

MASARYK UNIVERSITY  
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# Similarity of programming problems

BACHELOR'S THESIS

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*This is where a copy of the official signed thesis assignment and a copy of the Statement of an Author is located in the printed version of the document.*



## **Declaration**

Hereby I declare that this paper is my original authorial work, which I have worked out on my own. All sources, references, and literature used or excerpted during elaboration of this work are properly cited and listed in complete reference to the due source.

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**Advisor:** Radek Pelánek



## **Acknowledgements**

These are the acknowledgements for my thesis, which can span multiple paragraphs.

# **Abstract**

This is the abstract of my thesis, which can span multiple paragraphs.



## Keywords

similarity, metrics, programming, keyword2, ...



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# Introduction

Tutoring systems are computer-based systems designed to introduce users into various domains. They usually have large amount of items which enables them to provide personalized experience. To maintain this large pool of items efficiently we need to be able to decide which items are useful and which are not.

Besides Introduction and Conclusion chapters, this thesis is structured into three additional chapters. First chapter talks in general about problem of measuring similarity of programming problems. It explains difference between program and programming problem, which data we have available and techniques used for measuring similarity of problems. Second chapter advances level deeper and describe everything what is specific to data we used. First part of chapter describes programming environment of Robotanik and data from it. Second part focuses in detail on metrics we used in experiments. Last chapter gives overview of implementation and usage of metrics and their evaluation.



# 1 Similarity

In this chapter we will talk in general about questions in learning systems, and computing their similarity. Most of the chapter focuses on explaining what kinds of data are available when comparing questions in learning systems and techniques to do so. Last section describes goals of the thesis.

A lot of research has been dedicated to similarity in many different fields computer science like bioinformatics (sequence alignment, similarity matrix of proteins), information retrieval (document similarity), plagiarism detection and many more.

One closely related area is recommender systems which differs from problem similarity only slightly. Both areas are distinguishing users and items. Only difference is that we know how well user did while solving specific item and recommender systems use rating of the items.

Main difference is that we can use more data about problem. We also have some problem statement and data about performance of students when solving problem.

## 1.1 Items

In this work we use the term “items” (problems, questions, assignments) when we refer to single entry in educational system which users can answer to. Since many aspects of this work are generally applicable we decided to use this general term. In some learning systems this can refer to simple choice from two options in another complex tasks which user solves in matter of minutes. On other side of the spectrum are systems for teaching introductional programming. Users tend to spend few minutes solving each task and there is fewer of them.

To further specify the context of our research, we will describe characteristics of items. For computing similarity of items it is most important knowing which data are available to us. Therefore we describe items by sources of data can be used for measuring similarity.

## 1. SIMILARITY

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- **Item statement:** specification of the item that a learner should solve, e.g., as a natural language description of the task.
- **Item solutions:** details about solutions obtained from learners or sample solution to item.
- **Learner's performance:** for example item solving times, correctness of answer, number of attempts needed.

This description of item is broad enough to cover most of learning systems. In next chapters we will discuss two systems in particular - umimecesky a umimematiku.

### 1.2 Why is similarity of items useful

As we mentioned previously key part of learning solving of educational items.

### 1.3 Computing similarity of items

The general approach to measuring and using similarity of educational items

### 1.4 Used datasets

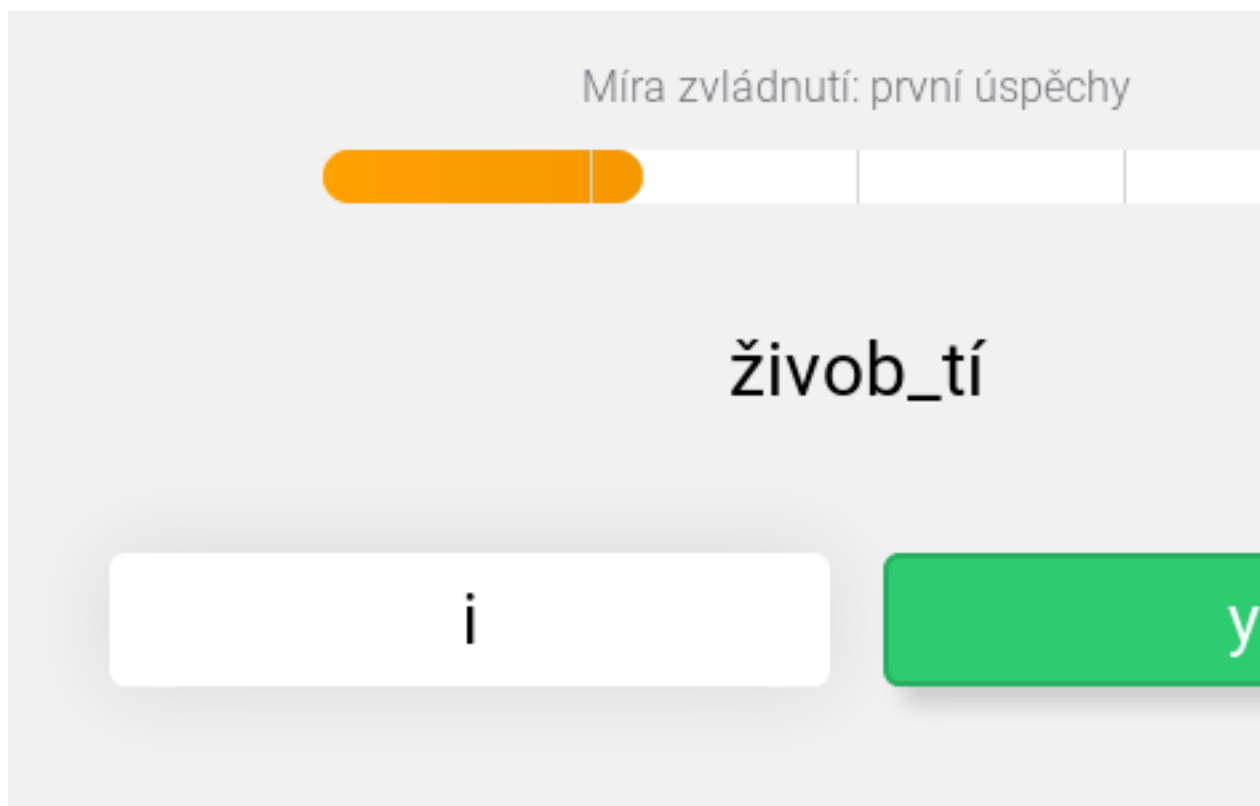
In our analysis we use both real data from educational system and simulated data. There is a reason why use both as only real-world data are useful for concluding any results. However evaluation of this data is often complicated as we do not know truth about many of their aspects. That's why we used simulated data for validating some of our conclusions. We will talk more in depth about how we generated simulated data in next chapter when describing their specific usage.

Most of used real-world data comes from system Umíme česky<sup>1</sup>. Later we have validated our results by also using data from its sibling

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1. <<https://umimecesky.cz/>>





system Umíme matiku<sup>2</sup>. We think it is useful as data come from another context but are provided in same format and therefore can be used directly in previously created tools.

#### 1.4.1 Umíme česky

Umíme česky<sup>3</sup> is system for practice of Czech grammar. System contains multiple exercise types, but in our analysis we use only one exercise - simple "fill-in-the-blank" with two possible answers. This type of exercise can be then viewed by student in multiple ways.

We focused only on "fill-in-the-blank" exercises but they can still be used to train many concepts of Czech grammar.

2. <<https://umimematiku.cz/>>

3. <<https://umimecesky.cz/>>

## 1. SIMILARITY

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### 1.4.2 Umíme matiku

## 2 Evaluation

it is hard to say anything about data when there is a lot of it we especially focused on systems which consist of 1000s of solvable items and even more users in cases like this it is not possible to look at data about each item individually possible with projection of many-dimensional data into 2 dimensions.

In general we want our projection to put similar items together. This can be achieved in many different ways. It is important to choose correct source of data and method of processing them prior to applying dimensionality reduction.

Figure 2.1 shows how common projection looks like. This particular projection shows 273 items of single concept from system. Each item is represented as one dot in the image and its proximity to others represents how similar they are.

### 2.1 Visible Properties of projection

we want to use results of calculated similarity and projections for managing item pool. That puts some constraints on how ideal results look like.

We want similar items to end as close to each other as possible. When using performance as data source this is especially items using same skill are projected near each other. E.g. figure 2.2 shows projection of questions about Czech language with highlighted a few similar words. This group consists of words which are based on single word with added suffix.

After looking at image you can notice some regularities.

#### 2.1.1 Computation of item similarity

To better understand how was this image created we have to understand how it is computed. We will describe it following section. This is default work-flow we used in most cases. Whenever we don't specify otherwise all projections were produced using this work-flow.

1. First step we have to do is converting raw logged information about user answers to performance matrix. This matrix consist

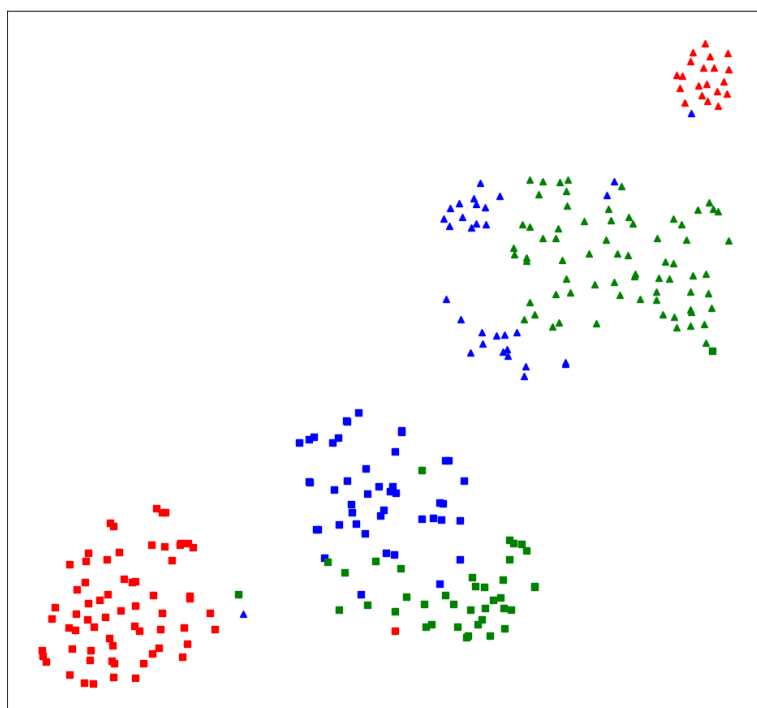


Figure 2.1: Basic projection of one knowledge component in Umíme česky

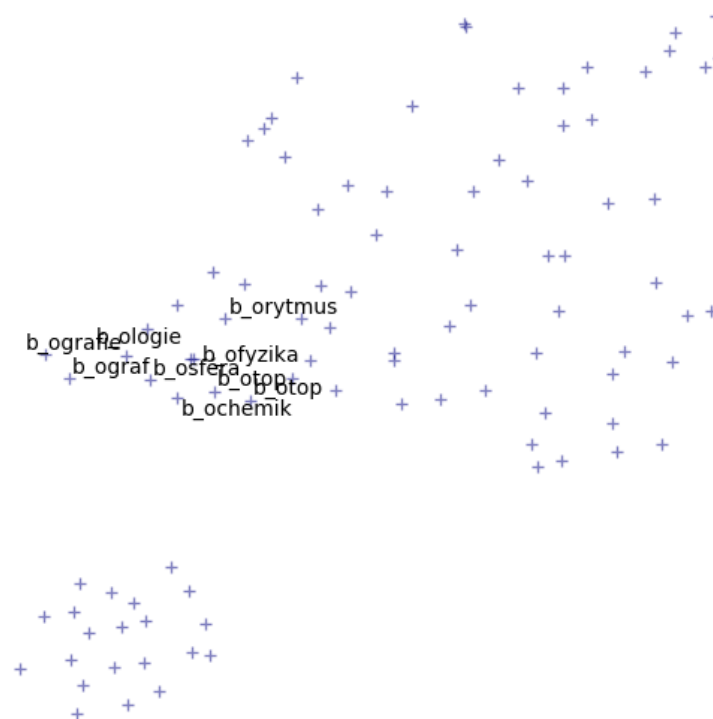


Figure 2.2: Similar words close to each other

of entries for each user-item pair. Columns of the matrix are items in educational system and each row of the matrix contains data about single user's performance. In most cases we used correctness of first users answer to specific item as his performance. This means value 1.0 in case of correct answer and 0.0 for incorrect. Another possible choice is to incorporate user solving time into this value. TODO possible choices are described in article [] Performance matrix is relatively sparse as it is not common for users to solve all the items in the system.

I tried using both first users answer and last in performance matrix. However there is no visible difference in resulting projection (same clusters are formed). This is clear when we compare first and last answers of users. There is only 5

2. Next step is computing similarity matrix. Matrix  $S$  is square matrix where each position  $S_{ij}$  denotes similarity of items  $i$  and  $j$ . In our case similarity is computed as correlation of two columns  $i$  and  $j$  in performance matrix. This means we look only at users who solved both items  $i$  and  $j$  and compute Pearson correlation coefficient of their performance.
3. The last (optional) step is producing 2D projection. This can be achieved by using many techniques for computing low dimensional projections.

We choose to use Principal component analysis (PCA) and there is several reasons for doing so. Result of PCA is deterministic. It produces same result for same input. This is not true for TSNA which is technique using machine learning and gradient descent for finding some local extreme. Stable results are more suitable for understanding data as there is one less variation to results caused by algorithm. It is easier to compare results when altering metrics used for computing item similarities.

First two principal components of PCA are then used for 2D visualizations.

We choose this specific work-flow as we think it is utilizing data about items which hold most information about their similarity. As other possible choices are item statement and solutions provided by students they do not hold as much information. Item statements in our particular exercises consist only of few Czech words. Also student solution is only choice from two provided options. Item statement and

solutions can be used more effectively in other contexts like programming, mathematics, physics, or chemistry.

This choice of work-flow is also relatively simple and easy to understand. It consists of few steps which can be studied separately and interchanged.

## 2.2 Level regularity

When you look back at figure 2.1 you can see that there are three colors of items. Most TODOknowledge components in system Umíme česky are spitted into multiple levels of difficulty. For this particular knowledge component there are three difficulty levels. First level is shown with red, second with green and third blue. This shows visible pattern in our data - each color (level) forms a distinct cluster. In following section we will try to explain factors that can affect resulting projections produced from real-world data.

As we mentioned before, only data about user performance (correctness of answers) are used when composing projections. And there is not a direct reason for this clusters of same levels to form as no information about belonging to particular level is presented to the algorithm.

Levels are not solved uniformly. It is not common for user to solve all three levels. Less experienced users tend to solve only first or first two levels. However typically older users solve only higher levels. Main cause for this is that system allows teachers to assign particular level of concepts as homework. Students then usually solve only this single level.

This phenomenon is not suitable for analysis of item similarity as it can cause misleading results. One particular example is when similar words are displayed far away from one another just because they belong to different levels. This is visible for words "bič" and "bičík" in problem set "Vyjmenovaná slova B".

### 2.2.1 Sparseness of performance matrix

For purpose of determining this, we designed an experiment. writing script that simulated answers provided by virtual students. Main

## 2. EVALUATION

problem we wanted to recreate was missing data in performance matrix. Each simulated user solved level and then with some probability continued to another. So most users answered only to one level, some users to 2 levels and only few to all 3 levels. Levels were chosen at random as users are not required to continue chronologically. Good enough as users do not solve levels in order from easy to hard. There are also users who solve only second or only highest difficulty level.

Results indicate that that structure of data can affect results only in really special cases. But this is not our case. The only case where projection is divided into clusters is when there is absolutely no performance data between any question of groups.

### 2.2.2 Users similarity projection

Insead we choose to analyse whether our data contains different groups of users. We are changing how we are looking at data. Up until now we used item-item similarity to calculate projection of items. Now we are going to to be using user-user similarity.

It is worth mentioning we will work with larger matrices as this forced us to do some optimalizations in code of our analysis. For example similariy matrix of items usualy has size between  $100 \times 100$  and  $300 \times 300$ . As we are looking only on items from single knowledge component. Hovewer user similarity matrix is square matrix with size around  $10000 \times 10000$ . This is also reason why current recommender systems use item similarity instead of user similarity. CITE

First attempt on projecting users can be seen in figure ??.

We say that user solved level when he answered at least 30 questions (which is 1/3 of questions for observed item set). Based on this we can divide users into 8 groups. We added color to each group so we can distinguish them in folowing plots easily.

Group: none	only 1st level	only 2nd level	only 3rd level	both 1th and 2nd	both 2nd and 3rd
red	green	blue	yellow	cyan	ma
4375	1285	1114	960	224	2

We can see that all formed custers of users contains in most cases users from single user group when we divide them by levels they solved. This brought us to more interesting discoveries. In general each level and each item has some mean performace. This is shown



in figure ???. Horizontal axis contains items sorted by level and mean performance. Vertical axis shows performance of each item. Given item sets have mean performance 94. After dividing users into 8 groups plot changes slightly. Some groups like "only 1st level" (its colored red and contains users who solved primarily first level and only few or none items from other levels) has much lower performance on other levels. We can conclude that users who tend to solve mostly first level are not as experienced as other users. On other hand users in group "both 2nd and 3rd" (cyan) are performing better than other users on all three levels.

At this point we have to return to simulation. We want to show that groups of users solving levels with different performance can cause forming of clusters of items from same level.

Answers are simulated pretty much same as in previous simulated experiments. We have 300 items divided into 3 levels. There is 3000 simulated users. Most of them solve levels with same skill but some 1/5 of users have smaller chance to solve second and third level. This is visible on item performance plot similar to one from real data.

Only changed variable was performance of some users for levels and this resulted in visible clusters in projection (figure ??).

From obtained information we can conclude that removing subnormal answers of users (few answers to other levels when they solved primarily one level) should remove clusters of levels.

But does it!?

### 2.3 Different performance metrics

We applied 4 different metrics for computing similarity matrix to verify that previous results aren't specific to single metric. Especially if it is true that similarity of items differ based on correct answer.

Pearson and yule produce almost identical results - this confirms previous research. This means plots produce same distinct clusters of answers and total similarities. However Jaccard measurement differs in this aspect. Similarity of items is not greater in one group of questions (based on correct answer).

Different methods for computing similarity may measure different aspects of items. This can be seen when using Jaccard and Sokal metrics.

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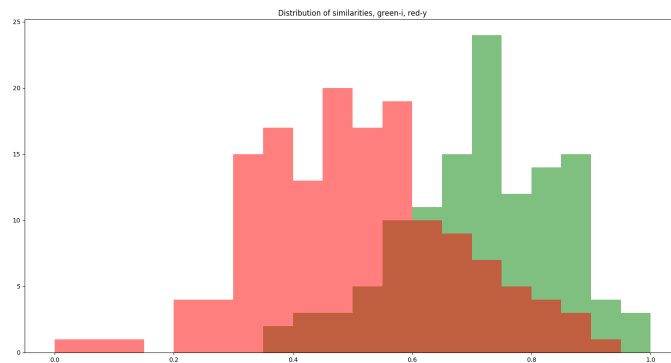


Figure 2.3: Histogram of similarities

Similarities provided by Jaccard metric differ greatly from other metrics. Resulting projection still shows same clusters of level and items are split based on correct answer but information is kept in another way than in correlation based metrics like Pearson.

On the other hand Sokal is heavily depending on performance of items. Items with higher performance are much more similar than items with lower performance. This is causing a packed cluster of first level (easy) and a spread out cluster of items from third level (harder).

### 2.4 Answer regularity

When exploring data, it may be useful to detect outsiders. It may be useful for multiple reasons [TODO cite]. In our particular case we declare an item an outsider when it is not similar to any other items in the problem set. It seems like a logical path to take.

In particular this means an item with a low sum of similarities to other items may be an outsider. This is where we encountered another regularity in data.

Sum of similarities is the sum of one column of the similarity matrix which we produced in our workflow for computing projection.

This is not specific to only one problem set (which was used in previous images), almost all problem sets display a similar pattern. However for some it is more distinct than for others. (Sets consisting of

items with many possible answers do not behave this way. But that is to be expected.)

Our next experiment was simulation of users preferring one answer in case they do not know what is the correct answer.

Answers are simulated for each user and question. There are no missing values. Answer is correct whenever random value is higher than logistic function of (users skill) - (difficulty of question). Half of questions has one correct answer and other half another answer. We used this to shift chance of answering correctly higher or lower (+0.1 for first answer and -0.1 for second).

Colors represent answer of each item (chance shifted up or down). There are formed visible clusters of same answers in result similar to real-world data. Using two uncorrelated skills cause clusters in projection. (When using only single skill for all questions results does not change and they are not required for this simulation.)

This is not specific to only one category (which was used in previous images), many more categories display similar pattern. However for some its more distinct than for others. For some distribution of similarities is same for all answers (psani-nn-a-n, vyjmenovana-slova-po-p,...).

I picked few which have very distinct answers and looked whether it is answer on left or on right in user interface.

We observed before that whole data set uses both answers the same but for single user this may not be true. There are even users who use only one answer as seen in following performance matrix. There is a line with all questions answered incorrectly for one answer and correctly for another.

We can filter this users out. Next three images show different levels of filtering. First uses no filtering at all (uses all users). Second and third image filter users by difference between performance on each answer. (So if users has same performance on question with both answers this value is 0.0 and when user uses only one of the answers (biggest possible difference) value is 1.0). Second image shows value of 0.3 (performance on one answer is 30% When we use only half of users which have uniform answers there are no clusters of question with same answers. (Half of users because median is used as filtering value.)

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We can look at histogram of difference between answers. For most of the users there is almost no difference but there are users with higher difference in performance between answers.

I look at difference between performance (amount of correctly answered questions) instead of usage of each answer because it is performance that affects calculated similarity of questions. However they should correlate somewhat. Another reason is that it is closer to simulated experiment so we can compare results directly.

When we simulated users we gave them all habit to use one answer more commonly. But not all users have this habit in real-world data. However there is quite large amount of users who do.

This resolves first problem we encountered but does not explain other regularities in data.

We succeeded in simulating data with clusters of same answers and showing that this is case in our real data. However there is still one more thing to explain - clusters of questions with same levels. Following same approach we can try to filter out users with large difference in how successful they are with solving different levels.

We used histogram of differences (variance of solved levels) to choose some value for filtering of users. As more than half of users solves only one level median of differences is 0.0. So we choose one value just by looking at histogram. We can see in following figure that this doesn't really matter as filtering users in this way does not help with eliminating clusters of same levels.

### 2.5 Second level of similarity

[Measuring Similarity of Educational Items Using Data on Learners' Performance] suggests applying one additional level of correlation to item similarity matrix. This means we are looking if items are behaving similarly with respect to other items. First two images (top) show data using only computed similarity of items. Second set of images shows same questions after applying Pearson correlation to similarity matrix. Plots on left show different possible answers (i/y) and plots on right difficulty levels of questions.

Applying one additional level of correlation to item similarity matrix was suggested [TODO]. This means we are looking whether

items are behaving similarly with respect to other items instead of similarity of user performance directly.

We can study possible usage of this technique little further

One approach is take a step back, do not use any similarity at all and compute projection directly from performance matrix. This is usually not useful as performance matrix has large amount of missing values and PCA works only with full matrices. However it is useful for exploring how adding computation of similarity affects projections.

We used only users who solved all questions.

## 2.6 User similarity

For explaining patterns of aquestions from same level we have to dig deeper and understand different fpgroups of users. One particular way how to acjive this is using owrkflow similar to previous. Althought there will be one difference, we will be using similarity of users instead of items. (item-item similarity matrix, user-user similarity matrix). This also meqns that we have to transpose performance matrix - so each column represents one user. Calculating correlarion between all columns gives us user similarity matrix. There is no difference in projection step, only used matrix is interexchnaged.

W pe ca.n try ploting this result directly using PCA. Hovewer we would notice that resulting image doesnt give us much information about users. reason for this is that two principal components reflect some property of data that we know about and dont wqnt to display. In particular users solving only one group are somewhat special. Columns representing users like this cannot be compared when they solved different levels - there is missinf information about their correlarion. PCA chooses this information with highest magnitude In presented figure this coresponds to choosen components reflecting solving of first and third level. (third principal domponent is corelates with solving of second level)

As users who solve only one level cause this behaviour. And they dont give us information about similarity of items in different levels we choose to exclude this users. After doing so we end up with projection similar to figure xx.

## 2. EVALUATION

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There are two visible clusters of users. Further analysis shows that difference between groups of users is caused by ?

### 2.7 Another context

### 3 Conclusion

We can conclude some recommendations. While trying to explain patterns in our particular used data we run into multiple situations which can repeat even when explaining some different data using similar techniques.

Technique we used for calculating projections is quite common in area of Adaptive learning and recommender systems. CITE.

Following section will summarize recommendations useful for explaining results - it is useful to look at both item and user similarity - some patterns in data can be results of habits of users. - we are using unsupervised learning like techniques - we obtain some results but it is hard to explain why they are like they are.. one possibility how to explain results is using simulations - we explained one possible way of simulating performance matrix - data come from users so identifying groups of users who behave same may be useful - we think most common groups which can be visible in data coming from online tutoring system are eager users and trolls - Main group of users tend to answer to questions in some regular pattern based on their knowledge while trolls follow different pattern (for example use same answer on all questions) - looking at total similarity of items - typically correlates with first dimension of PCA - variance of performance entries of items





## **A An appendix**

Here you can insert the appendices of your thesis.

