

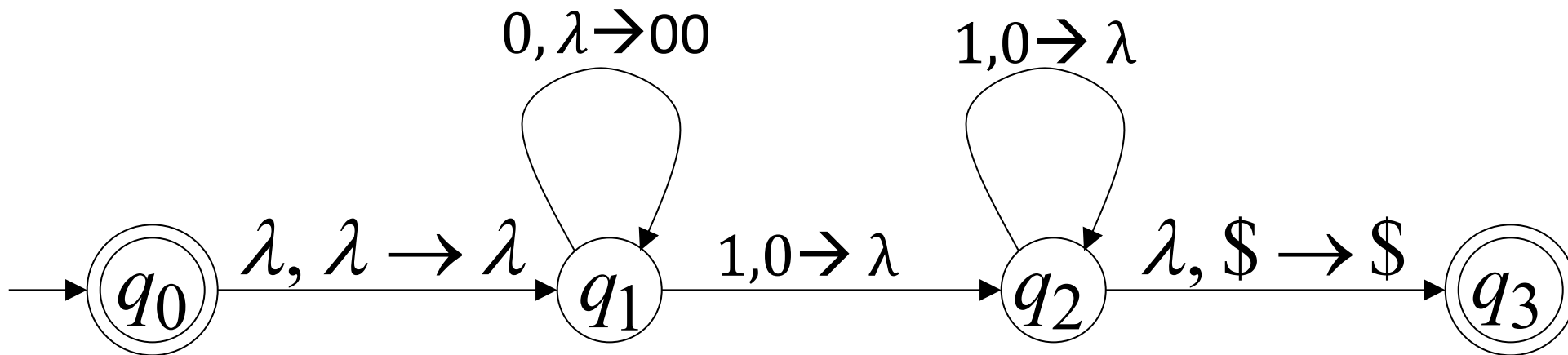
Tutorial #5

Push Down Automata (PDA)

Exercise 1

- Construct a PDA to accept the following languages:

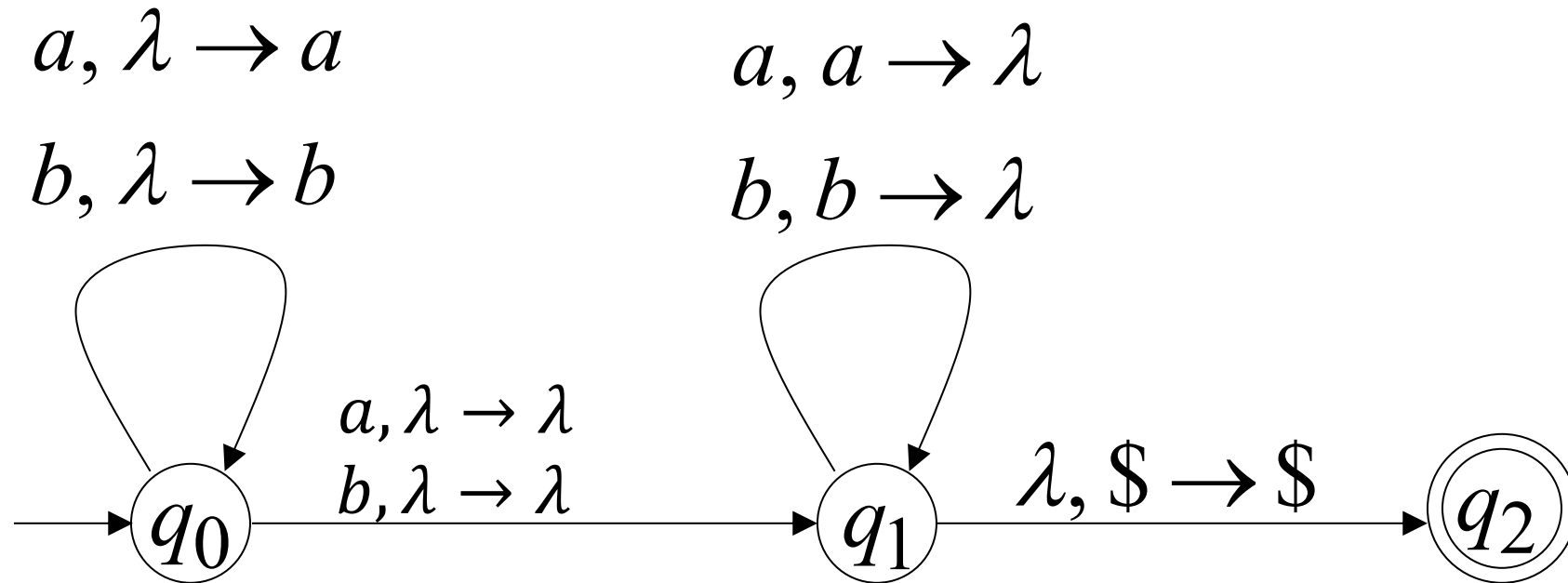
1. $L = \{0^n 1^{2n} \mid n \geq 0\}$



Exercise 1

- Construct a PDA to accept the following languages:

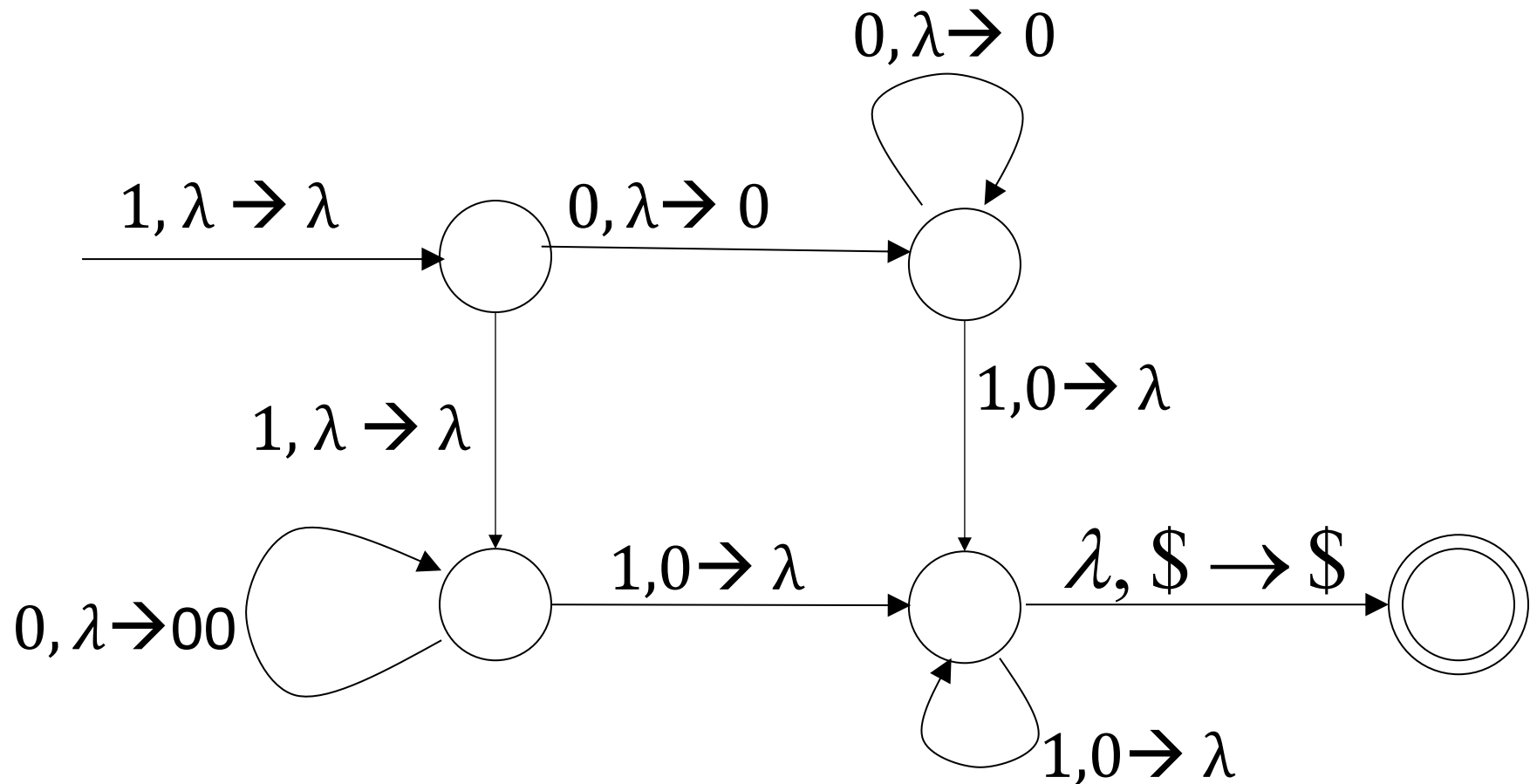
2. $L = \{w\sigma w^R \mid w \in \{a,b\}^*, \sigma \in \{a,b\}\}$



Exercise 1

- Construct a PDA to accept the following languages:

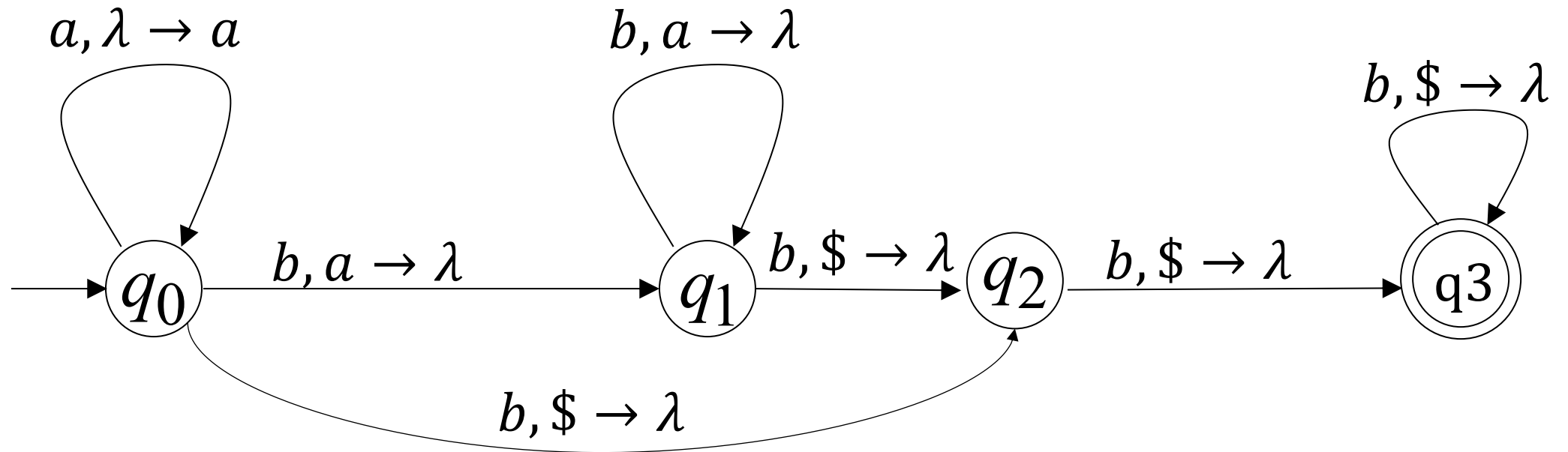
3. $L = \{10^n 1^n \mid n > 0\} \cup \{110^n 1^{2n} \mid n > 0\}$



Exercise 1

- Construct a PDA to accept the following languages:

4. $L = \{a^n b^m \mid m \geq n + 2\}$



Exercise 2

- Consider the following formal definition of a push-down automata (PDA):
 $P = (Q, \Sigma, \Gamma, \delta, q_0, \$, F)$, where $Q = \{q_0, q_1, q_2\}$, $\Sigma = \{a, b\}$, $\Gamma = \{A\}$, $F = \{q_2\}$ and δ is given as follows.

$$\delta(q_0, a, \lambda) = (q_0, A)$$

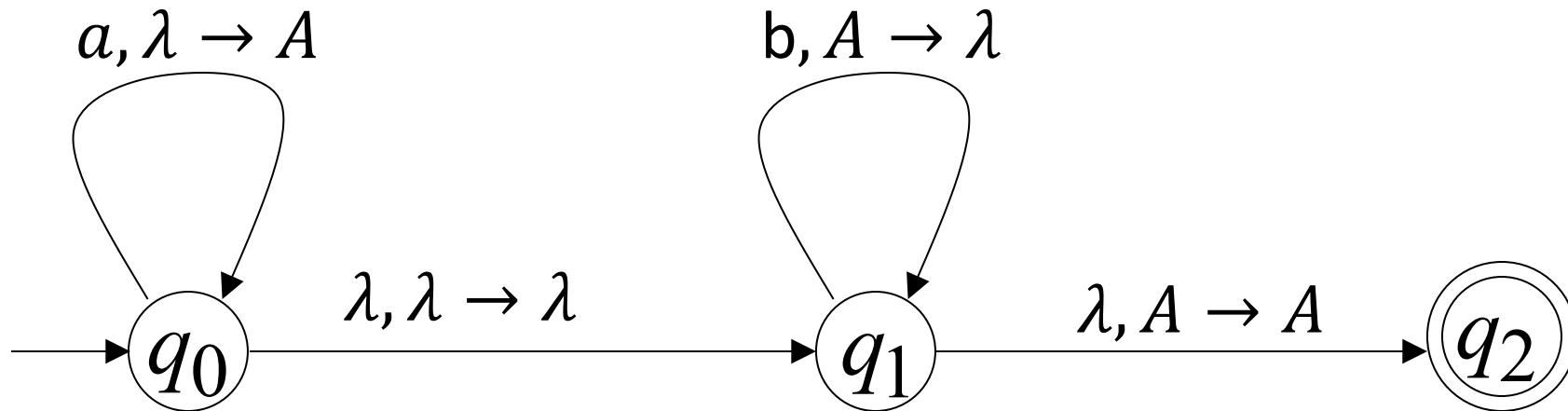
$$\delta(q_0, \lambda, \lambda) = (q_1, \lambda)$$

$$\delta(q_1, b, A) = (q_1, \lambda)$$

$$\delta(q_1, \lambda, A) = (q_2, A)$$

$$\delta(q, x, y) = \phi \text{ in all other cases } (x \in \Sigma \text{ and } y \in \Gamma).$$

$$L = \{a^m b^n \mid m > n \geq 0\}$$



Exercise 3

- Construct the PDA corresponding to the following grammar:

- $S \rightarrow aABB \mid aAA$

- $A \rightarrow aBB \mid a$

- $B \rightarrow bBB \mid A$

$$\lambda, S \rightarrow aABB$$

$$\lambda, S \rightarrow aAA$$

$$\lambda, A \rightarrow aBB$$

$$\lambda, A \rightarrow a$$

$$a, a \rightarrow \lambda$$

$$\lambda, B \rightarrow bBB$$

$$b, b \rightarrow \lambda$$

$$\lambda, B \rightarrow A$$

