Project 5 solution

1. Figure of the original image



Figure of the LoG filter ($\sigma = 3.5$, n = 21)

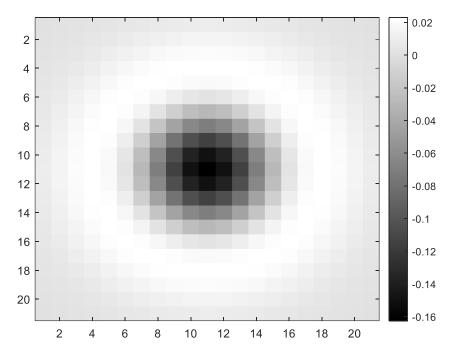


Figure of the LoG image

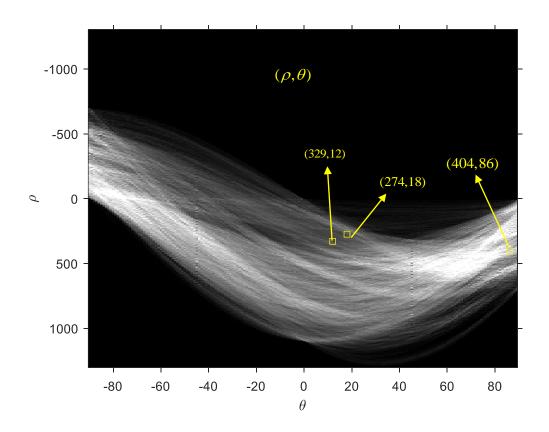


Binary images by zero-crossings with threshold of 0% of max(LoG)





Binary images by zero-crossings with threshold of 4% of max(LoG) 2. Figure of *Hough parameter space* and possible cells for license plate $(P, \theta) = (404, 86), (329, 12), (274, 18)$



3. Figure of linked edges alone

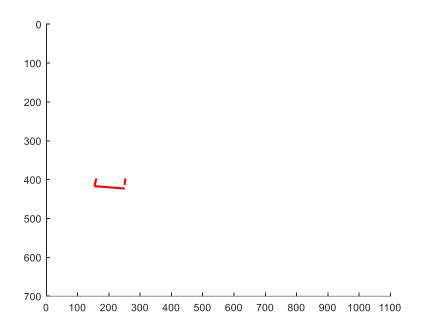


Figure of linked edges overlapped on the original image



4. source code

```
clear all
close all
%% Laplacian of Gaussian (1/(sigma^4))*((y*y+x*x)-2*(sigma*sigma))*
img_ori=imread('Car On Mountain Road.tif');
img_ori = im2double(img_ori);
```

```
M = size(img_ori, 1);
N = size(img ori, 2);
n = 21; sigma = 3.5; % n = 6*sigma + 1 (odd number)
h = zeros(n,n);
h n = (n-1)/2;
[x,y] = meshgrid(-h n:h n, -h n:h n);
% The two parts of the LoG equation
a = (x .^2 + y .^2 - 2 * sigma^2) / sigma^4;
b = exp(-(x .^2 + y .^2) / (2 * sigma^2));
b = b / sum(b(:));
% The LoG filter
LoG = a .* b;
% The normalized LoG filter
nLoG = LoG - mean2(LoG);
figure(1)
image(nLoG,'CDataMapping','scaled')
colormap(gray)
colorbar
%% zero padding and sptial filtering
zero img = zeros (M+floor(n/2)*2, N+floor(n/2)*2);
zero img(floor(n/2)+1:floor(n/2)+M,floor(n/2)+1:floor(n/2)+N) =
img ori;
for i = floor(n/2) + 1:floor(n/2) + M
   for j = floor(n/2) + 1:floor(n/2) + N
       img(i-floor(n/2), j-floor(n/2)) = sum(sum(zero img(i-
floor(n/2):i+floor(n/2), j-floor(n/2):j+floor(n/2)) .* nLoG));
   end
end
%img = imfilter(255*(img ori),nLoG,'replicate');
```

```
figure(2);
out = img - min(min(img)); out = 255 * (out / max(max(out)));
imshow(uint8(out));
%% check zero-crossing
[f, k] = size(img);
fk = zeros(f,k);
fk zct 0 = zeros(f,k);
fk zct = zeros(f,k);
threshold = 0;
threshold1 = 0.04;
for i=2:f-1
   for j=2:k-1
       if (img(i,j+1) \ge 0 \&\& img(i,j-1) < 0) \mid | (img(i,j+1) < 0 \&\&
img(i, j-1) >= 0)
          fk(i,j) = img(i,j);
          fk zct 0(i,j) = abs(img(i,j+1)-img(i,j-
1))>max(max(img))*threshold;
           fk zct(i,j) = abs(img(i,j+1)-img(i,j-
1))>max(max(img))*threshold1;
       elseif (img(i+1,j) \ge 0 \&\& img(i-1,j) < 0) || (img(i+1,j) < 0 \&\&
img(i-1, j) >= 0)
          fk(i,j) = img(i,j);
           fk zct 0(i,j) = abs(img(i+1,j)-img(i-1))
1,j))>max(max(img))*threshold;
          fk zct(i,j) = abs(img(i+1,j)-img(i-
1,j))>max(max(img))*threshold1;
       elseif (img(i+1,j+1) \ge 0 \&\& img(i-1,j-1) < 0) || (img(i+1,j+1) < 0)
&& img(i-1, j-1)>=0)
          fk(i,j) = img(i,j);
          fk zct 0(i,j) = abs(img(i+1,j+1)-img(i-1,j-1))
1))>max(max(img))*threshold;
          fk zct(i,j) = abs(img(i+1,j+1)-img(i-1,j-
1))>max(max(img))*threshold1;;
```

```
elseif (img(i-1,j+1) \ge 0 \&\& img(i+1,j-1) < 0) \mid | (img(i-1,j+1) < 0
&& img(i+1, j-1) >= 0)
          fk(i,j) = img(i,j);
          fk_zct_0(i,j) = abs(img(i-1,j+1)-img(i+1,j-1))
1))>max(max(img))*threshold;
          fk zct(i,j) = abs(img(i-1,j+1)-img(i+1,j-1)
1))>max(max(img))*threshold1;
       end
   end
end
figure(3); imshow(fk zct 0);
figure(4); imshow(fk_zct);
fk zct = logical(fk zct)
%% Hough trandform
%using 4% max(LoG) as the threshold
[H,T,R] = hough(fk zct, 'RhoResolution',1, 'Theta', -90:1:89);
%% find possible cells for license plate in Hough transform
%% Using houghpeaks function and find possible cells for license
plate by try and error
P = houghpeaks(H, 300, 'threshold', ceil(0.2*max(H(:))));
lines = houghlines(fk zct, T, R, P, 'FillGap', 5, 'MinLength', 7);
figure, imshow(img ori), hold on;
\max len = 0;
for k = 1:length(lines)
  xy = [lines(k).point1; lines(k).point2];
  plot(xy(:,1),xy(:,2),'LineWidth',2,'Color','red');
  % Determine the endpoints of the longest line segment
  len = norm(lines(k).point1 - lines(k).point2);
  if ( len > max len)
     \max len = len;
     xy long = xy;
  end
end
```

```
% highlight the longest line segment
plot(xy long(:,1),xy long(:,2),'LineWidth',3,'Color','red');
P=[900 1633 1578;5 103 109].';
figure(5);
%imshow(H,[],'XData',T,'YData',R,'InitialMagnification','fit');
imshow(imadjust(rescale(H)),'XData',T,'YData',R,'InitialMagnification
','fit');
xlabel('\theta'), ylabel('\rho');
axis on, axis normal, hold on;
set(findobj(get(gca, 'Children'), 'LineWidth', 0.5), 'LineWidth', 10);
plot(T(P(:,2)),R(P(:,1)),'s','color','yellow');
% extract line segments based on Hough transform
lines = houghlines(fk zct 0,T,R,P,'FillGap',5,'MinLength',5);
lines1 = houghlines(fk zct 0,T,R,[900 5],'FillGap',5,'MinLength',5);
lines2 = houghlines(fk zct 0,T,R,[1633
103], 'FillGap', 5, 'MinLength', 5);
lines3 = houghlines(fk zct 0,T,R,[1578
109], 'FillGap', 5, 'MinLength', 5);
%% License plate
% only plot line segment
figure(6), hold on;
axis([0 1100 0 700]);
set(gca, 'ydir', 'reverse');
for k = 4
  xy = [lines1(k).point1; lines1(k).point2];
  plot(xy(:,1),xy(:,2),'LineWidth',2,'Color','red');
end
for k = 8
  xy = [lines2(k).point1; lines2(k).point2];
```

```
plot(xy(:,1),xy(:,2),'LineWidth',2,'Color','red');
end
for k = 12
  xy = [lines3(k).point1; lines3(k).point2];
  plot(xy(:,1),xy(:,2),'LineWidth',2,'Color','red');
end
figure(7), imshow(img ori), hold on;
for k = 4
  xy = [lines1(k).point1; lines1(k).point2];
  plot(xy(:,1),xy(:,2),'LineWidth',2,'Color','red');
end
for k = 8
  xy = [lines2(k).point1; lines2(k).point2];
  plot(xy(:,1),xy(:,2),'LineWidth',2,'Color','red');
end
for k = 12
  xy = [lines3(k).point1; lines3(k).point2];
  plot(xy(:,1),xy(:,2),'LineWidth',2,'Color','red');
end
```