



Injection in SIMsalabim: including roughness



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- › **Injection model:**
 - image-force-lowering
 - Scott&Malliaras
- › **Effect of roughness**
 - enhanced field
 - enhanced injection
- › **SIMsalabim:**
 - implementation

- › Many different models exist...
- › Use a simple one: Scott & Malliaras*
- › Due to image force lowering, the carrier density at (close really) the electrode equals (eq. 11 in paper):

$$n_0 = 4\psi^2 N_c \exp \left(-\frac{\phi_b + \sqrt{f}}{kT} \right)$$

- › where: $f = qFr_c/kT$
- › S&M also give a formula for the current, but we don't need it as we can only use 1 formula (either for n or J).

- › George has shown that roughness at the electrode can enhance injection (the field, really)*
- › Injection current is exponential in the field => to get the average current, we need cannot simply insert the average field in the S&M formula.
- › George's formula for Schottky emission reads:

$$J_s c = A_S T^2 \exp \left(- \frac{\phi_b - \beta \sqrt{F}}{kT} \right)$$

- › Note: very similar to S&M's formula for n (previous slide)

*G. Palasantzas *et al.*, Phys. Rev. B **60**, 9157 (1999)

- › Enhanced injection current (Schottky emission) due to roughness:

$$\frac{J_{sc}}{J_{sc}^0} = \exp \left(\frac{\beta \sqrt{F_0}}{2kT} \frac{F_2}{F_0} \right)$$

- › F_2 is the second-order term in the Taylor series that George uses. We will calculate it later
- › This means that the carrier density in the S&M model is given by:

$$\frac{n_0^{\text{rough}}}{n_0} = \exp \left(\frac{\beta \sqrt{F_0}}{2kT} \frac{F_2}{F_0} \right)$$

- › where we assume that ψ does not change due to roughness.

- › Use George's eq. 31:

$$\frac{F_2}{F_0} = \Delta^2 L^2 \int_0^{q_c} \frac{q^2 \coth q}{(1 + aL^2 q^2)^{1+\alpha}} dq$$

- › $\Delta = w/h_0$. w =rms roughness, h_0 =film thickness
- › $a=0.5$ approximately. This is calculated from the roughness parameters (i.e. input from Solmaz)
- › $L = \xi/h_0$. ξ =lateral correlation length, ~ 100 nm.
- › $\alpha=0.5-0.7$: roughness exponent. Lower value means more spiky surface.

- › There are two effects (formulae shown in previous slides)
 - image-force lowering
 - roughness which enhances injection
- › The S&M equation (w or w/o roughness) for n_0 (carrier density at electrode) means that we can calculate the barrier lowering by assuming Boltzmann statistics.
- › Note: we need Boltzmann statistics at the contacts (V, n, p) to ensure that $J=0$ if $V=0$.
- › So: in every iteration, we adjust $V(0)$ and $n(0)$, $p(0)$.
 - so use law of mass action to get minority density
- › Note: F_2/F_0 is constant during the simulation, so it can be computed externally.

- › What about the sign of F_0 ?
- › lowering term only used if it really *lowers* the barrier, otherwise just use ϕ_b (=input value).