

## **King Saud University**

College of Computer and Information Sciences
Computer Science Department

CSC 339: Theory of Computation Final Exam: Second Semester 2020

**Duration: 3 Hours** 

Name: ID: Section: 44084

## True/False Questions [8 pts]

1. If $L$ is Turing-acceptable language; then $\overline{L}$ is not Turing-acceptable.	True
2. Halting problem is decidable.	False
3. Every two tapes Turing machine has an equivalent single tape Turing machine.	True
4. Universal Turing Machine are re-programmable.	True
5. All regular languages are Turing-decidable.	True
6. NP-Complete class includes all problems that can be solved only by exponential time algorithms.	False
7. The only way for a Turing machine to reject a string is to halt on a non-accepting state.	False
8. Every non-deterministic Turing machine has an equivalent deterministic Turing machine.	True

## Multiple Choice Questions [12 pts]

- 9. All NP-complete problems are also P-complete.
  - a. True b. False
- c. Unknown
- 10. Consider the following formal definition of the Turing machine in Figure 1:  $M = (Q, \Sigma, \Gamma, \#, q_0, F, \delta)$  where  $Q = \{q_0, q_1\}, \Sigma = \{0, 1\}, \Gamma = \{0, 1, \#\}, \text{ and } F = \{\}.$

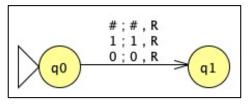


Figure 1: Turing Machine

The language decided by M is:

- a.  $\{\lambda\}$  c.  $\emptyset$
- b.  $\{0\}$  d.  $\emptyset^*$
- 11. Consider the following formal definition of the Turing machine in Figure 2:  $M = (Q, \Sigma, \Gamma, \#, q_0, F, \delta)$  where  $Q = \{q_0, q_1, q_2, q_3, q_4\}, \Sigma = \{a, b\}, \Gamma = \{a, b, \#\}, \text{ and } F = \{q_4\}.$

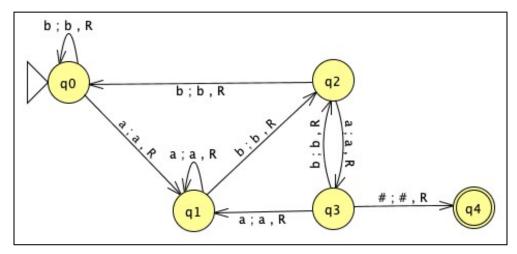


Figure 2: Turing Machine

The language accepted by M is:

- a. a\*b\*(a + b) c. (a + b)\*bab
- b. (a + b)\*aba d. (a + b)\*a\*b\*
- 12. Consider the following formal definition of the Turing machine in Figure 3:  $M = (Q, \Sigma, \Gamma, \#, q_0, F, \delta)$  where  $Q = \{q_0, q_1, q_2, q_3, q_4, q_5\}, \Sigma = \{a, b\}, \Gamma = \{a, b, x, \#\}, \text{ and } F = \{q_5\}.$

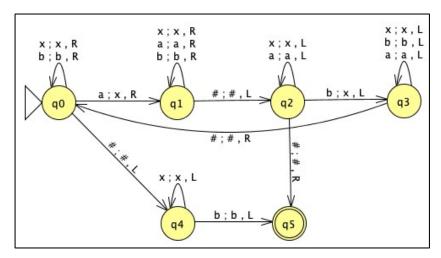


Figure 3: Turing Machine

The language accepted by M is:

a.  $a^nb^n$ 

c.  $a^n b^m$  where  $n \neq m$ 

b.  $a^n b^m$  where m > n

- d. None
- 13. Consider the following formal definition of the Turing machine in Figure 4: M =

$$(Q,\Sigma, \Gamma,\#, q_0,F, \delta)$$
 where  $Q = \{q_0,q_1,q_2, q_3,q_4, q_5\}, \Sigma = \{a,b\}, \Gamma = \{a,b,x,y,\#\}, \text{ and } F = \{q_5\}.$ 

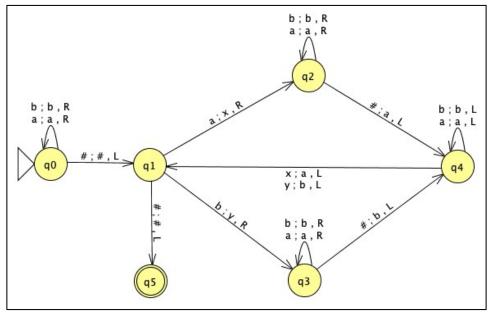


Figure 4: Turing Machine

What is the result configuration of the machine M if the initial configuration is  $\#q_0w\#$ ?

- a.  $q_5##ww^R#$  c.  $q_5###w#$
- b.  $q_5##ww#$  d. None
- 14. Consider the following formal definition of the Turing machine in Figure 5:  $M = (Q, \Sigma, \Gamma, \#, q_0, F, \delta)$  where  $Q = \{q_0, q_1, q_2, q_3\}, \Sigma = \{0,1\}, \Gamma = \{0,1,\#\}, \text{ and } F = \{q_3\}.$

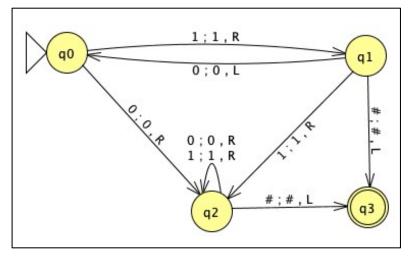


Figure 5: Turing Machine

Suppose the current configuration is  $#1q_10100#$ . The next configuration will be:

- a.  $#10q_0100#$  c.  $#q_010100#$
- b. #10q2100# d. None
- 15. Consider the following formal definition of the Turing machine in Figure 5:  $M = (Q, \Sigma, \Gamma, \#, q_0, F, \delta)$  where  $Q = \{q_0, q_1, q_2, q_3\}, \Sigma = \{0,1\}, \Gamma = \{0,1,\#\}, \text{ and } F = \{q_3\}.$

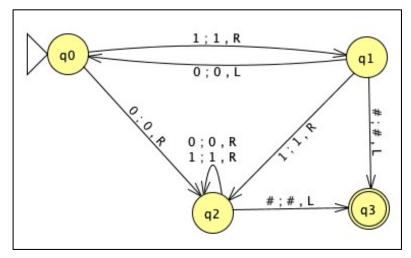


Figure 5: Turing Machine

Is the string 10100 accepted?

- a. Yes **b. No**
- 16. Consider the following formal definition of the Turing machine in Figure 5:  $M = (Q, \Sigma, \Gamma, \#, q_0, F, \delta)$  where  $Q = \{q_0, q_1, q_2, q_3\}, \Sigma = \{0,1\}, \Gamma = \{0,1,\#\}, \text{ and } F = \{q_3\}.$

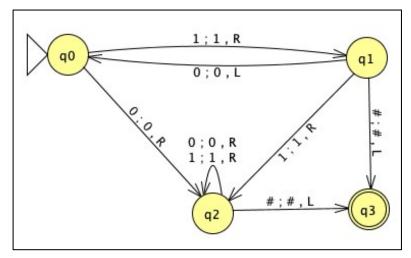


Figure 5: Turing Machine

Which statement is correct?

a. *M* halts on all inputs c. *M* does not halt on any input

- b. *M* never halts on some inputs d. None
- 17. Consider the following formal definition of the Turing machine in Figure 5:  $M = (Q, \Sigma, \Gamma, \#, q_0, F, \delta)$  where  $Q = \{q_0, q_1, q_2, q_3\}, \Sigma = \{0,1\}, \Gamma = \{0,1,\#\}, \text{ and } F = \{q_3\}.$

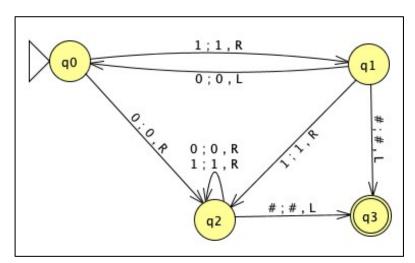


Figure 5: Turing Machine

The machine *M* is:

- a. A recognizer b. A decider
- 18. Consider the following formal definition of the Turing machine in Figure 6:  $M=(Q,\Sigma,\Gamma,\#,q_0,F,\delta)$  where  $Q=\{q_0,q_1,q_2,q_3,q_4,q_5,q_6,q_7,q_8\},\Sigma=\{0,1,\$\},\Gamma=\{0,1,\$,A,B,\#\},$  and  $F=\{q_8\}.$

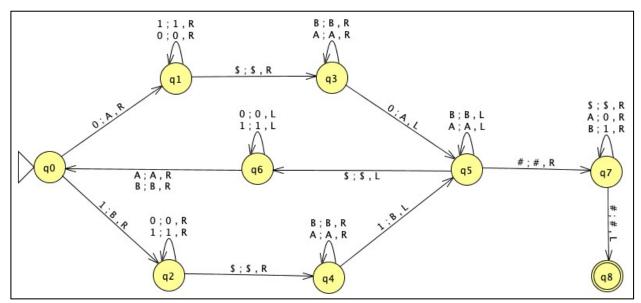


Figure 6: Turing Machine

The language accepted by M is:

a. 
$$L = \{0^n \$ 1^n \mid n > 0\}$$
 c.  $L = \{w \$ w \mid w \in \{0,1\}^+\}$ 

b. 
$$L = \{w \$ w^R \mid w \in \{0,1\}^+\}$$
 d. None

19. Consider the following formal definition of the Turing machine in Figure 6:  $M = (Q, \Sigma, \Gamma, \#, q_0, F, \delta)$  where  $Q = \{q_0, q_1, q_2, q_3, q_4, q_5, q_6, q_7, q_8\}, \Sigma = \{0,1,\$\}, \Gamma = \{0,1,\$, A,B,\#\}, \text{ and } F = \{q_8\}.$ 

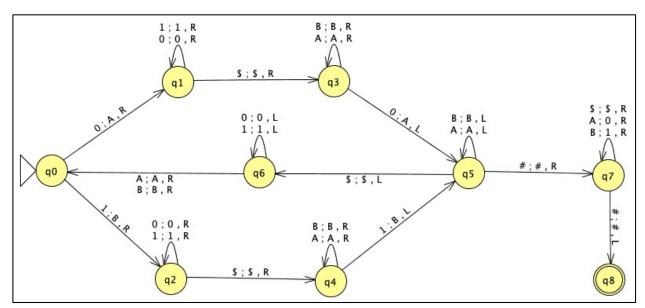


Figure 6: Turing Machine

What is the time complexity of the Turing machine above?

- a. O(n) c.  $O(n^3)$
- b.  $O(n^2)$  d. None
- 20. Consider the following formal definition of the Turing machine in Figure 6:  $M=(Q,\Sigma,\Gamma,\#,q_0,F,\delta)$  where  $Q=\{q_0,q_1,q_2,q_3,q_4,q_5,q_6,q_7,q_8\},\Sigma=\{0,1,\$\},\Gamma=\{0,1,\$,A,B,\#\}$ , and  $F=\{q_8\}$ .

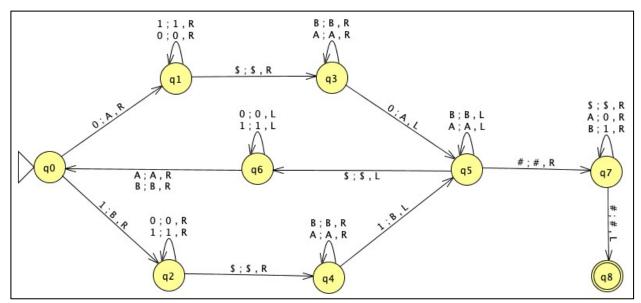


Figure 6: Turing Machine

Which class the time complexity of the given Turing machine belongs to?

- a. P c. NP-C
- b. *NP* d. None