



УНИВЕРСИТЕТ ИТМО

Синтез на основе синтаксиса (Syntax-guided synthesis)

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Сириус

Образовательный центр

Санкт-Петербург, 2020



ITMO UNIVERSITY

Saint Petersburg, Russia

Syntax-guided synthesis (SyGuS)

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This logo should also
be in English...



Сириус

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Saint Petersburg, 2020

Syntax-Guided Program Synthesis

$$\exists f \in \mathbf{Exp}. \forall x. \mathbf{Spec}(f, x)$$

Spec – logical formula that captures the desired functionality of f

$$(f(x, y) \geq x) \wedge (f(x, y) \geq y) \wedge (f(x, y) \in \{x, y\}) \quad \text{[Semantics]}$$

Exp – set of expressions specified by a context-free grammar that captures the candidate implementations of f

$$\begin{aligned} \text{fInt} &::= x \mid 0 \mid 1 \mid +(f\text{Int}, f\text{Int}) \mid \text{ite}(f\text{Bool}, f\text{Int}, f\text{Int}) \\ \text{fBool} &::= >(f\text{Int}, f\text{Int}) \mid =(f\text{Int}, f\text{Int}) \mid \neg(f\text{Bool}) \end{aligned} \quad \text{[Syntax]}$$

Applications

- Programming by examples (PBE)
 - ↳ Given some inputs and outputs, find a desired function
- Superoptimizing compiler
 - ↳ Replace code with more efficient (yet equivalent!) code
- Side-channel attacks on cryptographic circuits
 - ↳ Auto-synthesize FSA-attack-resilient cryptographic circuits
- Template-guided invariant generation
- ... many more ...

Programming by Examples (PBE)

$A ::= 0 \mid 1 \mid x \mid (\text{bvnot } A)$
 $\mid (\text{shl1 } A) \mid (\text{shr1 } A) \mid (\text{shr4 } A) \mid (\text{shr16 } A)$
 $\mid (\text{bvand } A A) \mid (\text{bvor } A A) \mid (\text{bvxor } A A)$
 $\mid (\text{bvadd } A A) \mid (\text{if0 } A A A)$

Grammar

Solution
(size = 29)

$f := \lambda x.$
 $(\text{if0 } (\text{bvand } (\text{bvnot } x) \text{ \#x00000000000000000001})$
 $(\text{if0 } (\text{bvand } (\text{bvnot } (\text{shr4 } x)) \text{ \#x00000000000000000001})$
 $(\text{if0 } (\text{bvand } (\text{shr1 } (\text{shr16 } x)) \text{ \#x00000000000000000001})$
 $(\text{if0 } (\text{bvand } (\text{bvnot } (\text{shr1 } x)) \text{ \#x00000000000000000001}) (\text{bvor } \text{ \#x00000000000000000001 } x) x)$
 $(\text{if0 } (\text{bvand } (\text{bvnot } (\text{shr1 } x)) \text{ \#x00000000000000000001}) x$
 $(\text{if0 } (\text{bvand } (\text{shr16 } x) \text{ \#x00000000000000000001}) x (\text{bvor } \text{ \#x00000000000000000001 } x))))$
 $(\text{if0 } (\text{bvand } (\text{shr1 } (\text{shr16 } x)) \text{ \#x00000000000000000001}) (\text{bvor } \text{ \#x00000000000000000001 } x) x))$
 $(\text{bvor } \text{ \#x00000000000000000001 } x))$

Examples
(inputs and outputs)

$\exists f.$

$f(\text{\#x28085a970e13e12c}) = \text{\#x28085a970e13e12d}$

$f(\text{\#xbe5341bebd2a0749}) = \text{\#xbe5341bebd2a0749}$

...

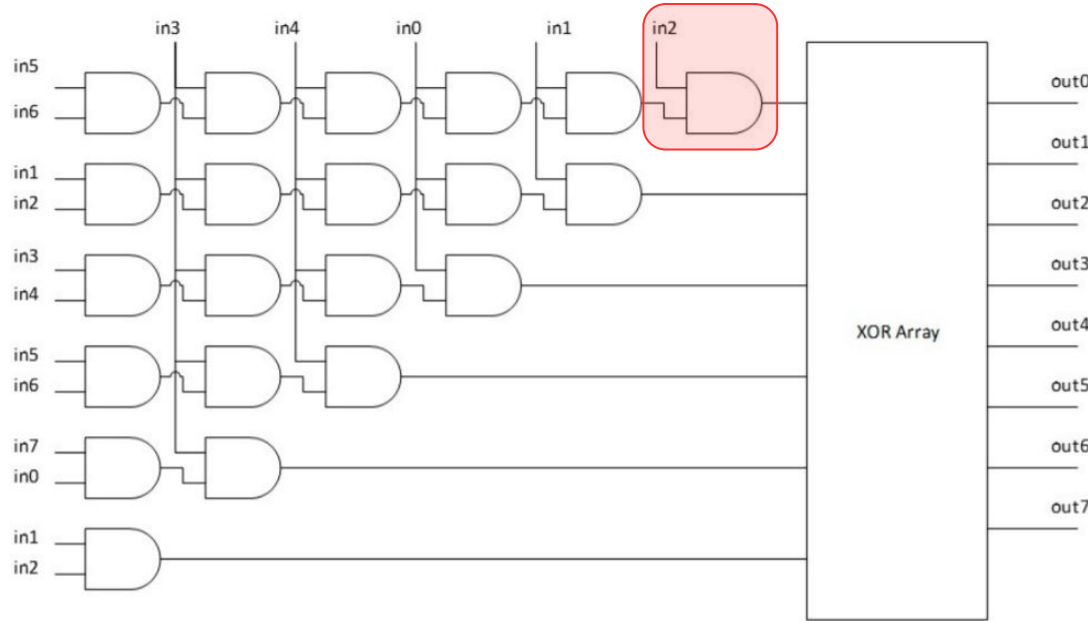
$f(\text{\#xcd67bd5beaac575e}) = \text{\#xcd67bd5beaac575e}$

Superoptimizing Compiler

```
multiply (x[1,n], y[1,n]) {  
    x1 = x[1,n/2];  
    x2 = x[n/2+1, n];  
    y1 = y[1, n/2];  
    y2 = y[n/2+1, n];  
    a = x1 * y1;  
    b = shift( x1 * y2, n/2);  
    c = shift( x2 * y1, n/2);  
    d = shift( x2 * y2, n);  
    return ( a + b + c + d)  
}
```

Replace with equivalent code
with only 3 multiplications

Side-channel Attacks on Cryptographic Circuits



Countermeasures:

1. Add delays to inputs
 - ↳ Verification problem
2. Auto-synthesize
 - ↳ the equivalent circuit
(**semantic constraint**),
 - ↳ where all input-to-output paths have the same length
(**syntactic constraint**)

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Synthesis Conjectures

$$\exists f. \forall x. P(f, x)$$

“There exists a function f for which property P holds for all x ”

conjecture

/kənˈdʒektʃə/

See definitions in:

All

Logic

Literature

noun

an opinion or conclusion formed on the basis of incomplete information.
“conjectures about the newcomer were many and varied”

Similar:

guess

speculation

surmise

fancy

notion

belief



Synthesis Conjectures Modulo T

$$\exists f. \forall x. P(f, x)$$

“There exists a function f for which property P holds for all x ”

Property is in some **background theory T** , for example:

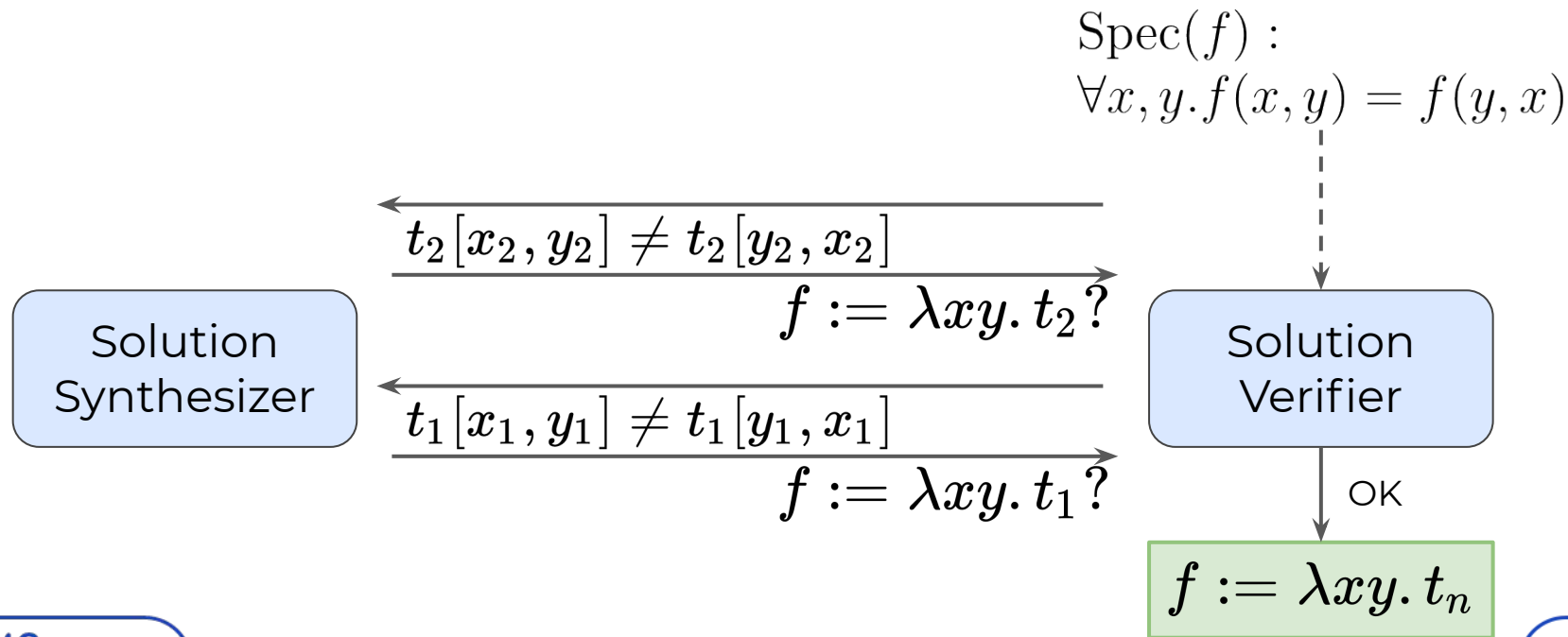
- Linear or non-linear arithmetics (LIA, NIA)
- Fixed-width bit-vectors (BV)
- Strings
- ...

⇒ **Satisfiability Modulo Theories (SMT)**

Approaches to Synthesis

- Naïve
 - Let f – free uninterpreted function (UF)
 - Use SMT solvers to find a model for f
 - Hard for SMT solvers :c
- Counterexample-guided Inductive Synthesis (CEGIS)
 - Enumerative
 - Symbolic
 - Stochastic
- Counterexample-guided quantifier instantiation (CEGQI)
 - https://doi.org/10.1007/978-3-319-21668-3_12

Counterexample-guided Inductive Synthesis (CEGIS)



Enumerative CEGIS

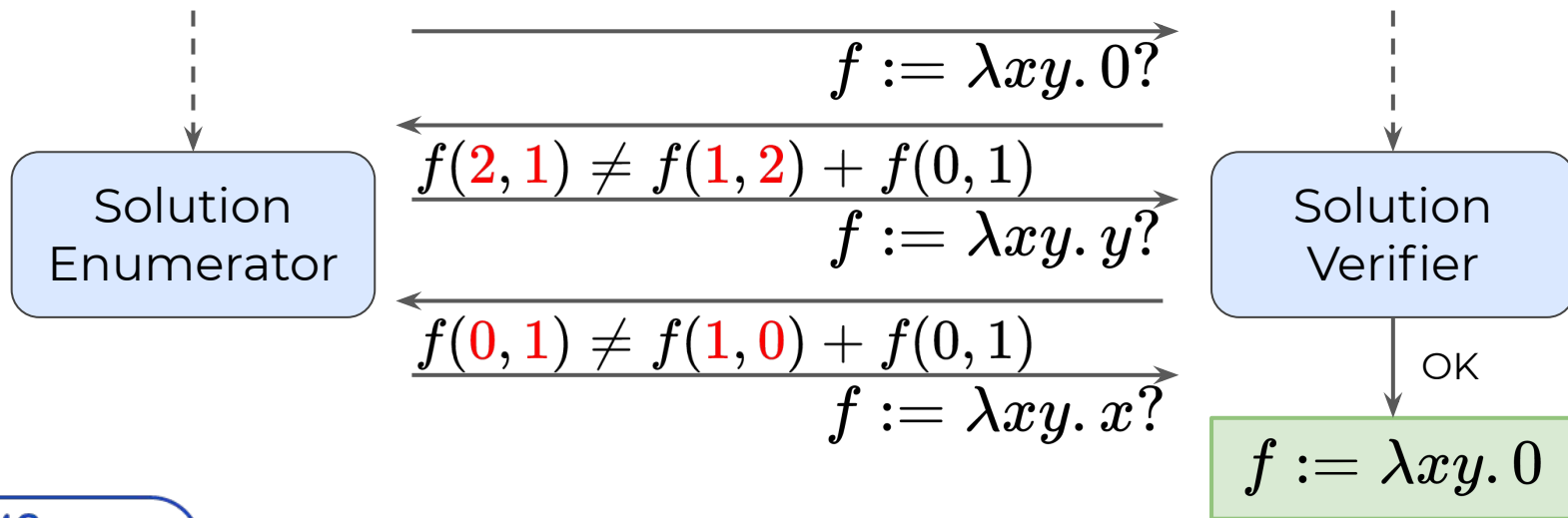
Syntax(f) :

$A ::= A+A \mid \neg A \mid x \mid y \mid 0 \mid 1 \mid \text{ite}(B,A,A)$

$B ::= B \wedge B \mid \neg B \mid A=A \mid A \geq A \mid \perp$

Spec(f) :

$\forall x, y. f(x, y) = f(y, x) + f(0, 1)$



Enumerative CEGIS + Unification

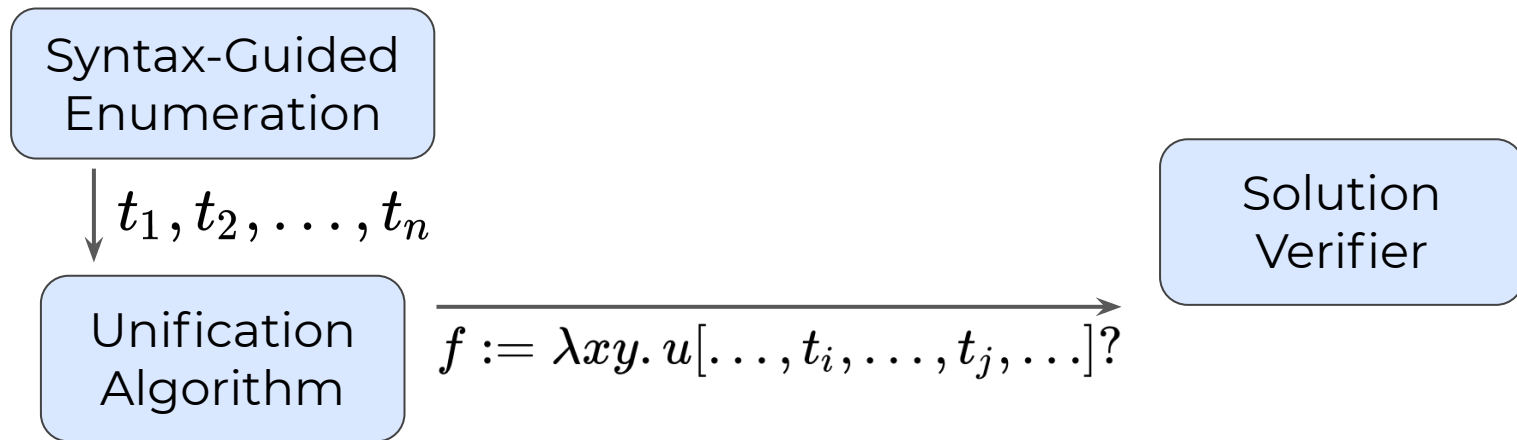
Syntax(f) :

$A ::= A+A \mid -A \mid x \mid y \mid 0 \mid 1 \mid \text{ite}(B,A,A)$

$B ::= B \wedge B \mid \neg B \mid A=A \mid A \geq A \mid \perp$

Spec(f) :

$\forall x, y. f(x, y) = f(y, x)$



CEGIS using SMT Solver

Syntax(f) :

$A ::= A+A \mid -A \mid x \mid y \mid 0 \mid 1 \mid \text{ite}(B,A,A)$

$B ::= B \wedge B \mid \neg B \mid A=A \mid A \geq A \mid \perp$

Syntax-Guided
Enumeration

Unification
Algorithm

Spec(f) :

$\forall x, y. f(x, y) = f(y, x)$

Solution
Verifier

SMT Solver

CEGIS inside an SMT Solver

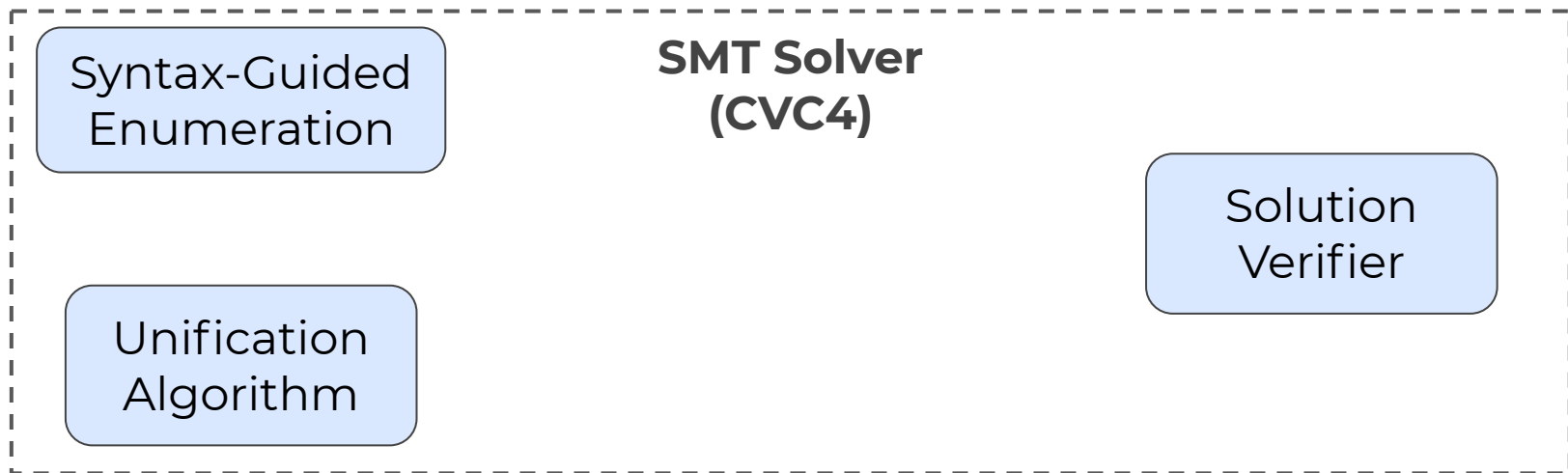
Syntax(f) :

$A ::= A+A \mid -A \mid x \mid y \mid 0 \mid 1 \mid \text{ite}(B,A,A)$

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Spec(f) :

$\forall x, y. f(x, y) = f(y, x)$

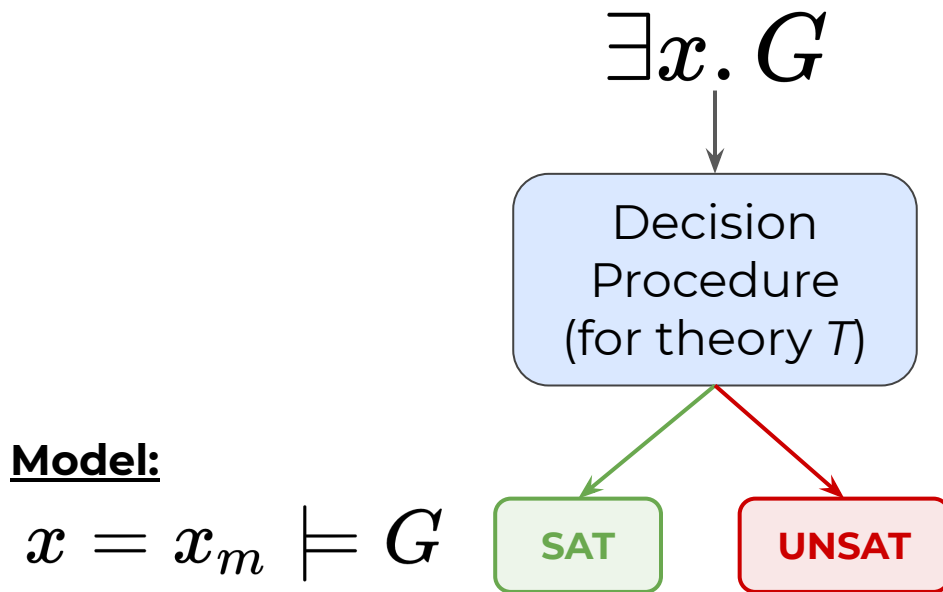


Enumerative Synthesis in SMT Solvers

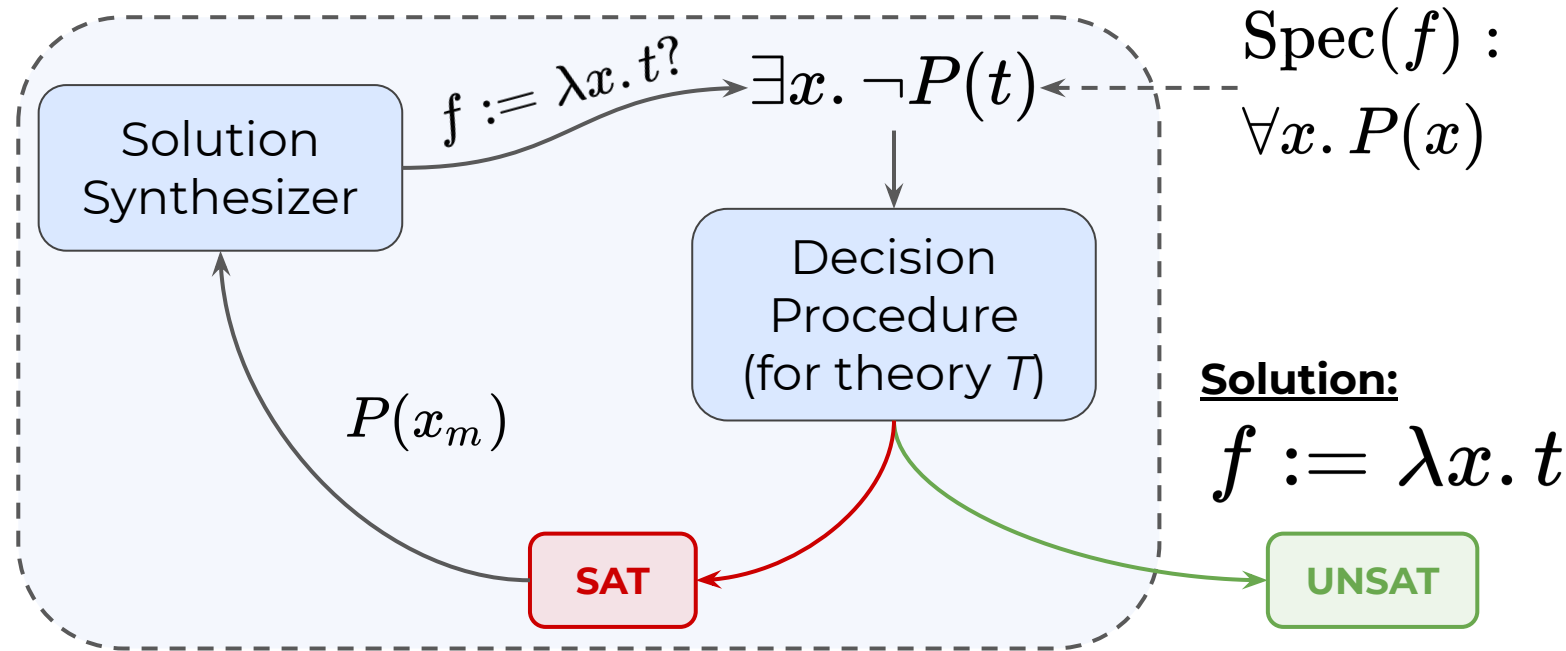
$\text{synth}(\exists f. \forall x. P(f, x))$:

1. Syntax-guided enumeration
 - ↳ Construct a set of “interesting” terms $\{t_1 \dots t_n\}$
2. Unification algorithms (https://doi.org/10.1007/978-3-662-54577-5_18)
 - ↳ From $\{t_1 \dots t_n\}$, construct candidate u for f
3. (Decision) Procedures
 - ↳ Check whether u satisfies the specification:
“Is $\neg \forall x. P(u, x)$ T -unsatisfiable?” $\Rightarrow \neg P(u, x_m)$

From Decision Procedures to Synthesis Procedures



From Decision Procedures to Synthesis Procedures



Ufff... Enough theory.

Demo time

Links

- <https://sygus.org/>
 - SyGuS specification: https://sygus.org/assets/pdf/SyGuS-IF_2.0.pdf
- <https://cvc4.github.io/>
 - Online playground: <https://cvc4.github.io/app>
- <http://smtlib.cs.uiowa.edu/>
 - Logics: <http://smtlib.cs.uiowa.edu/logics.shtml>
 - SMT specification: <http://smtlib.cs.uiowa.edu/language.shtml>
- ...

(Minimal) Boolean Formula Synthesis

```
(synth-fun f ((x Bool) (y Bool) (z Bool)) Bool
  ((Start Bool)) (
    (Start Bool (
      x y z
      (not Start)
      (and Start Start)
      (or Start Start)
    ))
  ))
```

<https://gist.github.com/Lipen/1bbf6586ad180ef8334a5e5a7efa1576>

; $f(x,y,z) = x \mid (y \& z) = 00011111$

```
(constraint (= (f' 0 0 0) 0 ))
(constraint (= (f' 0 0 1) 0 ))
(constraint (= (f' 0 1 0) 0 ))
(constraint (= (f' 0 1 1) 1 ))
(constraint (= (f' 1 0 0) 1 ))
(constraint (= (f' 1 0 1) 1 ))
(constraint (= (f' 1 1 0) 1 ))
(constraint (= (f' 1 1 1) 1 ))
```

; Solution: (or x (and y z))

Thanks for your attention.

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