كلية العلوم وقت التمارين:

قسم الرياضيات

1-If
$$A = \begin{pmatrix} 3 & 0 & 0 \\ 0 & 1 & 2 \\ 0 & 2 & 1 \end{pmatrix}$$
 find $A^2 - 2A - 3I$.

2- let A be a matrix of order 3 such that |A| = 3 and $|A^2 + I| = 2$.

Find
$$|A + A^{-1}|$$

3- Show that

$$\begin{vmatrix} a & a+1 & a+2 \\ b & b+1 & b+2 \\ c & c+1 & c+2 \end{vmatrix} = 0$$

4- Find the matrix
$$B = \begin{pmatrix} x & y \\ z & t \end{pmatrix}$$
 such that $B \begin{pmatrix} 1 \\ -2 \end{pmatrix} = \begin{pmatrix} 4 \\ -5 \end{pmatrix}$ and

$$B\begin{pmatrix}2\\1\end{pmatrix} = \begin{pmatrix}3\\5\end{pmatrix}$$

5- Find the values of a for which the system has infinite solutions then solve the system in this case.

$$\begin{cases} x - 2y + z = 0 \\ x + ay - 3z = 0 \\ -x + 6y - 5z = 0 \end{cases}$$