

$$\int u dv = uv - \int v du$$

**LIATE**

Logarithm, Inverse, Algebra, Trigonometric, Exponential

... الثاني حسب ترتيب الكلمات ...

$$\int \sin^n x dx = -\frac{1}{n} \cos x \sin^{n-1} x + \frac{n-1}{n} \int \sin^{n-2} x dx$$

$$\int \cos^n x dx = \frac{1}{n} \cos^{n-1} x \sin x + \frac{n-1}{n} \int \cos^{n-2} x dx$$

$$\int \sec^m x dx = \frac{\sec^{m-1} x \tan x}{m-1} + \frac{m-2}{m-1} \int \sec^{m-2} x dx$$

.. Important laws ..

$$\sin^2 x + \cos^2 x = 1$$

$$\sin^2 x = \frac{1 - \cos 2x}{2} \quad \text{الزاوية } 2x \text{ ضعف الزاوية}$$

$$1 + \tan^2 x = \sec^2 x$$

$$\cos^2 x = \frac{1 + \cos 2x}{2} \quad \text{ضعف}$$

$$1 + \cot^2 x = \csc^2 x$$

$$\sin 2x = 2 \sin x \cos x$$

$$\cos 2x = \cos^2 x - \sin^2 x$$

$$\cos u \cos v = \frac{1}{2} [\cos(u+v) + \cos(u-v)]$$

$$\sin u \cos v = \frac{1}{2} [\sin(u+v) + \sin(u-v)]$$

$$\sin u \sin v = \frac{1}{2} [\cos(u-v) - \cos(u+v)]$$

$$\cos u \sin v = \frac{1}{2} [\sin(u+v) - \sin(u-v)]$$

cos إذا الزوايا متساوية

Sin إذا الزوايا مختلفة

$$\int \sin^m x \cos^n x dx$$

**m**  
is odd

**n**  
is odd

**mn**  
both even

**mn**  
both odd

$$1 \int \sin^{m-1} x \cos x \sin x dx$$

$$1 \int \sin^m x \cos^{n-1} x \cos x dx$$

$$2 \sin^2 x = 1 - \cos^2 x$$

$$2 \cos^2 x = 1 + \sin^2 x$$

$$3 u = \cos x$$

$$3 u = \sin x$$

$$\begin{aligned} \sin^2 x &= \frac{1 - \cos 2x}{2} \\ \cos^2 x &= \frac{1 + \cos 2x}{2} \end{aligned}$$

اختار الأقوى.  
الأول.

إذا كان  $m \text{ و } n = 1$

نكامل بالتعويض (الطبيعي)

$$\int \tan^m x \sec^n x dx$$

$m$

$n$

$m$   $n$   
even odd

$m$   $n$   
odd even

is odd

is even

$$\textcircled{1} \tan^2 x = \sec^2 x - 1$$

$$\textcircled{1} \int \tan^{m-1} x \sec^{n-1} x \tan x \sec x dx$$

$$\textcircled{1} \int \tan^m x \sec^{n-2} x \sec^2 x dx$$

$$\textcircled{2} \int \sec^n x dx$$

• اختيار الأس الأول

$$\textcircled{2} \tan^2 x = \sec^2 x - 1$$

$$\textcircled{2} \sec^2 x = 1 + \tan^2 x$$

↓  
reduction  
formula

$$\textcircled{3} u = \sec x$$

$$\textcircled{3} u = \tan x$$

إذا كان  $m=1$  ||  $n=2$   
نكامل بالتعويض (البسيط)

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