Introduction of R in using optim() and Newton's Method

Linxi Li T00622714

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R Markdown

This is a tutorial on how to use optim() and Newton's Method to compute the maximum likelihood estimation of logistic regression.

At the beginning, you need to have your logit data. In my project, I simulated the data as:

Or you can also upload your data.csv by using read.csv("/your local location/filename.csv"), for example:

```
data <- read.csv("/Users/ccc/Desktop/data.csv")</pre>
data
##
         Ху
## 1 0.50 0
## 2 0.75 0
## 3 1.00 0
## 4 1.25 0
## 5
     1.50 0
## 6 1.75 0
## 7 1.75 1
## 8 2.00 0
## 9 2.25 1
## 10 2.50 0
## 11 2.75 1
## 12 3.00 0
## 13 3.25 1
## 14 3.50 0
## 15 4.00 1
## 16 4.25 1
## 17 4.50 1
## 18 4.75 1
## 19 5.00 1
## 20 5.50 1
```

and then you can assign your x and y from the data file you upload, such that:

```
x1 <- data$X
y1 <- data$y</pre>
```

In my project, at the really beginning, I used the glm() to estimate the MLE of my data by using the family of "binomial". Usually, glm() will give us a more realistic answer. Therefore, we can find out the different by comparing the answers given by optim(), Newton's method to the glm().

```
#qlm
mylogit <- glm(y ~ x, family = "binomial"(link = "logit"))</pre>
mylogit
##
## Call: glm(formula = y ~ x, family = binomial(link = "logit"))
##
## Coefficients:
## (Intercept)
        -4.078
                      1.505
##
##
## Degrees of Freedom: 19 Total (i.e. Null); 18 Residual
## Null Deviance:
                        27.73
## Residual Deviance: 16.06
                                AIC: 20.06
```

As we know that, b0 is intercept, and b1 represents the slope, so we can get our result from glm() that b0 is -4.078, and b1 is 1.505.

After getting the result from glm(), we can start using optim() to get MLE. optim()

```
#MLE for logistic
nlogL_logstic <- function(paravec){</pre>
  # paravec[1] - b0
  # paravec[2] - b1
  sum(y*paravec[1])+sum(y*paravec[2]*x)-sum(log(1+exp(paravec[1]+paravec[2]*x)))
}
MLE = optim(c(0,0), #because we have two parameters in the function;
            fn=nlogL_logstic,
            method = "L-BFGS-B",
            control = list(fnscale = -1),
            hessian = FALSE)
MLE
## $par
## [1] -4.077802 1.504685
##
## $value
## [1] -8.029878
```

```
##
## $counts
## function gradient
## 14 14
##
## $convergence
## [1] 0
##
## $message
## [1] "CONVERGENCE: REL_REDUCTION_OF_F <= FACTR*EPSMCH"</pre>
```

The optim() gives the result of b0 is -4.0778, and b1 is 1.504685, which are very much close to the glm() result.

Finally, we use Newton's Method to compare by using the derivative of the log likelihood function and derivative of the score function.

```
#Newton of b0 and b1
nlogL_log <- function(b0,b1){</pre>
  # b0
  # b1
  sum(y*(b0+b1*x))-sum(log(1+exp(b0+b1*x)))
nor_MLE_of_Newtown <- function (x, itr, b00=0,b11=0) {</pre>
  # input: x-vector of observations; itr- iteration times; b00,b11 - initial value
  # output: MLE estimate and maximum log-likelihood value
  b0 \leftarrow rep(0, itr+1)
  b1 \leftarrow rep(0, itr+1)
  b0[1] <- b00
  b1[1] <- b11
  for (i in 1:itr){
    \#b[n+1] = b[n] - l(bn)/l'(bn)
    b0[i+1] = b0[i] - (sum(y)-sum(exp(b0[i]+b1[i]*x)/(1+exp(b0[i]+b1[i]*x))))/
      (-sum((exp(b0[i]+b1[i]*x))/(exp(b0[i]+b1[i]*x)+1)^2))
    \#sigma2[i+1] = sigma[i] - sigma[i] + (1/n * sum((xi - mu)^2))
    b1[i+1]=b1[i] - (sum(x*y)-sum(x*exp(b0[i]+b1[i]*x)/(1+exp(b0[i]+b1[i]*x))))/
      (-sum(((x^2)*exp(b0[i]+b1[i]*x))/(exp(b0[i]+b1[i]*x)^2)))
  }
  data.frame(b0=b0, b1=b1,log.lik.value=nlogL_log(b0,b1))
nor_MLE_of_Newtown(n,1000) # iterate 1000 times
## Warning in b1 * x: longer object length is not a multiple of shorter object
## length
```

Warning in b1 * x: longer object length is not a multiple of shorter object ## length

```
##
                 b0
                            b1 log.lik.value
## 1
         0.0000000 0.00000000
                                    -405.7357
## 2
         0.0000000 0.05099150
                                    -405.7357
## 3
        -0.1426080 0.09803319
                                    -405.7357
## 4
        -0.2735782 0.14502350
                                    -405.7357
## 5
        -0.4044333 0.19124361
                                    -405.7357
## 6
        -0.5330174 0.23654028
                                    -405.7357
## 7
        -0.6588953 0.28072242
                                    -405.7357
## 8
        -0.7815187 0.32364509
                                    -405.7357
## 9
        -0.9004769 0.36519716
                                    -405.7357
## 10
        -1.0154598 0.40530102
                                    -405.7357
## 11
        -1.1262560 0.44390887
                                    -405.7357
## 12
        -1.2327412 0.48099863
                                    -405.7357
## 13
        -1.3348658 0.51656974
                                    -405.7357
## 14
        -1.4326417 0.55063898
                                    -405.7357
## 15
        -1.5261305 0.58323671
                                    -405.7357
## 16
        -1.6154315 0.61440352
                                    -405.7357
## 17
        -1.7006722 0.64418738
                                    -405.7357
## 18
        -1.7820000 0.67264124
                                    -405.7357
## 19
        -1.8595753 0.69982118
                                    -405.7357
## 20
        -1.9335660 0.72578477
                                    -405.7357
## 21
        -2.0041429 0.75058998
                                    -405.7357
## 22
        -2.0714769 0.77429418
                                    -405.7357
## 23
        -2.1357361 0.79695353
                                    -405.7357
## 24
        -2.1970838 0.81862245
                                    -405.7357
## 25
        -2.2556780 0.83935333
                                    -405.7357
## 26
        -2.3116698 0.85919629
                                    -405.7357
## 27
                                    -405.7357
        -2.3652031 0.87819903
##
  28
        -2.4164146 0.89640685
                                    -405.7357
## 29
        -2.4654335 0.91386258
                                    -405.7357
## 30
        -2.5123816 0.93060667
                                    -405.7357
## 31
        -2.5573736 0.94667723
                                    -405.7357
## 32
        -2.6005172 0.96211011
                                    -405.7357
## 33
        -2.6419136 0.97693904
                                    -405.7357
##
  34
        -2.6816575 0.99119567
                                    -405.7357
## 35
        -2.7198378 1.00490975
                                    -405.7357
## 36
        -2.7565377 1.01810919
                                    -405.7357
## 37
        -2.7918353 1.03082020
                                    -405.7357
## 38
        -2.8258036 1.04306736
                                    -405.7357
## 39
        -2.8585110 1.05487376
                                    -405.7357
## 40
        -2.8900215 1.06626108
                                    -405.7357
## 41
        -2.9203954 1.07724968
                                    -405.7357
## 42
        -2.9496890 1.08785868
                                    -405.7357
## 43
        -2.9779551 1.09810608
                                    -405.7357
## 44
        -3.0052434 1.10800878
                                    -405.7357
## 45
                                    -405.7357
        -3.0316004 1.11758270
## 46
        -3.0570699 1.12684282
                                    -405.7357
## 47
        -3.0816931 1.13580326
                                    -405.7357
## 48
        -3.1055088 1.14447733
                                    -405.7357
  49
        -3.1285534 1.15287756
                                    -405.7357
## 50
        -3.1508612 1.16101582
                                    -405.7357
```

```
## 51
        -3.1724646 1.16890328
                                    -405.7357
## 52
        -3.1933943 1.17655050
                                    -405.7357
        -3.2136789 1.18396749
## 53
                                    -405.7357
## 54
        -3.2333458 1.19116370
                                    -405.7357
##
  55
        -3.2524207 1.19814808
                                    -405.7357
        -3.2709280 1.20492911
## 56
                                    -405.7357
## 57
        -3.2888907 1.21151484
                                    -405.7357
## 58
        -3.3063305 1.21791288
                                    -405.7357
##
  59
        -3.3232684 1.22413048
                                    -405.7357
## 60
        -3.3397237 1.23017451
                                    -405.7357
##
  61
        -3.3557153 1.23605150
                                    -405.7357
        -3.3712606 1.24176767
##
  62
                                    -405.7357
##
   63
        -3.3863766 1.24732892
                                    -405.7357
##
  64
        -3.4010793 1.25274088
                                    -405.7357
## 65
        -3.4153837 1.25800892
                                    -405.7357
##
   66
        -3.4293045 1.26313813
                                    -405.7357
##
  67
        -3.4428552 1.26813339
                                    -405.7357
##
   68
        -3.4560492 1.27299935
                                    -405.7357
##
  69
        -3.4688989 1.27774044
                                    -405.7357
##
  70
        -3.4814162 1.28236089
                                    -405.7357
                                    -405.7357
## 71
        -3.4936125 1.28686477
## 72
        -3.5054988 1.29125594
                                    -405.7357
        -3.5170854 1.29553811
## 73
                                    -405.7357
        -3.5283823 1.29971482
##
  74
                                    -405.7357
                                    -405.7357
## 75
        -3.5393989 1.30378945
##
  76
        -3.5501445 1.30776528
                                    -405.7357
##
  77
        -3.5606277 1.31164541
                                    -405.7357
##
  78
        -3.5708569 1.31543282
                                    -405.7357
## 79
                                    -405.7357
        -3.5808401 1.31913040
## 80
        -3.5905850 1.32274088
                                    -405.7357
## 81
        -3.6000989 1.32626692
                                    -405.7357
##
  82
        -3.6093888 1.32971104
                                    -405.7357
##
  83
        -3.6184617 1.33307569
                                    -405.7357
##
  84
        -3.6273240 1.33636321
                                    -405.7357
##
   85
        -3.6359819 1.33957586
                                    -405.7357
        -3.6444415 1.34271580
##
  86
                                    -405.7357
## 87
        -3.6527086 1.34578512
                                    -405.7357
## 88
        -3.6607888 1.34878584
                                    -405.7357
## 89
        -3.6686874 1.35171989
                                    -405.7357
## 90
        -3.6764096 1.35458913
                                    -405.7357
        -3.6839603 1.35739536
## 91
                                    -405.7357
## 92
        -3.6913444 1.36014032
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##
  93
        -3.6985664 1.36282568
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##
  94
        -3.7056309 1.36545306
                                    -405.7357
## 95
        -3.7125421 1.36802401
                                    -405.7357
## 96
        -3.7193042 1.37054003
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##
  97
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## 98
        -3.7323969 1.37541307
                                    -405.7357
## 99
        -3.7387351 1.37777285
                                    -405.7357
##
  100
        -3.7449394 1.38008323
                                    -405.7357
## 101
        -3.7510132 1.38234548
                                    -405.7357
## 102
        -3.7569600 1.38456083
                                    -405.7357
## 103
        -3.7627830 1.38673046
                                    -405.7357
## 104 -3.7684853 1.38885552
                                    -405.7357
```

```
## 105
       -3.7740701 1.39093713
                                   -405.7357
## 106
        -3.7795402 1.39297637
                                   -405.7357
## 107
        -3.7848985 1.39497427
                                   -405.7357
## 108
        -3.7901479 1.39693185
                                   -405.7357
## 109
        -3.7952908 1.39885009
                                   -405.7357
        -3.8003301 1.40072993
## 110
                                   -405.7357
## 111
        -3.8052681 1.40257231
                                   -405.7357
        -3.8101074 1.40437811
## 112
                                   -405.7357
## 113
        -3.8148503 1.40614820
                                   -405.7357
## 114
        -3.8194991 1.40788342
                                   -405.7357
## 115
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## 116
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## 117
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                                   -405.7357
## 118
        -3.8371967 1.41449160
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## 119
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                                   -405.7357
## 120
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                                   -405.7357
## 121
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## 122
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## 123
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## 124
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                                   -405.7357
## 125
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        -3.8686940 1.42626131
## 126
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        -3.8723004 1.42760967
## 127
                                   -405.7357
## 128
        -3.8758387 1.42893270
                                   -405.7357
## 129
        -3.8793104 1.43023095
                                   -405.7357
## 130
        -3.8827169 1.43150497
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        -3.8860597 1.43275526
##
  131
                                   -405.7357
##
  132
        -3.8893401 1.43398235
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## 133
        -3.8925594 1.43518672
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## 134
        -3.8957190 1.43636885
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## 135
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##
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        -3.9018640 1.43866828
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##
  137
        -3.9048519 1.43978647
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## 138
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                                   -405.7357
  139
        -3.9106643 1.44196200
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## 140
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## 141
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## 142
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## 146
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## 150
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## 151
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                                   -405.7357
## 152
        -3.9436819 1.45432743
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## 153
        -3.9459152 1.45516425
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##
  154
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                                   -405.7357
## 155
        -3.9502640 1.45679394
                                   -405.7357
## 156
        -3.9523811 1.45758736
                                   -405.7357
## 157
        -3.9544609 1.45836688
                                   -405.7357
## 158 -3.9565042 1.45913276
                                   -405.7357
```

```
## 159
        -3.9585118 1.45988527
                                   -405.7357
        -3.9604841 1.46062465
## 160
                                   -405.7357
## 161
        -3.9624221 1.46135117
                                   -405.7357
## 162
        -3.9643263 1.46206506
                                   -405.7357
##
   163
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                                   -405.7357
## 164
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                                   -405.7357
## 165
        -3.9698426 1.46413339
                                   -405.7357
## 166
        -3.9716180 1.46479914
                                   -405.7357
## 167
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                                   -405.7357
## 168
        -3.9750773 1.46609645
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## 169
        -3.9767623 1.46672843
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##
  170
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                                   -405.7357
##
  171
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                                   -405.7357
## 172
        -3.9816458 1.46856012
                                   -405.7357
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        -3.9847636 1.46972968
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        -3.9877758 1.47085975
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        -3.9892436 1.47141042
## 177
                                   -405.7357
## 178
        -3.9906863 1.47195175
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## 179
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        -3.9934988 1.47300706
## 180
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        -3.9948695 1.47352138
## 181
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  184
        -3.9988439 1.47501287
                                   -405.7357
  185
        -4.0001243 1.47549340
                                   -405.7357
##
##
   186
        -4.0013831 1.47596585
                                   -405.7357
        -4.0026207 1.47643038
## 187
                                   -405.7357
## 188
        -4.0038376 1.47688712
                                   -405.7357
## 189
        -4.0050341 1.47733622
                                   -405.7357
## 190
        -4.0062105 1.47777780
                                   -405.7357
  191
        -4.0073672 1.47821202
                                   -405.7357
## 192
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                                   -405.7357
  193
        -4.0096230 1.47905883
                                   -405.7357
        -4.0107227 1.47947169
## 194
                                   -405.7357
## 195
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                                   -405.7357
## 196
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                                   -405.7357
        -4.0139132 1.48066953
## 197
                                   -405.7357
        -4.0149415 1.48105563
## 198
                                   -405.7357
  199
        -4.0159528 1.48143533
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## 200
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                                   -405.7357
## 201
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                                   -405.7357
## 202
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                                   -405.7357
## 203
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                                   -405.7357
        -4.0207633 1.48324171
## 204
                                   -405.7357
## 205
        -4.0216783 1.48358530
                                   -405.7357
## 206
        -4.0225781 1.48392323
                                   -405.7357
## 207
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                                   -405.7357
## 208
        -4.0243335 1.48458250
                                   -405.7357
## 209
        -4.0251896 1.48490403
                                   -405.7357
## 210
        -4.0260317 1.48522028
                                   -405.7357
## 211
       -4.0268599 1.48553135
                                   -405.7357
## 212 -4.0276745 1.48583732
                                   -405.7357
```

```
## 213 -4.0284757 1.48613827
                                   -405.7357
## 214
       -4.0292639 1.48643430
                                   -405.7357
## 215
        -4.0300391 1.48672549
                                   -405.7357
## 216
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                                   -405.7357
## 217
        -4.0315516 1.48729367
                                   -405.7357
        -4.0322894 1.48757082
## 218
                                   -405.7357
## 219
        -4.0330152 1.48784345
                                   -405.7357
## 220
        -4.0337291 1.48811164
                                   -405.7357
## 221
        -4.0344313 1.48837546
                                   -405.7357
## 222
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                                   -405.7357
## 223
        -4.0358017 1.48889029
                                   -405.7357
## 224
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                                   -405.7357
## 225
        -4.0371279 1.48938852
                                   -405.7357
        -4.0377748 1.48963158
## 226
                                   -405.7357
## 227
        -4.0384112 1.48987070
                                   -405.7357
##
   228
        -4.0390373 1.49010594
                                   -405.7357
                                   -405.7357
##
  229
        -4.0396533 1.49033737
   230
        -4.0402592 1.49056504
                                   -405.7357
##
  231
        -4.0408554 1.49078903
                                   -405.7357
##
  232
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                                   -405.7357
##
  233
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        -4.0425865 1.49143950
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##
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## 806
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##
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## 858
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                                   -405.7357
## 860
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## 883
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        -4.0777122 1.50464497
##
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##
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                                   -405.7357
  887
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##
##
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        -4.0777123 1.50464500
                                   -405.7357
   889
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                                   -405.7357
##
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                                   -405.7357
##
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        -4.0777124 1.50464503
##
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   895
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                                   -405.7357
##
        -4.0777124 1.50464504
##
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   897
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                                   -405.7357
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                                   -405.7357
        -4.0777125 1.50464507
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## 902
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##
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        -4.0777125 1.50464508
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        -4.0777125 1.50464509
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  904
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## 906
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## 907
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## 908
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## 910
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## 911
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## 912
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                                   -405.7357
## 913
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                                   -405.7357
## 914 -4.0777127 1.50464514
                                   -405.7357
```

```
## 915 -4.0777127 1.50464514
                                   -405.7357
## 916
       -4.0777127 1.50464515
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## 917
        -4.0777127 1.50464515
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## 918
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## 920
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        -4.0777127 1.50464517
## 921
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## 922
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## 923
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## 924
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## 925
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## 926
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## 927
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## 929
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        -4.0777128 1.50464521
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##
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## 933
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## 934
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## 935
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        -4.0777129 1.50464522
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## 936
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## 938
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## 939
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## 941
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## 942
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        -4.0777129 1.50464525
## 943
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## 944
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## 945
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##
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## 947
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## 948
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## 949
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## 950
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## 951
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## 952
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        -4.0777130 1.50464527
## 954
                                   -405.7357
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        -4.0777130 1.50464528
## 956
                                   -405.7357
##
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##
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## 960
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##
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## 962
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## 963
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## 964
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## 965
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## 967
        -4.0777131 1.50464530
                                   -405.7357
## 968
       -4.0777131 1.50464531
                                   -405.7357
```

```
-4.0777131 1.50464531
                                   -405.7357
## 970
        -4.0777131 1.50464531
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## 971
        -4.0777131 1.50464531
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## 972
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## 973
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## 974
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## 976
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## 977
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## 978
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## 980
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## 982
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## 984
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## 986
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## 990
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## 991
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## 992
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## 993
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## 994
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## 995
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## 996
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## 997
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## 998
        -4.0777132 1.50464535
                                   -405.7357
## 999
        -4.0777132 1.50464535
                                   -405.7357
## 1000 -4.0777132 1.50464535
                                   -405.7357
## 1001 -4.0777132 1.50464536
                                   -405.7357
```

After iterating 1000 times, we can see our result of b0 is -4.077132, and b1 is 1.50464534, which are also close to glm() result.