

If $(x, y, z) = (1, -1, -1)$ is a solution of the following linear system

$$x + y - z = \alpha$$

$$x + \beta y + z = \beta$$

$$x + y + \alpha z = \delta$$

then:

☐ $\alpha = -1, \beta = 0, \delta = 1$

☐ $\alpha = 1, \beta = \frac{1}{2}, \delta = -1$

☐ $\alpha = -1, \beta = \frac{1}{2}, \delta = 1$

☒ $\alpha = 1, \beta = 0, \delta = -1$

Scanned with CamScanner

Scanned with CamScanner

Let $\mathbf{A}^{-1} = \begin{bmatrix} 3 & -2 & -1 \\ -4 & 1 & -1 \\ 2 & 0 & 1 \end{bmatrix}$, where \mathbf{A} denote the matrix of coefficients of the following linear system:

$$x_1 + 2x_2 + 3x_3 = 0$$

$$2x_1 + 5x_2 + 7x_3 = 0$$

$$-2x_1 - 4x_2 - 5x_3 = 1.$$

Then its solution set is equal to:

- ☒ $\{(-1, -1, 1)\}$
- ☐ $\{(3, -4, 2)\}$
- ☐ $\{(1, -1, -1)\}$
- ☐ $\{(-1, 1, -1)\}$

Scanned with CamScanner

Scanned with CamScanner

If $(x, y, z) = (1, -1, -1)$ is a solution of the following linear system

$$x + y - z = \alpha$$

$$x + \beta y + z = \beta$$

$$x + y + \alpha z = \delta$$

then:

☐ $\alpha = -1, \beta = 0, \delta = 1$

☐ $\alpha = 1, \beta = \frac{1}{2}, \delta = -1$

☐ $\alpha = -1, \beta = \frac{1}{2}, \delta = 1$

☒ $\alpha = 1, \beta = 0, \delta = -1$

Scanned with CamScanner

Scanned with CamScanner

Let $\text{Adj}(\mathbf{A}) = \begin{bmatrix} -2 & 0 & 0 \\ 0 & -2 & 0 \\ 0 & 0 & -2 \end{bmatrix}$. Then $\det(\mathbf{A})$ is equal to:

- ☒ -2
- ☐ $-\sqrt[3]{2}$
- ☐ -2^3
- ☐ 2

Scanned with CamScanner

Scanned with CamScanner

Question 6

Let $\begin{bmatrix} 2 & 3 & \lambda^2 & 0 \\ 1 & 2 & 1 & 0 \\ 1 & 3 & 7 & 0 \end{bmatrix}$ be the augmented matrix of a homogeneous linear system.

Then the set of values of λ for which the system has a no nontrivial solution is equal to:

☒ \mathbb{R}

☐ $\mathbb{R} \setminus \{-2, 2\}$

☐ $\mathbb{R} \setminus \{2\}$

☐ $\{\}$

→ ⚠ Moving to the next question prevents changes to this answer.

Scanned with CamScanner

Scanned with CamScanner

Let the matrices $A, B \in M_3(\mathbb{R})$ be singular matrices. Then the determinant $|2I + 2B^T B \text{adj}(A)|$ is equal to:

- ☒ 8
- ☐ 4
- ☐ 2
- ☐ 1

Scanned with CamScanner

Scanned with CamScanner

Question 3

The matrix $\begin{bmatrix} 1 & 1 & 1 \\ 1 & m & 2 \\ 1 & 10 & m \end{bmatrix}$ is non-invertible if and only if:

- ☐ $m \notin \{-2, 4\}$
- ☐ $m \in \mathbb{R} \setminus \{-4, 2\}$
- ☒ $m \in \{-2, 4\}$
- ☐ $m \in \{2, -4\}$

Scanned with CamScanner

Scanned with CamScanner

Which of the following matrices is an elementary matrix?

☐ $\begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix}$

☒ $\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}^T$

☐ $\begin{bmatrix} \sqrt{2} & 1 \\ 0 & 1 \end{bmatrix}$

☐ $\begin{bmatrix} -2 & 0 \\ -2 & 1 \end{bmatrix}$

Scanned with CamScanner

Scanned with CamScanner

The reduced row echelon form of the matrix $\begin{bmatrix} 0 & 2 & -1 \\ -1 & 1 & 0 \\ 0 & -1 & 1 \end{bmatrix}$ is:

☐ $\begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$

☐ $\begin{bmatrix} 1 & 2 & -1 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$

☐ $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & 0 & 0 \end{bmatrix}$

☒ $\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$

Scanned with CamScanner

Scanned with CamScanner