

use definition of Limit to show that \square

$$\textcircled{1} \lim_{x \rightarrow 2} 3 + 4x = 11$$

$$\textcircled{4} \lim_{x \rightarrow 3} x = 3$$

$$\textcircled{2} \lim_{x \rightarrow -2} -5x - 11 = -1$$

$$\textcircled{5} \lim_{x \rightarrow -\frac{1}{2}} 9 = 9$$

$$\textcircled{3} \lim_{x \rightarrow -4} -\frac{1}{2} + \frac{5}{2}x = -\frac{21}{2}$$

$$\textcircled{6} \lim_{x \rightarrow 0^+} \sqrt{x} = 0$$

evaluate each of the following Limits (if exist)

$$\boxed{1} \quad \lim_{x \rightarrow 2} \frac{x-1}{x^2-1}$$

$$\boxed{2} \quad \lim_{x \rightarrow 0} \frac{x^2+3}{x+1}$$

$$\boxed{3} \quad \lim_{x \rightarrow 0} \frac{1+\sin x}{x^2-1}$$

$$\boxed{4} \quad \lim_{x \rightarrow 2} \frac{2x+3}{x^2-1}$$

$$\boxed{5} \quad \lim_{x \rightarrow 1} (2x+4)^2$$

$$\boxed{*} \quad \lim_{x \rightarrow 1} 2x^2 - 3 + \pi^2$$

$$\boxed{6} \quad \lim_{x \rightarrow 4} \frac{x-4}{\sqrt{x}-2}$$

$$\boxed{7} \quad \lim_{x \rightarrow 3} \frac{x^2-9}{x^2-x-6}$$

$$\boxed{8} \quad \lim_{x \rightarrow 3} \frac{\sqrt{x+1}-2}{x^2-4x+3}$$

$$\boxed{9} \quad \lim_{x \rightarrow 2} \frac{x^2-2x}{x^2-4}$$

$$\boxed{10} \quad \lim_{x \rightarrow 0} \frac{1 - \sqrt{x+1}}{x}$$

$$\boxed{11} \quad \lim_{x \rightarrow 8} \frac{3 - \sqrt{x+1}}{x-8}$$

$$\boxed{12} \quad \lim_{x \rightarrow 1} \frac{x^2 + 7x - 8}{1-x}$$

$$* \quad \lim_{x \rightarrow 9} \frac{x + \sqrt{x} - 12}{x-9}$$

$\boxed{3}$

$$\boxed{13} \quad \lim_{x \rightarrow 0} \frac{\sin^2 x + \sin 2x}{3x}$$

$$\boxed{14} \quad \lim_{x \rightarrow 0} \frac{\sin(5x) + \tan(3x)}{2x}$$

$$\boxed{15} \quad \lim_{x \rightarrow 0} \frac{3x - \sin 2x}{\tan x + 4x}$$

$$\boxed{16} \quad \lim_{x \rightarrow 0} \frac{1 + \sin 2x - \cos x}{2x}$$

$$\boxed{17} \quad \lim_{x \rightarrow 0} \frac{1 - \cos x}{3x^2}$$

$$\boxed{14} \quad \boxed{20} \quad \lim_{x \rightarrow 0} x^2 \sin\left(\frac{1}{x}\right) \quad (*)$$

$$\boxed{21} \quad \lim_{x \rightarrow \infty} \frac{\sin^2 x}{x^2 + 1}$$

$$\boxed{18} \quad \lim_{x \rightarrow 0} x^2 \cos\left(\frac{\pi}{x}\right)$$

$$\boxed{22} \quad \lim_{x \rightarrow \infty} \frac{\tan^{-1}(\sin x)}{x}$$

$$\boxed{19} \quad \lim_{x \rightarrow 0} x^4 \sin\left(\frac{1}{x^2}\right)$$

[33]

$$\lim_{x \rightarrow \infty} x^2 \left(1 - \cos\left(\frac{1}{x}\right) \right)$$

[5]

[35]

$$\lim_{x \rightarrow 2} \frac{2x-3}{x^2-4x+4}$$

[34]

$$\lim_{x \rightarrow 2} \frac{4x+3}{x-2}$$

[36]

$$\lim_{x \rightarrow -\infty} \frac{x^4 - x + 1}{x^2 + 5x + 3}$$

[37]

$$\lim_{x \rightarrow \infty} \sqrt[3]{\frac{x+4}{8x+3}}$$

$$\boxed{23} \quad \lim_{x \rightarrow 0} x^2 \left(1 - \cos\left(\frac{1}{x}\right) \right)$$

$$\boxed{25} \quad \lim_{x \rightarrow 1} \frac{2}{x^2 - 1} - \frac{1}{x - 1}$$

$$\boxed{24} \quad \lim_{x \rightarrow 1^+} \frac{x^2 - 1}{x^2 - 2x + 1}$$

$$\boxed{26} \quad \lim_{x \rightarrow \infty} \sin \left(\frac{\pi x^2 - x}{3x^2 + 5x} \right)$$

$$\boxed{7} \quad \boxed{29} \quad \lim_{x \rightarrow \infty} \tan \frac{\pi x^2 - x}{x^2 + 5x}$$

$$\boxed{27} \quad \lim_{x \rightarrow \infty} \left(1 + \cos \left(\frac{3}{2x+1} \right) \right)$$

$$* \quad \lim_{x \rightarrow \infty} \frac{2x^2 + 1}{x+1} - ax + b = 5$$

find the value a and b

$$\boxed{28} \quad \lim_{x \rightarrow \infty} \cos \left(\frac{\pi x + 1}{x^2 + 3} \right)$$

30. find all vertical and horizontal asymptotes (if any) for

$$30) f(x) = \frac{2x-6}{x^2-9}$$

$$31) f(x) = \frac{\sqrt{9x^2+13}}{2x-3}$$

32)

$$32) f(x) = \frac{x}{\sqrt{1-x^2}}$$

$$33) f(x) = \frac{4-x^2}{x^2-4|x|+4}$$

$$\boxed{33} \cdot f(x) = \frac{\sqrt{x^2 - 5}}{x+5}$$

$$\boxed{34} \quad f(x) = \frac{\sin x}{x}$$

$\boxed{35}$ discuss the continuity of $f(x) = \begin{cases} 6x^2 - 5 & x < 1 \\ 2x - 1 & x \geq 1 \end{cases}$ at $x=1$

$$\boxed{36} \quad f(x) = \begin{cases} x+3 & x \leq 0 \\ \frac{\sin 6x}{2x} & x > 0 \end{cases} \text{ at } x=0$$

~~32~~ find the value(s) if f is continuous

$$[33] \quad f(x) = \begin{cases} ax+b & x > 1 \\ 5x+2a & x < 1 \\ 4 & x = 1 \end{cases}$$

[30] [35] $f(x) = \begin{cases} \frac{2 \tan(kx)}{x} + 1 & x \neq 0 \\ 3k^2 + x & x = 0 \end{cases}$ at $x=0$

$$[36] \quad f(x) = \begin{cases} \frac{x^2 + 6x + 5}{x-1} & x \neq 1 \\ a & x = 1 \end{cases}$$

$$[34] \quad f(x) = \begin{cases} \frac{x^3 - 8}{x-2} & x \neq 2 \\ 3k+1 & x = 2 \end{cases} \text{ at } x=2$$

[37] Redefine $f(x) = x^2 \sin\left(\frac{1}{x}\right)$ to make it continuous at $x=0$

$$(*) \quad f(x) = \begin{cases} cx^2 + d & x > 1 \\ 6 & x = 1 \\ 2cx - d & x < 1 \end{cases}$$

[38] find the x -values (if any) at which the function

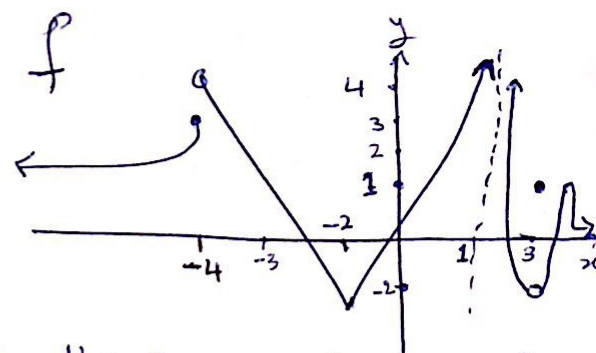
$$f(x) = \frac{\sqrt{x^2 - 6x + 9}}{x^2 - 6x + 8} \text{ is discontinuous.}$$

[40]

use the intermediate value theorem to show that the equation $\cos x = x$ has a solution in $[0, \frac{\pi}{2}]$

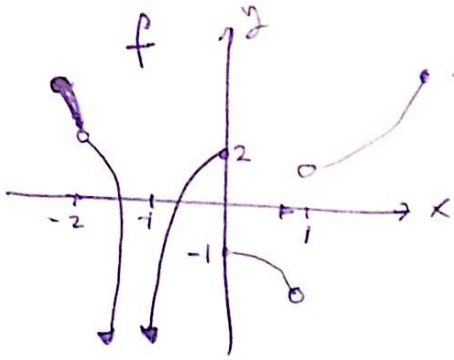
[39] use the intermediate value theorem to show that $f(x) = \frac{5}{x} - 4x^3 + 1$ has a zero in $[0, 1]$

[41]



Use the graph of $y = f(x)$ to find the following:

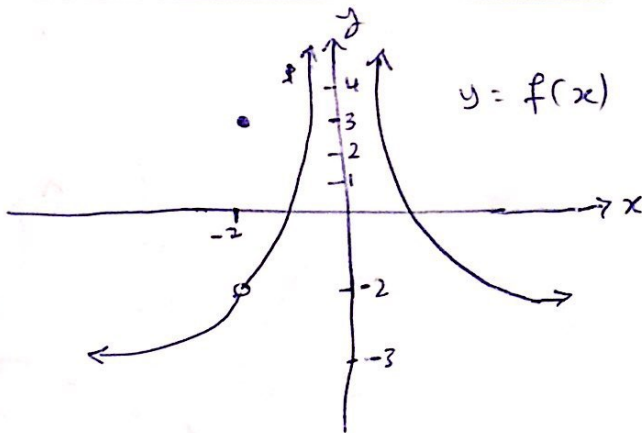
- ① $\lim_{x \rightarrow 3} f(x)$
- ② the horizontal and vertical asymptotes for the graph of $f(x)$
- ③ the x -value(s) in the domain at which $f(x)$ is not differentiable



① $\lim_{x \rightarrow 0^+} f(x) =$

② the vertical asymptotes for the graph of $f(x)$.

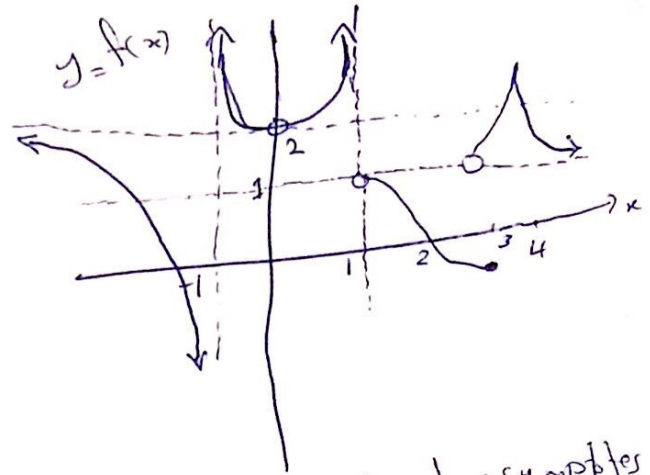
③ the x -values at which $f(x)$ is not continuous. $x =$



① $\lim_{x \rightarrow -2} f(x)$

② horizontal and vertical asymptotes

③ the x -values in the domain at which $f(x)$ is not differentiable.



① find the vertical asymptotes and horizontal asymptotes of f (state the reason).

② $\lim_{x \rightarrow 0} f(x)$

③ $\lim_{x \rightarrow 1} f(x)$

④ determine the x -coordinate in domain of f at which the function is not differentiable

[42] use the definition of ~~derivative~~ ^{to} find $f'(x)$

① $f(x) = x^2 + 2x - 4$

② $f(x) = x^2 + 3$

[43]

[44] the given $\lim_{h \rightarrow 0} \frac{f(1+h) - f(1)}{h}$ is a derivative, find the function and the point.

[45] find the equation of the tangent line

① $f(x) = x^5 + 4x^3 + \pi^2$ at $x=1$

[43] the $\lim_{h \rightarrow 0} \frac{(2+h)^2 - 4}{h}$ is a derivative find the function and the point

② $g(x) = 3x^2 + 5x + 1$ at $(1, 9)$

[246] Suppose f and g are differentiable at $x=3$

$$f(3) = 4, \quad f'(3) = -6$$

$$g(3) = 2, \quad g'(3) = 5$$

Prove that

$$(fg)' = \left(\frac{f}{f-g} \right)^2$$

[47] Find the derivative

$$\textcircled{1} y = \frac{1}{x^3} + \tan x + \cos(\pi)$$

[14]

$$\textcircled{2} y = x^2 \sec x$$

$$\textcircled{3} y = \sin x + 2 \cos x$$

[48] the position of is given by the equation $s(t) = \frac{\sin t}{t+3}$, s in meters and t in second what is the instantaneous of the Particle after 5 second?

$$\textcircled{2} s(t) = \frac{t-1}{t+1}, \text{ after 3 second}$$

3. $s(t) = \frac{t}{t+1}$, after 3 seconds

15

50) find the values of a and b if $f(x) = \begin{cases} ax^2 + b & x \leq -1 \\ 2x^5 + ax + 4 & x > -1 \end{cases}$ is differentiable.

49) find all points on the graph of $f(x)$ where the tangent line is horizontal

① $f(x) = x^2 - x - 1$

51) determine where $f(x) = \begin{cases} x^3 & x \leq 1 \\ 4x - 3 & x > 1 \end{cases}$

is differentiable at $x=1$ or not.

② $f(x) = 9 \sin x \cos x$

[52] discuss the
differentiability of
 $f(x) = x|x|$ at $x=0$