

chapter four

	Mean	Proportion
Central limit theorem	$\frac{\mu}{\sigma} = \mu$ $\frac{\sigma}{\sqrt{n}} = \frac{\sigma}{\sqrt{n}}$	$\mu_{\hat{p}} = p$ $\sigma_{\hat{p}} = \sqrt{p(1-p)/n}$
Z-Score	$\frac{\bar{x} - \mu}{\sigma}$	$\frac{\hat{p} - \mu_{\hat{p}}}{\sigma_{\hat{p}}}$
Confidence interval	$\mu \in \bar{x} \pm Z_{1-\alpha/2} \sigma / \sqrt{n}$	$p \in \hat{p} \pm Z_{1-\alpha/2} \sqrt{\hat{p}(1-\hat{p})/n}$
Margin error	$\delta_{\mu} = Z_{1-\alpha/2} \sigma / \sqrt{n}$	$\delta_p = Z_{1-\alpha/2} \sqrt{\hat{p}(1-\hat{p})/n}$
Sample size	$n = \left(Z_{1-\alpha/2} / \delta_{\mu} \right)^2$	$n = \hat{p}(1-\hat{p}) \left(Z_{1-\alpha/2} / \delta_p \right)^2$ $n = 0.25 \left(Z_{1-\alpha/2} / \delta_p \right)^2$
Confidence interval length		$L = 2\delta_p \rightarrow 2 Z_{1-\alpha/2} \sqrt{\hat{p}(1-\hat{p})/n}$ $n = \left(Z_{1-\alpha/2} / L \right)^2$

Hypothesis testing for the population mean:

1. Identify the hypothesis:

$$H_0: \mu = \mu_0$$

$$H_1: \mu =, >, < \mu_0$$

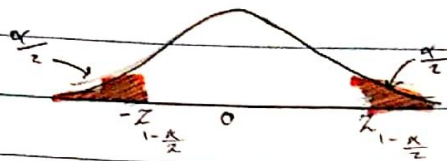
2. Test statistic:

$$Z_0 = \frac{\bar{x} - \mu_0}{\sigma / \sqrt{n}}$$

3. Critical region or P-value:

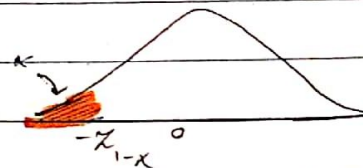
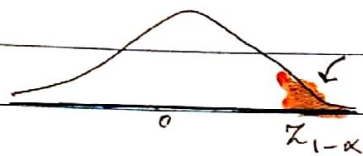
• Critical region:

i. $H_1: \mu \neq \mu_0$



ii. $H_1: \mu > \mu_0$

iii. $H_1: \mu < \mu_0$



• P-value:

i. $H_1: \mu \neq \mu_0 \rightarrow 2P(Z > |Z_0|)$

ii. $H_1: \mu > \mu_0 \rightarrow P(Z > Z_0)$

iii. $H_1: \mu < \mu_0 \rightarrow P(Z < -|Z_0|)$

4. Decision:

we reject H_0 when it falls in the critical region or α is greater than the P-value.

Hypothesis testing for the population proportion:

1. Identifying the hypothesis:

$$H_0: p = p_0$$

$$H_1: p =, <, > p_0$$

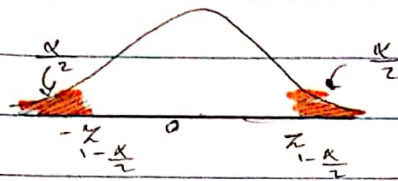
2. Test statistic:

$$Z_0 = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0(1-p_0)}{n}}}$$

3. Critical region or P-value:

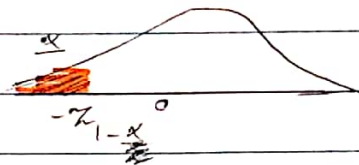
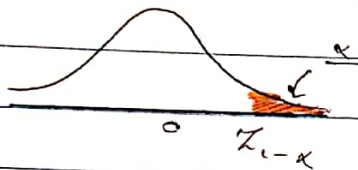
• Critical region:

i. $H_1: \mu \neq \mu_0$



ii. $H_1: \mu > \mu_0$

iii. $H_1: \mu < \mu_0$



• P-value:

i. $H_1: \mu \neq \mu_0 \rightarrow 2P(Z > |z_0|)$

ii. $H_1: \mu > \mu_0 \rightarrow P(Z_0 > z_0)$

iii. $H_1: \mu < \mu_0 \rightarrow P(Z < -|z_0|)$

4. Decision:

the same as before.

Chapter five

• Pearson's correlation coefficient: Also called Product moment correlation coefficient

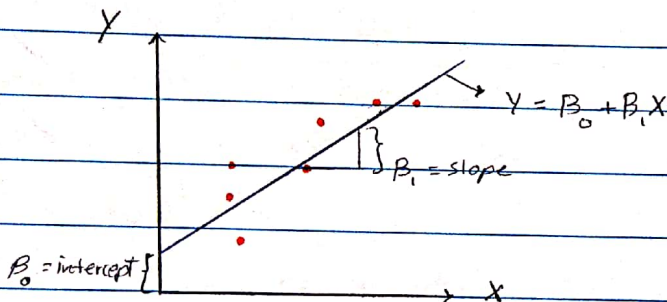
$$r = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum (x_i - \bar{x})^2} \sqrt{\sum (y_i - \bar{y})^2}}$$

$$r = \frac{n \sum x_i y_i - [\sum x_i][\sum y_i]}{\sqrt{n \sum x_i^2 - [\sum x_i]^2} \sqrt{n \sum y_i^2 - [\sum y_i]^2}}$$

• Simple linear regression line of a population: $Y = a + bX + \epsilon$

where, ϵ is a normal random variable with $E(\epsilon) = 0$.

a is the Y -intercept and b is the slope.



• The estimated regression line of a sample: $\hat{Y} = \hat{a} + \hat{b}X$

$$\hat{b} = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sum (x_i - \bar{x})^2}$$

$$\hat{b} = \frac{n \sum x_i y_i - \sum x_i \sum y_i}{n \sum x_i^2 - [\sum x_i]^2}$$

$$\hat{a} = \bar{y} - \hat{b} \bar{x}$$

$$\hat{a} = \frac{\sum y_i \sum x_i^2 - \sum x_i \sum x_i y_i}{n \sum x_i^2 - [\sum x_i]^2}$$

• Coefficient of determination:

$$r^2 = \frac{SSR}{SS_{tot}}, \quad r^2 = 1 - \frac{SSE}{SS_{tot}}$$

• Total sum of squared deviations (Total variation): $SS_{tot} = \sum (y_i - \bar{y})^2$,
 $SS_{tot} = SSR + SSE$

• Sum of squared regression error (Explained variation): $SSR = \sum (\bar{y} - \hat{y}_i)^2$

• Sum of squared error or residuals (Unexplained variation): $SSE = \sum (y_i - \hat{y}_i)^2 = \sum \epsilon_i^2$