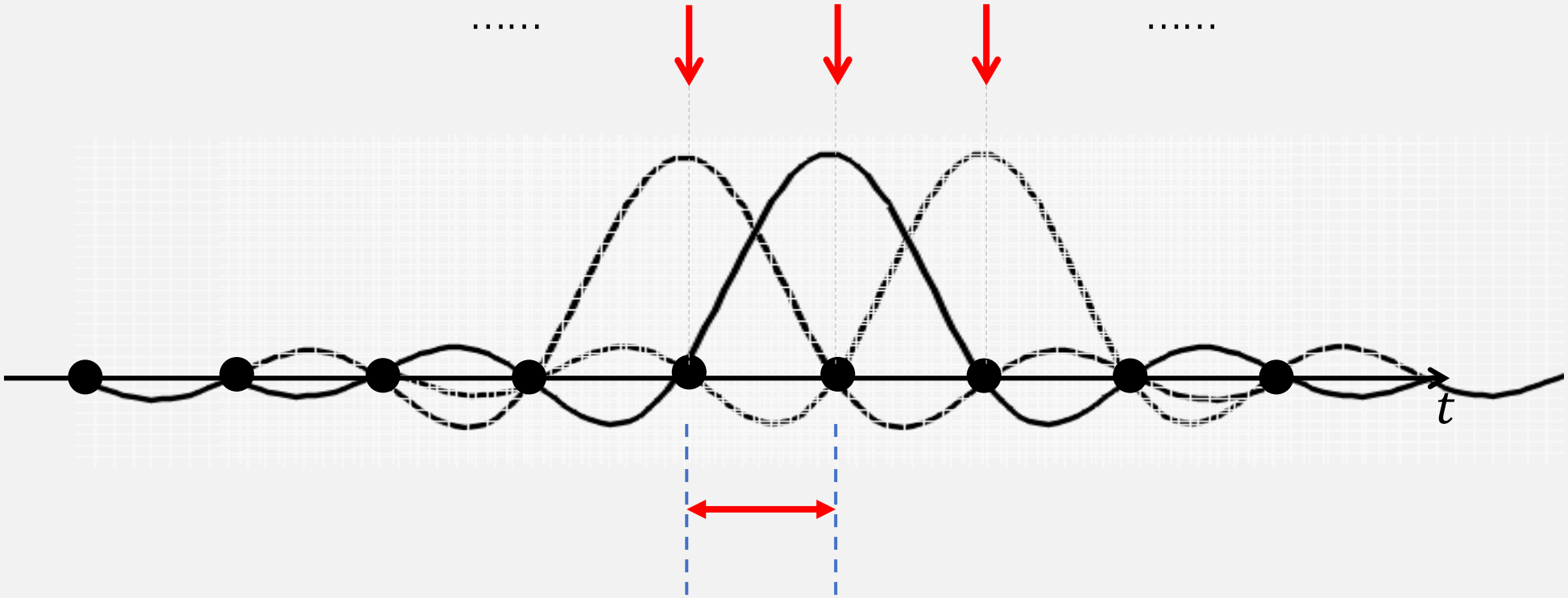
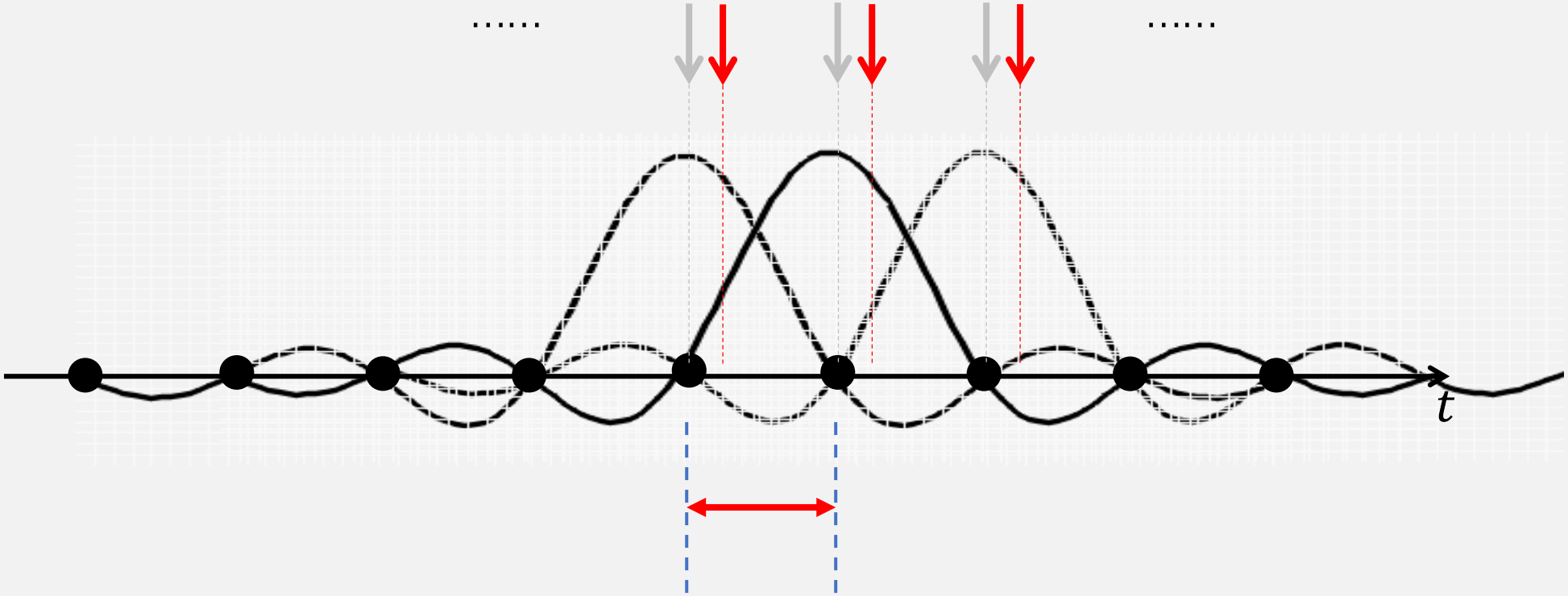
缺点：需要精确的信号同步

Sampling time



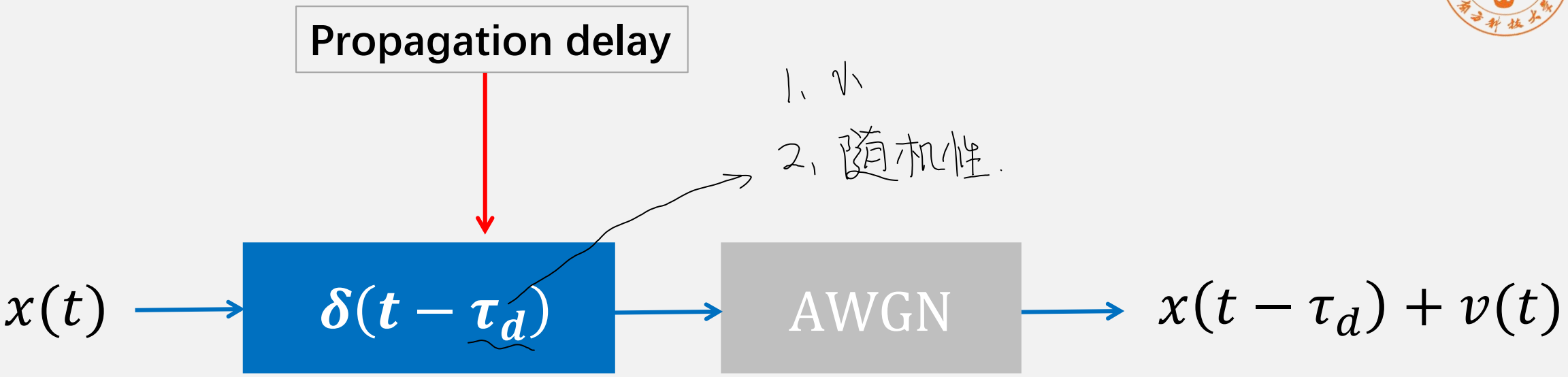
Sampling time



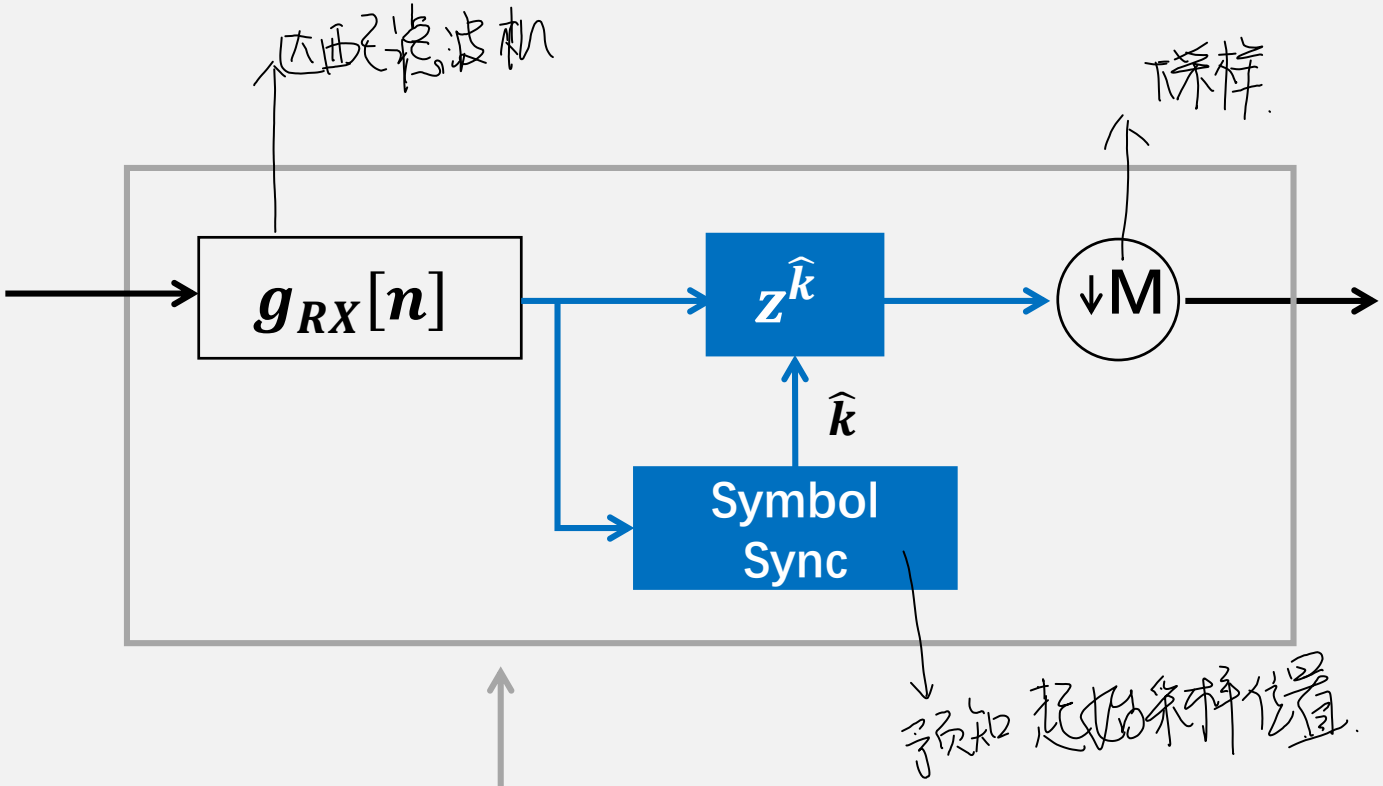
Lab 12 : Symbol Synchronization

主讲人：吴光 博士
Email: wug@sustech.edu.cn

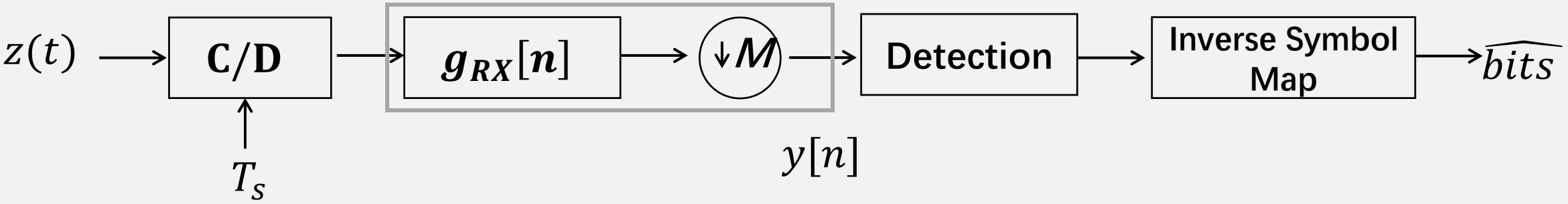
Demo: Symbol synchronization



$$z(t) = \alpha e^{j\varphi} x(t-\tau_d) + v(t)$$


匹配滤波机
下采样
$g_{RX}[n]$
$z^{\hat{k}}$
↓M
$\hat{k}$
Symbol Sync
预知起始采样位置

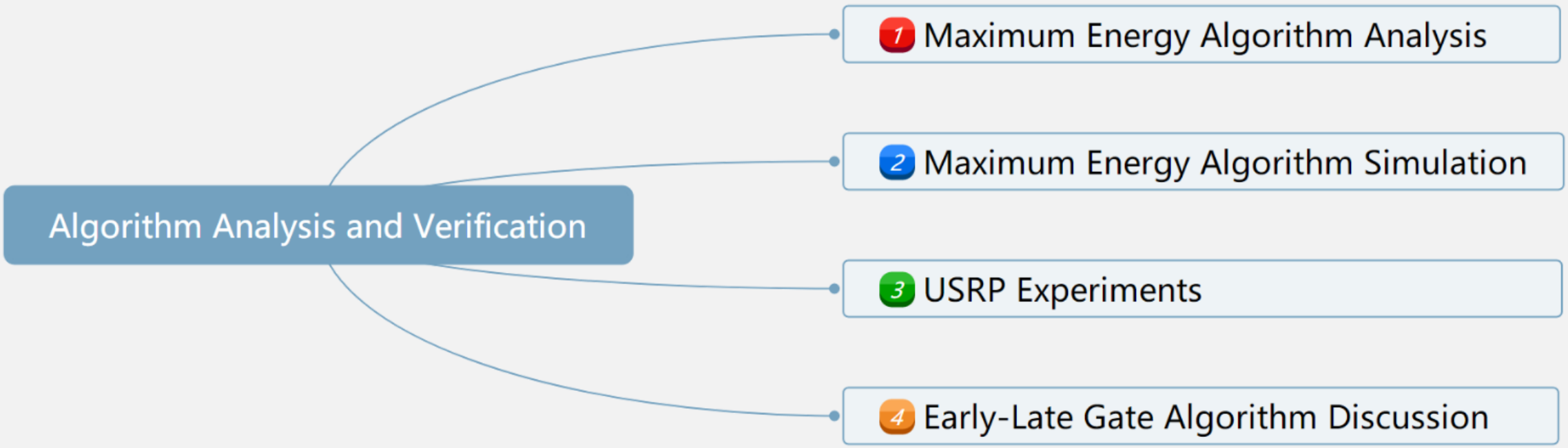
Receiver


$z(t)$
C/D
T_s
$g_{RX}[n]$
↓M
$y[n]$
Detection
Inverse Symbol Map
$\widehat{bits}$

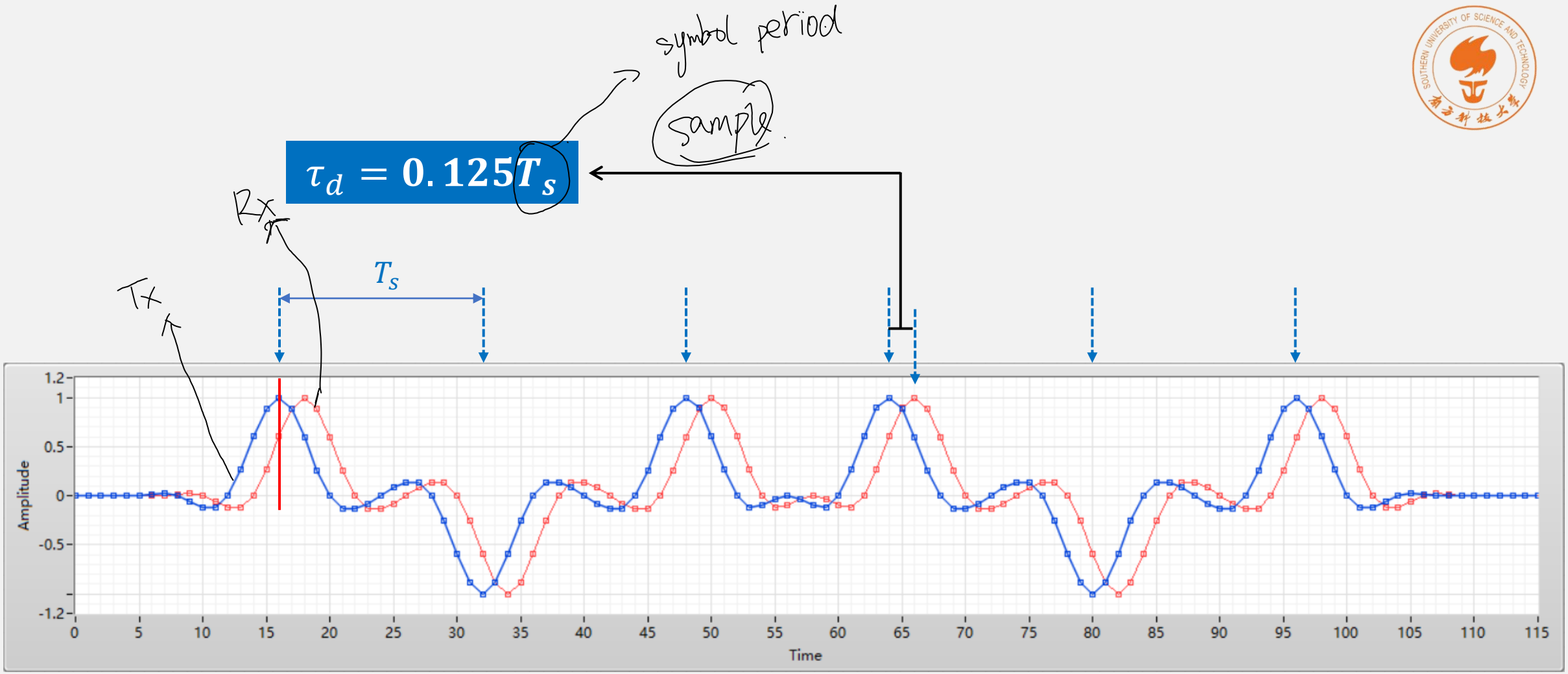
- External synchronization method
- Self-synchronization method

I have an ability to

- Understand the symbol Synchronization
- Design and implement the Maximum Energy Algorithm
- Design and implement the Early-Late gate Algorithm

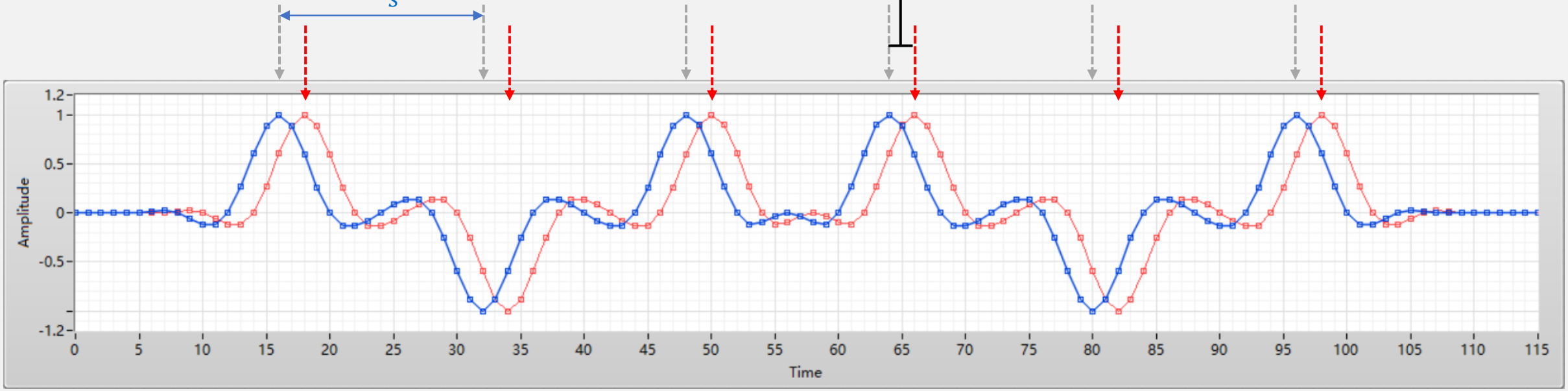

Algorithm Analysis and Verification
1 Maximum Energy Algorithm Analysis
2 Maximum Energy Algorithm Simulation
3 USRP Experiments
4 Early-Late Gate Algorithm Discussion

Maximum Energy Algorithm



The optimal sampling times are $\boldsymbol{kT_s}$

$\tau_d = 0.125T_s$

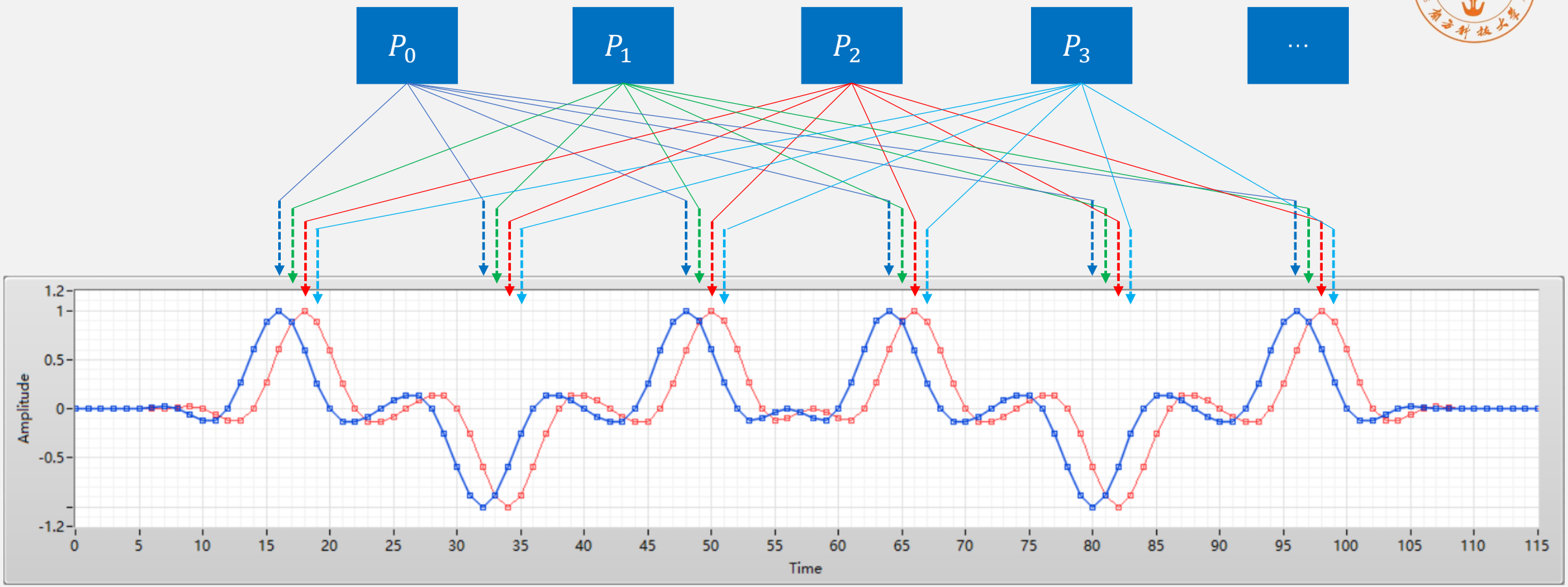


The optimal sampling times are $\boldsymbol{kT_s + \tau_d}$

Maximum Energy Method

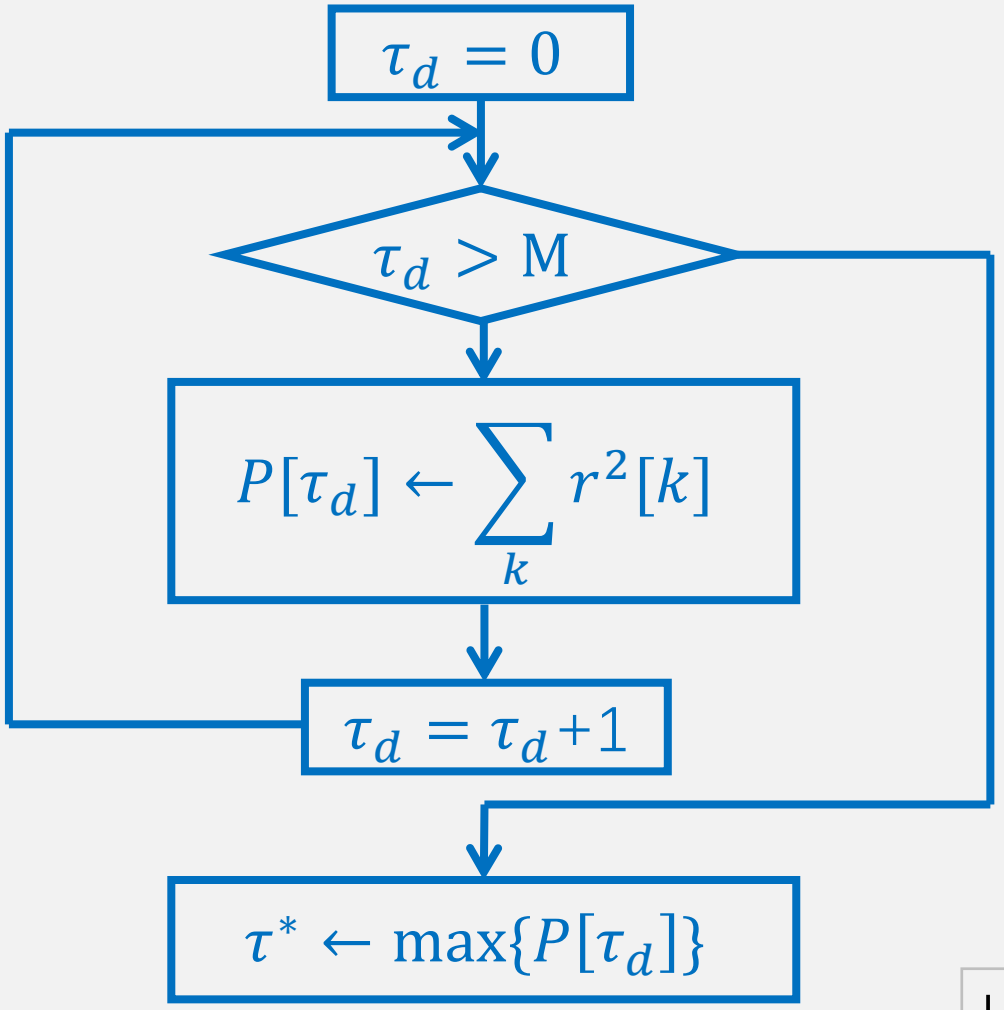
$$\hat{\tau}_d \approx arg\mathbf{max} \sum_k r^2(kT + \tau_d)$$

Attempt to find the sample point that maximizes the average received energy.



The optimal sampling times are $\boldsymbol{kT_s + \tau_d}$

Algorithm Analysis

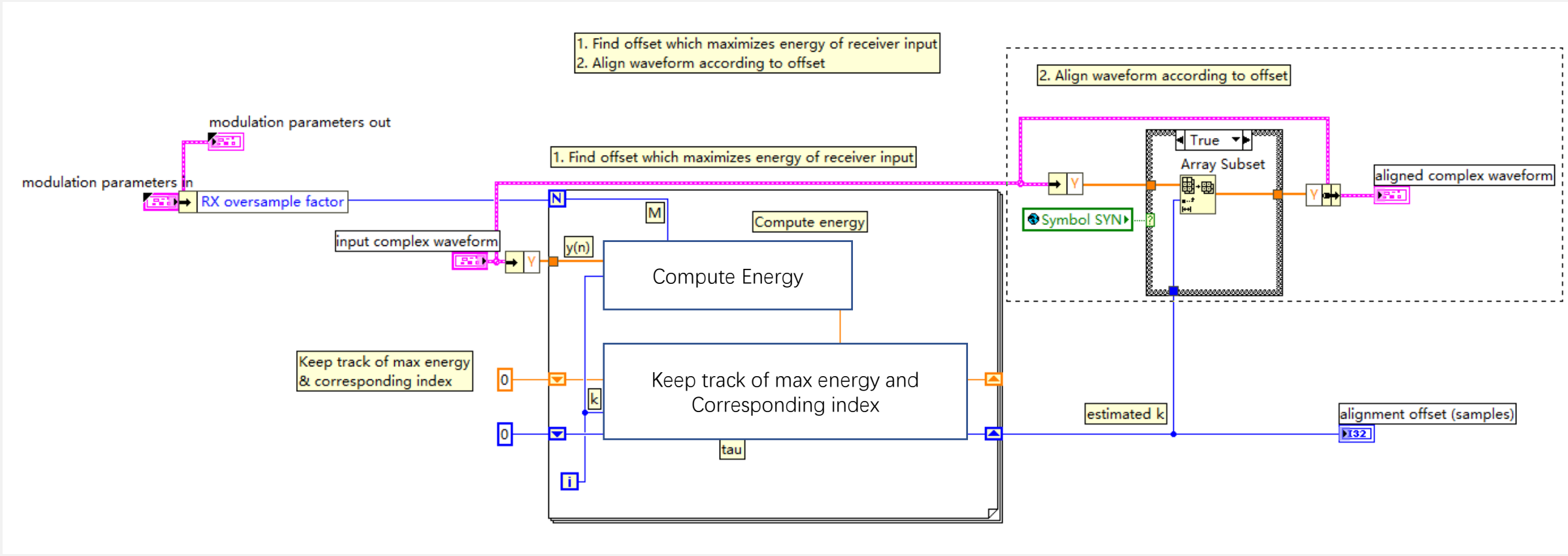


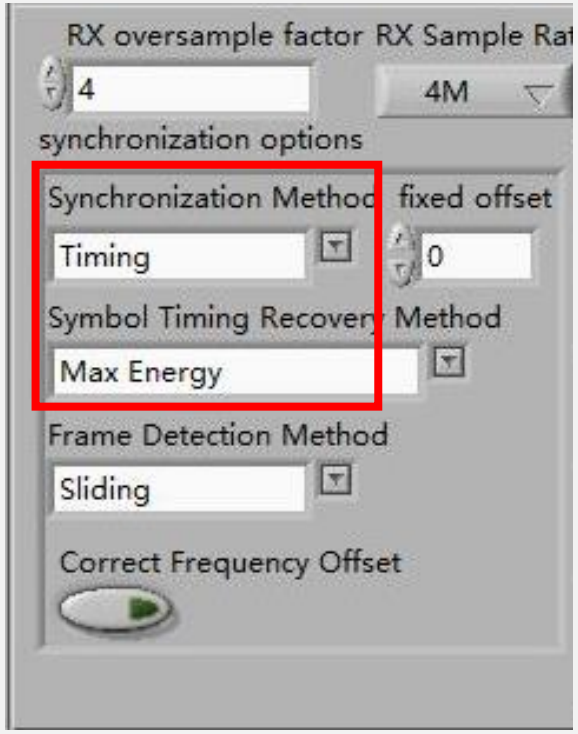
$$\hat{\tau}_d \approx arg\mathbf{max} \sum_i r^2(\tau_d + kT)$$

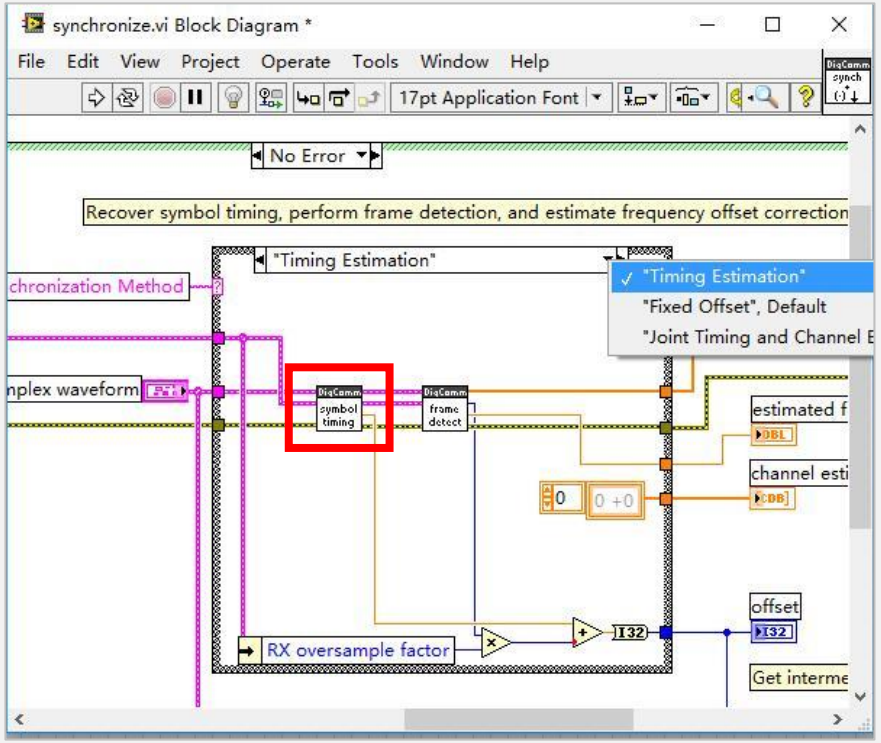
1. Find offset which maximizes energy of receiver input;
2. Align waveform according to offset;

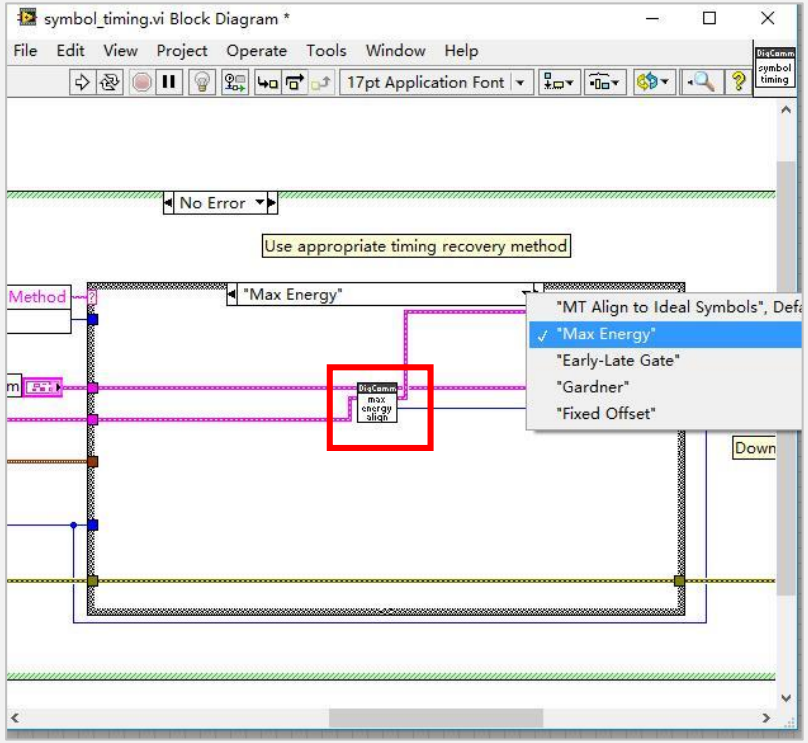
Hints: Use the shift register to save the array $\mathrm{P}[\tau_d]$

Programming for Maximum Energy Algorithm


1. Find offset which maximizes energy of receiver input
2. Align waveform according to offset
2. Align waveform according to offset
modulation parameters out
modulation parameters in
RX oversample factor
1. Find offset which maximizes energy of receiver input
input complex waveform
N
M
Compute energy
y(n)
Compute Energy
Keep track of max energy
& corresponding index
0
0
k
Keep track of max energy and
Corresponding index
tau
i
Y
Symbol SYN
True
Array Subset
Y
Y
aligned complex waveform
estimated k
alignment offset (samples)
I32


RX oversample factor
RX Sample Rat
4
4M
synchronization options
Synchronization Method
fixed offset
Timing
0
Symbol Timing Recovery Method
Max Energy
Frame Detection Method
Sliding
Correct Frequency Offset


synchronize.vi Block Diagram *
File Edit View Project Operate Tools Window Help
17pt Application Font
No Error
Recover symbol timing, perform frame detection, and estimate frequency offset correction
"Timing Estimation"
"Timing Estimation"
"Fixed Offset", Default
"Joint Timing and Channel E
chronization Method
nplex waveform
symbol timing
frame detect
estimated f
channel esti
offset
RX oversample factor
Get interme


symbol_timing.vi Block Diagram *
File Edit View Project Operate Tools Window Help
17pt Application Font
No Error
Use appropriate timing recovery method
Method
"Max Energy"
"MT Align to Ideal Symbols", Defa
"Max Energy"
"Early-Late Gate"
"Gardner"
"Fixed Offset"
max energy align
Down

Analysis for Maximum Energy Algorithm

$$z(t) = \alpha e^{j\phi}\sqrt{E_x}\sum_m s[m]g_{tx}(t - mT - \tau_d) + v(t)$$

$$y[n] = h\sum_m s[m]g\big((n-m)T - \tau_d\big) + v[n]$$

$$z(t) = \alpha e^{j\phi}\sqrt{E_x}\sum_m s[m]g_{tx}(t - mT - \tau_d) + v(t)$$

$$y[n] = h\sum_m s[m]g\big((n-m)T - \tau_d\big) + v[n]$$

$$y[n] = \underbrace{hs[n]g(\tau_d)}_{\text{理想值}} + \underbrace{h\sum_{m\neq n} s[m]g\big((n-m)T-\tau_d\big)}_{\text{ISI}} + \underbrace{v[n]}_{\text{噪声}}$$

$$y[n] = h\sum_{m} s[m]g\big((n-m)T-\tau_d\big) + v[n]$$

$$y(t) = h \sum_{m=-\infty}^{+\infty} s[m]g(t - mT - \tau_d) + v(t)$$

$$J(\tau) = E[|y(nT + \tau)|^2] = |h|^2 \sum_{m=-\infty}^{+\infty} |g(mT + \tau - \tau_d)|^2 + N_o$$

$$y(t) = h \sum_{m=-\infty}^{+\infty} s[m]g(t - mT - \tau_d) + v(t)$$

$$J(\tau) = E[|y(nT + \tau)|^2] = |h|^2 \sum_{m=-\infty}^{+\infty} |g(mT + \tau - \tau_d)|^2 + N_o$$

$$E[|y(nT+\tau)|^2] = |h|^2 \sum_{m=-\infty}^{+\infty} \left|g\left(mT+\tau_{frac}-\hat{\tau}_{frac}\right)\right|^2 + N_o$$

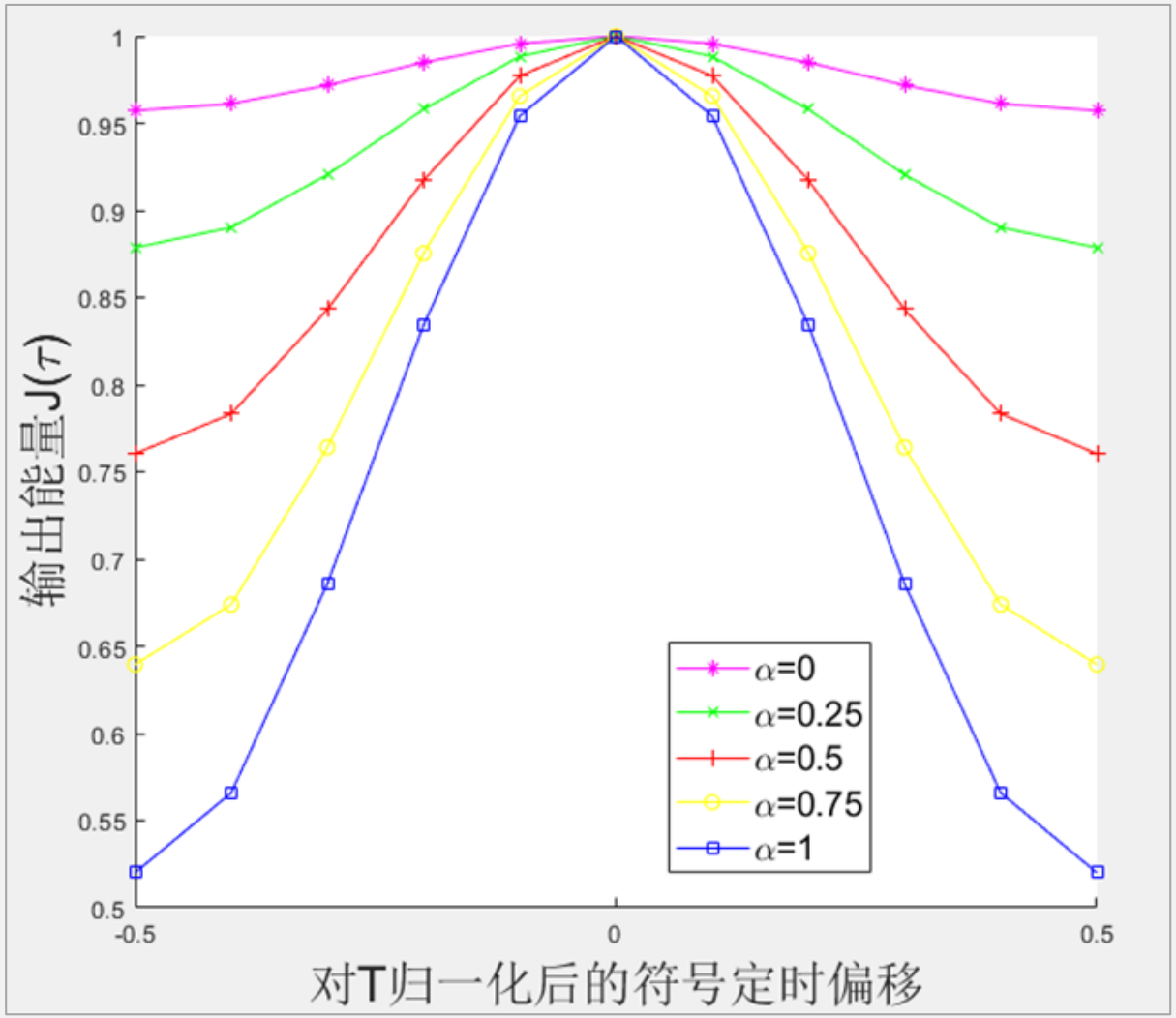
$dT + \tau_{frac}$ $\hat{d}T + \hat{\tau}_{frac}$

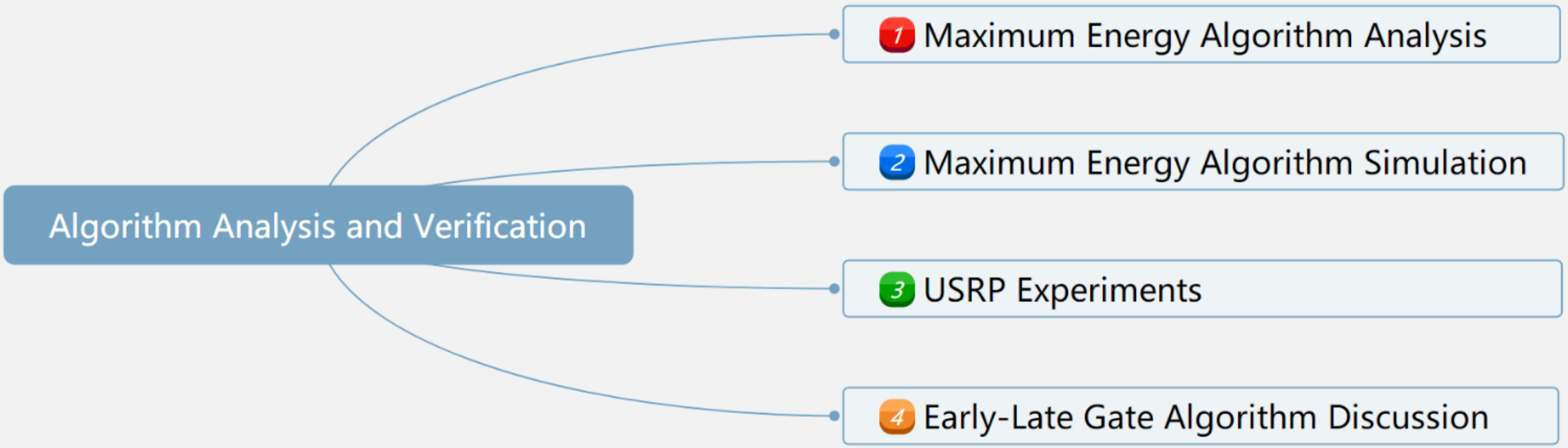
$$J(\tau) = E[|y(nT+\tau)|^2] = |h|^2 \sum_{m=-\infty}^{+\infty} |g(mT+\tau-\tau_d)|^2 + N_o$$

$$E[|y(nT+\tau)|^2] = |h|^2 \sum_{m=-\infty}^{+\infty} \left|g\left(mT+\tau_{frac}-\hat{\tau}_{frac}\right)\right|^2 + N_o$$

$$\hat{\tau}_d = \arg\max_{\tau\in[0,T)} J(\tau)$$

$$E[|y(nT+\tau)|^2] \leq |h|^2|g(0)|^2 + N_o$$


输出能量J(τ)
对T归一化后的符号定时偏移
1
0.95
0.9
0.85
0.8
0.75
0.7
0.65
0.6
0.55
0.5
-0.5
0
0.5
α=0
α=0.25
α=0.5
α=0.75
α=1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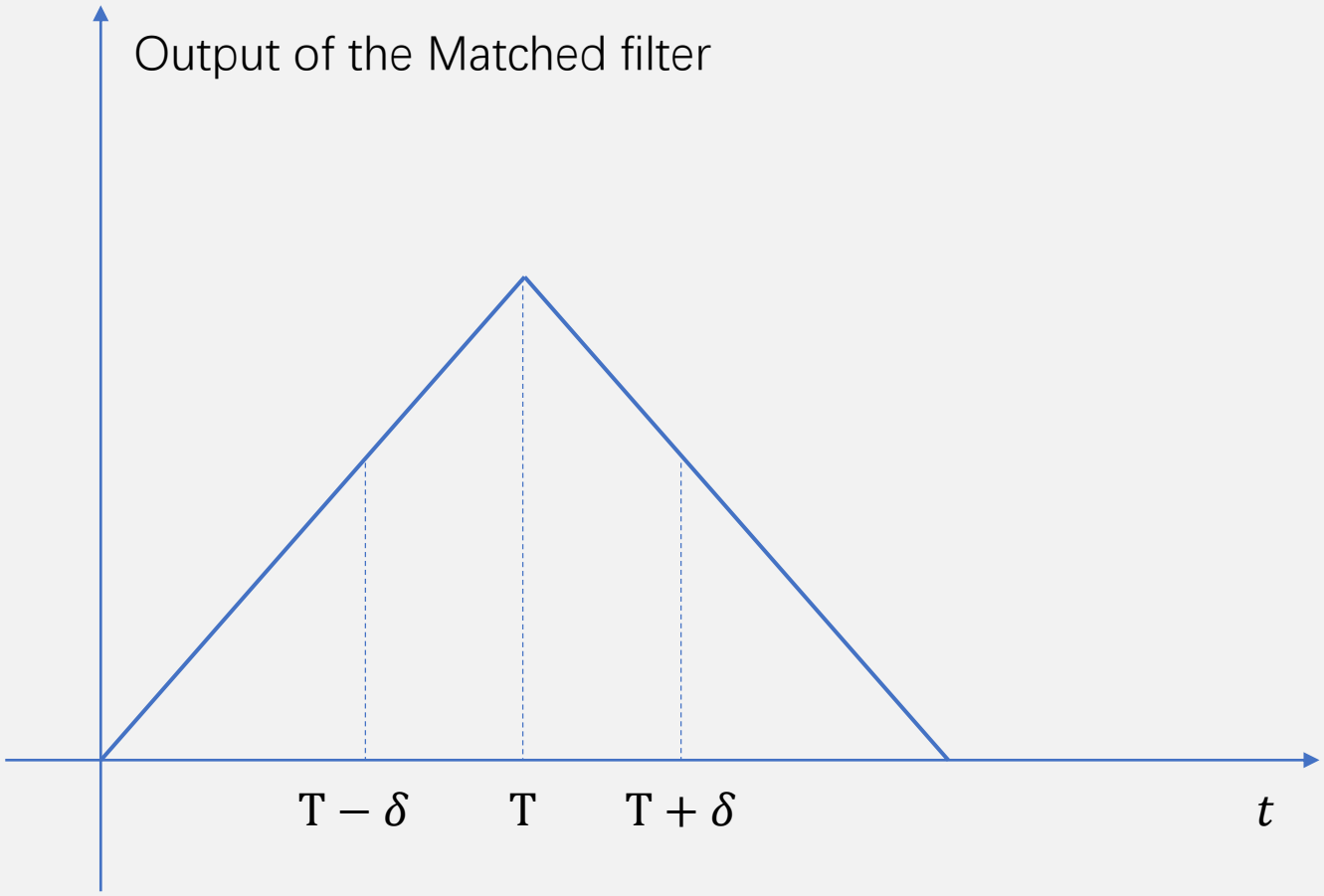
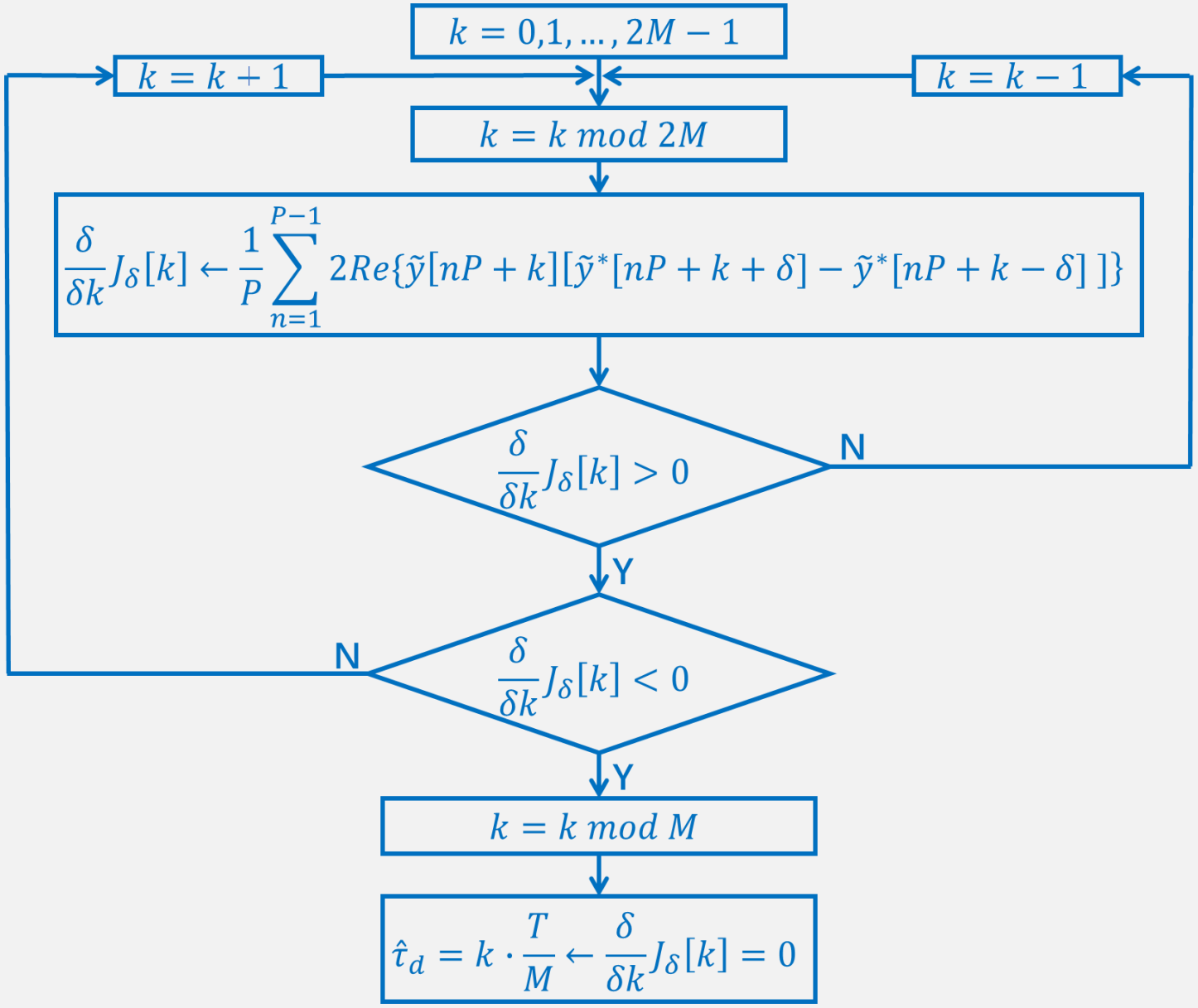
Early-Late Gate Algorithm


Output of the Matched filter
T − δ
T
T + δ
t

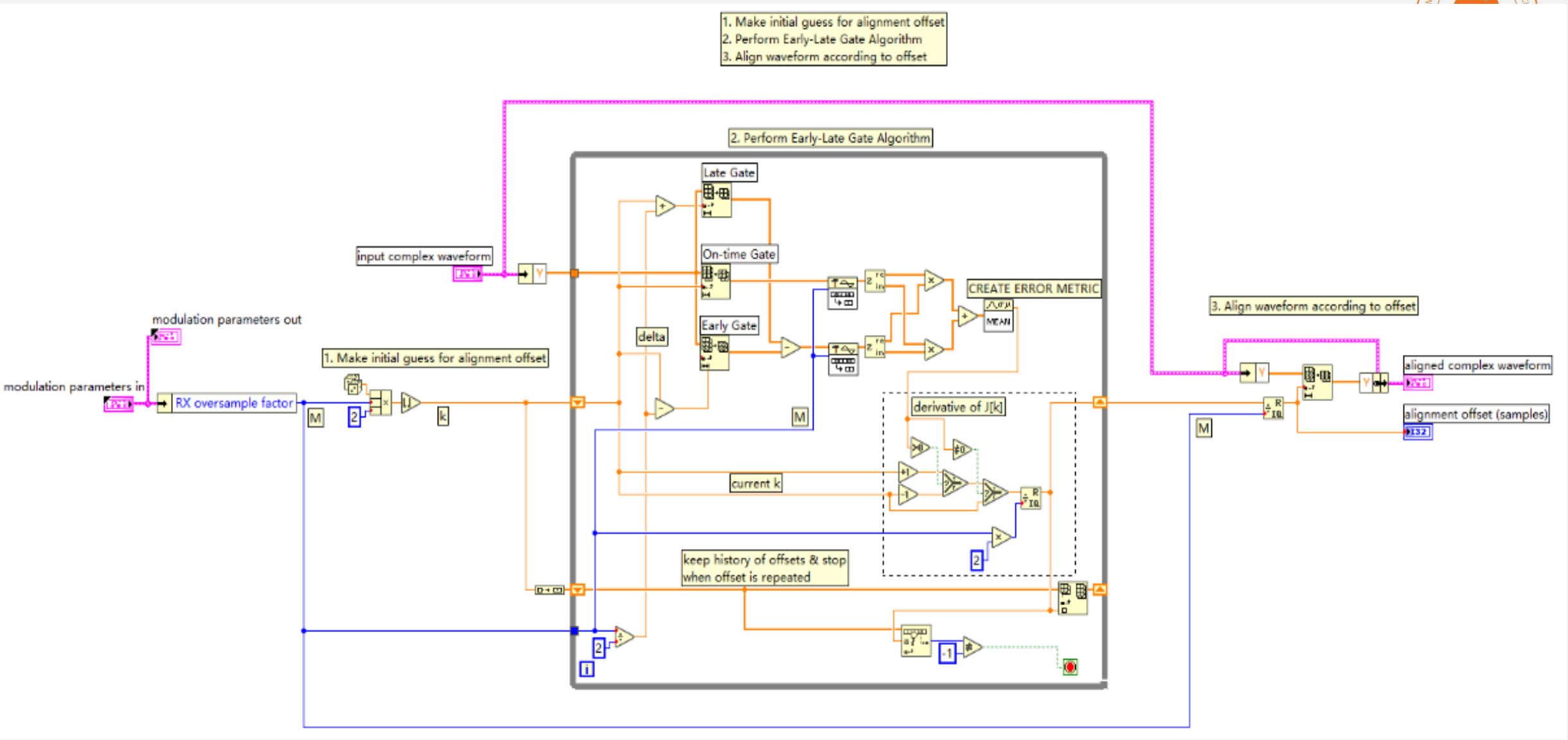
$$\frac{\delta}{\delta k}J_{\delta}[k] \cong \frac{1}{P}\sum_{n=1}^{P-1} 2Re\{\tilde{y}[nP+k][\tilde{y}^{*}[nP+k+\delta]-\tilde{y}^{*}[nP+k-\delta]\ ]\}$$

参考文献

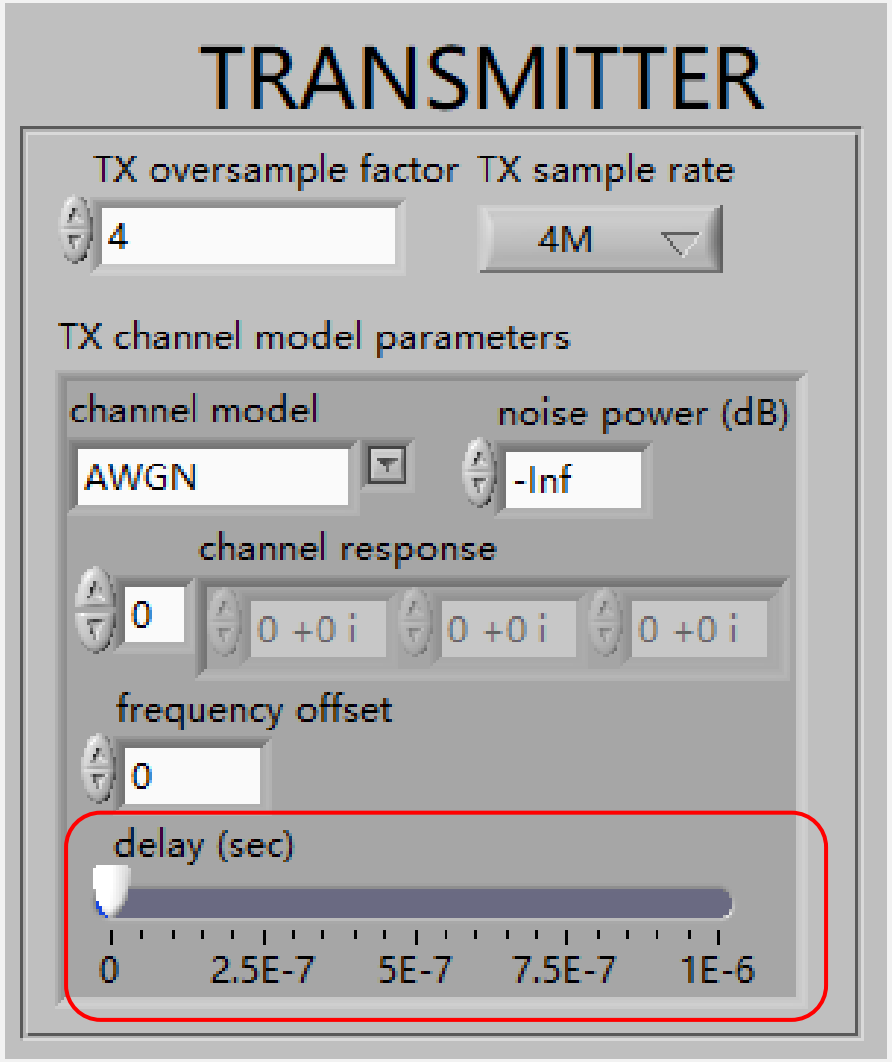
$$\frac{\delta}{\delta k}J_{\delta}[k] = 0$$

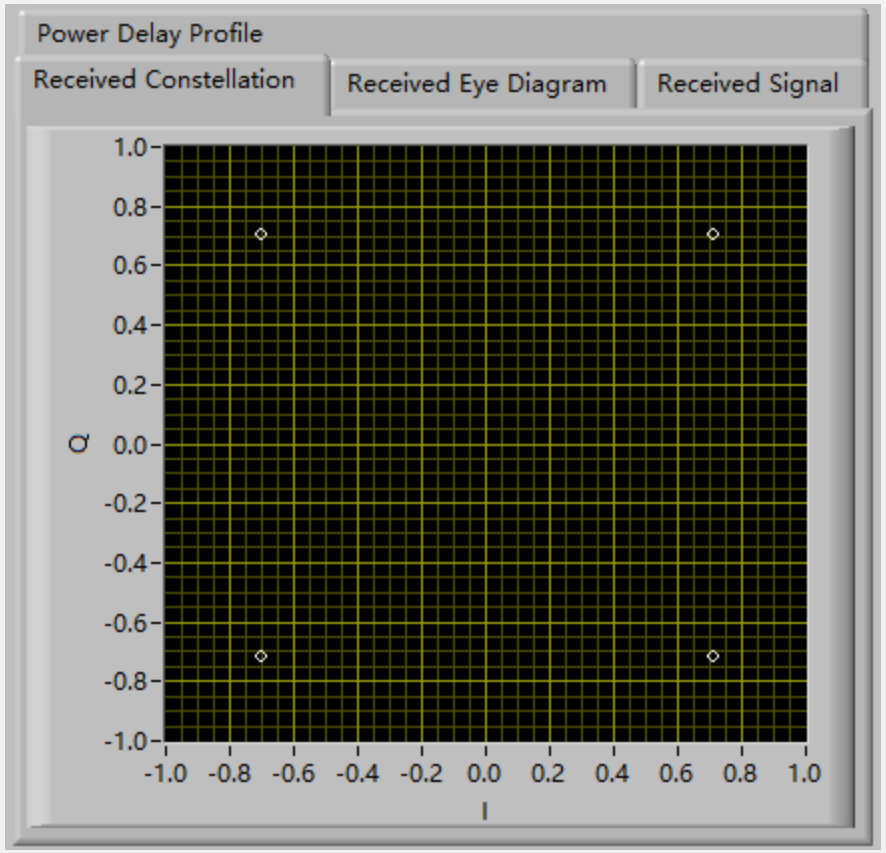

$k = 0,1,\ldots,2M-1$
$k = k+1$
$k = k-1$
$k = k \bmod 2M$
$\frac{\delta}{\delta k} J_\delta[k] \leftarrow \frac{1}{P}\sum_{n=1}^{P-1} 2Re\{\tilde{y}[nP+k][\tilde{y}^*[nP+k+\delta] - \tilde{y}^*[nP+k-\delta]\ ]\}$
$\frac{\delta}{\delta k} J_\delta[k] > 0$
N
Y
$\frac{\delta}{\delta k} J_\delta[k] < 0$
N
Y
$k = k \bmod M$
$\hat{\tau}_d = k \cdot \frac{T}{M} \leftarrow \frac{\delta}{\delta k} J_\delta[k] = 0$

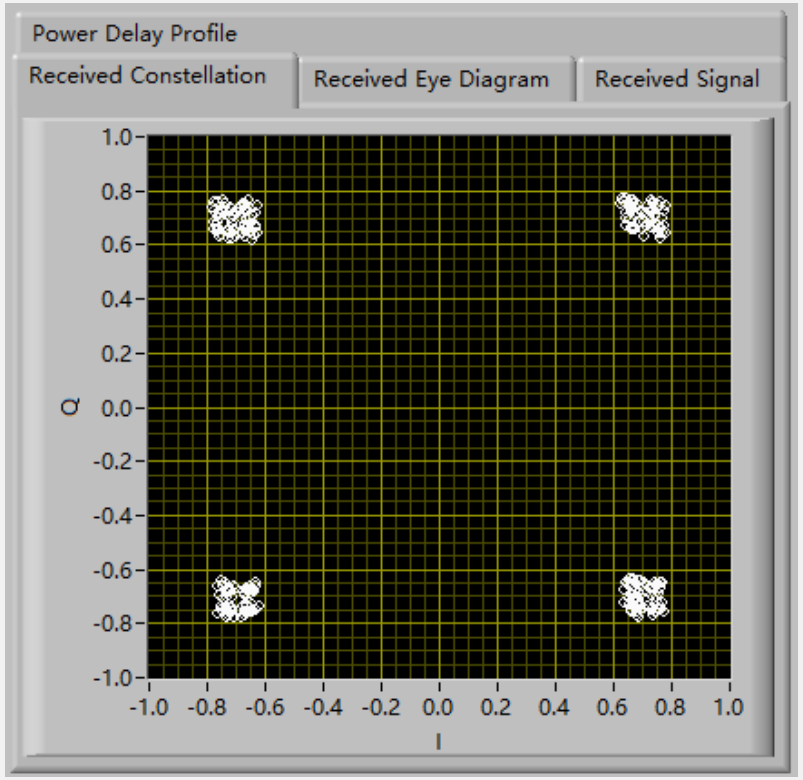
Programming for Early-Late Gate Algorithm

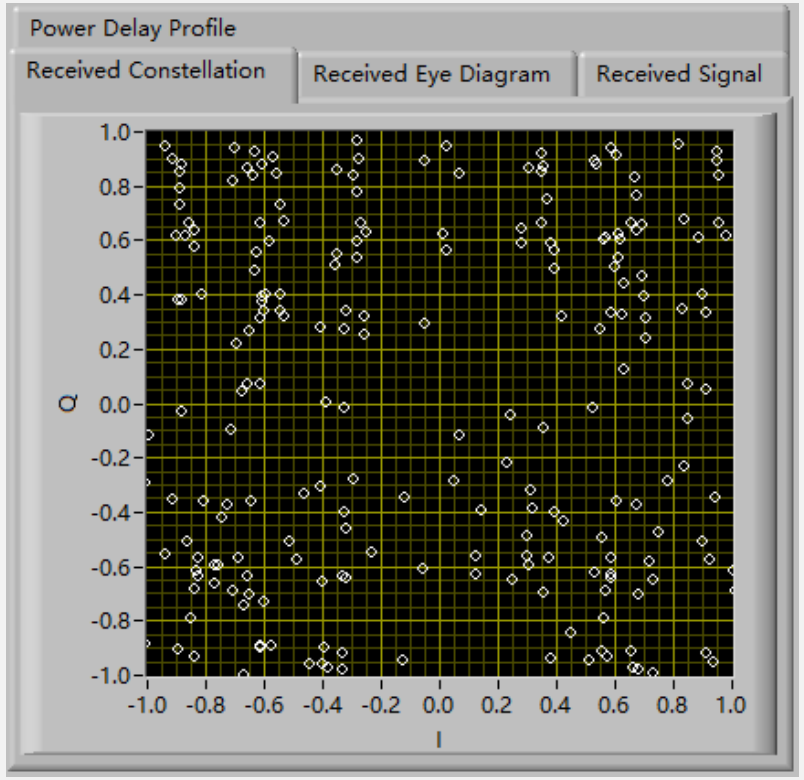

1. Make initial guess for alignment offset
2. Perform Early-Late Gate Algorithm
3. Align waveform according to offset
2. Perform Early-Late Gate Algorithm
Late Gate
On-time Gate
Early Gate
delta
CREATE ERROR METRIC
MEAN
derivative of J[k]
current k
keep history of offsets & stop when offset is repeated
input complex waveform
modulation parameters out
modulation parameters in
RX oversample factor
1. Make initial guess for alignment offset
3. Align waveform according to offset
aligned complex waveform
alignment offset (samples)
M
k
i

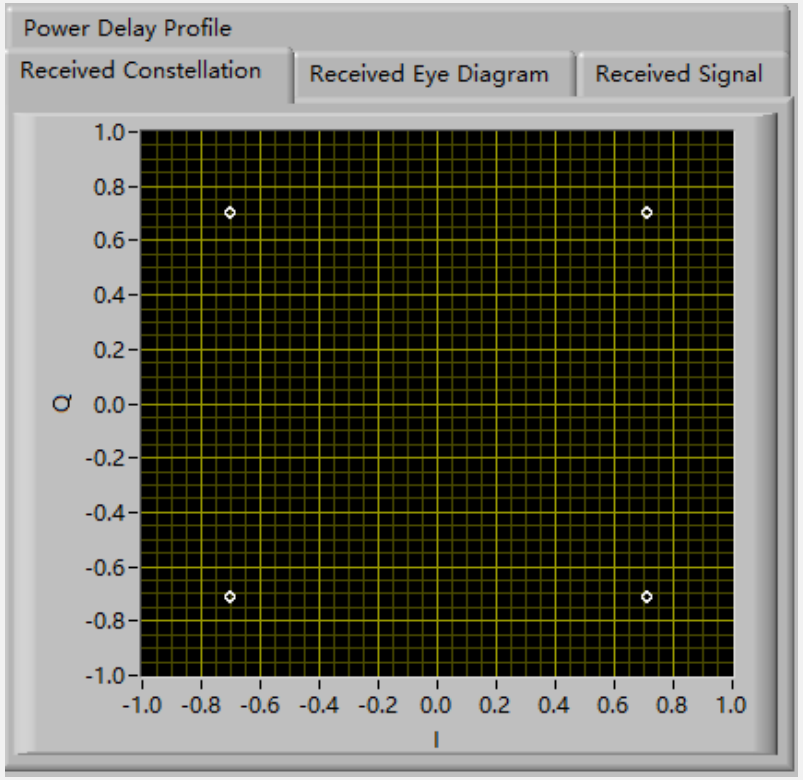
System Testing

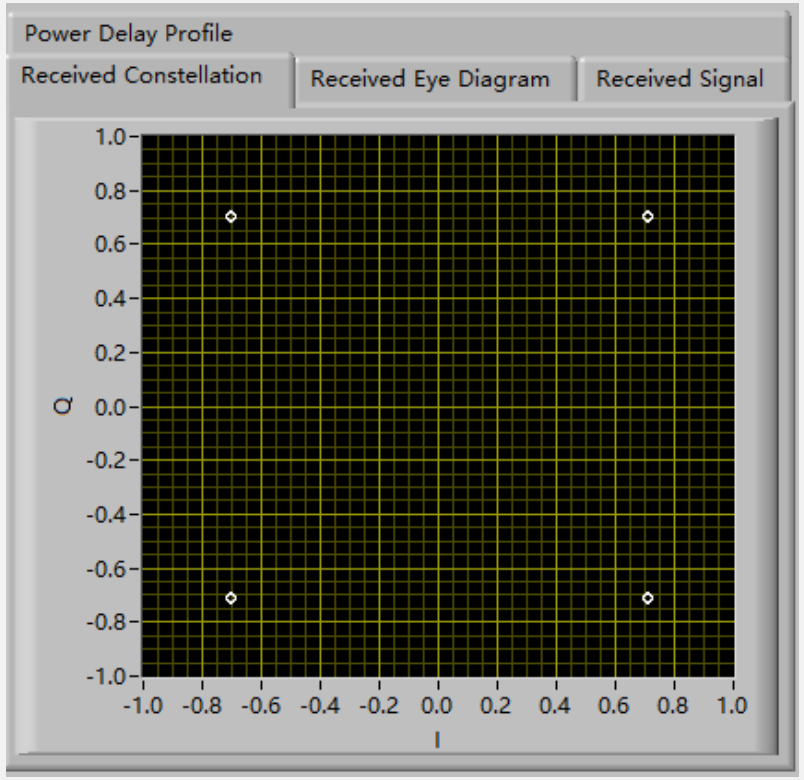

TRANSMITTER
TX oversample factor
4
TX sample rate
4M
TX channel model parameters
channel model
AWGN
noise power (dB)
-Inf
channel response
0
0 +0 i
0 +0 i
0 +0 i
frequency offset
0
delay (sec)
0
2.5E-7
5E-7
7.5E-7
1E-6

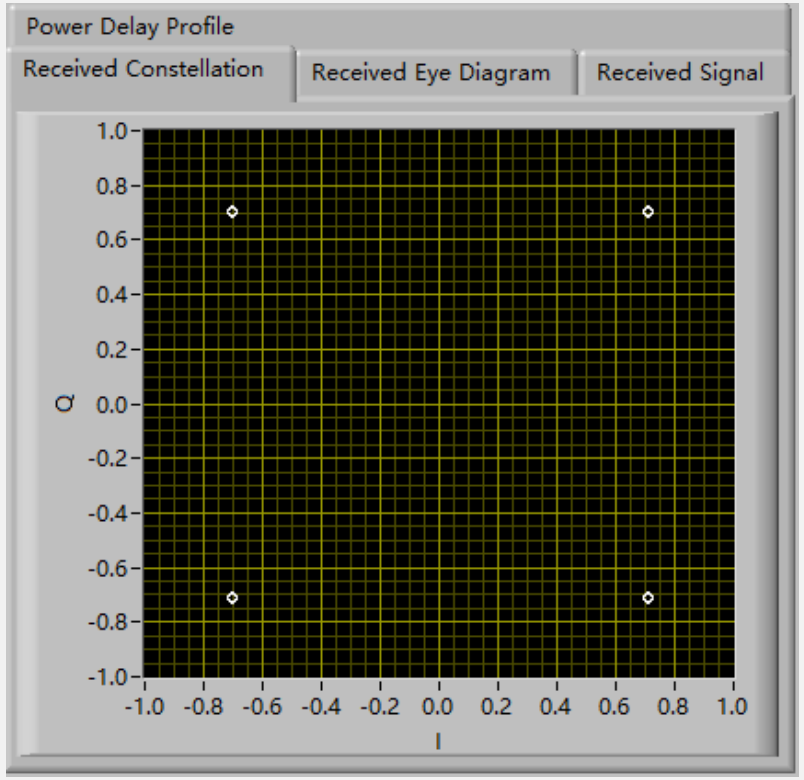

Power Delay Profile
Received Constellation
Received Eye Diagram
Received Signal
1.0
0.8
0.6
0.4
0.2
0.0
-0.2
-0.4
-0.6
-0.8
-1.0
Q
-1.0 -0.8 -0.6 -0.4 -0.2 0.0 0.2 0.4 0.6 0.8 1.0
I

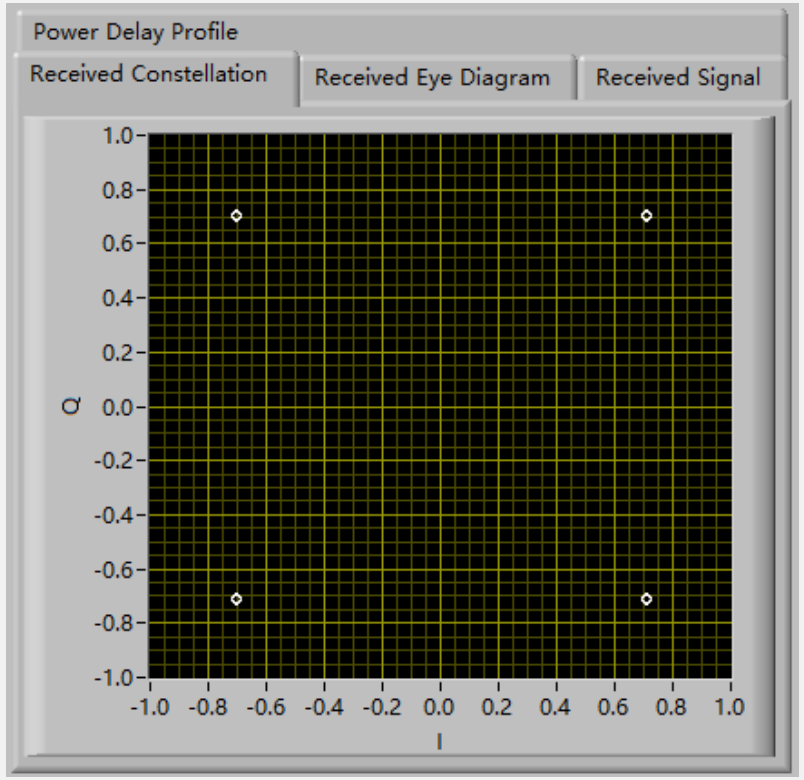

Power Delay Profile
Received Constellation
Received Eye Diagram
Received Signal
1.0
0.8
0.6
0.4
0.2
0.0
-0.2
-0.4
-0.6
-0.8
-1.0
Q
-1.0 -0.8 -0.6 -0.4 -0.2 0.0 0.2 0.4 0.6 0.8 1.0
I


Power Delay Profile
Received Constellation
Received Eye Diagram
Received Signal
1.0
0.8
0.6
0.4
0.2
0.0
-0.2
-0.4
-0.6
-0.8
-1.0
Q
-1.0 -0.8 -0.6 -0.4 -0.2 0.0 0.2 0.4 0.6 0.8 1.0
I

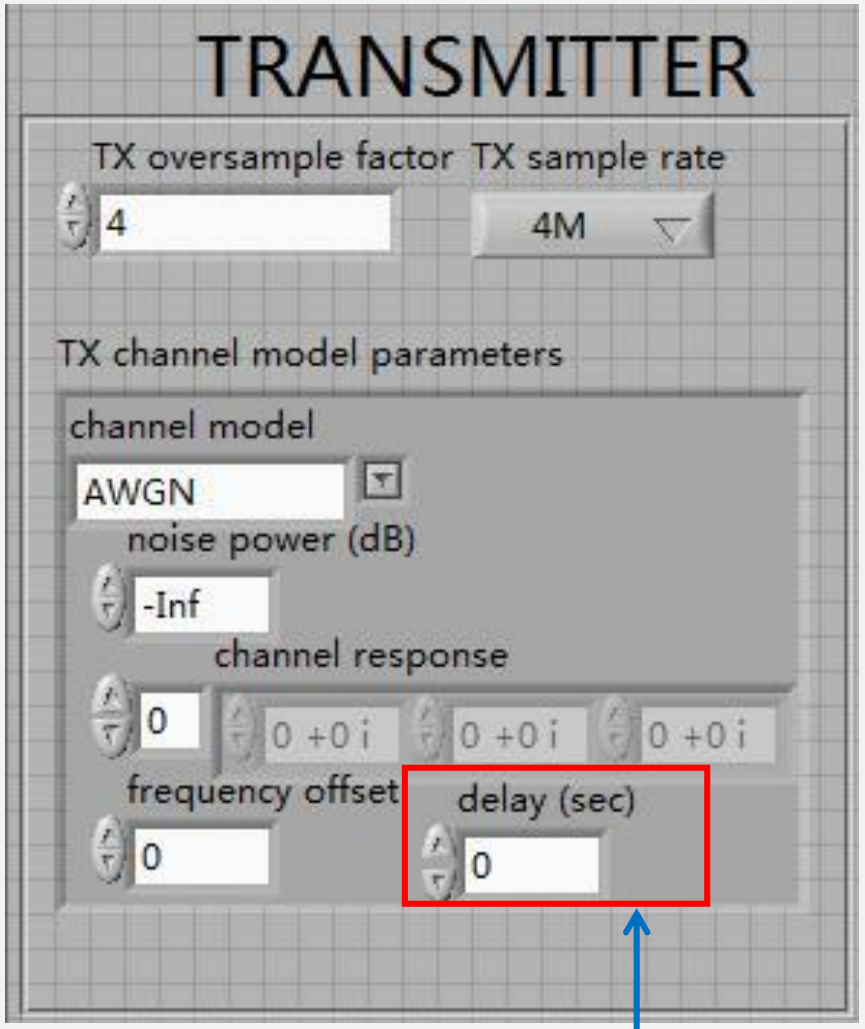

Power Delay Profile
Received Constellation
Received Eye Diagram
Received Signal
1.0
0.8
0.6
0.4
0.2
0.0
-0.2
-0.4
-0.6
-0.8
-1.0
Q
-1.0 -0.8 -0.6 -0.4 -0.2 0.0 0.2 0.4 0.6 0.8 1.0
I


Power Delay Profile
Received Constellation
Received Eye Diagram
Received Signal
1.0
0.8
0.6
0.4
0.2
0.0
-0.2
-0.4
-0.6
-0.8
-1.0
Q
-1.0 -0.8 -0.6 -0.4 -0.2 0.0 0.2 0.4 0.6 0.8 1.0
I

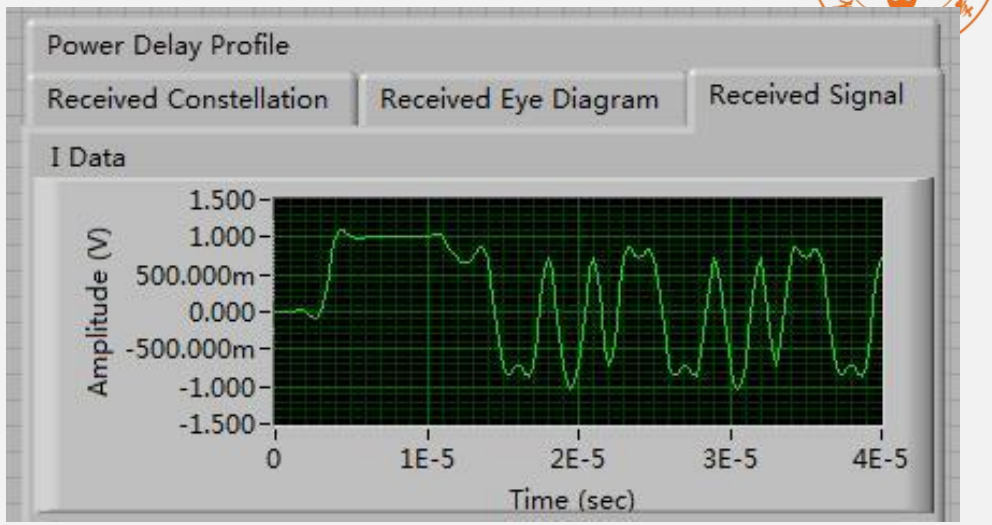

Power Delay Profile
Received Constellation
Received Eye Diagram
Received Signal
1.0
0.8
0.6
0.4
0.2
0.0
-0.2
-0.4
-0.6
-0.8
-1.0
Q
-1.0 -0.8 -0.6 -0.4 -0.2 0.0 0.2 0.4 0.6 0.8 1.0
I

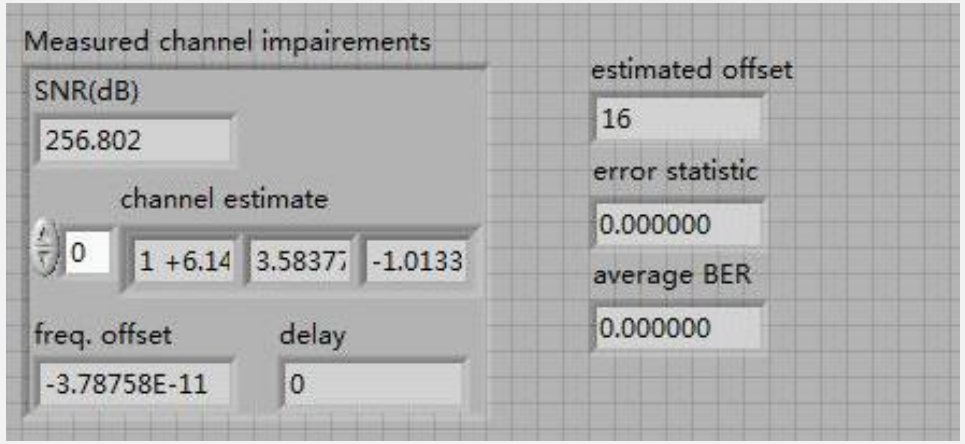

Power Delay Profile
Received Constellation
Received Eye Diagram
Received Signal
1.0
0.8
0.6
0.4
0.2
0.0
-0.2
-0.4
-0.6
-0.8
-1.0
Q
-1.0 -0.8 -0.6 -0.4 -0.2 0.0 0.2 0.4 0.6 0.8 1.0
I

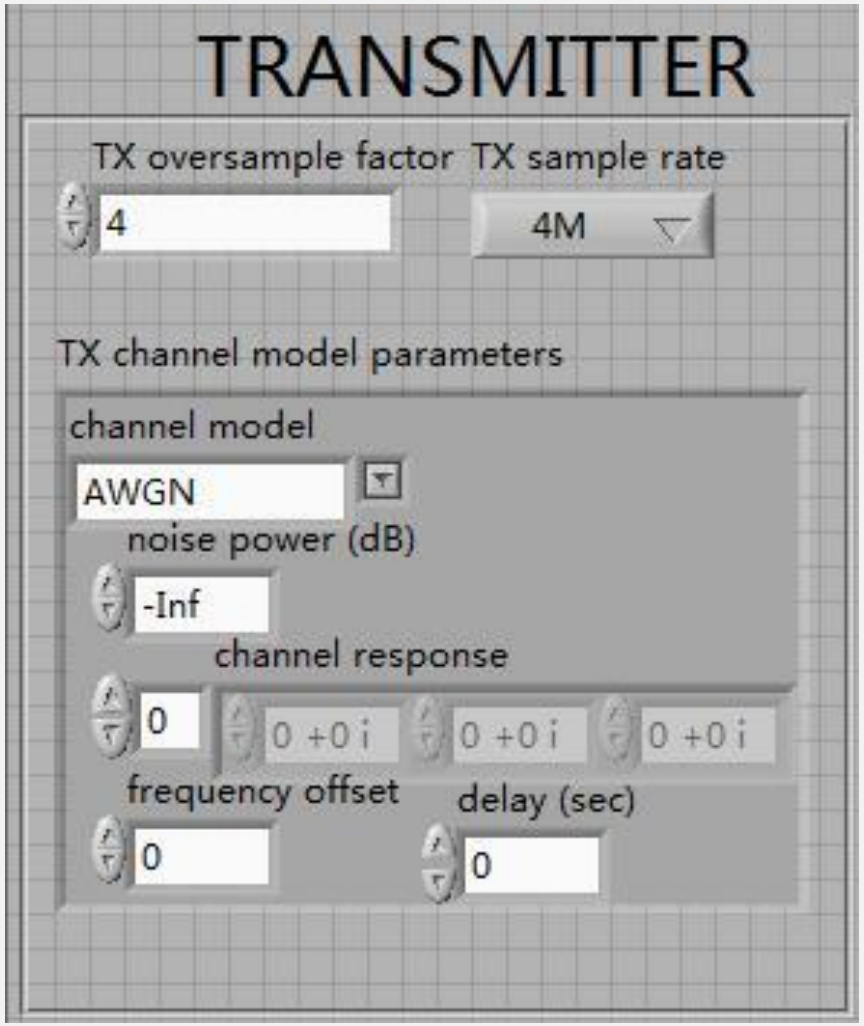
Accuracy Analysis

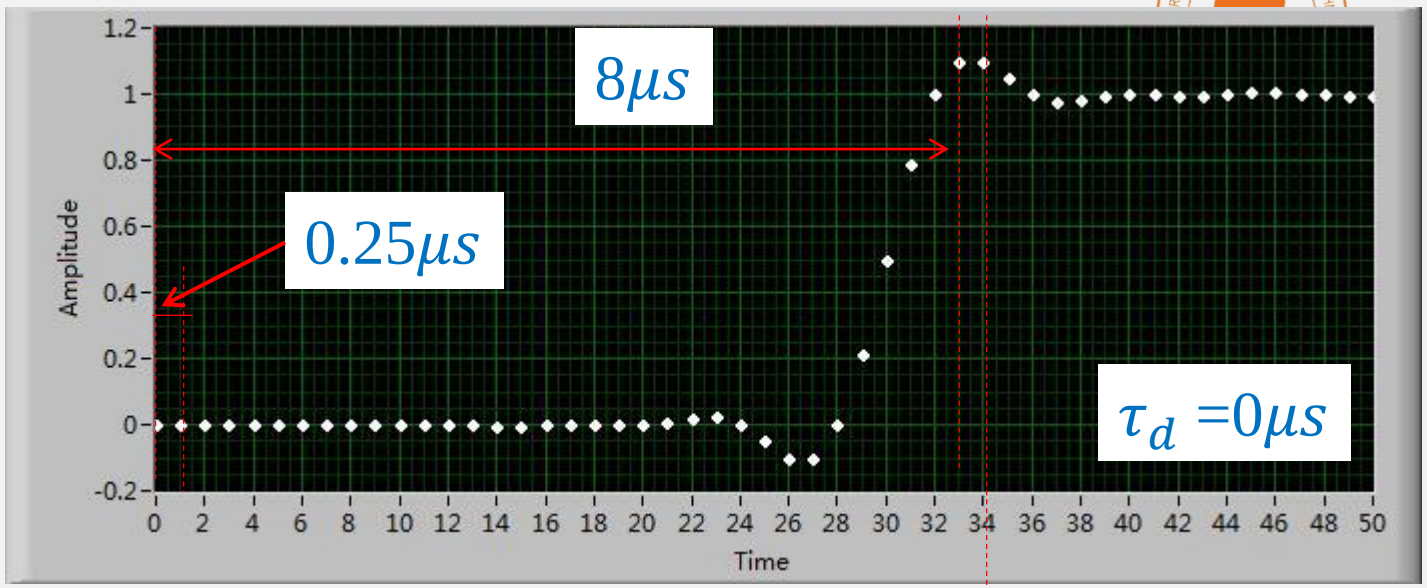


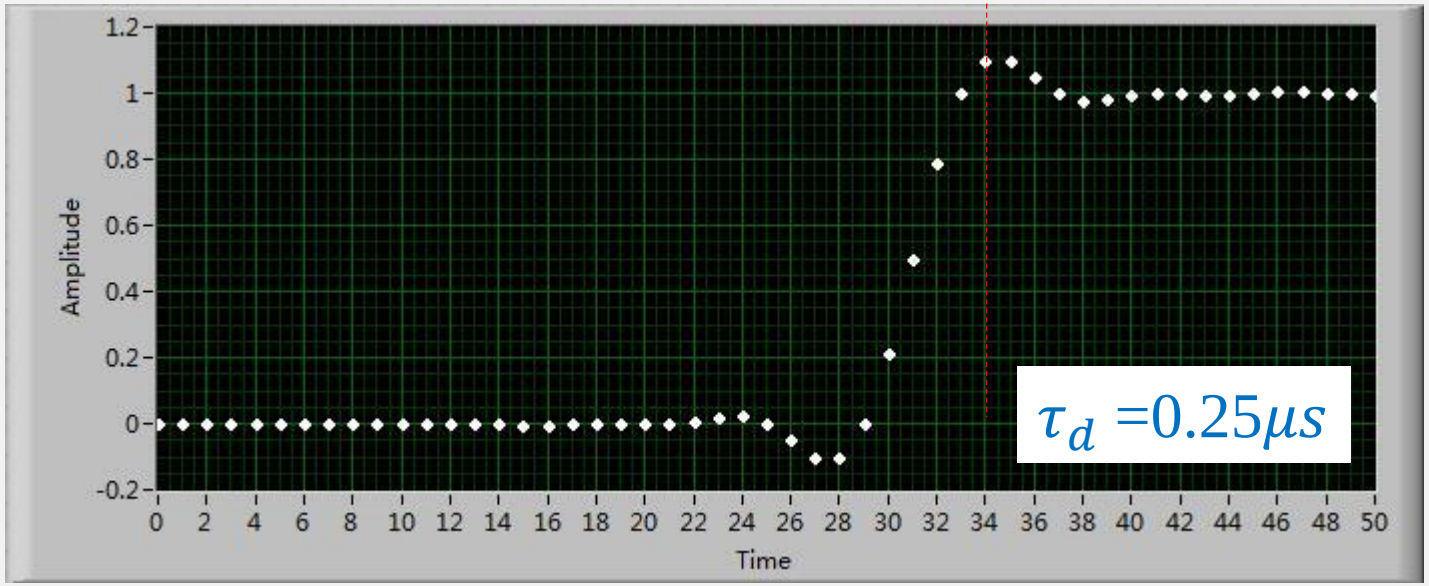
Set the propagation delay

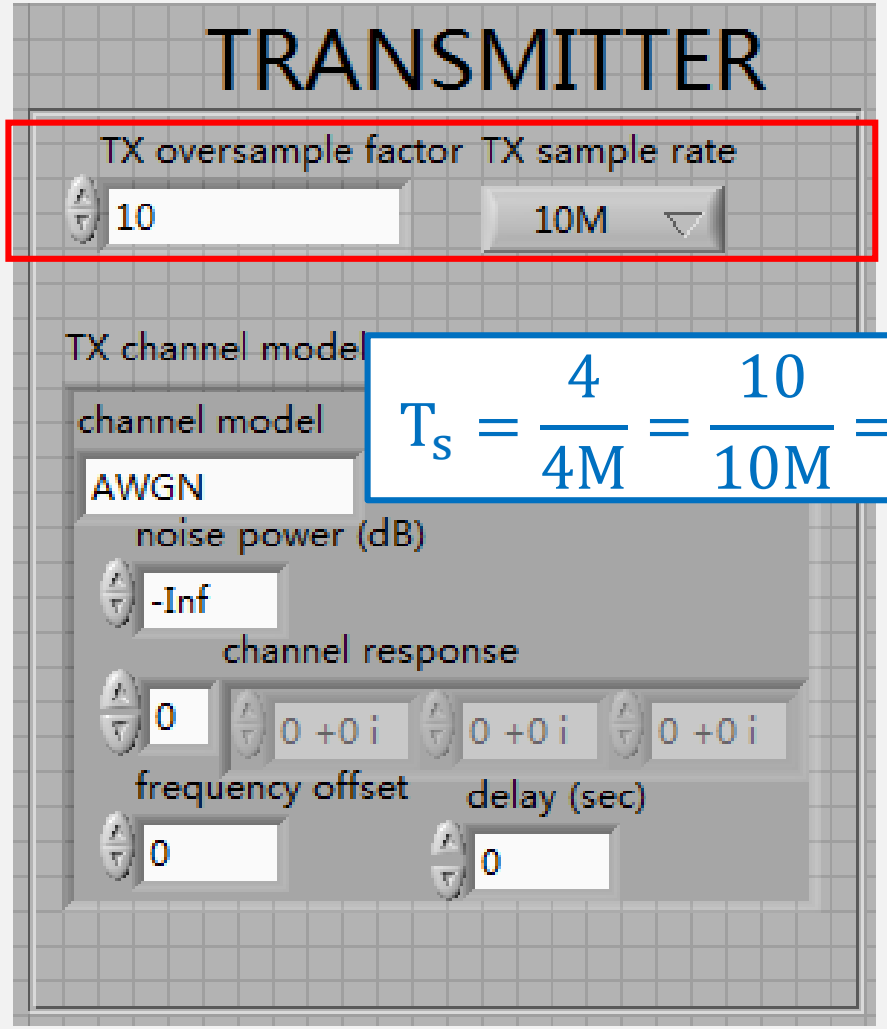




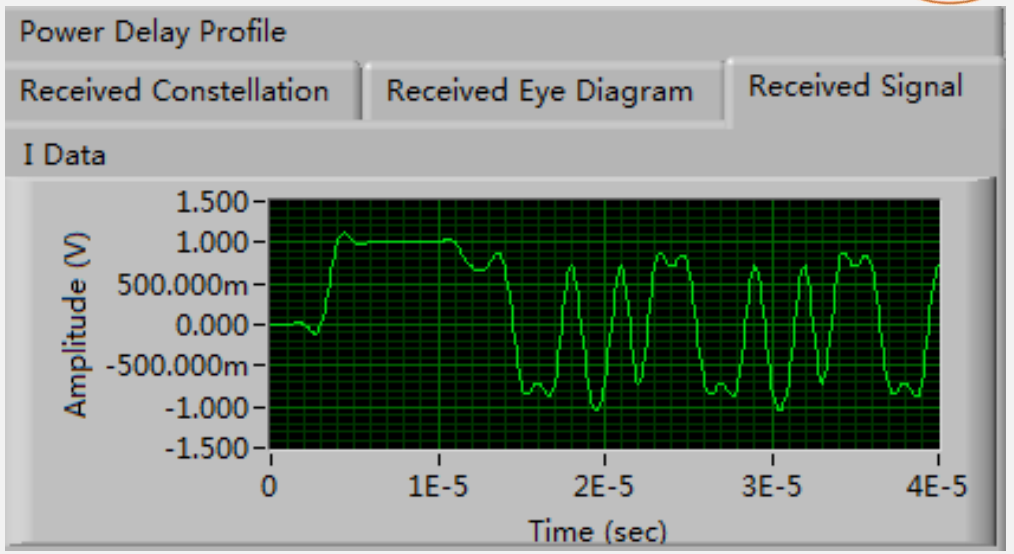

TRANSMITTER
TX oversample factor
TX sample rate
4
4M
TX channel model parameters
channel model
AWGN
noise power (dB)
-Inf
channel response
0
0 +0 i
0 +0 i
0 +0 i
frequency offset
delay (sec)
0
0

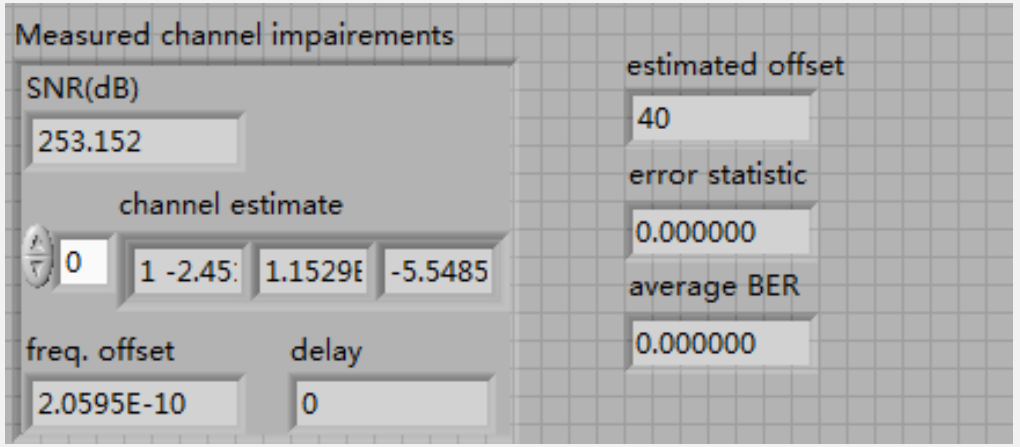

8μs
0.25μs
τd =0μs
Amplitude
Time

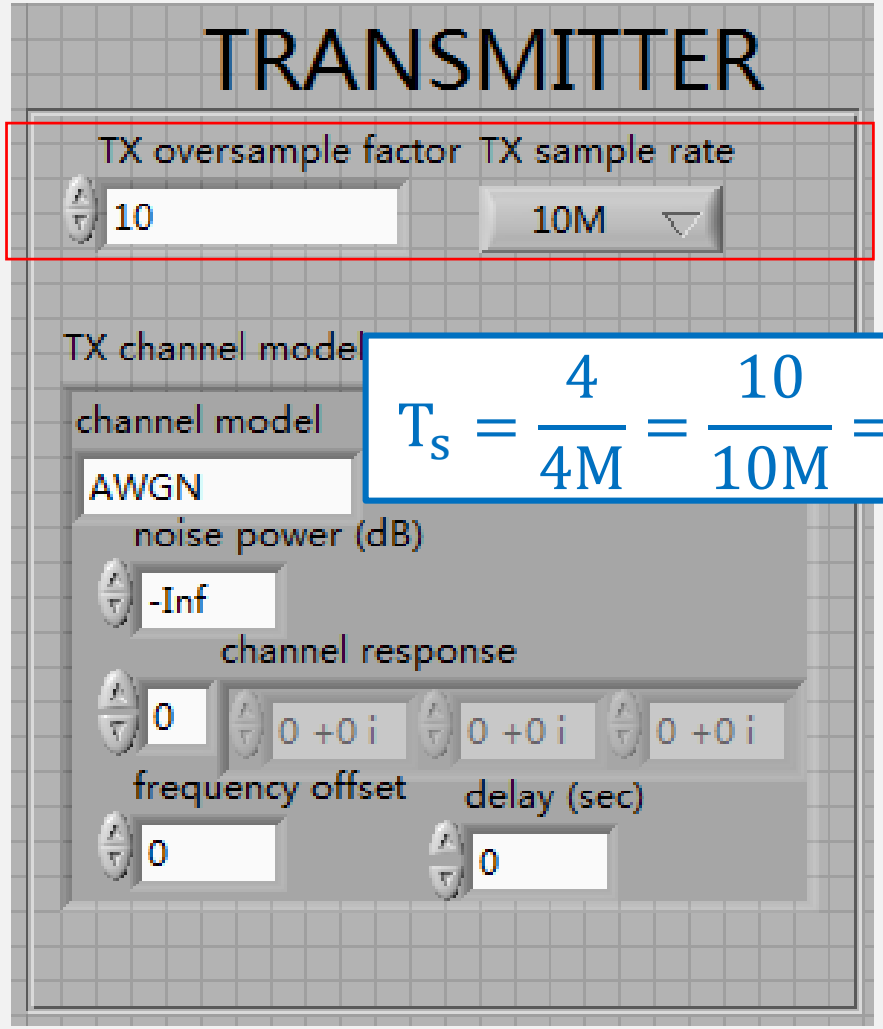

τd =0.25μs
Amplitude
Time



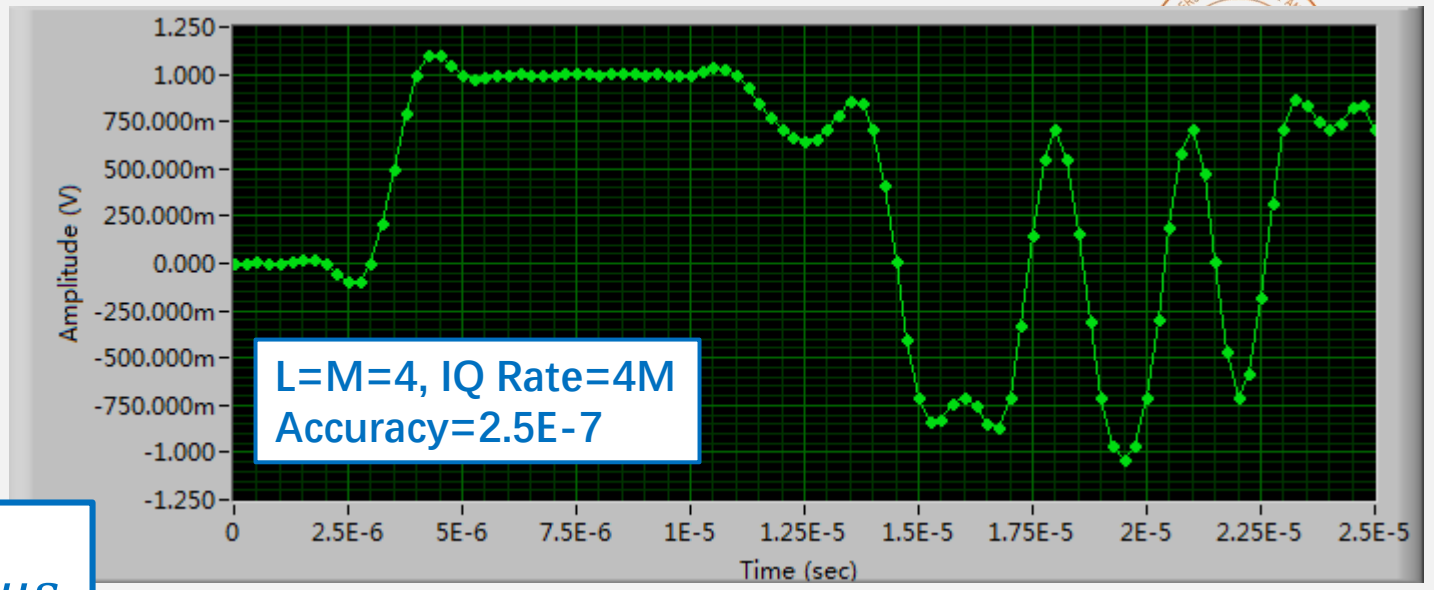
$$T_s = \frac{4}{4M} = \frac{10}{10M} = 1\mu s$$

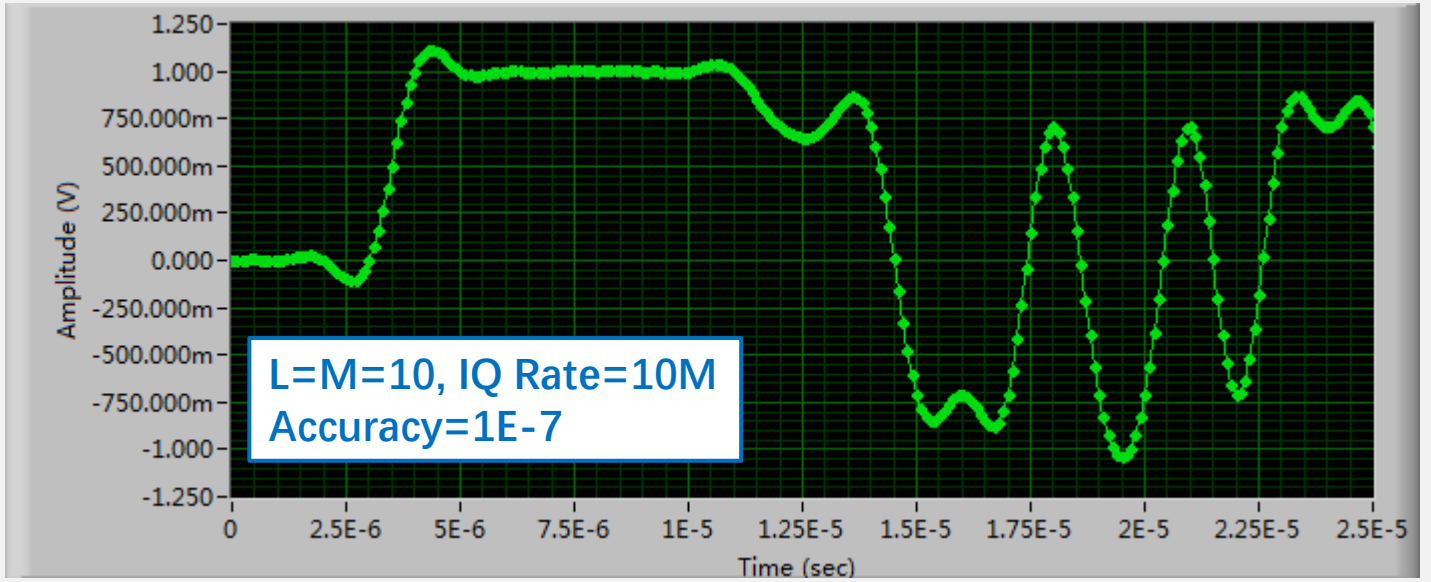






$$T_s = \frac{4}{4M} = \frac{10}{10M} = 1\mu s$$

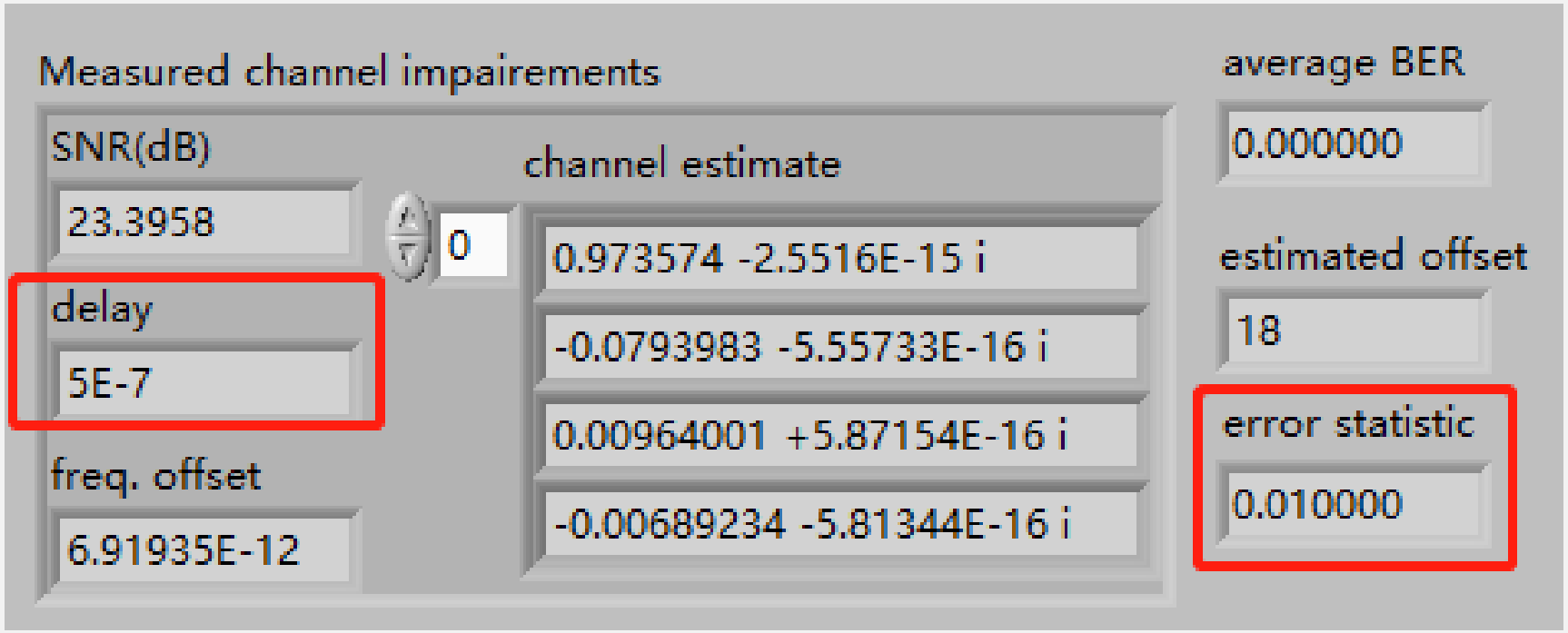




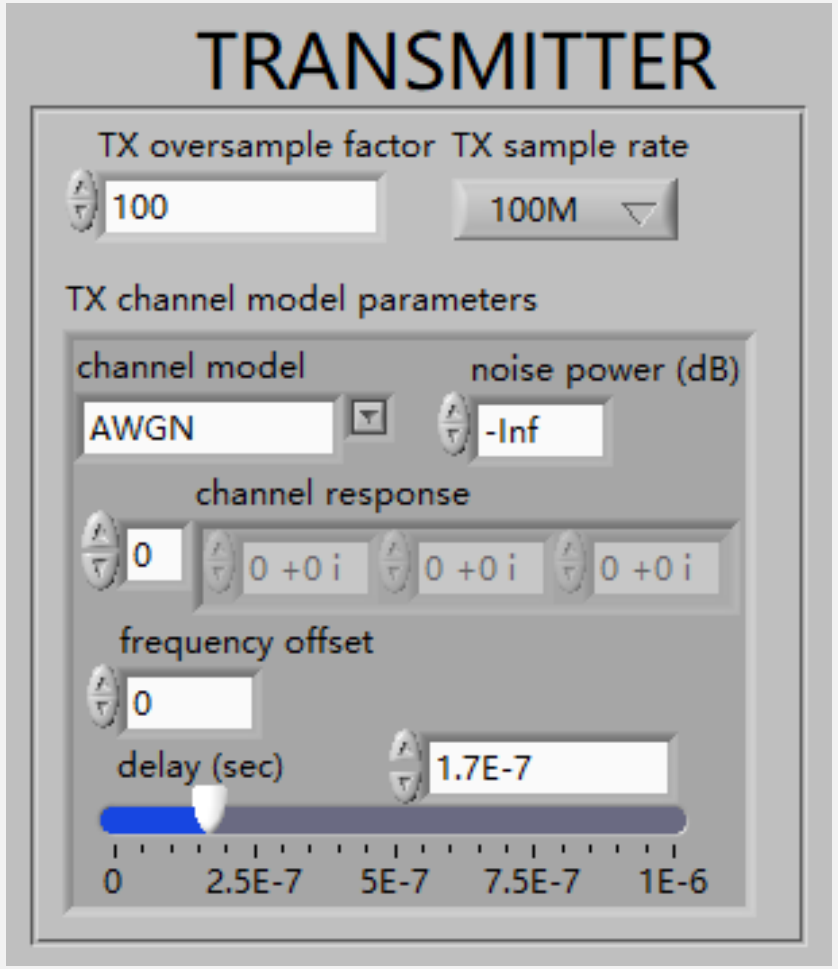
估计值

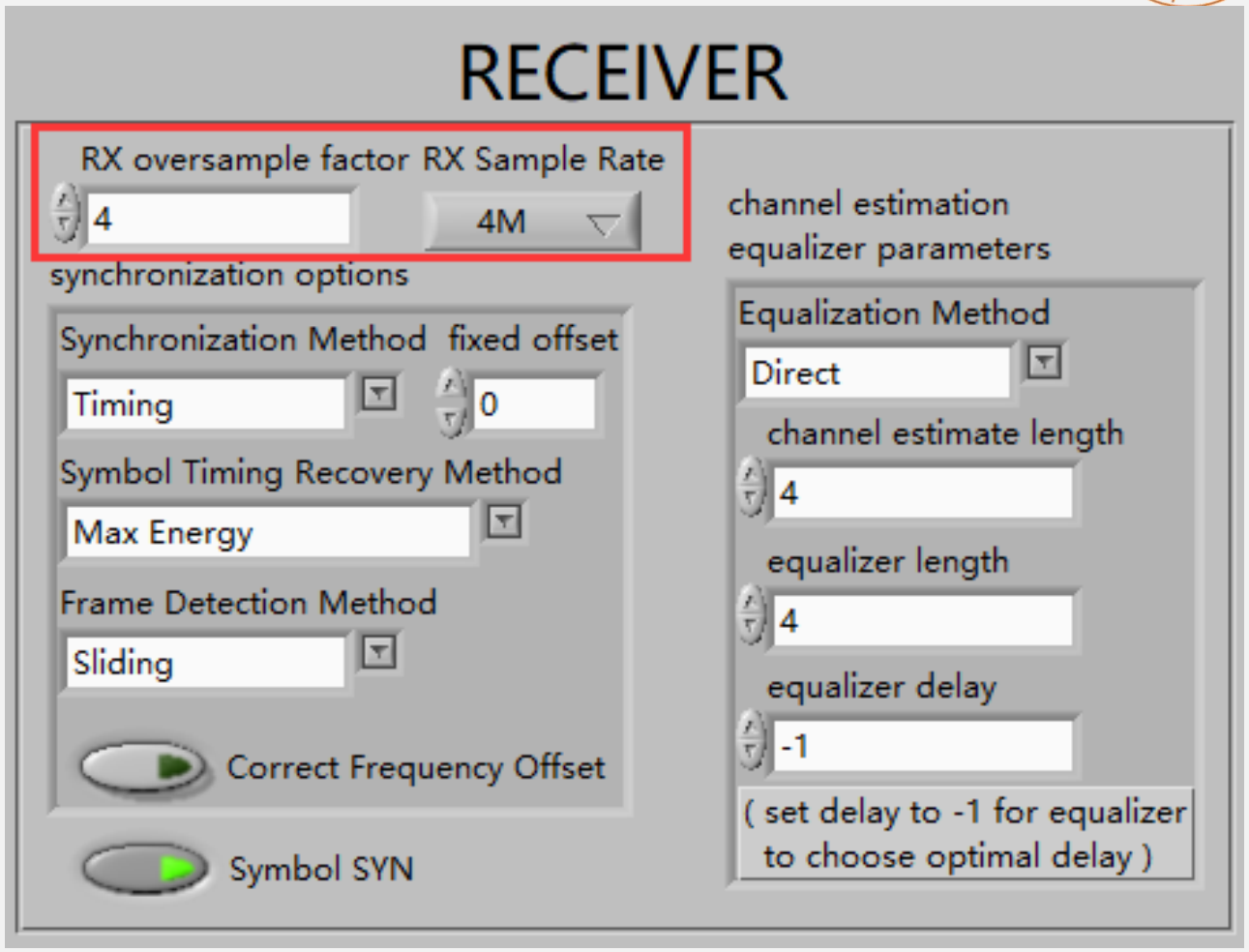
实际值

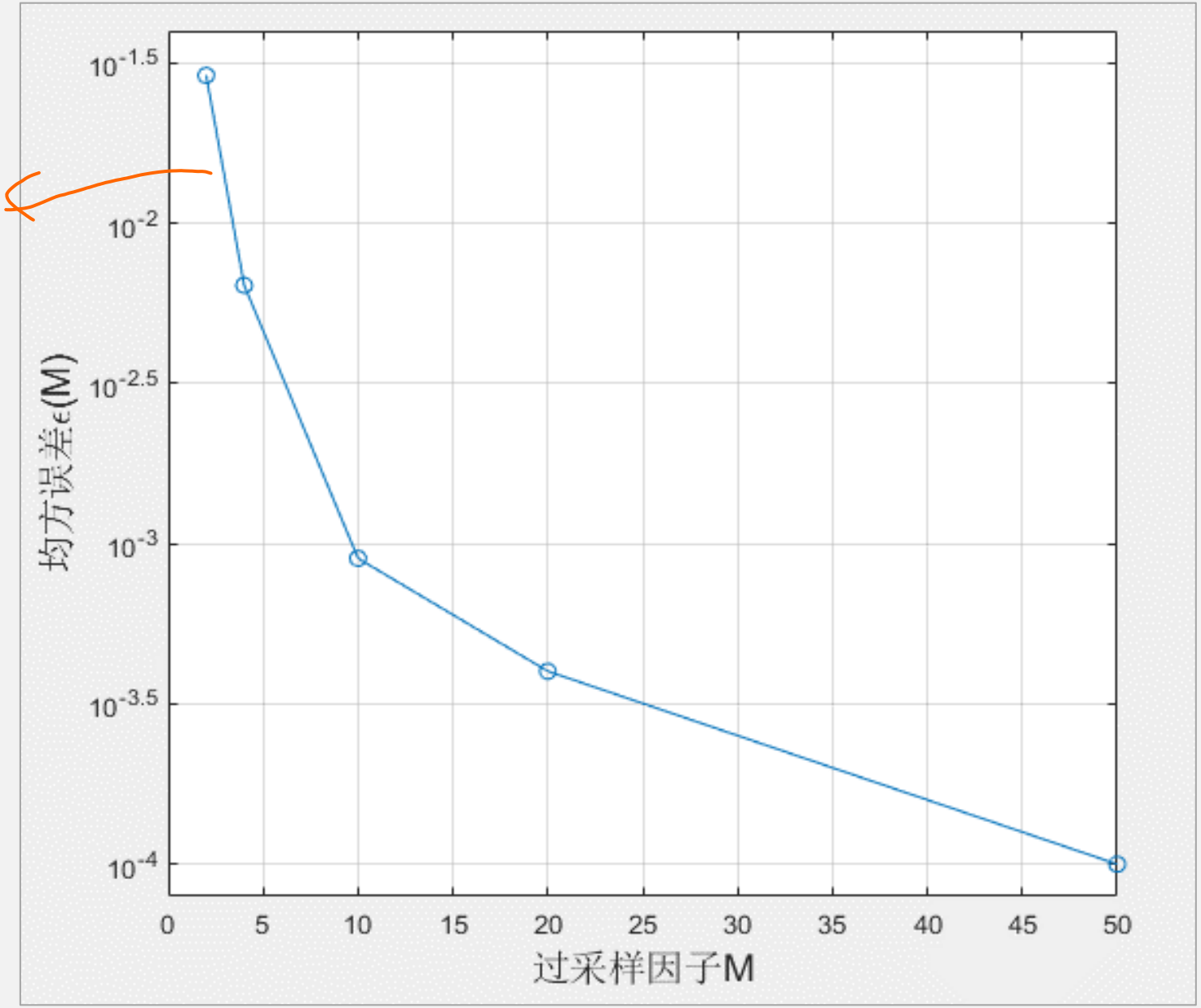
$$\epsilon[M] = \boldsymbol{E}\left\{\left\|\frac{\hat{\tau}(M) - \tau_d}{T_s}\right\|^2\right\}$$

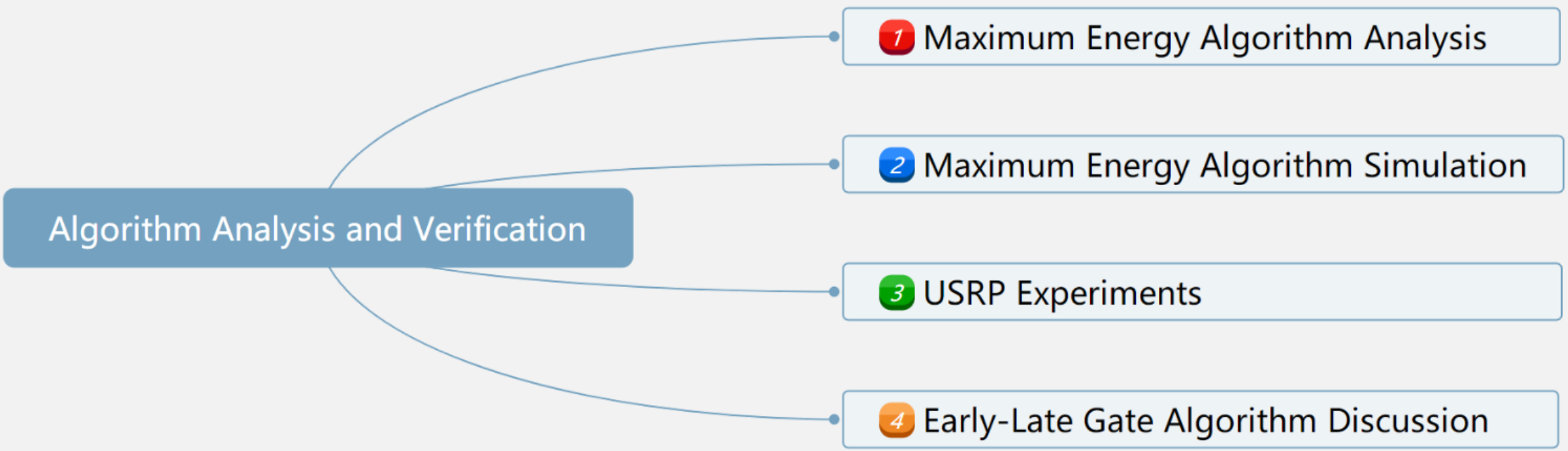

Measured channel impairements
SNR(dB)
23.3958
delay
5E-7
freq. offset
6.91935E-12
0
channel estimate
0.973574 -2.5516E-15 i
-0.0793983 -5.55733E-16 i
0.00964001 +5.87154E-16 i
-0.00689234 -5.81344E-16 i
average BER
0.000000
estimated offset
18
error statistic
0.010000

参数名	参数值
信道延迟τ_d	$0.17\mu s$
符号速率f_s	$1MHz$
发射端过采样因子M_{tx}	100
接收端过采样因子$M(M_{rx})$	2,4,10,20,50
传输信道	AWGN
信道信噪比(dB)	$-\infty$
符号定时同步方法	Max Energy

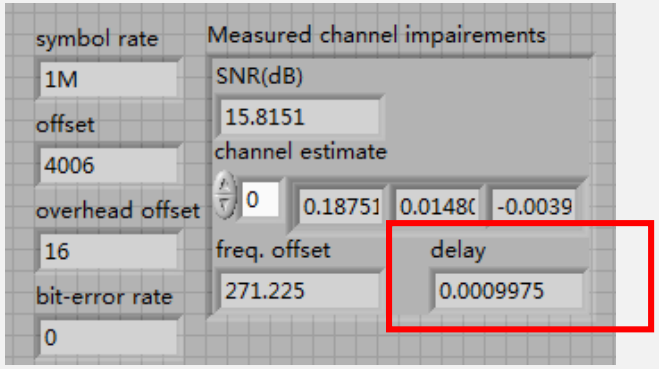

TRANSMITTER
TX oversample factor
100
TX sample rate
100M
TX channel model parameters
channel model
AWGN
noise power (dB)
-Inf
channel response
0
0 +0 i
0 +0 i
0 +0 i
frequency offset
0
delay (sec)
1.7E-7
0
2.5E-7
5E-7
7.5E-7
1E-6


RECEIVER
RX oversample factor
4
RX Sample Rate
4M
synchronization options
Synchronization Method
Timing
fixed offset
0
Symbol Timing Recovery Method
Max Energy
Frame Detection Method
Sliding
Correct Frequency Offset
Symbol SYN
channel estimation
equalizer parameters
Equalization Method
Direct
channel estimate length
4
equalizer length
4
equalizer delay
-1
(set delay to -1 for equalizer
to choose optimal delay)

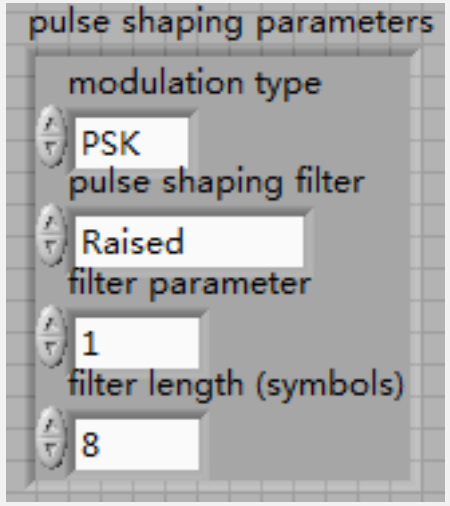

均方误差ε(M)
$10^{-1.5}$
10^{-2}
$10^{-2.5}$
10^{-3}
$10^{-3.5}$
10^{-4}
0
5
10
15
20
25
30
35
40
45
50
过采样因子M

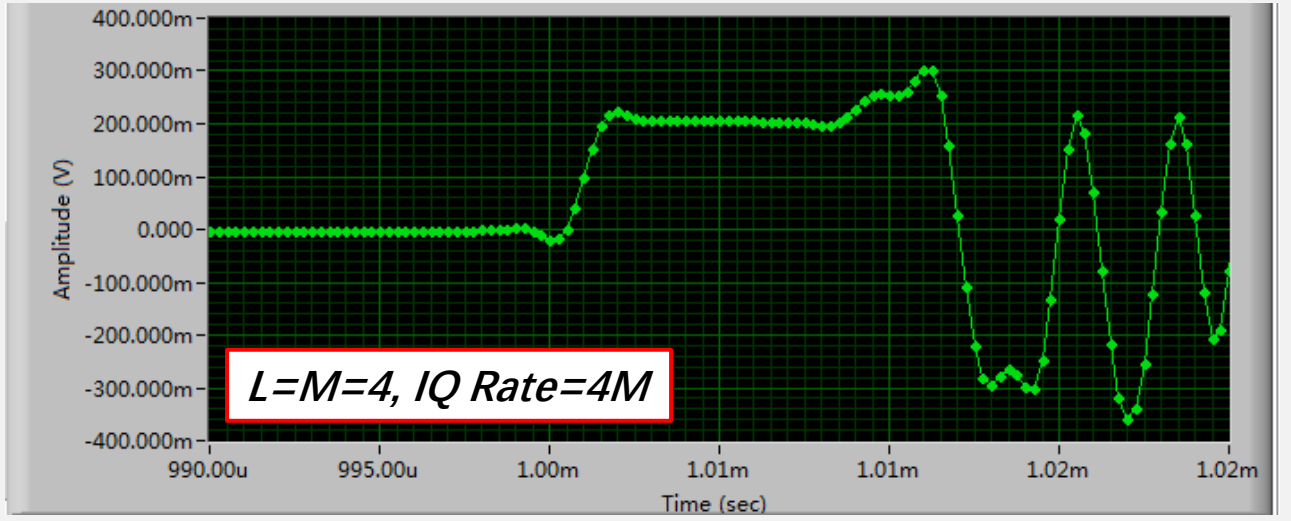

Algorithm Analysis and Verification
1 Maximum Energy Algorithm Analysis
2 Maximum Energy Algorithm Simulation
3 USRP Experiments
4 Early-Late Gate Algorithm Discussion

USRP Experiment

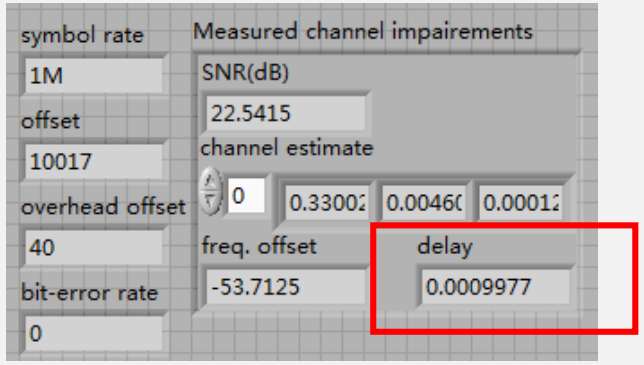


How to calculate the delay here ?

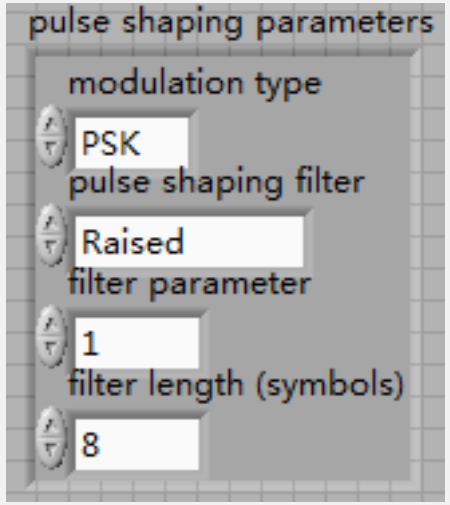


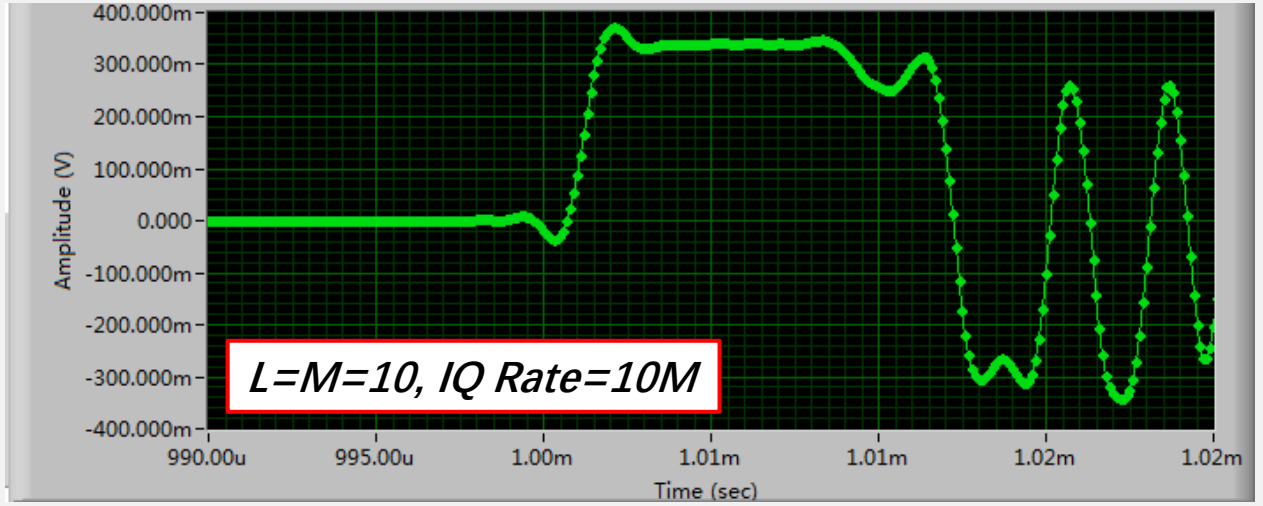


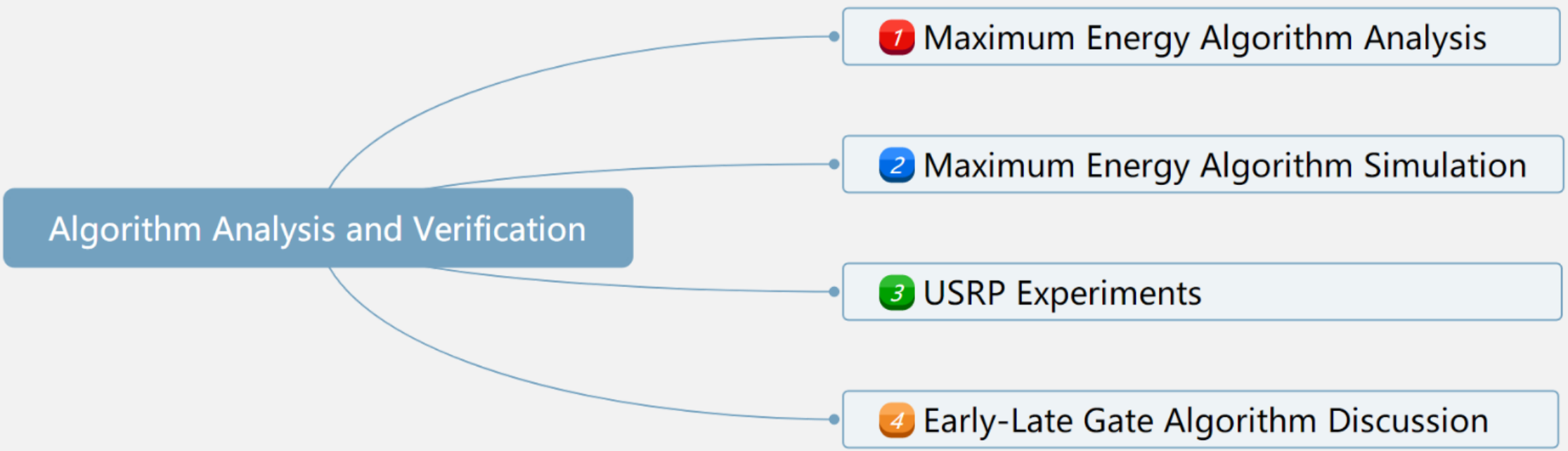
USRP Experiment



How to calculate the delay here ?



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- Question ?