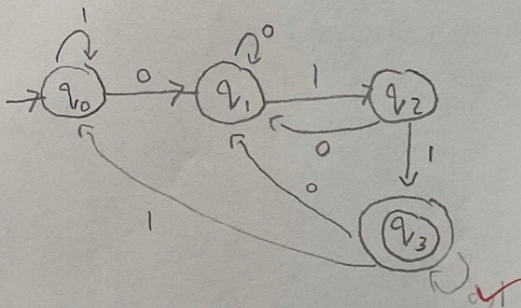
$$L = \{\lambda, aa, bb\} \text{ a b } \dots \dots \dots$$

0.5

## Question 2:

1. Draw a DFA to accept string of 0's and 1's ending with the string 011.

(2 points)



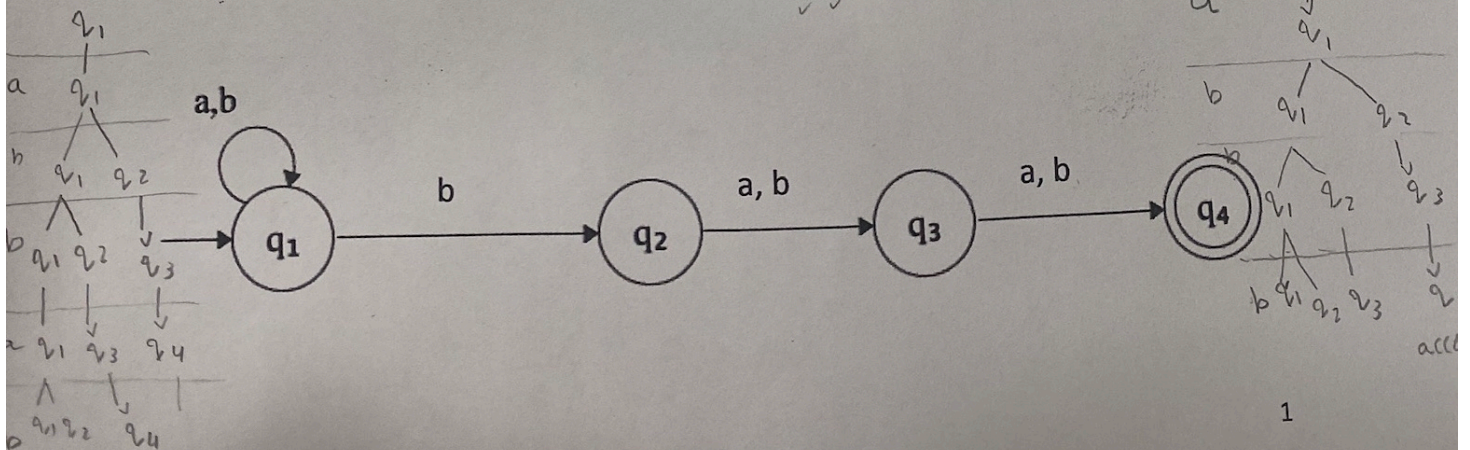
	0	1
$\lambda \cdot 0 = 0$	$q_0$	$q_1$
$\lambda \cdot 1 = \lambda$	$q_1$	$q_0$
$0 \cdot 0 = 00$	$q_1$	$q_2$
$0 \cdot 1 = 01$	$q_2$	$q_1$
$01 \cdot 0 = 010$	$q_1$	$q_3$
$01 \cdot 1 = 011$	$q_3$	$q_3$
$011 \cdot 0 = 0110$	$q_3$	$q_3$
$011 \cdot 1 = 0111$	$q_3$	$q_3$

3. Given the following automata, answer the following questions.

(6 points)

$abbb$

$abbb$





- A. What is the alphabet?  $\Sigma = \{a, b\}$  ✓
- B. Is the automata a DFA or NFA? NFA ✓
- C.  $\delta^*(q_1, abbb)$  is?  $\{q_1, q_2, q_3, q_4\}$  accepting ✓
- D. Does the machine accept the string **abbab**? yes ✓
- E. The language recognized by the FA?

a)  $L = \{w \mid w \in \Sigma^*\}$   $\{a, b\}$  no not accepting

b)  $L = \{w \mid w \text{ contains } b\}$  yes accepting ✗ -1 a and b are characters

c)  $L = \{w \mid w \text{ contains } b \text{ as 3rd char from the end}\}$  yes accepting

d)  $L = \{w \mid w \text{ contains } b\} \cup \lambda$  no not accepting

F. For the previous FA, to accept  $L = \{w \mid w \text{ starts with } b\}$  we need to change the following transitions:

a) Add  $\delta(q_4, a) = \delta(q_4, b) = \{q_4\}$

b) Delete  $\delta(q_1, a) = \delta(q_1, b) = \{q_1\}$

c) a and b

d) None