

## Informatics II, Spring 2023, Solution 7

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### Task 1.

1. PUSH(4) — 4  
PUSH(1) — 4 1  
PUSH(3) — 4 1 3  
POP() — 4 1  
PUSH(8) — 4 1 8  
POP() — 4 1

2. ENQUEUE(4) — 4  
ENQUEUE(1) — 4 1  
ENQUEUE(3) — 4 1 3  
DEQUEUE() — 1 3  
ENQUEUE(8) — 1 3 8  
DEQUEUE() — 3 8

3. The first stack starts at 1 and grows up towards  $n$ , while the second starts from  $n$  and decreases to 1. Stack overflow happens when an element is pushed when the two stack pointers are adjacent.

4. ENQUEUE:  $\Theta(1)$ .

DEQUEUE: worst  $O(n)$ , amortized  $\Theta(1)$ (on average).

Let the two stacks be  $A$  and  $B$ .

ENQUEUE pushes elements on  $B$ . ENQUEUE is always  $\Theta(1)$ . DEQUEUE pops elements from  $A$ . If  $A$  is empty, the contents of  $B$  are transferred to  $A$  by popping them out of  $B$  and pushing them to  $A$ . That way, they appear in reverse order and are popped in the original order.

DEQUEUE operation can perform in  $\Theta(n)$  time, but that will happen only when  $A$  is empty. If many ENQUEUEs and DEQUEUEs are performed, the total time will be linear to the number of elements. For example, we ENQUEUE  $n$  elements and DEQUEUE  $n$  elements. All  $n$  elements are transferred from  $B$  to  $A$  only once, so in total  $n$  times. The amortized complexity of DEQUEUE =  $n / n = 1$ , which is  $\Theta(1)$ (on average).

5. PUSH:  $\Theta(1)$ .

POP:  $\Theta(n)$ .

We have two queues —  $q_1$  and  $q_2$ . PUSH operation always enqueues elements in  $q_1$ . Assume that  $q_1$  contains  $i$  elements:  $e_1, \dots, e_i$ . POP operation: (1) dequeue  $e_1, \dots, e_{i-1}$  elements and remain element  $e$  in  $q_1$  (2) enqueue  $e_1, \dots, e_{i-1}$  in order to  $q_2$ . (3) dequeue  $e$  from  $q_1$  and return  $e$ .

The PUSH operation is  $\Theta(1)$ . The POP operation is  $\Theta(n)$  where  $n$  is the number of elements in the stack. In other words, there are  $n$  elements in  $q_1$ .

## Task 2.

### 1.

```
1  #include <stdio.h>
2  #define SIZE 10
3
4  int stack[SIZE];
5  int top = -1;
6
7  void push(int value)
8  {
9      if(top<SIZE-1)
10     {
11         if (top < 0)
12         {
13             stack[0] = value;
14             top = 0;
15         }
16         else
17         {
18             stack[top+1] = value;
19             top++;
20         }
21     }
22     else
23     {
24         printf("Stackoverflow!!!\n");
25     }
26 }
27
28 int isempty()
29 {
30     return top<0;
31 }
32
33 int pop()
34 {
35     if(!isempty())
36     {
37         int n = stack[top];
38         top--;
39         return n;
40     }
41     else
42     {
43         printf("Error: the stack is empty!\n");
44         return -99999;
45     }
46 }
47
48 int Top()
49 {
50     if (!isempty())
51     {
52         return stack[top];
53     }
54     else
55     {
56         printf("Error: the stack is empty!\n");
57         return -99999;
58     }
59 }
60
61 void display()
62 {
63     int i;
64     for(i=0;i<=top;i++)
65     {
```

```
66     printf("%d",stack[i]);
67 }
68 printf("\n");
69 }
70
71 int main()
72 {
73     push(4);
74     push(8);
75     printf("isempty:_%d\n", isempty());
76     printf("Top:_%d\n", Top());
77     display();
78
79     pop();
80     printf("\nisempty:_%d\n", isempty());
81     printf("Top:_%d\n", Top());
82     display();
83
84     pop();
85     printf("\nisempty:_%d\n", isempty());
86     printf("Top:_%d\n", Top());
87     display();
88
89     pop();
90
91     return 0;
92 }
```

## 2.

```
1  #include <stdio.h>
2  #define MAXSIZE 10
3
4  int queue[MAXSIZE];
5
6  int front = -1;
7  int rear = -1;
8  int size = -1;
9
10 int isempty()
11 {
12     return size <= 0;
13 }
14
15 int isfull()
16 {
17     return size == MAXSIZE;
18 }
19
20 void enqueue(int value)
21 {
22     if(size < MAXSIZE)
23     {
24         if(isempty())
25         {
26             queue[0] = value;
27             front = rear = 0;
28             size = 1;
29         }
30         else if(rear == MAXSIZE-1)
31         {
32             queue[0] = value;
33             rear = 0;
34             size++;
35         }
36         else
37         {
38             queue[rear+1] = value;
39             rear++;
40             size++;
41         }
42     }
43     else
44     {
45         printf("Queue is full\n");
46     }
47 }
48
49 int Front()
50 {
51     if(isempty())
52     {
53         printf("Queue is empty\n");
54         return -1;
55     }
56     else
57     {
58         return queue[front];
59     }
60 }
61
62 int dequeue()
63 {
64     int ret = Front();
65     size--;
66     front++;
67     if (front == MAXSIZE) {
68         front = 0;
```

```
69     }
70     return ret;
71 }
72
73 void display()
74 {
75     if(isempty())
76     {
77         printf("Queue is empty\n");
78         return;
79     }
80
81     int i;
82     if(rear>=front)
83     {
84         for(i=front;i<=rear;i++)
85         {
86             printf("%d,",queue[i]);
87         }
88     }
89     else
90     {
91         for(i=front;i<MAXSIZE;i++)
92         {
93             printf("%d,",queue[i]);
94         }
95         for(i=0;i<=rear;i++)
96         {
97             printf("%d,",queue[i]);
98         }
99     }
100     printf("\n");
101 }
102
103 int main()
104 {
105     display();
106     enqueue(4);
107     enqueue(8);
108     enqueue(10);
109     enqueue(20);
110     display();
111     dequeue();
112     printf("After dequeue\n");
113     display();
114     enqueue(50);
115     enqueue(60);
116     enqueue(70);
117     enqueue(80);
118     dequeue();
119     enqueue(90);
120     enqueue(100);
121     enqueue(110);
122     enqueue(120);
123     enqueue(130);
124     enqueue(140);
125     enqueue(150);
126     printf("After enqueue\n");
127     display();
128     dequeue();
129     printf("After dequeue\n");
130     display();
131     enqueue(160);
132     printf("After enqueue\n");
133     display();
134     return 0;
135 }
```

3.

```
1 #include <stdio.h>
2 #include <stdlib.h>
3 #define TRUE 1
4 #define FALSE 0
5
6 struct node
7 {
8     int data;
9     struct node *next;
10 };
11 typedef struct node node;
12
13 node *top;
14
15 void initialize()
16 {
17     top = NULL;
18 }
19
20 void push(int value)
21 {
22     node *tmp;
23     tmp = malloc(sizeof(node));
24     tmp -> data = value;
25     tmp -> next = top;
26     top = tmp;
27 }
28
29 int pop()
30 {
31     node *tmp;
32     int n;
33     tmp = top;
34     n = tmp->data;
35     top = tmp->next;
36     free(tmp);
37     return n;
38 }
39
40 int Top()
41 {
42     return top->data;
43 }
44
45 int isempty()
46 {
47     return top==NULL;
48 }
49
50 void display(node *head)
51 {
52     if(head == NULL)
53     {
54         printf("NULL\n");
55     }
56     else
57     {
58         printf("%d, ", head -> data);
59         display(head->next);
60     }
61 }
62
63 int main()
64 {
65     initialize();
66     push(10);
67     push(20);
68     push(30);
```

```
69 | printf("The_top_is_%d\n",Top());  
70 | pop();  
71 | printf("The_top_after_pop_is_%d\n",Top());  
72 | display(top);  
73 | return 0;  
74 | }
```

4.

```
1 #include <stdio.h>
2 #include <stdlib.h>
3 #define TRUE 1
4 #define FALSE 0
5 #define FULL 10
6
7 struct node
8 {
9     int data;
10    struct node *next;
11 };
12 typedef struct node node;
13
14 struct queue
15 {
16     int count;
17     node *front;
18     node *rear;
19 };
20 typedef struct queue queue;
21
22 void initialize(queue *q)
23 {
24     q->count = 0;
25     q->front = NULL;
26     q->rear = NULL;
27 }
28
29 int isempty(queue *q)
30 {
31     return (q->rear == NULL);
32 }
33
34 void enqueue(queue *q, int value)
35 {
36     if (q->count < FULL)
37     {
38         node *tmp;
39         tmp = malloc(sizeof(node));
40         tmp->data = value;
41         tmp->next = NULL;
42         if (!isempty(q))
43         {
44             q->rear->next = tmp;
45             q->rear = tmp;
46         }
47         else
48         {
49             q->front = q->rear = tmp;
50         }
51         q->count++;
52     }
53     else
54     {
55         printf("List is full\n");
56     }
57 }
58
59 int dequeue(queue *q)
60 {
61     node *tmp;
62     int n = q->front->data;
63     tmp = q->front;
64     q->front = q->front->next;
65     q->count--;
66     free(tmp);
67     return(n);
68 }
```



```
69
70 void display(node *head)
71 {
72     if(head == NULL)
73     {
74         printf("NULL\n");
75     }
76     else
77     {
78         printf("%d,", head -> data);
79         display(head->next);
80     }
81 }
82
83 int main()
84 {
85     queue *q;
86     q = malloc(sizeof(queue));
87     initialize(q);
88     enqueue(q,10);
89     enqueue(q,20);
90     enqueue(q,30);
91     printf("Queue before dequeue\n");
92     display(q->front);
93     dequeue(q);
94     printf("Queue after dequeue\n");
95     display(q->front);
96     return 0;
97 }
```

**Task 3.**

**Algorithm:** REVERSEVEN( $Q$ )

---

```
S = initStack()
qSize = queueSize(Q)
for  $i = 1$  to  $qSize$  do
    val = deQueue(Q)
    if  $val \% 2 == 0$  then
        | push(S, val)
    | enQueue(val)
for  $i = 1$  to  $qSize$  do
    val = deQueue(Q)
    if  $val \% 2 == 0$  then
        | enQueue(Q, pop(S))
    else
        | enQueue(val)
```