

#task1

restart;

with(DEtools) :

expr := diff(y(x), x) = 2 + (y(x))<sup>2</sup>;

$$\text{expr} := \frac{d}{dx} y(x) = 2 + y(x)^2 \quad (1)$$

solution := combine(dsolve({expr, y(1) = 2}), trig);

$$\text{solution} := y(x) = \sqrt{2} \tan(\arctan(\sqrt{2}) + \sqrt{2} x - \sqrt{2}) \quad (2)$$

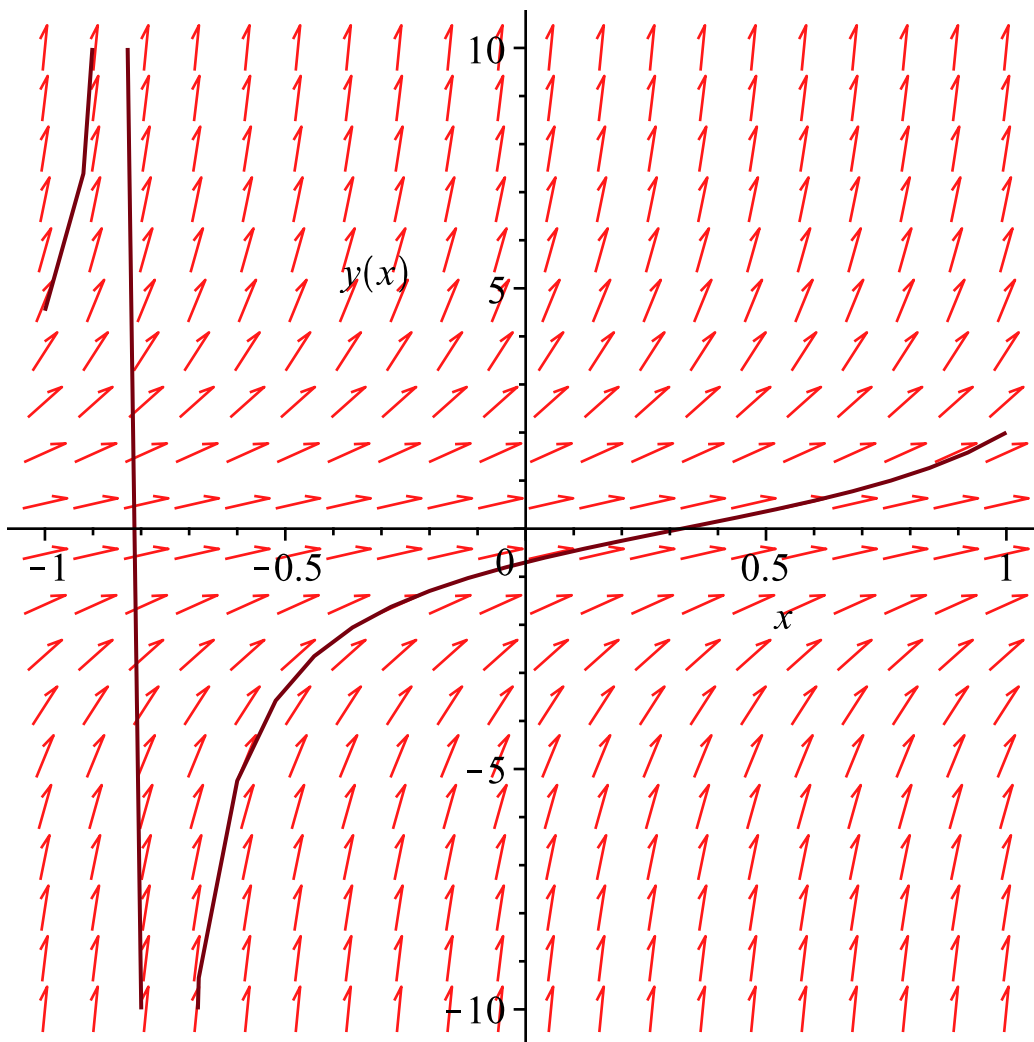
xr := -1 .. 1 :

yr := -10 .. 10 :

p1 := dfielfplot(expr, y(x), x = xr, y = yr) :

p2 := plots[implicitplot](solution, x = xr, y = yr) :

plots[display](p1, p2);



#task2

#1)

restart;

a := 20;

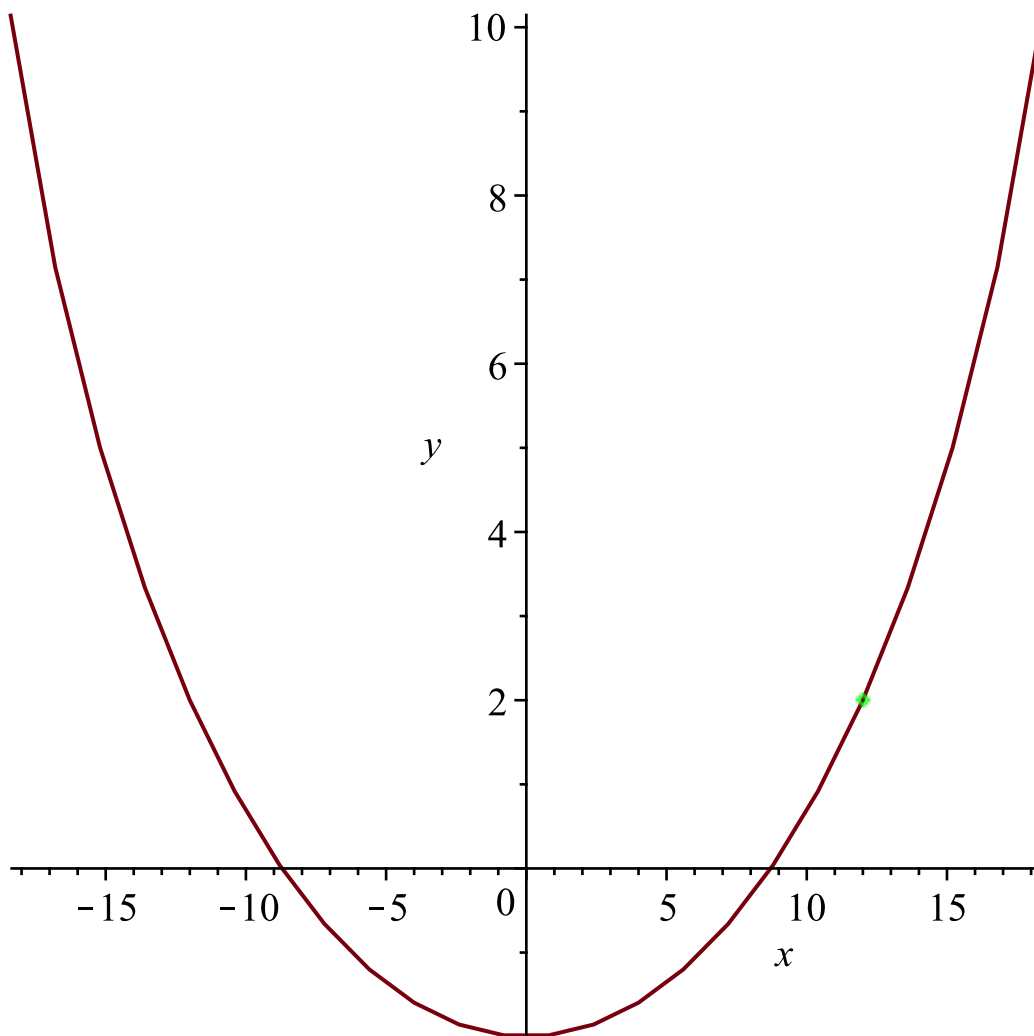
f := combine(dsolve({diff(y(x), x) =  $\frac{x}{\text{sqr}t(a^2 - x^2)}$ , y(12) = 2}), trig);

$$a := 20$$

$$f := y(x) = \frac{x^2 + 18\sqrt{-x^2 + 400} - 400}{\sqrt{-x^2 + 400}}$$

(3)

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p1 := plots[implicitplot](f, x=-20..20, y=-20..20) :
p2 := plot([[12, 2]], style=point, color=green) :
plots[display](p1, p2);
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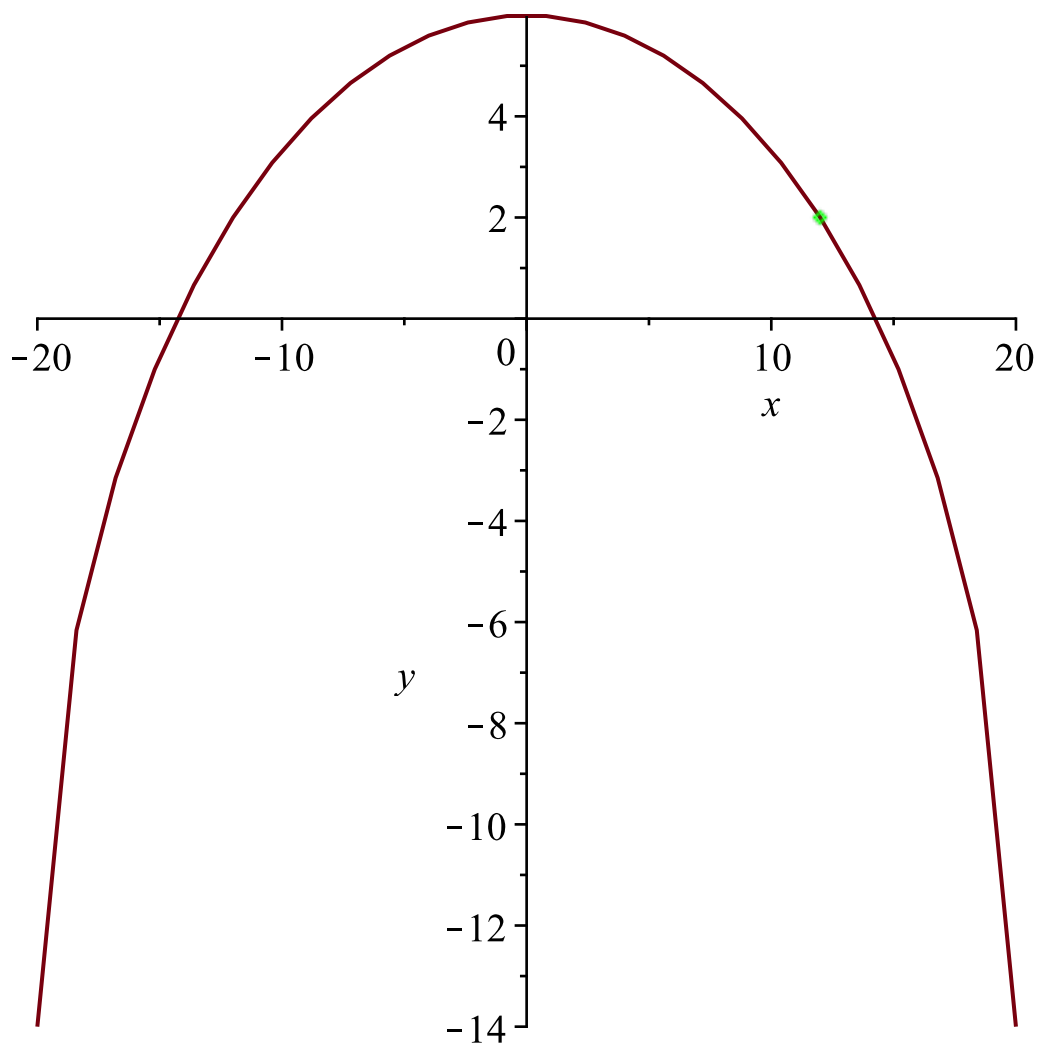


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f := combine( dsolve( { diff(y(x), x) = - x / sqrt(a^2 - x^2) , y(12) = 2 } ), trig );
```

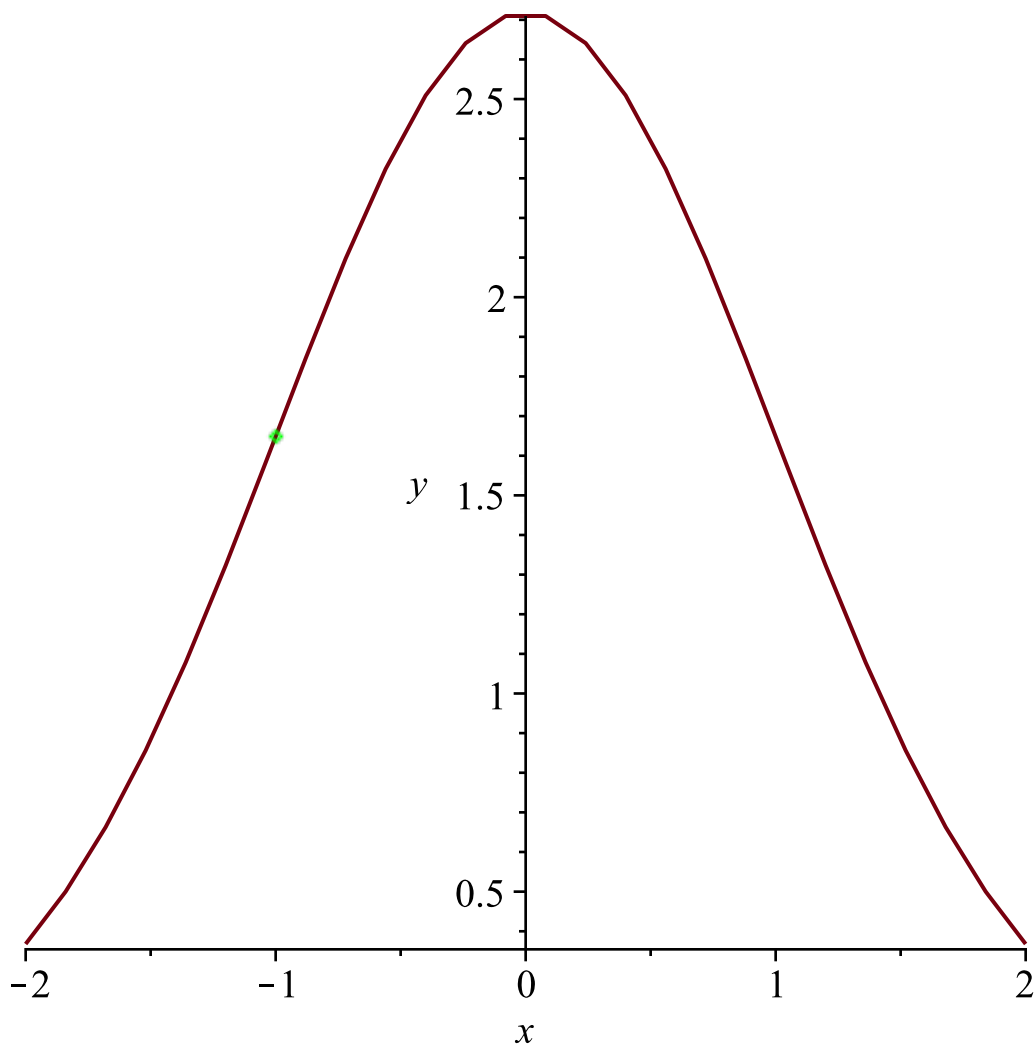
$$f := y(x) = \sqrt{-x^2 + 400} - 14$$

(4)

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p1 := plots[implicitplot](f, x=-20..20, y=-20..20) :
p2 := plot([[12, 2]], style=point, color=green) :
plots[display](p1, p2);
```



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#2)
restart;
a := -1 :
rez := simplify( dsolve( { d/dx y(x) = x*y(x)/a, y(-1) = exp(1/2) } ) ) :
p1 := plots[implicitplot](rez, x=-2..2, y=-10..10) :
p2 := plot( [ [ -1, exp(1/2) ] ], style=point, color=green ) :
plots[display](p1, p2);
```



#task3  
restart;

$$\text{expr} := \text{diff}(y(x), x) = \frac{-10 \cdot x + 26 \cdot y(x) - 16}{37 \cdot x + y(x) - 38};$$

$$\text{expr} := \frac{d}{dx} y(x) = \frac{-10x + 26y(x) - 16}{37x + y(x) - 38} \quad (5)$$

dsolve(expr);

sol := dsolve({expr, y(2) = 0})

$$-4 \ln\left(-\frac{y(x) - 2 + x}{x - 1}\right) + 3 \ln\left(-\frac{y(x) - 11 + 10x}{x - 1}\right) - \ln(x - 1) - \_C1 = 0$$

$$\text{sol} := y(x) = 2 - x \quad (6)$$

solve({-10·x + 26·y - 16 = 0, 37·x + y - 38 = 0});

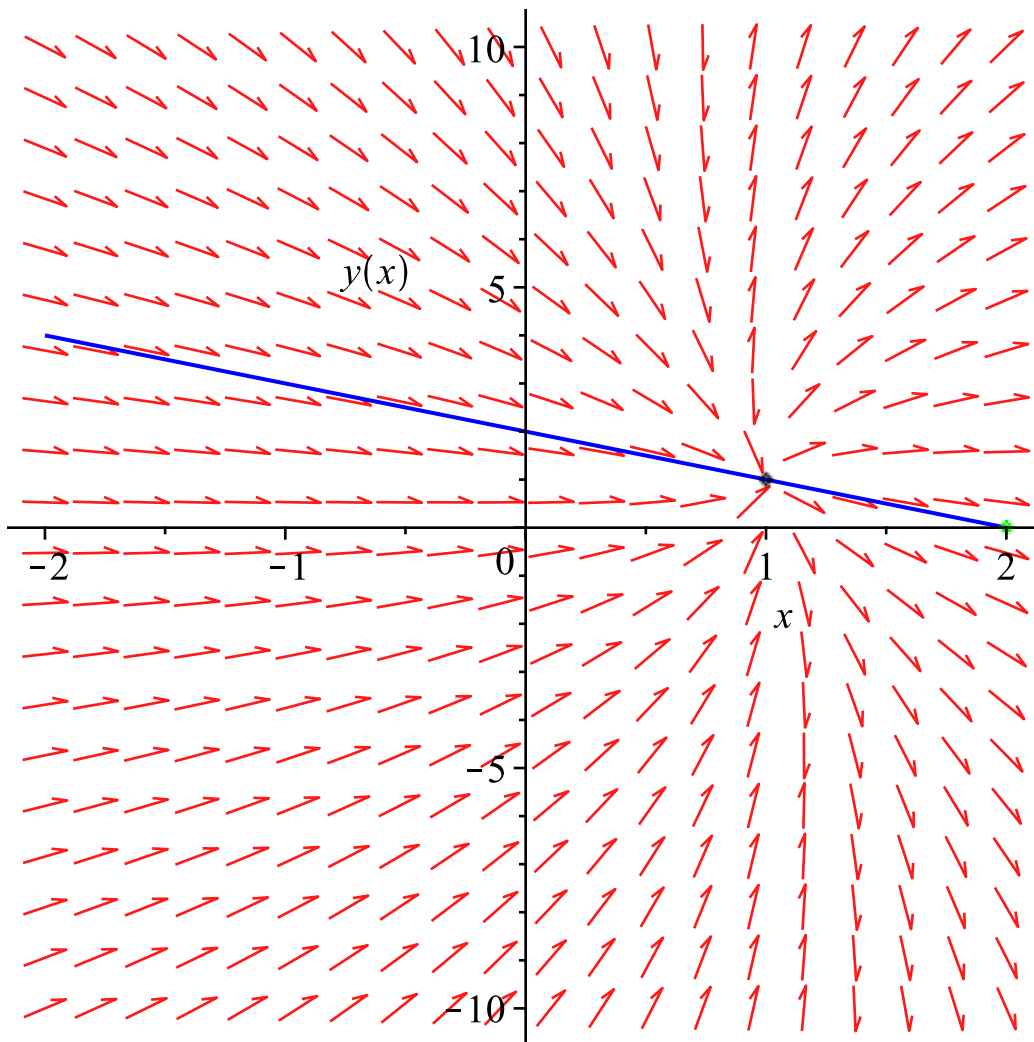
$$\{x = 1, y = 1\} \quad (7)$$

p1 := DEtools[dfieldplot](expr, y(x), x = -2..2, y = -10..10) :

p2 := plots[implicitplot](sol, x = -2..2, y = -10..10, color = blue) :

p3 := plots[pointplot]([ [2, 0], [1, 1] ], color = [green, black]) :

plots[display](p1, p2, p3);



#task4

restart;

$expr := 2(x \cdot y' + y) = x \cdot y^2;$

$$expr := 2x \left( \frac{d}{dx} y(x) \right) + 2y(x) = x y(x)^2 \quad (8)$$

$sol := dsolve(\{expr, y(1) = 2\});$

$$sol := y(x) = -\frac{2}{(\ln(x) - 1)x} \quad (9)$$

$p1 := DEtools[dfieldplot](expr, y(x), x = -10..10, y = -10..10);$

$p2 := plots[implicitplot](sol, x = -10..10, y = -10..10, color = blue);$

$p3 := plots[pointplot]([1, 2], color = green);$

$plots[display](p1, p2, p3);$

