

# Tutorial #8

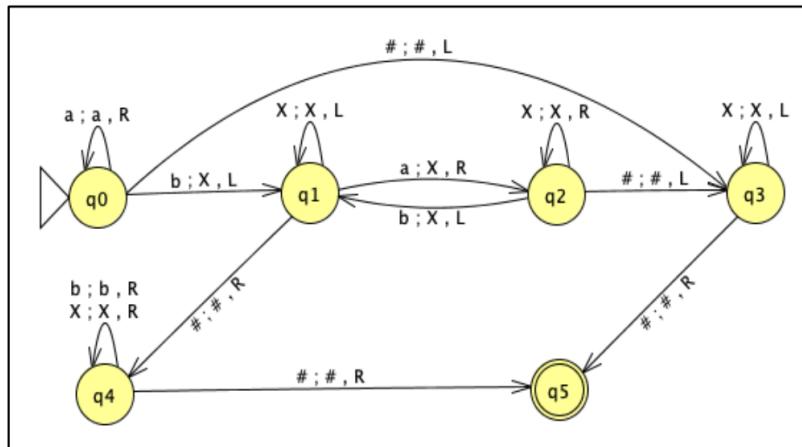
# Exercise 1

- Accepted language
- The time complexity and its corresponding class
- The space complexity and its corresponding class

$$L = \{ab^j \mid i \geq 0, j \geq i\},$$

time complexity:  $O(n^2) \rightarrow$  class  $P$

space complexity:  $O(n) \rightarrow$  class  $PS$



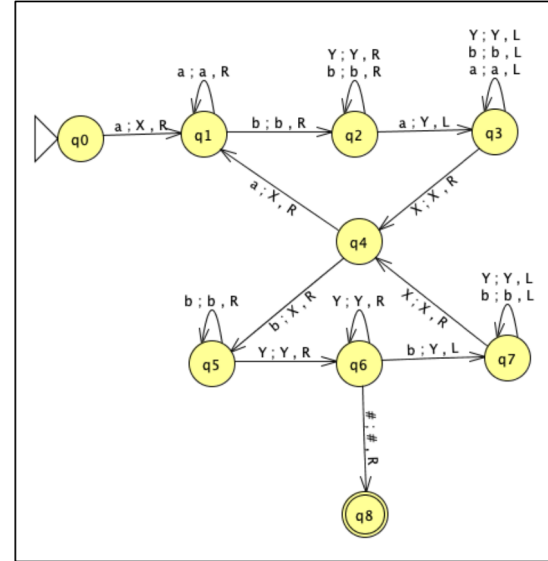
# Exercise 1

- Accepted language
- The time complexity and its corresponding class
- The space complexity and its corresponding class

$$L = \{a^i b^j a^i b^j \mid i > 0, j > 0\}$$

time complexity:  $O(n^2) \rightarrow$  class  $P$

space complexity:  $O(n) \rightarrow$  class  $PS$



## Exercise 2

Which of the following statements about the class  $P$  are correct?

- $P$  is the class of all languages that are decidable by deterministic single-tape Turing machines running in polynomial time
- $P$  is the class of all languages such that  $w \in P$  then there is a deterministic single-tape Turing machine which accepts the string  $w$  in polynomial time.
- $P$  is the class of all languages that are decidable by deterministic multi-tape Turing machines running in polynomial time
- A language  $L$  belongs to  $P$  if there is a constant  $k$  and a decider  $M$  running in time  $O(n^k)$  such that  $L = L(M)$
- A language  $L$  belongs to  $P$  if  $L \in TIME(2^i)$

## Exercise 2

Which of the following statements about the class  $P$  are correct?

- $P$  is the class of all languages that are decidable by deterministic single-tape Turing machines running in polynomial time. → **Correct**
- $P$  is the class of all languages such that  $w \in P$  then there is a deterministic single-tape Turing machine which accepts the string  $w$  in polynomial time. → **Incorrect**
- $P$  is the class of all languages that are decidable by deterministic multi-tape Turing machines running in polynomial time. → **Correct**
- A language  $L$  belongs to  $P$  if there is a constant  $k$  and a decider  $M$  running in time  $O(n^k)$  such that  $L = L(M)$ . → **Correct**
- A language  $L$  belongs to  $P$  if  $L \in TIME(2^n)$ . → **Incorrect**

## Exercise 3

Below are some definitions of the class  $NP$ , Which ones are correct?

- $NP$  is the class of languages which have polynomial time verifiers.
- $NP$  is the class of languages that cannot be decided in polynomial time using a deterministic Turing machine.
- $NP$  is the class of languages that have non-deterministic verifiers.
- $NP$  is the class of languages that can be decided in polynomial time on a non-deterministic Turing machine.

## Exercise 3

Below are some definitions of the class  $NP$ , Which ones are correct?

- $NP$  is the class of languages which have polynomial time verifiers. → **Correct**
- $NP$  is the class of languages that cannot be decided in polynomial time using a deterministic Turing machine. → **Incorrect**
- $NP$  is the class of languages that have non-deterministic verifiers. → **Incorrect**
- $NP$  is the class of languages that can be decided in polynomial time on a non-deterministic Turing machine. → **Correct**