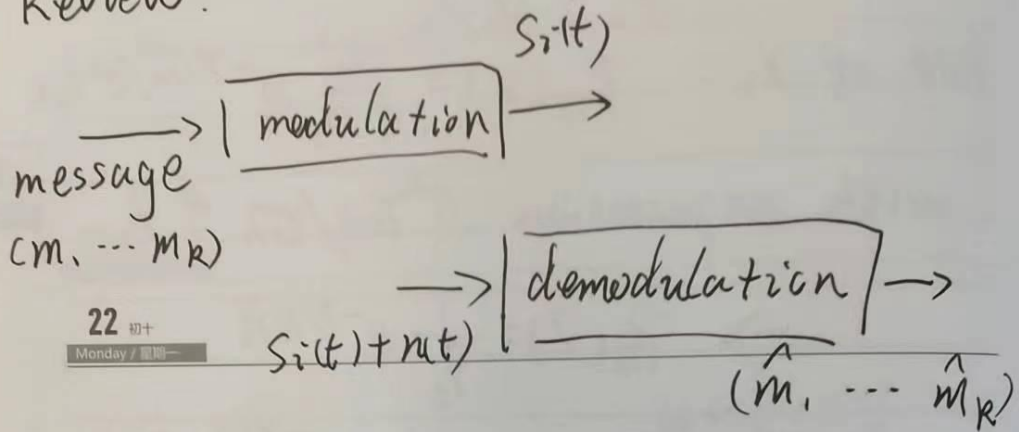
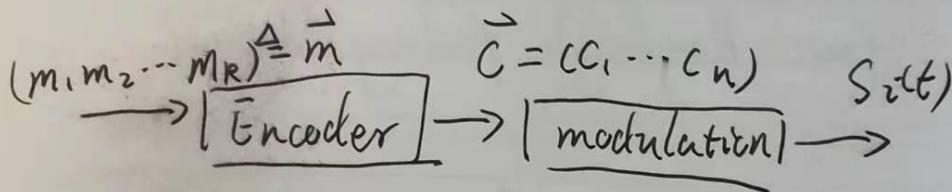


Review:



22 初十

Monday / 星期一

Error:  $m_1, \dots, m_k \neq \hat{m}_1, \dots, \hat{m}_k$ 

23 +

Tuesday / 星期二



$\{\vec{C}_1, \vec{C}_2, \dots, \vec{C}_{2^k}\} \Rightarrow \min_{i=1, \dots, 2^k} \Delta(\vec{\gamma}, \vec{C}_i)$

(Code rate =  $k/n$ )

(Hamming distance  $\neq \Delta(\vec{C}_1, \vec{C}_2)$ )

24 十一

Wednesday / 星期三

$\{\vec{c}_1, \dots, \vec{c}_n\}$  has a  
 A code ~~with~~ min hamming distance  $d$ .  
 if  $d = \min_{a, b} \Delta(\vec{c}_a, \vec{c}_b)$

$\Rightarrow$  Detect  $d-1$  errors, correct  $\lfloor \frac{d-1}{2} \rfloor$  errors <sup>3</sup> MAR

#### 1. Linear block code

$$0+0=0, \quad 0+1=1, \quad 1+1=0,$$

$$0 \times 0 = 0, \quad 0 \times 1 = 0, \quad 1 \times 1 = 1$$

$$\vec{m} G = \vec{c}$$

$$1 \times k \quad k \times n \quad 1 \times n$$

$\uparrow$

Generator Matrix

Special Case:  $G = [I \quad P]$

$$k \times k \quad k \times (n-k)$$

$$\vec{m} G = [\vec{m} \quad \vec{m} P]$$

$$\underbrace{\hspace{1.5cm}}_{\vec{c}}$$

$R_x$ : parity check matrix.  $H = [P^T \ I]$

$$\Rightarrow \vec{m} G H^T = 0. \quad \begin{matrix} (n-k) \times k & \text{cancel} & (n-k) \times (n-k) \\ & & (n-k) \times k \end{matrix}$$

$\Rightarrow$  Correct receiving will pass the check matrix

$$\vec{c} = "1100"$$

$\vec{e} = "0010"$  error vector for the 3rd bit

$$\vec{r} = \vec{c} + \vec{e} = "1110"$$

$$\vec{r} H^T = \vec{c} H^T + \vec{e} H^T = \vec{e} H^T$$

$$\begin{matrix} \text{cancel} & (n-k) & (n-k) \\ (1 \times n) & n \times k & \Rightarrow 1 \times k \end{matrix}$$

Pattern of  $\vec{r} H^T$  ( $\vec{e} H^T$ ) can be used to detect / correct error.

△ Convolution Code.

△ Interleaving

				1	2	3
				愚人节	廿一	廿二
4	5	6	7	8	9	10
清明节	廿四	廿五	廿六	廿七	廿八	廿九
11	12	13	14	15	16	17
三十	三月	初二	初三	初四	初五	初六
18	19	20	21	22	23	24
初七	初八	初九	初十	十一	十二	十三
25	26	27	28	29	30	
十四	十五	十六	十七	十八	十九	

$$\text{AWGN: } \vec{y} = \vec{x} + \vec{n}$$

Thursday / 星期四

Two-dimensional signal. — AWGN

$$\begin{pmatrix} y_1 \\ y_2 \end{pmatrix} = \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} + \begin{pmatrix} n_1 \\ n_2 \end{pmatrix} \quad \text{vector}$$

$$y_1 + jy_2 = x_1 + jx_2 + n_1 + jn_2. \quad \text{baseband.}$$

2 廿一

Friday / 星期五

$$y = x + n. \quad \text{complex.}$$

~~Narrowband~~ transmit signal energy  $|x|^2 = (x_1, x_2) \begin{pmatrix} x_1 \\ x_2 \end{pmatrix}$   
 Narrowband. (flat fading) — two-dimensional.

3 廿二

Saturday / 星期六

$$y = hx + n.$$

↑  
channel gain.

4 清明

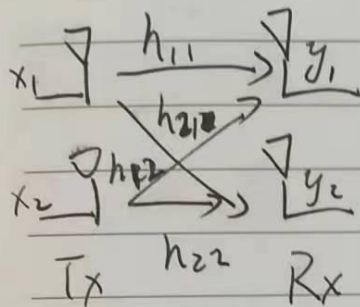
Sunday / 星期日

$$x \rightarrow \boxed{\text{AWGN}} \rightarrow y = x + n$$

$$x \rightarrow \boxed{\text{Flat}} \rightarrow y = hx + n.$$

SISO: Single input Single output

# Δ Narrowband MIMO Model



$$y_1 = h_{11}x_1 + h_{12}x_2 + n_1$$

$$= (h_{11} \ h_{12}) \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} + n_1$$

$$y_2 = h_{21}x_1 + h_{22}x_2 + n_2$$

$$= (h_{21} \ h_{22}) \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} + n_2$$

$$\begin{pmatrix} y_1 \\ y_2 \end{pmatrix} = \begin{pmatrix} h_{11} & h_{12} \\ h_{21} & h_{22} \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} + \begin{pmatrix} n_1 \\ n_2 \end{pmatrix}$$

Suppose  $M_t$  transmit antennas and  $M_r$  receive antennas. channel gain for  $i$ -th transmit antenna to the  $j$ -th receive antenna is  $h_{ji}$

$$\begin{pmatrix} y_1 \\ y_2 \\ \vdots \\ y_{M_r} \end{pmatrix} = \begin{bmatrix} h_{11} & \dots & h_{M_t 1} \\ \vdots & \ddots & \vdots \\ h_{M_r 1} & \dots & h_{M_r M_t} \end{bmatrix} \begin{pmatrix} x_1 \\ x_2 \\ \vdots \\ x_{M_t} \end{pmatrix} + \begin{pmatrix} n_1 \\ n_2 \\ \vdots \\ n_{M_r} \end{pmatrix}$$

$$\vec{y} = H\vec{x} + \vec{n}$$