Stat 346 Homework 2

Nathan Jarus

Feb. 13, 2014

1 Problem 1

1.1 Part a

The residuals are not normally distributed, indicating a nonlinear relationship. Possible fixes include non-linear regression or a transformation on X.

1.2 Part b

These residuals seem to be normally distributed with constant variance. This indicates that the model is a good fit.

1.3 Part c

The errors are not normally distributed. This might be fixed with a transformation on Y.

1.4 Part d

The variance on the residuals is not constant. This might be fixed with a transformation on Y.

2 Problem 2

2.1 Part a

The residuals seem normally distributed and support a linear trend.

2.2 Part b

```
s\{b_1\} = 2.125 \times 10^{-2}

t(1 - 0.05/2, 16 - 2) = t(0.975, 14) = 2.145

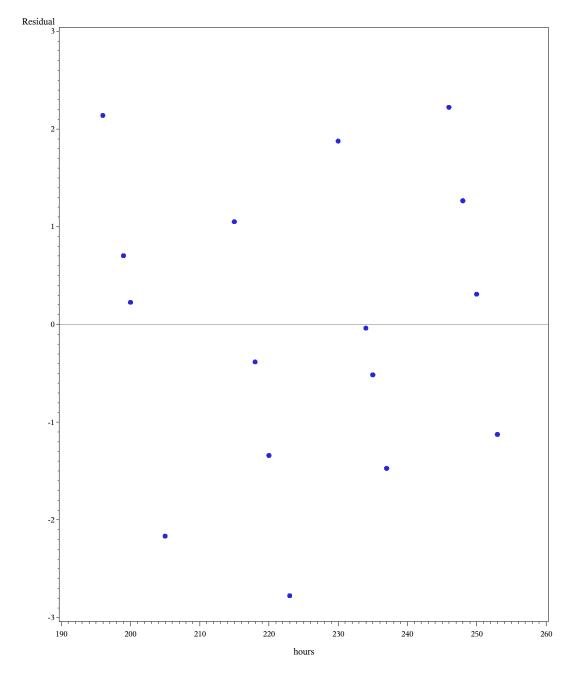
b_1 = 0.47833 \pm 2.145 * 2.125 \times 10^{-2}

(0.43275, 0.52392)
```

2 Problem 2

00:27 Thursday, February 20, 2014 1

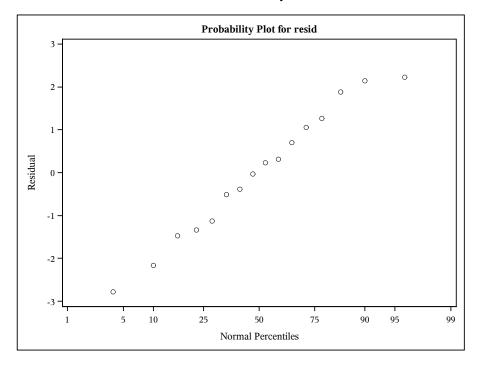
Plastic Hardness Residuals vs. time



2 Problem 2 3

Plastic Hardness Normal Probability

00:27 Thursday, February 20, 2014 1



3 Problem 3

2.3 Part c

$$\begin{split} &\hat{Y} = 37.7759 \\ &s\{\hat{Y}\} = 0.5851 \\ &\hat{Y} \pm t(1-0.05/2, 16-2)s\{\hat{Y}\} = 2.145*0.5851 \\ &(36.5209, 39.0309) \end{split}$$

2.4 Part d

$$R^2 = 1 - \frac{SSE}{SSTO} = 1 - \frac{34.342802}{1280} = 0.9731$$

2.5 Part e

- 1. General Linear Test
- 2. ANOVA
- 3. T-test

3 Problem 3

3.1 Part a

	ORIGINAL REGRESSION	REGRESSION WITH OUTLIER
Fitted Regression Equation	$\hat{Y} = 2.11405 + 0.03883X$	$\hat{Y} = 3.04977 + 0.00090502X$
R-Square	0.0726	0.0011
MSE	0.38829	0.41822
$SE\{b_1\}$	0.01277	0.00250
P-Value	0.0029	0.7178

3.2 Part b

The residuals plot is much more extreme.

3.3 Part c

Yes, you could construct a sequence diagram over the dates, or perhaps school years, at which the GPA and ACT scores were collected.

4 Problem 4

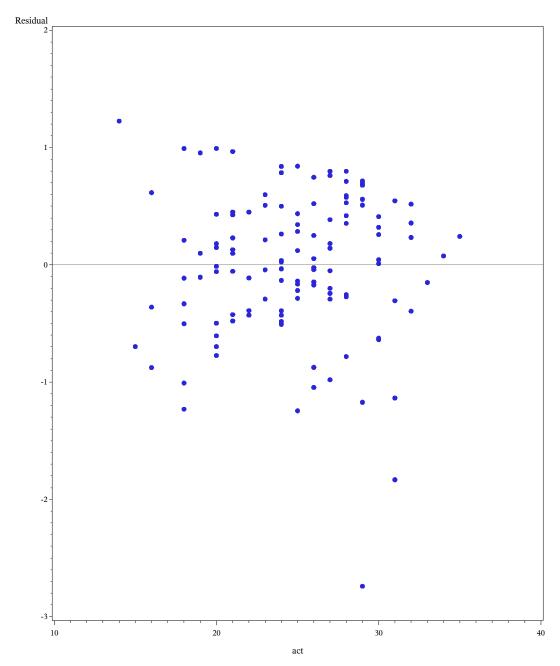
5 Problem 5, KNN #3.23

Full Model:

$$Y_{ij} = \mu_j + \epsilon_{ij} \tag{1}$$

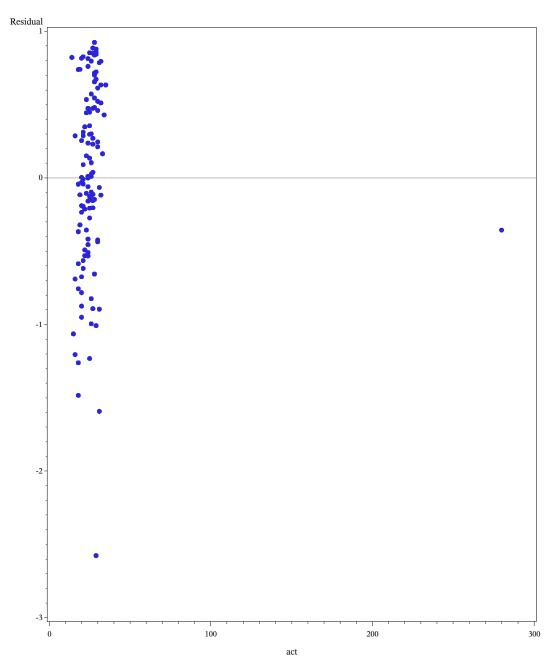
01:31 Thursday, February 20, 2014 1

GPA and ACT Residuals vs. time



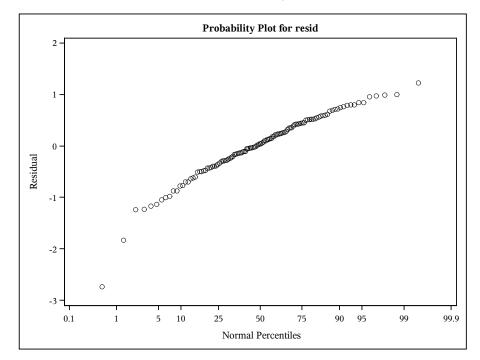
01:31 Thursday, February 20, 2014 1

GPA and ACT with typo Residuals vs. time



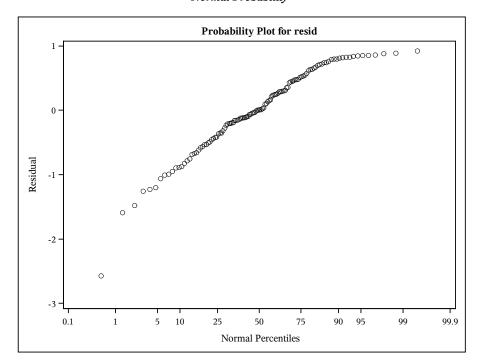
GPA and ACT Normal Probability

01:31 Thursday, February 20, 2014 1



GPA and ACT with typo Normal Probability

01:31 Thursday, February 20, 2014 1



Degrees of freedom: n-c

Reduced Model:

$$Y_{ij} = \beta_1 X_j + \epsilon_{ij} \tag{2}$$

Degrees of freedom: n-2