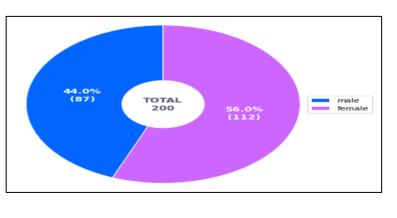
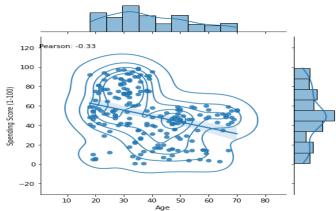
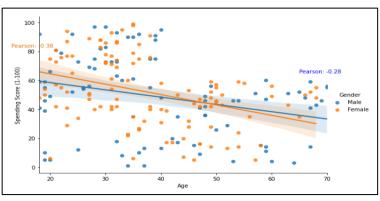
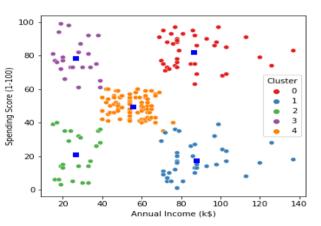
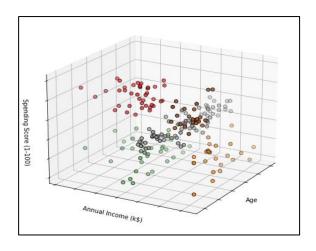
# Implementation of 4 Clustering Algorithms: K-Means, DBSCAN, MeanShift and Agglomerative on a customer dataset and their comparison

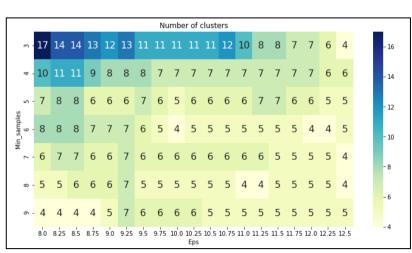












```
#Importing Libraries
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import seaborn as sns
from scipy import stats
import warnings
warnings.filterwarnings("ignore")

from sklearn.metrics import silhouette_score
from scipy.cluster.hierarchy import linkage
from scipy.cluster.hierarchy import dendrogram
from scipy.cluster.hierarchy import cut_tree

#Importing dataset
data = pd.read_csv('Customers.csv')
print("There are {} rows and {} columns in the dataset".format(data.shape[0], data.shape[1]))
```

There are 200 rows and 5 columns in the dataset

### Exploratory Data Analysis (EDA)

data.head()

|   | CustomerID | Gender | Age | Annual Income (k\$) | Spending Score (1-100) |
|---|------------|--------|-----|---------------------|------------------------|
| 0 | 1          | Male   | 19  | 15                  | 39                     |
| 1 | 2          | Male   | 21  | 15                  | 81                     |
| 2 | 3          | Female | 20  | 16                  | 6                      |
| 3 | 4          | Female | 23  | 16                  | 77                     |
| 4 | 5          | Female | 31  | 17                  | 40                     |

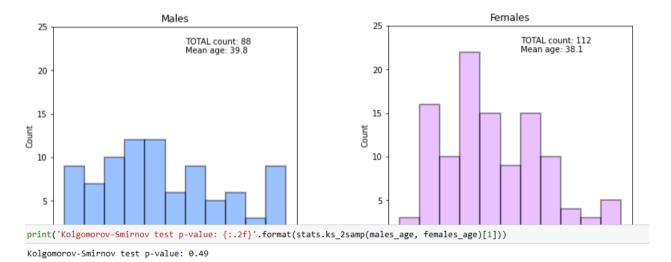
data.describe()

|       | CustomerID | Age        | Annual Income (k\$) | Spending Score (1-100) |
|-------|------------|------------|---------------------|------------------------|
| count | 200.000000 | 200.000000 | 200.000000          | 200.000000             |
| mean  | 100.500000 | 38.850000  | 60.560000           | 50.200000              |
| std   | 57.879185  | 13.969007  | 26.264721           | 25.823522              |
| min   | 1.000000   | 18.000000  | 15.000000           | 1.000000               |
| 25%   | 50.750000  | 28.750000  | 41.500000           | 34.750000              |
| 50%   | 100.500000 | 36.000000  | 61.500000           | 50.000000              |
| 75%   | 150.250000 | 49.000000  | 78.000000           | 73.000000              |
| max   | 200.000000 | 70.000000  | 137.000000          | 99.000000              |

```
data.isnull().sum()
CustomerID
```

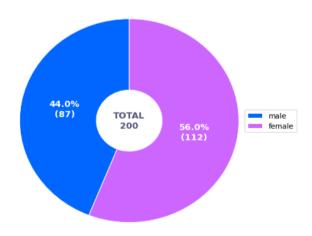
CustomerID 0
Gender 0
Age 0
Annual Income (k\$) 0
Spending Score (1-100) 0
dtype: int64

```
males_age = data[data['Gender']=='Male']['Age']
females_age = data[data['Gender']=='Female']['Age']
age\_bins = range(15,75,5)
#males histogram
fig2, (ax1,ax2) = plt.subplots(1,2, figsize=(12,5), sharey=True)
sns.distplot(males_age, bins=age_bins, kde=False, color='#0066ff', ax=ax1, hist_kws=dict(edgecolor="k",linewidth=2))
ax1.set_xticks(age_bins)
ax1.set_ylim(top=25)
ax1.set_title('Males')
ax1.set_ylabel('Count')
ax1.text(45,23, 'TOTAL count: {}'.format(males_age.count()))
ax1.text(45,22, 'Mean age: {:.1f}'.format(males_age.mean()))
#females histogram
fig2, (ax1,ax2) = plt.subplots(1,2, figsize=(12,5), sharey=True)
sns.distplot(females_age, bins=age_bins, kde=False, color='#cc66ff', ax=ax1, hist_kws=dict(edgecolor="k",linewidth=2))
ax1.set_xticks(age_bins)
ax1.set_ylim(top=25)
ax1.set title('Females')
ax1.set_ylabel('Count')
ax1.text(45,23, 'TOTAL count: {}'.format(females_age.count()))
ax1.text(45,22, 'Mean age: {:.1f}'.format(females_age.mean()))
plt.show()
```

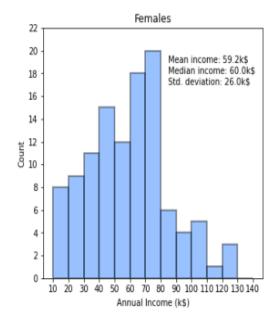


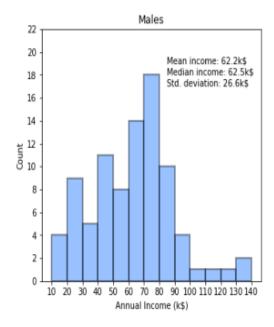
Kolgomorov-Smirnov test shows that the differences between these two groups are statistically insignificant

```
def labeler(pct, allvals):
    absolute = int(pct/100.*np.sum(allvals))
return "{:.1f}%\n({:d})".format(pct,absolute)
sizes = [males_age.count(), females_age.count()]
fig0, ax1 = plt.subplots(figsize =(6,6))
wedges, texts, autotexts = ax1.pie(sizes,
                                   autopct=lambda pct: labeler(pct, sizes),
                                   radius=1,
                                   colors=['#0066ff', '#cc66ff'],
                                   startangle=90,
                                   textprops=dict(color='w'),
                                   wedgeprops=dict(width=0.7, edgecolor='w'))
ax1.legend(wedges, ['male', 'female'],
          loc='center right',
          bbox_to_anchor=(0.7,0,0.5,1))
ha='center', va='center')
plt.setp(autotexts, size=12, weight='bold')
ax1.axis('equal')
plt.show()
```



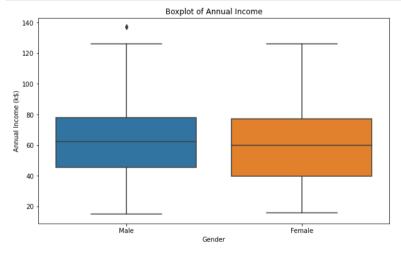
```
males_income = data[data['Gender']=='Male']['Annual Income (k$)']
females_income = data[data['Gender']=='Female']['Annual Income (k$)']
my_bins = range(10, 150, 10)
#males histogram
fig2, (ax1,ax2,ax3) = plt.subplots(1,3, figsize=(18,5))
sns.distplot(males_income, bins=my_bins, kde=False, color='#0066ff', ax=ax1, hist_kws=dict(edgecolor="k",linewidth=2))
ax1.set_xticks(my_bins)
ax1.set_yticks(range(0,24,2))
ax1.set_ylim(0,22)
ax1.set_title('Males')
ax1.set_ylabel('Count')
ax1.text(85,19, 'Mean income: {:.1f}k$'.format(males_income.mean()))
ax1.text(85,18, 'Median income: {:.1f}k$'.format(males_income.median()))
ax1.text(85,17, 'Std. deviation: {:.1f}k$'.format(males_income.std()))
#females histogram
fig2, (ax1,ax2,ax3) = plt.subplots(1,3, figsize=(18,5))
sns.distplot(females_income, bins=my_bins, kde=False, color='#0066ff', ax=ax1, hist_kws=dict(edgecolor="k",linewidth=2))
ax1.set_xticks(my_bins)
ax1.set_yticks(range(0,24,2))
ax1.set_ylim(0,22)
ax1.set_title('Females')
ax1.set_ylabel('Count')
ax1.text(85,19, 'Mean income: {:.1f}k$'.format(females_income.mean()))
ax1.text(85,18, 'Median income: {:.1f}k$'.format(females_income.median()))
ax1.text(85,17, 'Std. deviation: {:.1f}k$'.format(females_income.std()))
plt.show()
```





```
#boxplot
sns.boxplot(x='Gender',y='Annual Income (k$)', data=data, ax=ax3)
ax3.set_title('Boxplot of Annual Income')
plt.show()

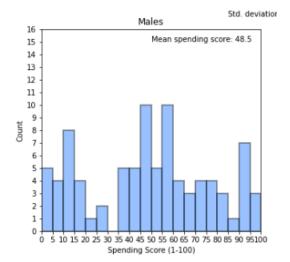
plt.figure(figsize=(10, 6)) # Adjust the size as needed
sns.boxplot(x='Gender', y='Annual Income (k$)', data=data)
plt.title('Boxplot of Annual Income')
plt.show()
```

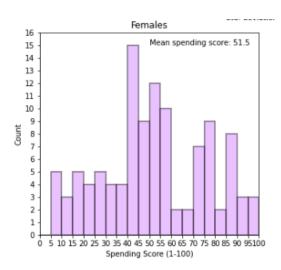


```
print('Kolgomorov-Smirnov test p-value: {:.2f}'.format(stats.ks_2samp(males_income, females_income)[1]))
```

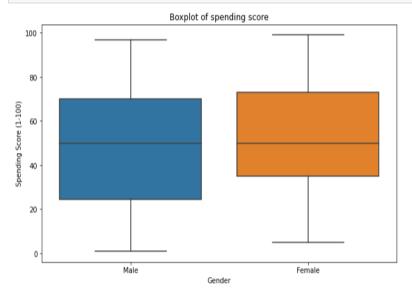
Kolgomorov-Smirnov test p-value: 0.78

```
males_spending = data[data['Gender']=='Male']['Spending Score (1-100)']
females_spending = data[data['Gender']=='Female']['Spending Score (1-100)']
spending_bins = range(0,105,5)
#males histogram
fig2, (ax1,ax2,ax3) = plt.subplots(1,3, figsize=(18,5))
sns.distplot(males_spending, bins=spending_bins, kde=False, color='#0066ff', ax=ax1, hist_kws=dict(edgecolor='k",linewidth=2))
ax1.set_xticks(spending_bins)
ax1.set_xlim(0,100)
ax1.set_yticks(range(0,17,1))
ax1.set_ylim(0,16)
ax1.set_title('Males')
ax1.set_ylabel('Count')
ax1.text(59,15, 'Mean spending score: {:.1f}'.format(males_spending.mean()))
ax1.text(85,18, 'Median spending score: {:.1f}'.format(males_spending.median()))
ax1.text(85,17, 'Std. deviation spending score: {:.1f}'.format(males_spending.std()))
#females histogram
fig2, (ax1,ax2,ax3) = plt.subplots(1,3, figsize=(18,5))
sns.distplot(females_spending, bins=spending_bins, kde=False, color='#cc66ff', ax=ax1, hist_kws=dict(edgecolor="k",linewidth=2))
ax1.set_xticks(spending_bins)
ax1.set xlim(0,100)
ax1.set_yticks(range(0,17,1))
ax1.set_ylim(0,16)
ax1.set_title('Females')
ax1.set_ylabel('Count')
ax1.text(50,15, 'Mean spending score: {:.1f}'.format(females_spending.mean()))
ax1.text(85,18, 'Median spending score: {:.1f}'.format(females_spending.median()))
ax1.text(85,17, 'Std. deviation spending score: {:.1f}'.format(females_spending.std()))
plt.show()
```





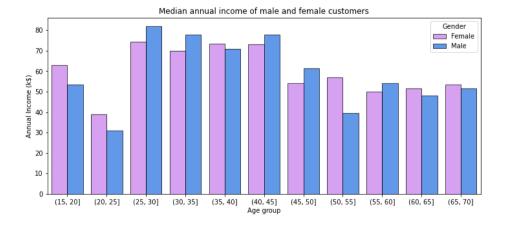
```
plt.figure(figsize=(10, 6)) # Adjust the size as needed
sns.boxplot(x='Gender', y='Spending Score (1-100)', data=data)
plt.title('Boxplot of spending score')
plt.show()
```



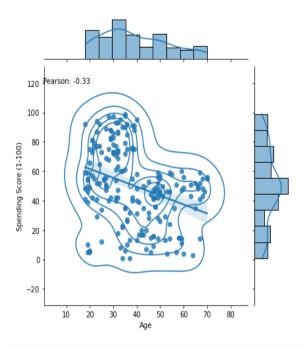
```
print('Kolgomorov-Smirnov test p-value: {:.2f}'.format(stats.ks_2samp(males_spending, females_spending)[1]))
```

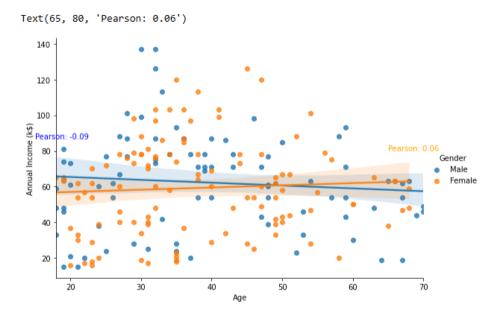
Kolgomorov-Smirnov test p-value: 0.29

```
medians_by_age_group = data.groupby(["Gender", pd.cut(data['Age'],age_bins)]).median()
medians_by_age_group.index = medians_by_age_group.index.set_names(['Gender', 'Age_group'])
medians_by_age_group.reset_index(inplace=True)
```



### Correlations



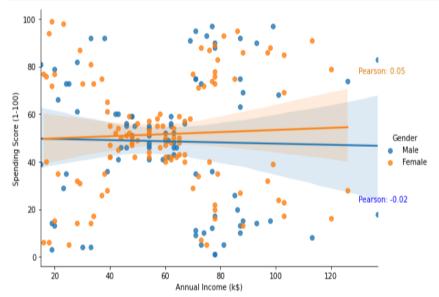


There is a negligible correlation between age and annule income of customers for both sex

### Slope is almost parallel to x-axis

```
#Calculating Pearson's correlations
corr1, _ = pearsonr(males_age.values, males_spending.values)
corr2, _ = pearsonr(females_age.values, females_spending.values)
{\tt sns.lmplot('Age', 'Spending \ Score \ (1-100)', \ data=data, \ hue='Gender',}\\
               aspect=1.5)
plt.text(65,65, 'Pearson: {:.2f}'.format(corr1),color ='blue')
plt.text(13,83, 'Pearson: {:.2f}'.format(corr2),color ='#d97900')
Text(13, 83, 'Pearson: -0.38')
      100
       80
  Spending Score (1-100)
                                                                                                      Pearson: -0.28
                                                                                                                      Male
                                                                                                                      Female
       40
       20
              20
                                 30
                                                                        50
                                                                                           60
```

- There are weak negative corrleations (<0.5) between age and spending score of customers for both sex groups
- slope is slight negative here
- It says that with increase in age there is decrease in spending score



- There is a negligible correlation between annual income and spending score of customers for both sex groups

# CLUSTERING - 1.K Means, 2.DBSCAN, 3.MeanShift, 4.Agglomerative

### K-Means

```
from sklearn.cluster import KMeans

#subset with numeric variables only
X_numerics = data[['Age','Annual Income (k$)', 'Spending Score (1-100)']]

X_numerics.head()
```

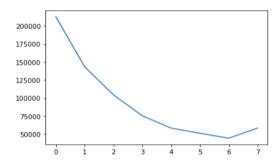
|   | Age | Annual Income (k\$) | Spending Score (1-100) |
|---|-----|---------------------|------------------------|
| 0 | 19  | 15                  | 39                     |
| 1 | 21  | 15                  | 81                     |
| 2 | 20  | 16                  | 6                      |
| 3 | 23  | 16                  | 77                     |
| 4 | 31  | 17                  | 40                     |

```
# k-means with some arbitrary k
kmeans = KMeans(n_clusters=4, max_iter=50)
kmeans.fit(X_numerics)
kmeans.labels
array([3, 3, 0, 3, 0, 3, 0, 3, 0, 3, 0, 3, 0, 3, 0, 3, 0, 3, 0, 3, 0, 3,
      0, 3, 0, 3, 0, 3, 0, 3, 0, 3, 0, 3, 0, 3, 0, 3, 0, 3, 0, 3, 0, 3,
      0, 3, 0, 0, 0, 0, 3, 0, 0, 0, 0, 0, 0, 0, 0, 3, 0, 0, 3,
      0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 2, 1, 2, 1, 2, 1, 2, 1, 2,
      1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2,
      1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2,
      1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2,
      1, 2])
# elbow-curve/SSD
ssd = []
range_n_clusters = [2, 3, 4, 5, 6, 7, 8]
for num_clusters in range_n_clusters:
   kmeans = KMeans(n_clusters=num_clusters, max_iter=50)
   kmeans.fit(X_numerics)
   ssd.append(kmeans.inertia_)
# plot the SSDs for each n clusters
# ssd
plt.plot(ssd)
[<matplotlib.lines.Line2D at 0x14573124070>]
 200000
175000
150000
125000
 100000
 75000
 50000
# silhouette analysis
range_n_clusters = [2, 3, 4, 5, 6, 7, 8]
for num_clusters in range_n_clusters:
    # intialise kmeans
    kmeans = KMeans(n_clusters=num_clusters, max_iter=50)
    kmeans.fit(X_numerics)
    cluster_labels = kmeans.labels_
    silhouette_avg = silhouette_score(X_numerics, cluster_labels)
    print("For n_clusters={0}, the silhouette score is {1}".format(num_clusters, silhouette_avg))
For n_clusters=2, the silhouette score is 0.293166070535953
For n clusters=3, the silhouette score is 0.3839349967742105
For n_clusters=4, the silhouette score is 0.40546302077733304
For n_clusters=5, the silhouette score is 0.44428597560893024
For n_clusters=6, the silhouette score is 0.4523443947724053
For n_clusters=7, the silhouette score is 0.43978902692261157
For n_clusters=8, the silhouette score is 0.4280971079746162
# final model with k=6
kmeans = KMeans(n_clusters=6, max_iter=50)
kmeans.fit(X_numerics)
```

ssd.append(kmeans.inertia\_)

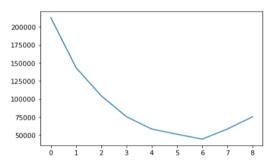
plt.plot(ssd)

### [<matplotlib.lines.Line2D at 0x145732ab250>]



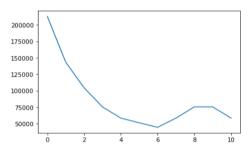
```
# final model with k=5
kmeans = KMeans(n_clusters=5, max_iter=50)
kmeans.fit(X_numerics)
ssd.append(kmeans.inertia_)
plt.plot(ssd)
```

[<matplotlib.lines.Line2D at 0x14573300970>]



```
KM_6_clusters = KMeans(n_clusters=6, init='k-means++').fit(X_numerics)
ssd.append(KM_6_clusters.inertia_)
plt.plot(ssd)
```

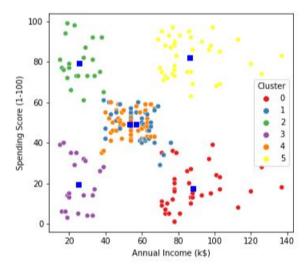
[<matplotlib.lines.Line2D at 0x145734ae340>]



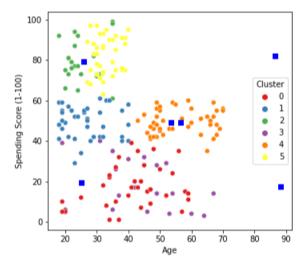
```
KM_6_clustered = X_numerics.copy()
KM_6_clustered.loc[:,'Cluster'] = KM_6_clusters.labels_
```

fig1, (axes) = plt.subplots(1,2,figsize=(12,5)) scat\_1 = sns.scatterplot('Annual Income (k\$)', 'Spending Score (1-100)', data=KM\_6\_clustered, hue='Cluster', ax=axes[0], palette='Set1', legend='full') sns.scatterplot('Age', 'Spending Score (1-100)', data=KM\_6\_clustered, hue='Cluster', ax=axes[0], palette='Set1', legend='full')

 $axes[0].scatter(KM\_6\_clusters.cluster\_centers\_[:,1], KM\_6\_clusters.cluster\_centers\_[:,2], marker='s',s=40, c="blue") \\ axes[1].scatter(KM\_6\_clusters.cluster\_centers\_[:,0], KM\_6\_clusters.cluster\_centers\_[:,0], KM\_6\_cluster_center\_centers\_[:,0], KM\_6\_cluster_center\_center\_[:,0], KM\_6\_cluster_center\_cent$ 

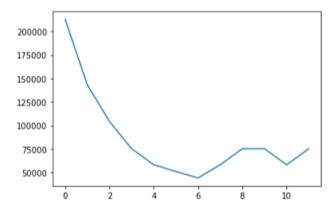


<matplotlib.collections.PathCollection at 0x1456f14c430>

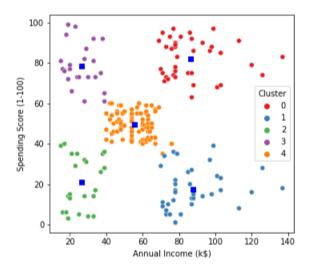


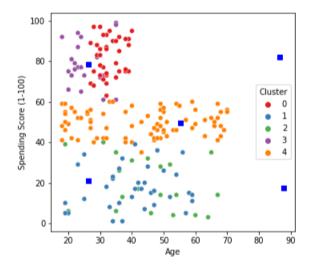
```
KM_5_clusters = KMeans(n_clusters=5, init='k-means++').fit(X_numerics)
ssd.append(KM_5_clusters.inertia_)
plt.plot(ssd)
```

[<matplotlib.lines.Line2D at 0x14574777370>]



<matplotlib.collections.PathCollection at 0x1457335bc10>





```
KM 5 clusters.labels
```

```
array([2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3,
```

```
# assign the label
X_numerics['cluster_id'] = KM_5_clusters.labels_
X_numerics.head()
```

|   | Age | Annual Income (k\$) | Spending Score (1-100) | cluster_id |
|---|-----|---------------------|------------------------|------------|
| 0 | 19  | 15                  | 39                     | 2          |
| 1 | 21  | 15                  | 81                     | 3          |
| 2 | 20  | 16                  | 6                      | 2          |
| 3 | 23  | 16                  | 77                     | 3          |
| 4 | 31  | 17                  | 40                     | 2          |

### KM\_6\_clusters.labels\_

```
# assign the Label
X_numerics['cluster_id'] = KM_6_clusters.labels_
X_numerics.head()
```

# Age Annual Income (k\$) Spending Score (1-100) cluster\_id 0 19 15 39 3 1 21 15 81 2 2 20 16 6 3 3 23 16 77 2 4 31 17 40 3

```
KM5_clustered = X_numerics.copy()
KM5_clustered.loc[:,'Cluster'] = KM_5_clusters.labels_
```

```
KM5_clust_sizes = KM5_clustered.groupby('Cluster')
KM5_clust_sizes.columns = ["KM5_size"]
KM5_clust_sizes.describe()
```

Annual Income Age ... cluster\_id Labels min 25% 50% 75% max count mean std min 25% 50% 75% max count mean ... 75% max count mean std Cluster **0** 39.0 32.692308 3.728650 27.0 30.0 32.0 35.50 40.0 39.0 86.538462 ... 1.0 1.0 39.0 2.000000 0.000000 2.0 2.0 2.0 2.0 **1** 36.0 40.666667 11.496583 19.0 34.0 41.5 47.25 59.0 36.0 87.750000 ... 2.0 2.0 36.0 0.055556 0.232311 0.0 0.0 0.0 0.0 1.0 23.0 26.304348 ... **2** 23.0 45.217391 13.228607 19.0 35.5 46.0 53.50 67.0 4.0 4.0 23.0 4.000000 0.000000 4.0 4.0 4.0 4.0 4.0 3 23.0 25.521739 5.273170 18.0 21.5 24.0 30.00 35.0 23.0 26.304348 ... 3.0 3.0 23.0 2.739130 0.688700 1.0 3.0 4 79.0 43.088608 16.478572 18.0 27.0 47.0 54.50 70.0 79.0 55.291139 ... 0.0 2.0 79.0 0.987342 0.112509 0.0 1.0 1.0 1.0 1.0 5 rows x 40 columns

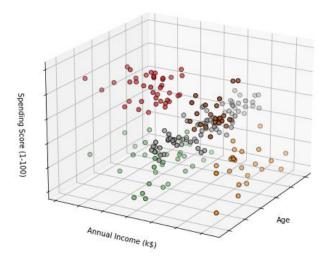
```
KM6_clustered = X_numerics.copy()
KM6_clustered.loc[:,'Cluster'] = KM_6_clusters.labels_

KM6_clust_sizes = KM6_clustered.groupby('Cluster')
KM6_clust_sizes.columns = ["KM6_size"]
KM6_clust_sizes.describe()
```

|         | Age   |           |           |      |       |      |       |      | Annual<br>(k\$) | Income    | <br>cluste | er_id | Labels |          |          |     |     |     |     |     |
|---------|-------|-----------|-----------|------|-------|------|-------|------|-----------------|-----------|------------|-------|--------|----------|----------|-----|-----|-----|-----|-----|
|         | count | mean      | std       | min  | 25%   | 50%  | 75%   | max  | count           | mean      | <br>75%    | max   | count  | mean     | std      | min | 25% | 50% | 75% | max |
| Cluster |       |           |           |      |       |      |       |      |                 |           |            |       |        |          |          |     |     |     |     |     |
| 0       | 35.0  | 41.685714 | 10.897305 | 19.0 | 35.00 | 43.0 | 47.50 | 59.0 | 35.0            | 88.228571 | <br>2.0    | 2.0   | 35.0   | 0.000000 | 0.000000 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1       | 38.0  | 27.000000 | 7.032742  | 18.0 | 21.00 | 26.5 | 31.75 | 40.0 | 38.0            | 56.657895 | <br>0.0    | 3.0   | 38.0   | 1.000000 | 0.000000 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 |
| 2       | 22.0  | 25.272727 | 5.257030  | 18.0 | 21.25 | 23.5 | 29.75 | 35.0 | 22.0            | 25.727273 | <br>3.0    | 3.0   | 22.0   | 2.818182 | 0.588490 | 1.0 | 3.0 | 3.0 | 3.0 | 3.0 |
| 3       | 21.0  | 44.142857 | 13.089254 | 19.0 | 35.00 | 45.0 | 53.00 | 67.0 | 21.0            | 25.142857 | <br>4.0    | 4.0   | 21.0   | 4.000000 | 0.000000 | 4.0 | 4.0 | 4.0 | 4.0 | 4.0 |
| 4       | 45.0  | 56.155556 | 8.543886  | 43.0 | 49.00 | 54.0 | 65.00 | 70.0 | 45.0            | 53.377778 | <br>0.0    | 4.0   | 45.0   | 1.133333 | 0.625227 | 1.0 | 1.0 | 1.0 | 1.0 | 4.0 |
| 5       | 39.0  | 32.692308 | 3.728650  | 27.0 | 30.00 | 32.0 | 35.50 | 40.0 | 39.0            | 86.538462 | <br>1.0    | 1.0   | 39.0   | 2.000000 | 0.000000 | 2.0 | 2.0 | 2.0 | 2.0 | 2.0 |

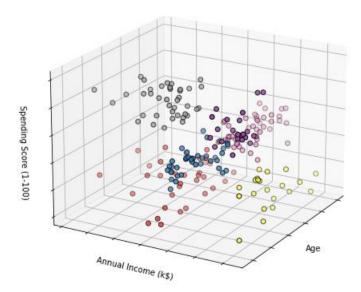
6 rows × 40 columns

```
from mpl toolkits.mplot3d import Axes3D
fig = plt.figure(figsize=(7,7))
ax = Axes3D(fig, rect=[0, 0, .99, 1], elev=20, azim=210)
ax.scatter(KM5_clustered['Age'],KM5_clustered['Annual Income (k$)'],
           KM5 clustered['Spending Score (1-100)'],
           c=KM_5_clusters.labels_,
           s=35, edgecolor='k', cmap=plt.cm.Set1)
ax.w xaxis.set ticklabels([])
ax.w yaxis.set_ticklabels([])
ax.w zaxis.set ticklabels([])
ax.set_xlabel('Age')
ax.set ylabel('Annual Income (k$)')
ax.set zlabel('Spending Score (1-100)')
ax.set_title('3D view of K-Means 5 clusters')
ax.dist = 12
plt.show()
```



```
KM_6_clustered = X_numerics.copy()
KM_6_clustered.loc[:,'Cluster'] = KM_6_clusters.labels_
```

3D view of K-Means 6 clusters



# **DBSCAN Clustering Algorithm**

```
from sklearn.cluster import DBSCAN
```

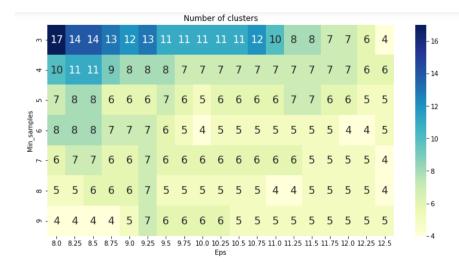
```
from itertools import product

eps_values = np.arange(8,12.75,0.25) #eps values to be investigated
min_samples = np.arange(3,10) #min_samples values to be investigated

DBSCAN_params = list(product(eps_values, min_samples))

no_of_clusters = []
sil_score = []
for p in DBSCAN_params:
    DBS_clustering = DBSCAN(eps=p[0], min_samples=p[1]).fit(X_numerics)
    no_of_clusters.append(len(np.unique(DBS_clustering.labels_)))
    sil_score.append(silhouette_score(X_numerics, DBS_clustering.labels_))
```

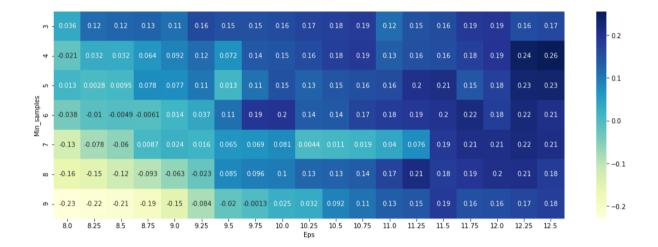
```
tmp = pd.DataFrame.from_records(DBSCAN_params, columns=['Eps','Min_samples'])
tmp['No_of_clusters'] = no_of_clusters
pivot_1 = pd.pivot_table(tmp, values='No_of_clusters', index='Min_samples', columns='Eps')
fig, ax = plt.subplots(figsize=(12,6))
sns.heatmap(pivot_1, annot=True, annot_kws={"size":16}, cmap="YlGnBu", ax=ax)
ax.set_title('Number of clusters')
plt.show()
```



From the above heatmap the number of clusters can range from 4 to 17.

Given sample size of 3 observations and eps = 8, it have 17 clusters.

```
tmp = pd.DataFrame.from_records(DBSCAN_params, columns=['Eps','Min_samples'])
tmp['Sil_score'] = sil_score
pivot_1 = pd.pivot_table(tmp, values='Sil_score', index='Min_samples', columns='Eps')
fig, ax = plt.subplots(figsize=(18,6))
sns.heatmap(pivot_1, annot=True, annot_kws={"size":10}, cmap="YlGnBu", ax=ax)
plt.show()
```



The silhouette score in the above heatmap is 0.26 for eps value=12.5 and sample size=4.

#### This is Global Maximum

```
DBS_clustering = DBSCAN(eps=12.5, min_samples=4).fit(X_numerics)

DBSCAN_clustered = X_numerics.copy()
DBSCAN_clustered.loc[:,'Cluster'] = DBS_clustering.labels_

DBSCAN_clust_sizes = DBSCAN_clustered.groupby('Cluster')
DBSCAN_clust_sizes.columns = ["DBSCAN_size"]
DBSCAN_clust_sizes.describe()
```

|         | Age   |           |           |      |       |      |       |      | Annual<br>(k\$) | Income | <br>Spendii<br>Score ( |      | cluster | _id      |          |     |     |     |      |     |
|---------|-------|-----------|-----------|------|-------|------|-------|------|-----------------|--------|------------------------|------|---------|----------|----------|-----|-----|-----|------|-----|
|         | count | mean      | std       | min  | 25%   | 50%  | 75%   | max  | count           | mean   | <br>75%                | max  | count   | mean     | std      | min | 25% | 50% | 75%  | max |
| Cluster |       |           |           |      |       |      |       |      |                 |        |                        |      |         |          |          |     |     |     |      |     |
| -1      | 18.0  | 36.944444 | 12.316762 | 20.0 | 32.00 | 34.5 | 36.50 | 67.0 | 18.0            | 74.000 | <br>77.75              | 99.0 | 18.0    | 2.611111 | 1.974511 | 0.0 | 0.5 | 3.0 | 4.75 | 5.0 |
| 0       | 112.0 | 39.142857 | 16.002735 | 18.0 | 24.00 | 37.0 | 50.00 | 70.0 | 112.0           | 48.250 | <br>58.25              | 92.0 | 112.0   | 2.491071 | 1.355639 | 0.0 | 1.0 | 2.0 | 4.00 | 4.0 |
| 1       | 8.0   | 53.250000 | 7.382412  | 42.0 | 48.25 | 53.5 | 58.50 | 64.0 | 8.0             | 27.750 | <br>14.25              | 17.0 | 8.0     | 3.000000 | 0.000000 | 3.0 | 3.0 | 3.0 | 3.00 | 3.0 |
| 2       | 34.0  | 32.882353 | 3.859382  | 27.0 | 30.00 | 32.0 | 36.00 | 40.0 | 34.0            | 82.000 | <br>90.75              | 97.0 | 34.0    | 5.000000 | 0.000000 | 5.0 | 5.0 | 5.0 | 5.00 | 5.0 |
| 3       | 24.0  | 45.583333 | 8.303570  | 34.0 | 39.25 | 44.0 | 52.50 | 59.0 | 24.0            | 85.875 | <br>23.25              | 39.0 | 24.0    | 0.000000 | 0.000000 | 0.0 | 0.0 | 0.0 | 0.00 | 0.0 |
| 4       | 4.0   | 20.750000 | 2.872281  | 19.0 | 19.00 | 19.5 | 21.25 | 25.0 | 4.0             | 76.250 | <br>10.50              | 12.0 | 4.0     | 0.000000 | 0.000000 | 0.0 | 0.0 | 0.0 | 0.00 | 0.0 |

6 rows x 32 columns

### cluster -1 is an outlier. There are 18 outliers present

```
DBS_clustering.labels_
array([ 0, 0, -1, 0, 0, 0, -1, -1, 1, 0, -1, -1, 1,
                                                  0, -1, 0,
      0, 0, -1, 0, 0, 1, 0, 1,
                                 0,
                                     0,
                                        0, 0,
                                               0, 1,
                                                     0, 1,
      1, 0, 1, 0, 0, 0, -1,
                             0,
                                 0,
                                    0,
                                       0,
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      0, 0, 0,
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                0,
                    2,
                       0,
                          2,
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                                 2,
                                     3,
                                        2,
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                                                     2,
                                                         4,
                                                            2,
                                        0,
             4,
                2,
                   3, 2, 0,
                             2, 4, 2,
                                                     3,
                                                         2,
                                                            3,
      3, 2,
                                           2,
                                               3,
                                                  2,
      2, 3, 2,
                3, 2, -1, 2, 3, 2, 4, 2, 3,
                                               2, 3, 2, 3, 2,
      3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3, 2, 3,
      -1, 3, 2, 3, -1, -1, 2, -1, -1, -1, -1, -1], dtype=int64)
```

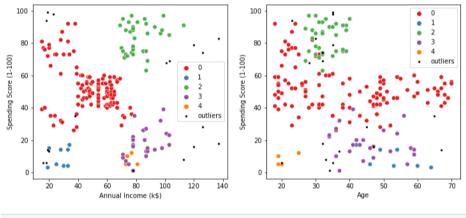
### DBSCAN created 5 clusters plus outlier cluster [-1]. Sizes of cluster 0-4 vary significantly

```
# assign the label
X_numerics['cluster_id'] = DBS_clustering.labels_
X_numerics.head(10)
```

|   | Age | Annual Income (k\$) | Spending Score (1-100) | cluster_id |
|---|-----|---------------------|------------------------|------------|
| 0 | 19  | 15                  | 39                     | 0          |
| 1 | 21  | 15                  | 81                     | 0          |
| 2 | 20  | 16                  | 6                      | -1         |
| 3 | 23  | 16                  | 77                     | 0          |
| 4 | 31  | 17                  | 40                     | 0          |
| 5 | 22  | 17                  | 76                     | 0          |
| 6 | 35  | 18                  | 6                      | -1         |
| 7 | 23  | 18                  | 94                     | -1         |
| 8 | 64  | 19                  | 3                      | 1          |
| 9 | 30  | 19                  | 72                     | 0          |

```
# assign the label
X_numerics['cluster_id'] = DBS_clustering.labels_
X_numerics.tail(10)
```

|     | Age | Annual Income (k\$) | Spending Score (1-100) | cluster_id |
|-----|-----|---------------------|------------------------|------------|
| 190 | 34  | 103                 | 23                     | 3          |
| 191 | 32  | 103                 | 69                     | -1         |
| 192 | 33  | 113                 | 8                      | -1         |
| 193 | 38  | 113                 | 91                     | 2          |
| 194 | 47  | 120                 | 16                     | -1         |
| 195 | 35  | 120                 | 79                     | -1         |
| 196 | 45  | 126                 | 28                     | -1         |
| 197 | 32  | 126                 | 74                     | -1         |
| 198 | 32  | 137                 | 18                     | -1         |
| 199 | 30  | 137                 | 83                     | -1         |



```
dbscan_clustered = X_numerics.copy()
dbscan_clustered.loc[:,'Cluster'] = DBS_clustering.labels_
```

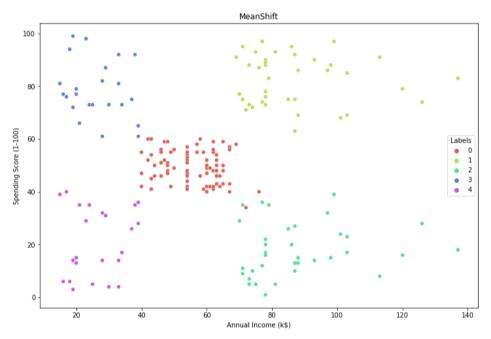
```
dbscan_clust_sizes = dbscan_clustered.groupby('Cluster')
dbscan_clust_sizes.columns = ["dbscan_size"]
dbscan_clust_sizes.describe()
```

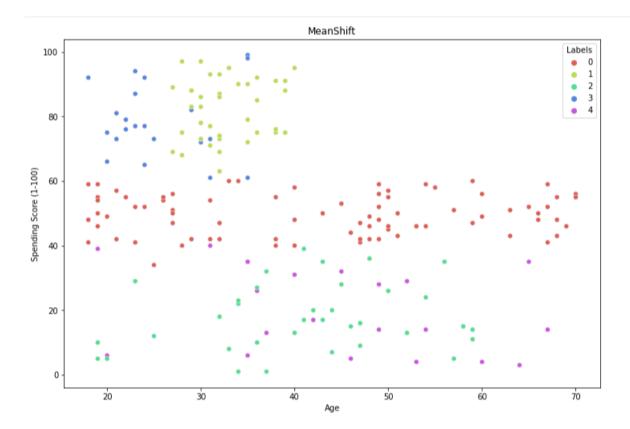
|         | Age   |           |           |      |       |      |       |      | Annual II<br>(k\$) | ncome  | <br>cluste | er_id | Labels |          |          |     |     |     |      |     |
|---------|-------|-----------|-----------|------|-------|------|-------|------|--------------------|--------|------------|-------|--------|----------|----------|-----|-----|-----|------|-----|
|         | count | mean      | std       | min  | 25%   | 50%  | 75%   | max  | count              | mean   | <br>75%    | max   | count  | mean     | std      | min | 25% | 50% | 75%  | max |
| Cluster |       |           |           |      |       |      |       |      |                    |        |            |       |        |          |          |     |     |     |      |     |
| -1      | 18.0  | 36.944444 | 12.316762 | 20.0 | 32.00 | 34.5 | 36.50 | 67.0 | 18.0               | 74.000 | <br>3.75   | 4.0   | 18.0   | 2.166667 | 1.581139 | 0.0 | 0.5 | 2.0 | 3.75 | 4.0 |
| 0       | 112.0 | 39.142857 | 16.002735 | 18.0 | 24.00 | 37.0 | 50.00 | 70.0 | 112.0              | 48.250 | <br>3.00   | 4.0   | 112.0  | 1.553571 | 1.064067 | 0.0 | 1.0 | 1.0 | 1.00 | 4.0 |
| 1       | 8.0   | 53.250000 | 7.382412  | 42.0 | 48.25 | 53.5 | 58.50 | 64.0 | 8.0                | 27.750 | <br>4.00   | 4.0   | 8.0    | 4.000000 | 0.000000 | 4.0 | 4.0 | 4.0 | 4.00 | 4.0 |
| 2       | 34.0  | 32.882353 | 3.859382  | 27.0 | 30.00 | 32.0 | 36.00 | 40.0 | 34.0               | 82.000 | <br>1.00   | 1.0   | 34.0   | 2.000000 | 0.000000 | 2.0 | 2.0 | 2.0 | 2.00 | 2.0 |
| 3       | 24.0  | 45.583333 | 8.303570  | 34.0 | 39.25 | 44.0 | 52.50 | 59.0 | 24.0               | 85.875 | <br>2.00   | 2.0   | 24.0   | 0.000000 | 0.000000 | 0.0 | 0.0 | 0.0 | 0.00 | 0.0 |
| 4       | 4.0   | 20.750000 | 2.872281  | 19.0 | 19.00 | 19.5 | 21.25 | 25.0 | 4.0                | 76.250 | <br>2.00   | 2.0   | 4.0    | 0.000000 | 0.000000 | 0.0 | 0.0 | 0.0 | 0.00 | 0.0 |

6 rows × 40 columns

# MeanShift Clustering Algorithm ¶

```
# k-means with some arbitrary k
ms = MeanShift(bandwidth=25)
ms.fit(X_numerics)
ms.labels_
4, 3, 4, 3, 4, 3, 4, 3, 4, 3, 4, 3, 4, 3, 4, 3, 4, 3, 4, 3, 4, 3,
     0, 1, 2, 1, 2, 1, 2, 1, 2, 1, 0, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1,
    2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1,
     2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1, 2, 1,
     2, 1], dtype=int64)
from sklearn.cluster import MeanShift, estimate_bandwidth
ms=MeanShift(bandwidth=25).fit(X_numerics)
X_numerics['Labels'] = ms.labels_
plt.figure(figsize=(12,8))
sns.scatterplot(X_numerics['Annual Income (k$)'], X_numerics['Spending Score (1-100)'], hue=X_numerics['Labels'],
          palette = sns.color_palette('hls', np.unique(ms.labels_).shape[0]))
plt.plot()
plt.title('MeanShift')
plt.show()
```





```
MS_clustered = X_numerics.copy()
MS_clustered.loc[:,'cluster'] = ms.labels_

# assign the label
X_numerics['cluster_id'] = ms.labels_
X_numerics.head(10)
```

|   | Age | Annual Income (k\$) | Spending Score (1-100) | cluster_id | Labels |
|---|-----|---------------------|------------------------|------------|--------|
| 0 | 19  | 15                  | 39                     | 4          | 4      |
| 1 | 21  | 15                  | 81                     | 3          | 3      |
| 2 | 20  | 16                  | 6                      | 4          | 4      |
| 3 | 23  | 16                  | 77                     | 3          | 3      |
| 4 | 31  | 17                  | 40                     | 4          | 4      |
| 5 | 22  | 17                  | 76                     | 3          | 3      |
| 6 | 35  | 18                  | 6                      | 4          | 4      |
| 7 | 23  | 18                  | 94                     | 3          | 3      |
| 8 | 64  | 19                  | 3                      | 4          | 4      |
| 9 | 30  | 19                  | 72                     | 3          | 3      |

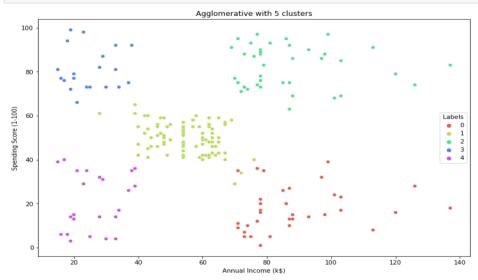
```
ms_clustered = X_numerics.copy()
ms_clustered.loc[:,'Cluster'] = ms.labels_

ms_clust_sizes = ms_clustered.groupby('Cluster')
ms_clust_sizes.columns = ["ms_size"]
ms_clust_sizes.describe()
```

|         | Age   |           |           |      | (k\$) | Income | <br>cluste | er_id | Labels |           |         |     |       |          |          |     |     |     |     |     |
|---------|-------|-----------|-----------|------|-------|--------|------------|-------|--------|-----------|---------|-----|-------|----------|----------|-----|-----|-----|-----|-----|
|         | count | mean      | std       | min  | 25%   | 50%    | 75%        | max   | count  | mean      | <br>75% | max | count | mean     | std      | min | 25% | 50% | 75% | max |
| Cluster |       |           |           |      |       |        |            |       |        |           |         |     |       |          |          |     |     |     |     |     |
| 0       | 79.0  | 42.860759 | 16.603779 | 18.0 | 27.0  | 47.0   | 54.50      | 70.0  | 79.0   | 55.303797 | <br>0.0 | 0.0 | 79.0  | 1.000000 | 0.000000 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 |
| 1       | 39.0  | 32.692308 | 3.728650  | 27.0 | 30.0  | 32.0   | 35.50      | 40.0  | 39.0   | 86.538462 | <br>1.0 | 1.0 | 39.0  | 2.000000 | 0.000000 | 2.0 | 2.0 | 2.0 | 2.0 | 2.0 |
| 2       | 36.0  | 41.166667 | 11.182895 | 19.0 | 34.0  | 42.5   | 47.25      | 59.0  | 36.0   | 87.722222 | <br>2.0 | 2.0 | 36.0  | 0.027778 | 0.166667 | 0.0 | 0.0 | 0.0 | 0.0 | 1.0 |
| 3       | 23.0  | 25.521739 | 5.273170  | 18.0 | 21.5  | 24.0   | 30.00      | 35.0  | 23.0   | 26.304348 | <br>3.0 | 3.0 | 23.0  | 2.739130 | 0.688700 | 1.0 | 3.0 | 3.0 | 3.0 | 3.0 |
| 4       | 23.0  | 45.217391 | 13.228607 | 19.0 | 35.5  | 46.0   | 53.50      | 67.0  | 23.0   | 26.304348 | <br>4.0 | 4.0 | 23.0  | 4.000000 | 0.000000 | 4.0 | 4.0 | 4.0 | 4.0 | 4.0 |

5 rows × 40 columns

### **Agglomerative Clustering**



```
from scipy.cluster import hierarchy
 from scipy.spatial import distance_matrix
 dist = distance_matrix(X_numerics, X_numerics)
 print(dist)
 [[ 0.
                   42.07136794 33.03028913 ... 117.16654813 124.55520864
    130.20752666]
  [ 42.07136794
                    0.
                                  75.02666193 ... 111.7855089 137.7824372
    122.36829655]
   [ 33.03028913 75.02666193 0.
                                                ... 129.92690253 122.26610323
   143.81585448]
   [117.16654813 111.7855089 129.92690253 ... 0.
                                                                     57.11392125
     14.35270009]
   [124.55520864 137.7824372 122.26610323 ... 57.11392125 0.
     65.06919394]
   [130.20752666 122.36829655 143.81585448 ... 14.35270009 65.06919394
      0.
                 ]]
 Z = hierarchy.linkage(dist, 'complete')
 plt.figure(figsize=(18,50))
 dendro = hierarchy.dendrogram(Z, leaf_rotation = 0, leaf_font_size = 12, orientation='right')
   51
43
45
68
65
61
27
23
21
31
35
25
17
9
39
37
15
13
5
3
    1
33
Z = hierarchy.linkage(dist, 'average')
plt.figure(figsize=(18,50))
dendro = hierarchy.dendrogram(Z, leaf_rotation = 0, leaf_font_size = 12, orientation='right')
 183
181
179
189
189
185
191
187
163
145
175
143
135
151
141
127
123
171
165
177
169
169
 139
Agg_clustered = X_numerics.copy()
Agg_clustered.loc[:,'Cluster'] = agglom.labels_
Agg_clust_sizes = Agg_clustered.groupby('Cluster')
Agg_clust_sizes.columns = ["Agg_size"]
Agg_clust_sizes.describe()
```

```
Agg_clustered = X_numerics.copy()
Agg_clustered.loc[:,'Cluster'] = agglom.labels_

Agg_clust_sizes = Agg_clustered.groupby('Cluster')
Agg_clust_sizes.columns = ["Agg_size"]
Agg_clust_sizes.describe()

Age Annual Income (k$) ... cluster_id Labels
```

|         | Age   |           |           |      |      |      |       |      | Annual | Income (k\$) | <br>clust | er_id | Labels |      |     |     |     |     |     |     |
|---------|-------|-----------|-----------|------|------|------|-------|------|--------|--------------|-----------|-------|--------|------|-----|-----|-----|-----|-----|-----|
|         | count | mean      | std       | min  | 25%  | 50%  | 75%   | max  | count  | mean         | <br>75%   | max   | count  | mean | std | min | 25% | 50% | 75% | max |
| Cluster |       |           |           |      |      |      |       |      |        |              |           |       |        |      |     |     |     |     |     |     |
| 0       | 35.0  | 41.685714 | 10.897305 | 19.0 | 35.0 | 43.0 | 47.50 | 59.0 | 35.0   | 88.228571    | <br>2.0   | 2.0   | 35.0   | 0.0  | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 1       | 83.0  | 42.156627 | 16.533397 | 18.0 | 27.0 | 45.0 | 54.00 | 70.0 | 83.0   | 54.759036    | <br>0.0   | 3.0   | 83.0   | 1.0  | 0.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 |
| 2       | 39.0  | 32.692308 | 3.728650  | 27.0 | 30.0 | 32.0 | 35.50 | 40.0 | 39.0   | 86.538462    | <br>1.0   | 1.0   | 39.0   | 2.0  | 0.0 | 2.0 | 2.0 | 2.0 | 2.0 | 2.0 |
| 3       | 20.0  | 24.850000 | 5.029126  | 18.0 | 21.0 | 23.0 | 29.25 | 35.0 | 20.0   | 24.950000    | <br>3.0   | 3.0   | 20.0   | 3.0  | 0.0 | 3.0 | 3.0 | 3.0 | 3.0 | 3.0 |
| 4       | 23.0  | 45.217391 | 13.228607 | 19.0 | 35.5 | 46.0 | 53.50 | 67.0 | 23.0   | 26.304348    | <br>4.0   | 4.0   | 23.0   | 4.0  | 0.0 | 4.0 | 4.0 | 4.0 | 4.0 | 4.0 |

5 rows × 40 columns

## **COMPARISON:**

| Cluster | KM5_size | KM6_size | DBSCAN_size | MS_size | Agg_size |
|---------|----------|----------|-------------|---------|----------|
| -1      | NaN      | NaN      | 18.0        | NaN     | NaN      |
| 0       | 23.0     | 39.0     | 112.0       | 79.0    | 35.0     |
| 1       | 79.0     | 44.0     | 8.9         | 39.0    | 83.0     |
| 2       | 30.0     | 35.0     | 34.0        | 36.0    | 39.0     |
| 3       | 36.0     | 22.0     | 24.0        | 23.0    | 20.0     |
| 4       | 23.0     | 22.0     | 4.0         | 23.0    | 23.0     |
| 5       | NaN      | 38.0     | NaN         | NaN     | NaN      |