Some books on Lisp and Lisp programming:

- ABELSON, H. AND SUSSMAN, G. J. (1985), Structure and Interpretation of Computer Programs, New York: McGraw-Hill.
- Franz Inc. (1988), Common Lisp: The Reference, Reading, MA: Addison-Wesley.
- Steele, Guy L. (1990), Common Lisp: The Language, second edition, Bedford, MA: Digital Press.
- Winston, Patrick H. and Berthold K. P. Horn, (1988), *LISP*, 3rd Ed., New York: Addison-Wesley.

Further development depends on the users of Lisp-Stat:

- If people find the system useful, new methods for handling a variety of problems will become available (e.g. through statlib).
- As new ideas are implemented, the need for new tools and primitives, or for modifications to existing ones, will become evident.

ASA, August 1992 Tierney

## Where Lisp-Stat is headed

Lisp-Stat is an evolving system.

Plans for the near term are to

- improve and update current versions
- develop a Common Lisp version

### Longer-term plans include

- improving the support for compound data objects
- some support for missing data conventions
- increased graphics capabilities
- support for constraints

ASA, August 1992 Tierney

#### Electronic sources of information

There is a mailing list of users who help to answer questions, share ideas, etc.

To join the mailing list, send mail to:

stat-lisp-news-request@umnstat.stat.umn.edu

Once you are on the list, you can send mail to all members of the list by sending a message to

stat-lisp-news@umnstat.stat.umn.edu

The statlib archive contains contributed Lisp-Stat code, as well as the source code for XLISP-STAT.

To find out what is available from statlib, send mail to

statlib@lib.stat.cmu.edu

containing the single line

send index

statlib can also be accessed by ftp.

## Where can you go from here?

Get a copy of the software for your computer and try it on your problems:

- try the standard tools
- try building tools of your own
- try graphics tailored to your problems

If you develop new tools and ideas that might be useful to others, please share them (e.g. by submitting them to statlib or the stat-lisp-news mailing list).

# Final Notes

### Some computational issues:

- For point clouds, image rendering is quite fast, even on stock hardware.
- This is not true of lines and surfaces.
- The effective use of high performance 3D hardware is worth exploring.
- For data sets derived from models, computing speed can still be limiting
- Pre-computation can help, but limits interaction.

#### **Comments**

#### Some statistical issues:

- Many good ideas for viewing higher-dimensional data are available
- There is room for many more ideas
- Eventually, it will be useful to learn to quantify the effectiveness of different viewing methods in different situations.
- It is also important to explore numerical enhancements as well as combinations of different graphical strategies.

#### Some References

ASIMOV, D., (1985), "The grand tour: a tool for viewing multidimensional data," SIAM J. of Scient. and Statist. Comp. 6, 128-143.

BECKER, R. A. AND CLEVELAND, W. S., (1987), "Brushing scatterplots," *Technometrics* 29, 127-142, reprinted in *Dynamic Graphics for Statistics*, W. S. Cleveland and M. E. McGill (eds.), Belmont, Ca.: Wadsworth.

BECKER, R. A., CLEVELAND, W. S. AND WEIL, G., (1988), "The use of brushing and rotation for data analysis," in *Dynamic Graphics for Statistics*, W. S. Cleveland and M. E. McGill (eds.), Belmont, Ca.: Wadsworth.

BOLORFORUSH, M., AND WEGMAN, E. J. (1988), "On some graphical representations of multivariate data," Computing Science and Statistics: Proceedings of the 20th Symposium on the Interface, E. J. Wegman, D. T. Ganz, and J. J. Miller, editors, Alexandria, VA: ASA, 121-126.

Buja, A., Asimov, D., Hurley, C., and McDonald, J. A., (1988), "Elements of a viewing pipeline for data analysis," in *Dynamic Graphics for Statistics*, W. S. Cleveland and M. E. McGill (eds.), Belmont, Ca.: Wadsworth.

DONOHO, A. W., DONOHO, D. L. AND GASKO, M., (1988), "MACSPIN: Dynamic Graphics on a Desktop Computer," п *Dynamic Graphics for Statistics*, W. S. Cleveland and M. E. McGill (eds.), Belmont, Ca.: Wadsworth.

FISHERKELLER, M. A., FRIEDMAN, J. H. AND TUKEY, J. W., (1974), "PRIM-9: An interactive multidimensional data display and analysis system," in *Data: Its Use, Organization and Management*, 140-145, New York: ACM, reprinted in *Dynamic Graphics for Statistics*, W. S. Cleveland and M. E. McGill (eds.), Belmont, Ca.: Wadsworth.

INSELBERG, A., AND DIMSDALE, B. (1988), "Visualizing multi-dimensional geometry with parallel coordinates," Computing Science and Statistics: Proceedings of the 20th Symposium on the Interface, E. J. Wegman, D. T. Ganz, and J. J. Miller, editors, Alexandria, VA: ASA, 115-120.

ASA, August 1992 Tierney

## Some examples to try:

- independent gamma variates
- normal mixtures
- likelihood function
- posterior densities

## Some possible enhancements:

- normal curve for comparison
- replay tools
- integration with transformations
- guided tour

Two additional methods:

```
(defmeth ncheck-plot-proto :do-idle ()
  (send self :tour-step))
(defmeth ncheck-plot-proto :menu-template ()
  (append
   (call-next-method)
   (list (send run-item-proto :new self))))
Finally, the initialization method sets up the
plot:
(defmeth ncheck-plot-proto :isnew (f d)
  (setf (slot-value 'function) f)
  (setf (slot-value 'direction) d)
  (setf (slot-value 'xvals) (rseq -3 3 7))
  (call-next-method 2)
  (send self :range 0 -3 3)
  (send self :range 1 0 1.2)
  (send self :x-axis t nil 7)
  (send self :y-axis nil)
  (send self :set-image))
```

The method for moving the direction is similar to the tour method used earlier:

```
(defmeth ncheck-plot-proto :tour-step ()
  (when (< (slot-value 'tour-count) 0)</pre>
        (let* ((d (slot-value 'direction))
               (n (length d))
               (a (abs (slot-value 'angle))))
          (setf (slot-value 'tour-count)
                (random (floor (/ pi
                                   (* 2 a)))))
          (setf (slot-value 'tour-trans)
                (make-rotation d
                                (normal-rand n)
                                a))))
  (setf (slot-value 'direction)
        (matmult (slot-value 'tour-trans)
                 (slot-value 'direction)))
  (send self :set-image)
  (setf (slot-value 'tour-count)
        (- (slot-value 'tour-count) 1)))
```

The normality checking plot can be implemented as a prototype:

```
(defproto ncheck-plot-proto
   '(function direction xvals
      tour-count tour-trans angle)
   ()
   scatterplot-proto)

(send ncheck-plot-proto :slot-value
      'tour-count -1)
(send ncheck-plot-proto :slot-value
      'angle 0.2)
```

The method for adjusting the image to the current state is

A similar idea can be used for examining functions.

As an example, suppose we want to determine if f(x) looks like a multivariate standard normal density.

This is true if and only if g(z) = f(zu) looks like a univariate standard normal density for any unit vector u.

By moving u through space with a series of random rotations, we can look at these univariate densities for a variety of different directions.

ASA, August 1992 Tierney

#### Some variations and additions:

- Make new rotation orthogonal to current viewing plane
- Controls for replaying parts of the tour
- Touring on only some of the variables (independent variables only)
- Constraints on the tour (Correlation Tour)
- Integration with slicing/conditioning
- Guided tours (Projection Pursuit XGobi)

The sphere-rand function can be defined as

Some examples to try the tour on:

- Diabetes data
- Iris data
- Stack loss data
- 4D structures

### A simple Grand Tour function:

```
(defun tour-plot (&rest args)
  (let ((p (apply #'spin-plot args)))
    (send p :add-slot 'tour-count -1)
    (send p :add-slot 'tour-trans nil)
    (defmeth p :tour-step ()
      (when (< (slot-value 'tour-count) 0)
        (let ((vars (send self :num-variables))
              (angle (send self :angle)))
          (setf (slot-value 'tour-count)
                (random 20))
          (setf (slot-value 'tour-trans)
                (make-rotation
                 (sphere-rand vars)
                 (sphere-rand vars)
                 angle))))
      (send self :apply-transformation
            (slot-value 'tour-trans))
      (setf (slot-value 'tour-count)
            (- (slot-value 'tour-count) 1)))
    (defmeth p :do-idle ()
      (send self :tour-step))
    (send (send p :menu) :append-items
          (send run-item-proto :new p))
   p))
```

#### The Grand Tour

The Grand Tour provides a way of examining "all" one- or two-dimensional projections of a higher-dimensional data set.

The projections are moved smoothly in a way that eventually brings them near every possible projection.

One way to construct a Grand Tour is to repeat the following steps:

- Choose two directions at random to define a rotation plane.
- Rotate in this plane by a specified angle a random number of times.

### Some points:

- The definition allows keywords to be passed on to plot-points.
- The plot w and the matrix m are locked into the environment of interpolate.
- The slider is registered as a subordinate.

### Some examples to try:

- Stack loss data
- Places rated data
- Iris data

A simple function to set up an interpolation plot for a data set with four variables:

```
(defun interp-plot (data &rest args)
 ;; Should check here that data is 4D
 (let ((w (apply #'plot-points data
                  :scale 'variable args))
        (m (matrix '(4 4) (repeat 0 16))))
    (flet ((interpolate (p)
             (let* ((a (* (/ pi 2) p))
                    (s (sin a))
                    (c (cos a)))
               (setf (select m 0 0) c)
               (setf (select m 0 2) s)
               (setf (select m 1 1) c)
               (setf (select m 1 3) s)
               (send w :transformation m))))
      (let ((s (interval-slider-dialog
                (0 1)
                :points 25
                :action #'interpolate)))
        (send w :add-subordinate s)))
   W))
```

## Plot Interpolation

Plot interpolation provides a way of examining the relation among 4 variables.

The idea is to take two scatterplots and rotate from one to the other.

(Interpolate using trigonometric interpolation.)

Watching the interpolation allows you to

- track groups of points from one plot to another
- identify clusters based on both location and velocity

ASA, August 1992

Tierney

## Some specific implementations:

- scatterplot matrix
- linked 2D plots
- 3D plot linked with a histogram
- plot interpolation
- grand tours and variants
- parallel coordinates

## Useful general techniques include

- glyph augmentation
  - colors
  - symbol types
  - symbol sizes
- dimension reduction
  - projection
  - slicing, masking, conditioning

### Some issues to keep in mind:

- using symbols or colors loses ordering
- projections to 2D will only become 1D if part of the structure is linear
- masking/conditioning requires large data sets

A rough ranking of types of structures that can be detected might look like this:

- points (zero-dimensional structures) in 1D and 2D plots
- curves (one-dimensional structures) in 2D and 3D plots
- surfaces (two-dimensional structures) in 3D plots

Possible structures in four dimensions include

- separate point clusters
- curves
- 2D surfaces
- 3D surfaces

## 4D and Beyond

## Introduction and Background

As with two and three dimensional plots, the objectives of higher dimensional graphics are, among others, to

- detect groupings or clusters
- detect lower dimensional structure
- detect other patterns

Higher dimensions introduce new difficulties:

- sparseness
- loss of intuition

To allow rotation to be done by direct manipulation, we can add a new mouse mode

```
(send spin-proto :add-mouse-mode 'hand-rotate
     :title "Hand Rotate"
     :cursor 'hand
     :click :do-hand-rotate)
```

and define the :do-hand-rotate method as

```
(defmeth spin-proto :do-hand-rotate (x y m1 m2)
  (flet ((calcsphere (x y)
           (let* ((norm-2 (+ (* x x) (* y y)))
                  (rad-2 (^ 1.7 2))
                  (z (if (< norm-2 rad-2) (sqrt (- rad-2 norm-2)) 0)))
             (if (< norm-2 rad-2)
                 (list x y z)
                 (let ((r (sqrt (max norm-2 rad-2))))
                   (list (/ x r) (/ y r) (/ z r))))))
    (let* ((oldp (apply #'calcsphere
                        (send self :canvas-to-scaled x y)))
           (p oldp)
           (vars (send self :content-variables))
           (trans (identity-matrix (send self :num-variables))))
      (send self : idle-on nil)
      (send self : while-button-down
            #'(lambda (x y)
                (setf oldp p)
                (setf p (apply #'calcsphere
                               (send self :canvas-to-scaled x y)))
                (setf (select trans vars vars) (make-rotation oldp p))
                (when m1
                      (send self :slot-value 'rotation-type trans)
                      (send self :idle-on t))
                (send self :apply-transformation trans))))))
```

A method for rotating around a specified data axis is

```
(defmeth spin-proto :data-rotate
         (axis &optional (angle pi))
 (let* ((alpha (send self :angle))
         (cols (column-list
                (send self :transformation)))
         (m (case axis
              (x (make-rotation (select cols 1)
                                 (select cols 2)
                                 alpha))
              (y (make-rotation (select cols 0)
                                 (select cols 2)
                                 alpha))
              (z (make-rotation (select cols 0)
                                 (select cols 1)
                                 alpha)))))
    (dotimes (i (floor (/ angle alpha)))
      (send self :apply-transformation m))))
```

### Some Examples

By rocking the plot back and forth we can get the 3D illusion while keeping the view close to fixed.

A method for rocking the plot can be defines as

## Implementation Issues

The default scaling used by the rotating plot is variable.

You can change the scale type with the **Options** dialog or the :scale-type message.

You can implement non-standard scaling strategies by overriding the default :adjust-to-data method.

The standard rotating plot has controls for screen axis rotation.

You can use the :transformation and :apply-transformation methods to implement alternate control methods.

Plot overlays can be used to hold controls for these strategies. The nature of the rotation controls may also affect the illusion.

Some possible control strategies are

- rotation around screen axes: horizontal (Pitch), vertical (Yaw), out-of-screen (Roll)
- rotation around data axes: X, Y, Z
- direct manipulation (like a globe)

Rotation is still a fairly new technique; we are still learning how to use it effectively.

Some questions to keep in mind as you use rotation to explore your data sets:

- What types of phenomena are easy to detect?
- What is hard to detect?
- What enhancements aid in detection?

It may help to try rotation on some artificial structures and see if you can identify these structures.

Scaling can have a significant effect on the shape of a point cloud.

Possible scaling strategies include

- fixed scaling comparable scales
- variable scaling non-comparable scales
- combinations

Several methods are available for enhancing the 3D illusion produced by rotation

- depth cuing
- framed box
- Rocking
- slicing

#### Some Issues in Rotation

#### Statistical Issues

Rotation is a method for viewing a three dimensional set of data.

The objective of rotation is to create an illusion of 3D structure on a 2D screen.

Factors that can be used to produce or enhance such an illusion are

- stereo imaging
- perspective
- lighting
- motion parallax

Motion parallax is the principle driving rotation.

#### Some notes:

- :canvas-to-real converts the click coordinates to data coordinates.
- The dolist loop is needed to smooth out the curve if the mouse is moved rapidly.
- If the plot is to be normalized as a density, it can be adjusted before the :redraw-content message is sent.

A method for retrieving the lines is given by

### The drawing method is defined as

```
(defmeth p :mouse-drawing (x y m1 m2)
  (let* ((n (send self :num-lines))
         (rxy (send self :canvas-to-real x y))
         (rx (first rxy))
         (ry (second rxy))
         (old-i (max 0 (min (- n 1) (floor (* n rx)))))
         (old-y ry))
    (flet ((adjust (x y)
             (let* ((rxy (send self :canvas-to-real x y))
                    (rx (first rxy))
                    (ry (second rxy))
                    (new-i (max 0))
                                 (min (-n 1)
                                      (floor (* n rx)))))
                    (y ry))
               (dolist (i (iseq old-i new-i))
                 (let ((p (if (= old-i new-i)
                               (abs
                               (/ (- i old-i)
                                  (- new-i old-i))))))
                   (send self :linestart-coordinate 1 i
                         (+ (* p y) (* (- 1 p) old-y))))
               (send self :redraw-content)
               (setf old-i new-i old-y y))))
          (adjust x y)
          (send self :while-button-down #'adjust))))
```

As another example, we can set up a plot for obtaining graphical function input.

Start by setting up the plot, turning off the y axis, and adding a new mouse mode:

We can put the plot in our new mode with

```
(send p :mouse-mode 'drawing)
```

If we want to change the fitting method, we only need to change the :calculate-coefs method.

Finally, add a regression line and put the plot into point moving mode

```
(send p :set-regression-line)
(send p :mouse-mode 'point-moving)
```

Several enhancements and variations are possible:

- The plot can be modified to use only visible points for fitting the line.
- Several fitting methods can be provided, with a dialog to choose among them.
- The same idea can be used to study the effect of outliers on smoothers.

The point moving method can be broken down into several pieces:

```
(defmeth p :do-point-moving (x y a b)
 (let ((p (send self :drag-point
                 x y :draw nil)))
    (if p (send self :set-regression-line))))
(defmeth p :set-regression-line ()
  (let ((coefs (send self :calculate-coefs)))
    (send self :clear-lines :draw nil)
    (send self :abline
          (select coefs 0)
          (select coefs 1))))
(defmeth p :calculate-coefs ()
 (let* ((i (iseq (send self :num-points)))
         (x (send self :point-coordinate 0 i))
         (y (send self :point-coordinate 1 i))
         (m (regression-model x y :print nil)))
    (send m :coef-estimates)))
```

## Using New Mouse Modes

We have already seen a few examples of useful new mouse modes.

As another example, let's make a plot for illustrating the sensitivity of least squares to points with high leverage.

Start with a plot of some simulated data:

```
(setf x (append (iseq 1 18) (list 30 40)))
(setf y (+ x (* 2 (normal-rand 20))))
(setf p (plot-points x y))
```

Next, add a new mouse mode:

```
(send p :add-mouse-mode 'point-moving
     :title "Point Moving"
     :cursor 'finger
     :click :do-point-moving)
```

Next, set up the covariate plot and a plot of the Kaplan-Meier estimator for all survival times:

Finally, write an :adjust-screen method for p that changes the Kaplan-Meier estimator in q to use only the currently selected and highlighted points in p:

Another example was recently posted to statlib by Neely Atkinson, M. D. Anderson Cancer Center, Houston.

Here is a simplified version:

Suppose we have some censored survival data and a number of covariates.

To examine the relationship between the covariates and the times

- put the covariates in a plot, for example a scatterplot matrix
- in a second plot show the Kaplan-Meier estimate of the distribution of the survival times for points selected in the covariate plot.

To speed up performance, first define a faster Kaplan-Meier estimator that assumes the data are properly ordered:

```
(defun km (x s)
  (let ((n (length x)))
      (accumulate #'* (- 1 (/ s (iseq n 1))))))
```

A similar idea is useful for multivariate response data (e.g repeated measures or time series).

Suppose p is a plot of covariates and q is a plot of m responses, contained in the list resp, against their indices.

Then the method

shows in q the average response profile for the highlighted and selected observations.

To have control over the smoother bandwidth, we can add a slot and accessor method, modify the :adjust-screen method, and add a slider:

```
(send p :add-slot 'kernel-width 50)
(defmeth p :kernel-width (&optional width)
  (when width
        (setf (slot-value 'kernel-width) width)
        (send self :adjust-screen))
  (slot-value 'kernel-width))
(defmeth p :adjust-screen ()
  (call-next-method)
  (let ((i (union
            (send self :points-selected)
            (send self :points-hilited))))
    (send self :clear-lines :draw nil)
    (if (< 1 (length i))
        (let ((x (select tensile-strength i))
              (y (select abrasion-loss i))
              (w (send self :kernel-width)))
          (send self :add-lines
                (kernel-smooth x y :width w)))
        (send self :redraw-content))))
(interval-slider-dialog '(20 100)
  :action #'(lambda (w) (send p :kernel-width w)))
```

Suppose we have a histogram of hardness and a scatterplot of abrasion-loss against tensile-strength for the abrasion loss data

(setf h (histogram hardness))

adds a kernel smooth to the plot if at least two points are selected or hilited.

## Modifying Mouse Responses

## Modifying Selection and Brushing

We have already seen several examples of using the standard selecting and brushing modes.

The series of messages used to implement these modes lets us modify what happens when the brush is moved or points are selected.

The simplest way to build on the standard modes is to modify the :adjust-screen method.

This message is sent each time the set of selected or highlighted points is changed with the mouse.

As an example, if we are using selection or brushing to examine a bivariate conditional distribution, it may be useful to augment the bivariate plot with a smoother. We can use this distribution to animate the plot:

A run item lets us control the animation:

Another way to think of this animation is as a simulation from an approximation to the sampling distribution.

We can put a copy of the estimated hazard increments in a slot:

For certain prior distributions, a Bayesian analysis produces approximately a gamma posterior distribution for the hazard increments.

A similar idea may be useful for estimated survival curves.

Suppose s is a survival distribution object.

A plot of the Fleming-Harrington estimator is

Another possible problem is that the curve may jump around too much to make it easy to watch.

We can reduce this jumping by changing one observation at a time instead of changing all at once:

```
(send w :slot-value
        'kernel-data (copy-list precipitation))

(defmeth w :do-idle ()
    (let ((d (slot-value 'kernel-data))
                (i (random 30))
                (j (random 30)))
                (setf (select d i)
                      (select precipitation j))
                (send self :set-lines)))
```

A problem with this version is that the x values at which the density estimate is evaluated change with the sample.

To avoid this, we can add another slot and accessor method,

```
(send w :add-slot
      'xvals
      (rseq (min precipitation)
            (max precipitation)
            30))
(defmeth w :xvals () (slot-value 'xvals))
and change the :set-lines method to use
these values:
(defmeth w :set-lines ()
  (let ((width (send self :kernel-width))
        (xvals (send self :xvals)))
    (send self :clear-lines :draw nil)
    (send self :add-lines
          (kernel-dens (send self :kernel-data)
                       :width width
                       :xvals xvals))))
```

We have already used such an item once; since we may need one again, it is probably worth constructing a prototype:

```
(defproto run-item-proto
          '(graph) () menu-item-proto)
(send run-item-proto :key #\R)
(defmeth run-item-proto :isnew (graph)
  (call-next-method "Run")
  (setf (slot-value 'graph) graph))
(defmeth run-item-proto :update ()
  (send self :mark
        (send (slot-value 'graph) :idle-on)))
(defmeth run-item-proto :do-action ()
  (let ((graph (slot-value 'graph)))
    (send graph :idle-on
          (not (send graph :idle-on)))))
We can now add a run item to the menu by
(send (send w :menu) :append-items
      (send run-item-proto :new w))
```

### Assessing Variability by Animation

One way to get a feeling for the uncertainty in a density estimate is to re-sample the data with replacement, i.e. to look at bootstrap samples, and see how the estimate changes.

We can do this by defining a :do-idle method:

We can turn the animation on and off with the :idle-on message, but it is better to use a menu item.

It may also be useful to store the data in a slot and provide an accessor method:

```
(send w :add-slot 'kernel-data precipitation)
(defmeth w :kernel-data ()
  (slot-value 'kernel-data))
The method for changing the plot is
(defmeth w :set-lines ()
  (let ((width (send self :kernel-width))
        (data (send self :kernel-data)))
    (send self :clear-lines :draw nil)
    (send self :add-lines
          (kernel-dens data:width width))))
and a slider for controlling the width is given by
(interval-slider-dialog '(.25 1.5)
  :action
  #'(lambda (s) (send w :kernel-width s)))
```

### Density Estimation

Choosing a bandwidth for a kernel density estimator is a difficult problem.

It may help to have an animation that shows the effect of changes in the bandwidth on the estimate.

An initial plot can be set up as

The initial bandwidth can be stored in a slot

```
(send w :add-slot 'kernel-width 1)
```

and the accessor method for the slot can adjust the plot when the width is changed:

The new :change-power method transforms the dependent variable in the regression model and then changes the plot using the new residuals:

Again, a slider for controlling the animation is set up by

```
(interval-slider-dialog '(-1 2)
   :action
   #'(lambda (pow) (send p :change-power pow)))
```

Since the point indices in the plot correspond to the indices in the regression, it is possible to track the positions of the residuals for groups of observations as the power is changed. Let's use the stack loss data as an illustration.

A set of approximate expected normal order statistics and a set of indices are set up as

The same idea can be used with a regression model.

To transform the dependent variable and scale the residuals, define the functions

To change the coordinates, we need a list of the indices of all points.

To avoid generating this list every time, we can store it in a slot:

```
(send p :add-slot 'indices (iseq 30))
(defmeth p :indices () (slot-value 'indices))
```

The method for changing the power now becomes

To avoid losing color, symbol or state information in the points, we can change the coordinates of the points in the plot instead of replacing the points.

To preserve the original data ordering, we need to base the x values on ranks instead of ordering the data

```
(let ((ranks (rank precipitation)))
  (setf nq (normal-quant (/ (+ ranks 1) 31))))
and use these to construct our plot:
(setf p (plot-points nq (bc precipitation 1)))
```

```
To view a range of powers, you can use a dolist loop

(dolist (pow (rseq -1 2 20))
    (send p :change-power pow))

or you can use one of two modeless dialogs to get finer control over the animation:

(sequence-slider-dialog (rseq -1 2 21) :action #'(lambda (pow) (send p :change-power pow)))

or

(interval-slider-dialog '(-1 2) :points 20 :action
```

#'(lambda (pow) (send p :change-power pow)))

We can construct an initial plot as

```
(setf p (plot-points nq (bc x 1)))
```

To change the plot content to reflect a square-root transformation, we can use the :clear and :add-points messages:

```
(send p :clear)
(send p :add-points nq (bc x 0.5))
```

To achieve a smooth transition, you can give the :clear message a keyword argument :draw with value nil:

```
(send p :clear :draw nil)
(send p :add-points nq (bc x 0.0))
```

These steps can be built into a :change-power method:

```
(defmeth p :change-power (pow)
  (send self :clear :draw nil)
  (send self :add-points nq (bc x pow)))
```

## Dynamic Box-Cox Plots

Fowlkes's implementation of dynamic transformations in the late 1960's was one of the earliest examples of dynamic statistical graphics.

Start by defining a function to compute the transformation and scale the data to the unit interval:

Next, construct an ordered sample and a set of approximate expected normal order statistics:

```
(setf x (sort-data precipitation))
(setf nq (normal-quant (/ (iseq 1 30) 31)))
```

## Some Examples of Animation

The basic idea in animation is to display a sequence of views rapidly enough and smoothly enough to

- create an illusion of motion
- allow the change in related elements to be tracked visually

The particular image is determined by the values of one or more parameters.

- For a small number of parameters, (1 or 2), the values can be controlled directly, e.g. using scroll bars.
- For more parameters, automated methods of exploring the parameter space are useful.

Research on the effective use of dynamic graphics is just beginning.

Some of the questions to keep in mind are

- How should dynamic graphs be used?
- What should you plot?
- How do you interpret dynamic images?
- What techniques are useful, and for which problems?

Even in simple two-dimensional graphics there are difficult open issues.

Answering these questions will take time.

We can make a start by learning how to try out some of the more promising dynamic graphical ideas, and variations on these ideas.

## Some Background

Dynamic graphs usually have some of the following characteristics:

- high level of interaction
- motion
- more than two dimensional data
- require high performance graphics display hardware

Some of the basic techniques that appear to be useful are

- animation
  - controlled interactively
  - controlled by a program
- direct interaction and manipulation
  - linking and brushing
- rotation

Many ideas are described in the papers in the book edited by Cleveland and McGill (1988).

# Some Dynamic Graphics Examples

### Standard Statistical Graphs

Each of the standard plot prototypes needs only a few new methods.

The main additional or changes methods are:

```
scatterplot-proto:
    Overrides: :add-points, :add-lines, :adjust-to-data.
    New messages: :add-boxplot, :add-function-contours,
    :add-surface-contour.:add-surface-contours.
scatmat-proto:
    Overrides: :add-lines, :add-points, :adjust-points-in-rect,
    :adjust-screen-point,:do-click,:do-motion,:redraw-background,
    :redraw-content, :resize.
spin-proto:
    Overrides: :adjust-to-data, :current-variables, :do-idle, :isnew,
    :resize,:redraw-content.
    New methods: :abcplane, :add-function, :add-surface, :angle,
    :content-variables, :depth-cuing, :draw-axes, :rotate,
    :rotation-type,:showing-axes
histogram-proto:
    Overrides: :add-points,:adjust-points-in-rect,:adjust-screen,
    :adjust-screen-point,:adjust-to-data,:clear-points,:drag-point,
    :isnew,:redraw-content,:resize.
    New methods: :num-bins, :bin-counts.
name-list-proto:
    Overrides: :add-points, :adjust-points-in-rect, :adjust-screen-point,
    :redraw-background, :redraw-content.
```

Standard items can be specified as symbols in the template:

- color
- dash
- focus-on-selection
- link
- mouse
- options
- redraw
- erase-selection
- rescale
- save-image
- selection
- show-all
- showing-labels
- symbol

#### Menus and Menu Items

To help construct standard menus

- :menu-title returns the title to use
- :menu-template returns a list of items or symbols
- :new-menu constructs and installs the new menu

The :isnew method sends the plot the :new-menu message when it is created.

Plot overlays are useful for holding controls.

- Overlays inherit from graph-overlay-proto.
- Overlays are like transparent sheets of plastic.
- Overlays are drawn from the bottom up.
- Overlays can intercept mouse clicks.
- Clicks are processed from the top down:
  - Each overlay is sent the :do-click
     message until one returns a non-nil
     result.
  - Only if no overlay accepts a click is the click passed to the current mouse mode.

The controls of a rotating plot are implemented as an overlay.

Other examples of overlays are in plotcontrols.lsp in the **Examples** folder.

The aspect type used can be changed by

(send w :fixed-aspect t)

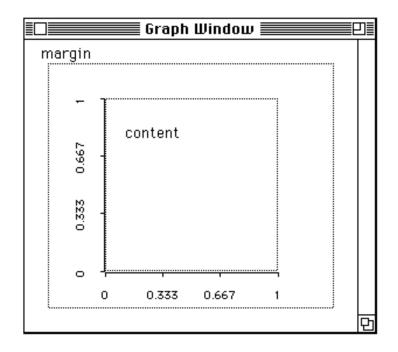
The :redraw method sends three messages:

- :redraw-background erases the canvas and draws the axes
- :redraw-overlays sends each overlay the :redraw message
- :redraw-content redraws points, lines, etc.

Many methods, like :rotate-2, also send :redraw-content.

## Window Layout and Redrawing

The :resize method maintains a margin and a content rectangle



- The plot is surrounded by a margin, used by plot controls.
- The content rectangle can use a fixed or a variable aspect ratio.
- The size of the content depends on the aspect ratio and the axes.
- The plot can be covered by overlays, resized with :resize-overlays.

ASA, August 1992 Tierney

#### Some useful messages:

For points specified by index:

:point-showing

:point-hilited

:point-selected

For sets of indices:

:selection or :points-selected

:points-hilited

:points-showing

Other operations:

:erase-selection

:show-all-points

:focus-on-selection

:adjust-screen

Some useful predicates:

:any-points-selected-p

:all-points-showing-p

When a point's state is changed in a plot,

- Each linked plot (and the plot itself) is sent the :adjust-screen-point message with the index as argument.
- The action taken by the method for :adjust-screen-point may depend on both current and previous states.

Since it is not always feasible to redraw single points,

- the :needs-adjusting method can be used to check or set a flag
- the :adjusting-screen method can redraw the entire plot if the flag is set

The easiest, though not necessarily the most efficient, way to augment standard mouse modes is to define a new :adjust-screen method

Tierney

Points can be in four states:

invisible
normal
hilited
selected.

Linking is based on a *loose linking* model:

- points are related by index number
- only point states are adjusted

The system uses two messages to determine which plots are linked:

- :links returns a list of plots linked to the plot (possibly including the plot itself)
- :linked determines if the plot is linked, and turns linking on and off.

### In brushing mode, a click

- Sends : unselect-all-points unless the extend modifier is used.
- While the mouse is dragged, sends :adjust-points-in-rect with the brush rectangle and selected as arguments.

In brushing mode, moving the mouse

• Sends :adjust-points-in-rect with the brush rectangle and hilited as arguments.

### Standard Mouse Modes and Linking

The click and motion methods of the two standard modes use a number of messages.

In selecting mode, a click

- Sends :unselect-all-points, unless the extend modifier is used.
- Sends :adjust-points-in-rect with click x and y coordinates, width and height returned by :click-range, and the symbol selected as arguments.
- While the button is down, a dashed rectangle is stretched from the click to the mouse.

When the button is released, :adjust-points-in-rect is sent with the rectangle coordinates and selected as arguments.

The button down action does nothing; it just waits.

An alternative is to allow the label to be dragged, perhaps to make it easier to read:

```
(defmeth w :do-identify (x y m1 m2)
  (let* ((cr (send self :click-range))
         (p (first
             (send self :points-in-rect
                   (- x 2) (- y 2) 4 4))))
    (if p
        (let ((mode (send self :draw-mode))
              (lbl (send self :point-label p)))
          (send self :draw-mode 'xor)
          (send self :draw-string lbl x y)
          (send self :while-button-down
                #'(lambda (new-x new-y)
                    (send self :draw-string lbl x y)
                    (setf x new-x)
                    (setf y new-y)
                    (send self :draw-string lbl x y)))
          (send self :draw-string lbl x y)
          (send self :draw-mode mode)))))
```

Initially there are two mouse modes, selecting and brushing.

We can add a new mouse mode by

```
(send w :add-mouse-mode 'identify
    :title "Identify"
    :click :do-identify
    :cursor 'finger)
```

The :do-identify method can be defined as

### Mouse Events and Mouse Modes

The graph prototype organizes mouse interactions into mouse modes.

Each mouse mode includes

- a symbol for choosing the mode from a program
- a title string used in the mode selection dialog
- a cursor to visually identify the mode
- mode-specific click and motion messages

It should not be necessary to override a graph's :do-click or :do-motion methods.

A transformation can also be applied incrementally:

A simpler message allows rotation within coordinate planes:

```
(dotimes (i 10)
  (send w :rotate-2 0 2 (/ pi 20) :draw nil)
  (send w :rotate-2 1 3 (/ pi 20)))
```

Several messages are available for accessing data values in raw, scaled, and screen coordinates.

Other messages are available for converting among coordinate systems.

Initially there is no transformation:

```
> (send w :transformation)
NIL
```

If the current variables are 0 and 1, a rotation can be applied to replace air by conc and temp by loss:

```
(send w:transformation '#2A((0 0-1 0)
(0 0 0-1)
(1 0 0 0)
(0 1 0 0)))
```

The transformation can be removed by

```
(send w :transformation nil)
```

### Scaling and Transformations

The scale type controls the action of the default :adjust-to-data method.

The initial scale type is nil:

```
> (send w :scale-type)
NIL
> (send w :range 0)
(50 80)
> (send w :scaled-range 0)
(50 80)
```

Two other scale types are variable and fixed. For variable scaling:

```
> (send w :scale-type 'variable)
VARIABLE
> (send w :range 0)
(35 95)
> (send w :scaled-range 0)
(-2 2)
```

The :scale, :center, and :adjust-to-data messages let you build your own scale types.

Initially, the plot shows the first two variables:

```
> (send w :current-variables)
(0 1)
```

This can be changed:

```
> (send w :current-variables 2 3)
(2 3)
> (send w :current-variables 0 1)
(0 1)
```

Plot data can be cleared by several messages:

```
(send w :clear-points)
(send w :clear-lines)
(send w :clear)
```

If the :draw keyword argument is nil the plot is not redrawn.

The default value is t.

You can control whether axes are drawn with the :x-axis and :y-axis messages:

```
> (send w :x-axis t)
(T NIL 4)
```

The range shown can be accessed and changed:

```
> (send w :range 0)
(50 80)
> (send w :range 1)
(17 27)
> (send w :range 1 15 30)
(15 30)
```

The function get-nice-range helps choosing a range and the number of ticks:

```
> (get-nice-range 17 27 4)
(16 28 7)
```

To remove the axis:

```
> (send w :x-axis nil)
(NIL NIL 4)
```

### Data and Axes

The :isnew method for the graph prototype requires one argument, the number of variables:

```
> (setf w (send graph-proto :new 4))
#<Object: 302823396, prototype = GRAPH-PROTO>
```

Using the stack loss data as an illustration, we can add data

and adjust scaling to make the data visible:

```
> (send w :adjust-to-data)
NIL
```

We can also add line segments:

```
> (send w :add-lines (list air temp conc loss))
NIL
```

The graph prototype adds the following features:

- m-dimensional point and line start data
- affine transformations consisting of
  - centering and scaling
  - a linear transformation
- ranges for raw, scaled and canvas coordinates
- mouse modes for controlling interaction
- linking strategy
- window layout management
  - margin, content and aspect
  - background (axes)
  - overlays
  - content
- standard menus and menu items

The graph prototype is a view into m dimensional space.

It allows the display of both points and connected line segments

The default methods in this prototype implement a simple scatterplot of two of the m dimensions.

Many features of graphics windows are enhanced to simplify adding new features to graphs.

## Statistical Graphics Windows

graph-proto is the statistical graphics prototype.

It inherits from graph-window-proto.

The graph prototype is responsible for managing the data used by all statistical graphs.

Variations in how these data are displayed are implemented in separate prototypes for the standard graphs.

There may be some flickering when the random walk is running.

This flickering can be eliminated by modifying the :redraw method to use double buffering:

It would also be nice to have a menu item for restarting the walk:

```
(setf restart-item
      (send menu-item-proto :new "Restart"
            :action
            #'(lambda () (send w :restart))))
The :restart method is defined as
(defmeth w :restart ()
  (let ((width (send self :canvas-width))
        (height (send self :canvas-height)))
    (send self :x (/ width 2))
    (send self :y (/ height 2))
    (send self :redraw)))
and a menu with the two items is installed by
(setf menu
      (send menu-proto :new "Random Walk"))
(send menu :append-items restart-item run-item)
(send w :menu menu)
```

```
We can turn the random walk on by typing
(send w :idle-on t)
and we can turn it off with
(send w :idle-on nil)
A better solution is to use a menu item:
(setf run-item
      (send menu-item-proto :new "Run"
            :action
            #'(lambda ()
              (send w :idle-on
                    (not (send w :idle-on)))))
To put a check mark on this item when the
walk is running, define an :update method:
(defmeth run-item :update ()
   (send self :mark (send w :idle-on)))
```

The :do-click message positions the symbol at the click and then allows it to be dragged:

The :do-idle method can be used to move the symbol in a random walk:

The :resize method positions the point at the center of the canvas:

The :redraw method erases the window and redraws the symbol at the location specified by the coordinate values:

### An Example

As a simple example to illustrate the handling of events, let's construct a window that shows a single highlighted symbol at its center.

The window is constructed by

```
(setf w (send graph-window-proto :new))
```

We can add slots for holding the coordinates of our point:

New coordinate values are rounded since drawing operations require integer arguments.

# Graphics Window Menus

Every graphics window can have a menu.

The user interface guidelines of the window system determine how the menu is presented:

- On the Macintosh, the menu is installed in the menu bar when the window is the front window.
- In MS Windows, the menu is installed in the application's menu bar when the window is the front window.
- In SunView, the menu is popped up when the right mouse button is pressed in the window.
- Under X11, the menu is popped up when the mouse is clicked in a **Menu** button at the top of the window.

The :menu message retrieves a graph window's menu or installs a new menu.

## Handling Events

User actions produce various *events* that the system handles by sending messages to the appropriate objects.

There are several types of events:

- resize events
- exposure or redraw events
- mouse events motion and click
- key events
- idle "events"

Resize and redraw events cause :resize and :redraw messages to be sent to the window object.

Mouse and key events produce :do-click, :do-motion, and :do-key messages.

In idle periods, the :do-idle message is sent.

The :while-button-down message can be used to follow the mouse inside a click (for dragging, etc.)

### Using XOR drawing:

(send w :start-buffering)

(send w :draw-symbol 'disk t i i)

(send w :buffer-to-screen)))

(send w :erase-window)

### Lisp-Stat uses

- XOR drawing for moving the brush rectangle
- double buffering for rotation

As an example, let's move a highlighted symbol down the diagonal of a window using both methods.

A new graphics window is constructed by

```
(setf w (send graph-window-proto :new))
```

### Animation Techniques

There are two basic animation methods

- XOR drawing drawing "inverts" the colors on the screen
- double buffering a picture is built up in a background buffer and then copied to the screen

#### Some tradeoffs:

- XOR drawing is usually faster
- XOR drawing automatically preserves the background
- XOR drawing distorts background and object during drawing
- XOR drawing inherently involves a certain amount of flicker
- Moving several objects by XOR causes distortion only one can move at a time
- *Inverting* is not well-defined on color displays

The precise effect of drawing operations depends on the *state* of the drawing system.

Drawing system state components include

- colors foreground and background
- drawing mode normal or XOR
- line type dashed or solid
- pen width an integer
- use color on or off
- buffering on or off

A number of drawing operations are available.

# Drawable objects include

- $\bullet$  rectangles
- ovals
- arcs
- polygons

### These can be

- framed
- painted
- erased

### Other drawables are

- $\bullet$  symbols
- strings
- $\bullet$  bitmaps



The canvas has a coordinate system.

- coordinate units are pixels
- the origin is the top-left corner
- $\bullet$  the x coordinate increases from left to right
- the y coordinate increases from top to bottom

### **Graph Windows**

### Outline of the Drawing System

A graphics window is a view onto a *drawing* canvas.

The dimensions of the canvas can be fixed or elastic.

- If a dimension is fixed, it has a scroll bar.
- If it is elastic, it fills the window.

The name list window uses one fixed dimension; all other standard plots use elastic dimensions by default.

All top-level windows share certain common features:

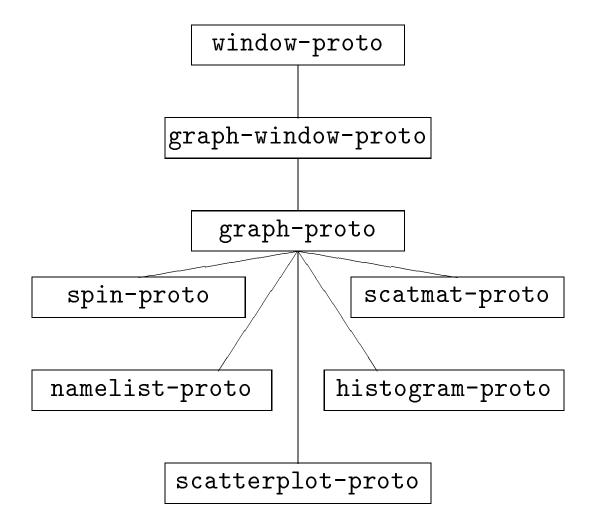
- a title
- a way to be moved
- a way to be resized

These common features are incorporated in the window prototype window-proto.

Both dialog and graphics windows inherit from the window prototype.

# **Overview**

The graphics window object tree:



# Outline of the Graphics System

# Custom Dialogs

If the standard dialogs are not sufficient, you can construct custom modal or modeless dialogs using a variety of items:

- static and editable text fields
- radio button groups
- check boxes
- sliders
- scrollable lists
- push buttons

## Modeless Dialogs

Two standard modeless slider dialogs are available:

• sequence-slider-dialog – a slider for scrolling through a sequence.

An action function is called each time the slider is adjusted.

The current sequence value or a value from a display sequence is displayed.

• interval-slider-dialog – similar to the sequence slider, except that a range to be divided up into a reasonable number of points is given.

By default, the range and number of points are adjusted to produce nice printed values.

There are two dialogs for dealing with files:

• (open-file-dialog) – presents a standard Open File dialog and returns a file name string or nil.

Resets the working folder on **OK**.

• (set-file-dialog prompt) - presents a standard **Save File** dialog.

Returns a file name string or nil.

Resets the working folder on **OK**.

In the X11 versions of these are currently just get-string-dialogs.

The MS Windows versions are also not yet fully developed.

• (get-string-dialog < prompt > [:initial < expr >])

presents a dialog with a prompt, an editable text field, an **OK** and a **Cancel** button.

The initial contents of the editable field is empty or the "a-formated version of  $\langle expr \rangle$ .

The result is a string or nil.

- > (get-string-dialog
   "New variable label:"
   :initial "X")
  "Tensile Strength"
- (get-value-dialog cprompt> [:initial <expr>])
  like get-string-dialog, except
  - the initial value expression is converted to a string with "s formatting
  - the text is interpreted as a lisp expression and is evaluated
  - the result is a list of the value, or nil

• (choose-item-dialog <string> <string-list>) presents a heading and a set of radio
buttons for choosing one of the strings.
Returns the index of the selected string on
OK or nil on Cancel.

```
> (choose-item-dialog
   "Dependent variable:"
   '("X" "Y" "Z"))
1
```

• (choose-subset-dialog < string> < string-list>) - presents a heading and a set of check boxes for indicating which items to select.

Returns a list of the list of selected indices on **OK** or nil on **Cancel**.

## Modal Dialogs

Modal dialogs are designed to ask specific questions and wait until they receive a response.

All other interaction is disabled until the dialog is dismissed – they place the system in dialog mode.

Six functions are available for producing some standard modal dialogs:

- (message-dialog < string>) presents a message with an **OK** button; returns nil when the button is pressed.
- (ok-or-cancel-dialog <string>) –
   presents a message with an OK and a
   Cancel button; returns t or nil according to the button pressed.

## **Dialogs**

Dialogs are similar to menus in that they are based on a dialog prototype and dialog item prototypes.

There are, however many more variations.

Fortunately most dialogs you need fall into one of several categories and can be produced by custom dialog construction functions.

On the Macintosh, the :key message adds a keyboard equivalent to an item:

```
> (send desc :key #\D)
#\D
```

This message is ignored on most other systems.

You can also enable and disable an item with the :enabled message:

```
> (send desc :enabled)
T
> (send desc :enabled nil)
NIL
> (send desc :enabled t)
T
```

Before a menu is presented, the system sends each of its menu items the :update message.

You can define a method for this message that enables or disables the item, or adds a check mark, as appropriate.

You can force an item's action to be invoked by sending it the :do-action message:

> (send desc :do-action)
This is a data set
The sample mean is 4.165463
The sample SD is 1.921366

The system sends the :do-action message when you select the item in a menu.

The :append-items message adds the items to the menu:

> (send data-menu :append-items desc plot)
NIL

Suppose we assign a data set object as the value of some global symbol:

```
(setf *current-data-set* x)
```

Two menu items for dealing with the current data set are:

Initially a menu contains no items.

Items are created using the menu-item-proto prototype.

The initialization method requires one argument, the item's title.

It also accepts several keyword arguments, including

- :action a function to be called when the item is selected
- :enabled true by default
- :key a character to serve as the keyboard equivalent
- :mark nil (the default) or t to indicate a check mark.

Analogous messages are available for accessing and changing these values in existing menu items.

### **Menus**

Menus are created using the menu-proto prototype.

The initialization method requires a single argument, the menu title.

A menu bar is available for holding menus not associated with a graph.

The :install message installs a menu; :remove removes it:

```
> (send data-menu :install)
NIL
> (send data-menu :remove)
NIL
```

#### Some other variations include:

- size and location of windows may have to be determined by the user
- resizing or moving windows from within a program may not be possible
- menus may be popped up or pulled down
- mouse buttons may mean different things in different settings
- mice have different numbers of buttons

The user interface conventions of the window system determine what objects receive what messages.

Several variations are possible:

• On the Macintosh the front window receives all input.

A window becomes the front window by clicking on it.

• Under twm in an X11 system, the window containing the locator cursor receives all input.

Most window management systems are object-oriented in design.

The window system is responsible for converting user actions into messages.

The programmer is responsible for defining any methods objects need in order to respond to the user's actions.

### OOP and User Interfaces

Users of a graphics workstation can take a limited set of actions.

They can

- hit keys
- move the pointer
- click the pointer

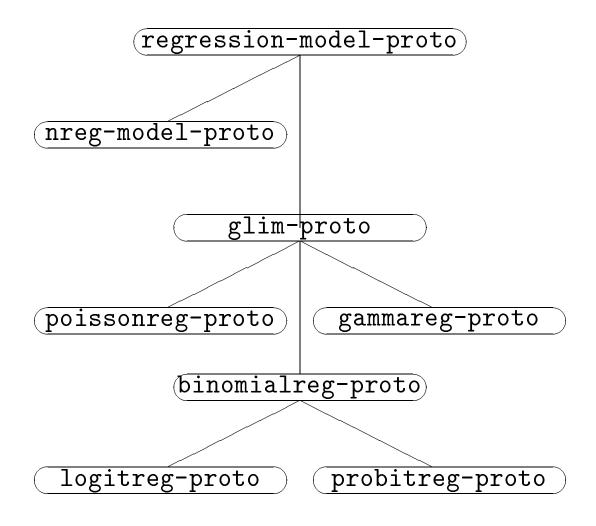
These actions can be viewed as messages that are being sent to objects on the screen.

Graphical user interfaces present users with a model based on a desk:

- Overlapping windows act like sheets of paper
- Different windows represent different software objects on the screen
- Each object may respond differently to key stroke or locator click messages

## Model Prototypes

Linear regression, nonlinear regression and GLIM model prototypes are arranged as:



A method for the Kaplan-Meier estimator:

Methods for the Fleming-Harrington estimator and standard errors based on Greenwood's formula and Tsiatis' formula are

# The :isnew method fills in the data: (defmeth survival-proto :isnew (times status &optional title) (send self :data times status) (if title (send self :title title))) A :describe method: (defmeth survival-proto :describe (&optional (stream t)) (let ((title (send self :title)) (data (send self :data))) (format stream "This is ~a~%" title) (format stream "The mean time is ~a~%" (mean (first data))) (format stream "The number of failures is ~a~%" (sum (second data))))) A :plot method: (defmeth survival-proto :plot () (let ((km (send self :km-estimator)) (udt (send self :death-times))) (plot-lines (make-steps udt km))))

The data slot can be used to hold both the times and the death indicators.

The accessor method can be defined as

```
(defmeth survival-proto :data
         (&optional times status)
  (when times
    (call-next-method (list times status))
    (let* ((i (which (= 1 status)))
           (dt (select times i))
           (dt-list (coerce dt 'list))
           (udt (sort-data (remove-duplicates
                             dt-list
                             :test #'=)))
           (d (mapcar
               #'(lambda (x)
                 (count x dt-list :test #'=))
               udt))
           (r (mapcar
               #'(lambda (x)
                 (count x times :test #'<=))</pre>
               udt)))
      (setf (slot-value 'death-times) udt)
      (setf (slot-value 'num-deaths) d)
      (setf (slot-value 'num-at-risk) r)))
  (slot-value 'data))
```

### Examples

#### Survival Function Estimator

We can use an object to organize our tools for fitting a survival function.

Since we need the unique death times, death counts, and numbers at risk, we can define a prototype that adds slots to hold these values:

Accessors for these three slots are defined as

```
(defmeth survival-proto :death-times ()
  (slot-value 'death-times))
(defmeth survival-proto :num-deaths ()
  (slot-value 'num-deaths))
(defmeth survival-proto :num-at-risk ()
  (slot-value 'num-at-risk))
```

#### Some Cautions

- Unfortunately the object system does not allow you to hide slots and messages intended for internal use from public access.
- To protect yourself against breaking inherited methods you need to follow a few guidelines:
  - Don't use slot names you didn't add yourself.
  - Don't modify slots unless you are sure it is safe.
  - Don't define methods for messages unless you know this won't do any harm.

Instead of overriding the :describe method completely, we can augment it:

The call-next-method function calls the next method for the current selector

```
(call-next-method < arg-1 > \dots < arg-n >)
```

The autocor function can be defined as

## Overriding and Modifying Inherited Methods

The inherited :plot and :describe methods are not optimal for a time series.

We can override the :plot method with the definition

An example – a short moving average series:

An equally-spaced time series prototype might add origin and spacing slots:

Accessor methods for the new slots:

and default values for the title slot and the new slots can be set as

```
(send time-series-proto :title "a time series")
(send time-series-proto :origin 0)
(send time-series-proto :spacing 1)
```

## Prototypes and Inheritance

Prototypes can inherit from other objects, usually other prototypes.

The full form of a defproto expression is

```
egin{aligned} (	ext{defproto} & < name> \\ & < instance \ slots> \\ & < shared \ slots> \\ & < parents> \\ & < doc \ string>) \end{aligned}
```

All arguments except the first are evaluated.

<instance slots> and <shared slots> should be
nil or lists of symbols.

We won't be using shared slots.

should be a single object or a list of
objects - the default is the root object.

The instance slots of the new prototype are the union of the  $\langle instance\ slots \rangle$  in the call and the instance slots of all ancestors.

So you only need to specify additional slots you want.

Any data set needs its own data.

We can define an :isnew method that requires a data argument:

It is often useful to define an appropriate :isnew initialization method.

It is (almost) never necessary to define a new : new method.

The root object :isnew initialization method allows slots to be initialized by keyword arguments:

## Creating Instances from Prototypes

An instance is created by sending a prototype the :new message.

The method for this message does the following:

- creates a new object that inherits from the prototype
- adds a slot for each symbol in the prototype's instance-slots list
- sets the value of each new slot to its value in the prototype
- sends the new object the :isnew message with the arguments given to :new
- returns the new object

```
We can define a prototype for our data set as
(defproto data-set-proto '(data title))
Prototype objects are like any other objects.
We can place values in their slots
(send data-set-proto :slot-value
      'title "a data set")
and we can define methods for them:
(defmeth data-set-proto
         :title (&optional (title nil set))
  (if set (setf (slot-value 'title) title))
  (slot-value 'title))
(defmeth data-set-proto :data ...)
(defmeth data-set-proto :describe ...)
(defmeth data-set-proto :print ...)
(defmeth data-set-proto :plot ()
  (histogram (send self :data)
             :title (send self :title)))
```

### Prototypes

## Creating Simple Prototypes

Instead of repeating the process used so far for each new data set, we can construct a *dataset* prototype using defproto.

The simplest form of a defproto expression is

(defproto < name > < instance slots >)

defproto evaluates  $< instance \ slots >$  and

- constructs a new object, assigns it to the global variable < name >
- installs a slot proto-name with value name
- installs a slot instance-slots with the symbols from <instance slots>
- installs a slot with value nil for each symbol in the instance-slots list

Different instances created from a prototype usually differ only in the values of their instance slots.

## Help Information for Messages

If we change the definition of the :describe method to

then the string is used as a documentation string:

```
> (send x :help :describe)
:DESCRIBE
Method args: (&optional (stream t))
Prints a simple description of the object
to STREAM.
NIL
```

## Printing Objects

The printing system prints objects by sending them the :print message.

A method for :print must take an optional stream argument.

A simple :print method for our data set:

```
(defmeth x :print (&optional (stream t))
  (format stream "#<~a>" (send self :title)))
```

The result is

```
> x
#<a data set>
```

It is good programming practice not to assume too much about the slots an object has.

For our data set object, we can write accessor methods for the title and data slots:

```
(defmeth x :title (&optional (title nil set))
  (if set (setf (slot-value 'title) title))
  (slot-value 'title))
(defmeth x :data (&optional (data nil set))
  (if set (setf (slot-value 'data) data))
  (slot-value 'data))
Using these accessors we can rewrite the
```

:describe method:

```
(defmeth x :describe (&optional (stream t))
  (let ((title (send self :title))
        (data (send self :data)))
    (format stream "This is ~a~%" title)
    (format stream
            "The sample mean is ~a~%"
            (mean data))
    (format stream
            "The sample SD is ~a~%"
     (standard-deviation data))))
```

#### A few notes:

- Within a method, the variable self refers to the object receiving the message.
- self is needed since methods can be inherited.
- self is added to the environment for the function body before the other arguments.
- Within a method, the function slot-value can be used to access a slot.

  Using this function is more efficient than
  - Using this function is more efficient than using the :slot-value message.
- The slot-value function can *only* be used in the body of a method.
- Within a method, slot-value can be used as a place form with setf.

### An example:

The definition looks like a **defun**, except for the object expression appearing as the first argument.

The new :describe method can be used like any other method:

```
> (send x :describe)
This is a data set
The sample mean is 0.127521
The sample SD is 1.0005
NIL
```

## Defining New Methods

The code used to respond to a message is called a *method*.

send searches the receiving object and its ancestors until it finds a method.

All messages used so far used methods in the root object.

New methods can be defined using defmeth.

The general form of a defmeth expression is:

```
\begin{array}{ll} (\texttt{defmeth} & <\! object \!\! > <\! selector \!\! > <\! parameters \!\! > \\ & <\! body \!\! >) \end{array}
```

The argument  $\langle object \rangle$  is evaluated, the others are not.

We can add a slot for some data and a slot for a title string:

```
> (send x :add-slot 'data (normal-rand 50))
(1.39981 -0.0601746 ....)
> (send x :add-slot 'title)
NIL
> (send x :own-slots)
(TITLE DATA)
> (send x :slot-value 'title)
NIL
> (send x :slot-value 'title "a data set")
"a data set"
> (send x :slot-value 'title)
"a data set"
```

# Constructing New Objects

The root object is a *prototype* object.

Prototypes serve as templates for building new objects -instances.

The :new message is used to ask a prototype for a new instance.

Let's use an object to represent a data set:

```
> (setf x (send *object* :new))
#<Object: 1750672, prototype = *OBJECT*>
```

Initially, the object has no slots of its own:

```
> (send x :own-slots)
NTI.
```

### Some examples:

```
> (send *object* :own-slots)
(DOCUMENTATION PROTO-NAME INSTANCE-SLOTS)
> (send *object* :slot-value 'proto-name)
*OBJECT*

> *object*
#<Object: 302253140, prototype = *OBJECT*>
> (send *object* :slot-value 'instance-slots)
NIL
```

# Inheritance and the Root Object

Objects are organized in an *inheritance* hierarchy.

At the top is the *root object*, the value of \*object\*.

The root object contains methods for standard messages, such as

:own-slots - list of slots in an object

:add-slot - insert a new slot

:delete-slot - delete a slot

:slot-value - access or modify a slot's
value

As an example, the histogram function returns a histogram object:

```
> (setf p (histogram (normal-rand 20)))
#<Object: 1750540, prototype = HISTOGRAM-PROTO>
```

The object can be sent a message to add an additional set of points:

```
> (send p :add-points (normal-rand 20))
NIL
```

The message selector for the message is :add-points.

The message argument is the sample of normal variables generated by the expression (normal-rand 20).

The *message* consists of the selector and the arguments.

The procedure called to respond to this message is the *method* for the message.

#### Some Terms

An *object* is a data structure that contains information in slots.

Objects respond to *messages* asking them to take certain actions.

A message is *sent* to an object using the function **send** in an expression like

 $(send < object > < selector > < arg-1 > \dots < arg-n >)$ 

The *<selector>* is a keyword symbol used to identify the message.

Now suppose we come up with a fourth type, a simple time series.

We would have to edit this function, possibly breaking good code.

An alternative is to arrange for the appropriate code to be looked up in the data set itself – to dispatch on the data set type.

We would need some way of defining new data types and actions.

This is the basis of object oriented programming.

#### **Introduction**

Suppose we would like to build an "intelligent" function for describing or plotting a data set.

Initially we are looking at three types of data:

- single samples
- multiple samples
- paired samples

A describe-data function might be written as

#### References on OOP

Abelson, H. and Sussman, G. J., (1985), Structure and Interpretation of Computer Programs, Cambridge, Ma: MIT Press.

Winston, P. H. and Horn, B. K. P., (1988), Lisp, 3rd Edition, Reading, Ma: Addison Wesley.

Keene, S. E., (1989), Object-Oriented Programming in Common Lisp: A Programmer's Guide to CLOS, Reading, Ma: Addison Wesley.

Proceedings of the ACM Conference on Object-Oriented Systems, Languages and Applications (OOPSLA), in ACM SIGPLAN Notices, (1986-91).

Wegner, P., (1990), "Concepts and paradigms of object-oriented programming," *ACM SIGPLAN Messenger*, vol. 1.

ASA, August 1992 Tierney

# Some OOP Systems

- $\bullet$  C++ from ATT
- Objective C, used in NeXT computers.
- Smalltalk-80
- Object Pascal, for programming the Macintosh.
- Flavors, on Symbolics Lisp machines
- Lisp Object Oriented Programming System (LOOPS)
- ullet Object Lisp
- Portable Common LOOPS
- CLOS, the new Common Lisp standard
- Common Objects, from HP Labs.

ASA, August 1992

Tierney

#### Some Variations

- Languages/systems can be purely object oriented or just support object oriented programming.
- Two different approaches are used:
  - class/inheritance systems
  - prototype/delegation systems
- Most newer systems support some form of multiple inheritance.

# Origins of OOP

- Earliest example: Simula, a simulation language.
- First "pure" object oriented language: Smalltalk.
- Smalltalk was used for interacting with graphical objects, building graphical user interfaces.
- The Macintosh user interface inherits many features from the Smalltalk-based Xerox system.

ASA, August 1992

Tierney

# Some Background

Some basic features of object oriented programming include

- mutable state information
- messages and methods
- inheritance

Some people add other features, or place different emphasis on different features.

# **Objects**

Reasonable initial estimates for the parameters might be  $\alpha = 1$ ,

$$\beta_0 = \frac{\sum s_i}{\sum t_i}$$

for the constant term, and  $\beta_i = 0$  for all other i. For a single covariate:

```
> (newtonmax
   #'(lambda (theta)
     (llw x
          times
          status
          (first theta)
          (rest theta)))
   (list 0 (/ (sum status) (sum times)) 0))
maximizing...
Iteration 0.
Criterion value = -510.668
. . .
Iteration 8.
Criterion value = -47.0641
Reason for termination: gradient size ...
(0.311709 - 4.80158 1.73087)
```

# Weibull Regression

Suppose times are survival times, status contains death/censoring indicators, and x contains a matrix of covariates, including a column of ones.

A Weibull model for these data has a log likelihood of the form

$$\sum s_i \log \alpha + \sum (s_i \log \mu_i - \mu_i)$$

where

$$\log \mu_i = \alpha \log t_i + \eta_i$$
$$\eta_i = x_i \beta$$

and  $\alpha$  is the Weibull exponent,  $\beta$  is a vector of parameters.

A function to compute this log likelihood is

Greenwood's formula for the variance is

```
(* (^ km 2) (cumsum (/ d r (pmax (- r d) 1))))
```

The pmax expression prevents a division by zero.

Tsiatis' formula leads to

```
(* (^ km 2) (cumsum (/ d (^ r 2))))
```

To construct a plot we need a function that builds the consecutive corners of a step function:

Then

```
(plot-lines (make-steps udt km))
```

produces a plot of the Kaplan-Meier estimator.

Next, we need the number of deaths and the number at risk at each death time:

Using these values, we can compute the Kaplan-Meier estimator at the death times as

```
(setf km (accumulate \#'* (/ (- r d) r)))
```

The Fleming-Harrington estimator is

```
(setf fh (exp (- (cumsum (/ d r)))))
```

# Example

# Estimating a Survival Function

Suppose the variable times contains survival times and status contains status values, with 1 representing death and 0 censoring.

To compute a Kaplan-Meier or Fleming-Harrington estimator, we first need the death times and the unique death times:

#### Odds and Ends

#### **Errors**

The error functions signals an error:

```
> (error "bad value")
```

error: bad value

> (error "bad value: ~s" "A")

error: bad value: "A"

# Debugging

Several debugging functions are available:

debug/nodebug – toggle debug mode; in debug mode, an error puts you into a break loop.

break - called within a function to enter a
break loop

baktrace - prints traceback in a beak loop.

step - single steps through an evaluation.

### Interpolation and Smoothing

```
(spline x y :xvals xv)
(lowess x y)
(kernel-smooth x y :width w)
(kernel-dens x)
```

#### Linear Algebra Functions

```
(identity-matrix 4)
(diagonal '(1 2 3))
(diagonal '#2a((1 2)(3 4)))
(transpose '#2a((1 2)(3 4)))
(transpose '((1 2)(3 4)))
(matmult a b)
(make-rotation '(1 0 0) '(0 1 0) 0.05)
(lu-decomp a)
(inverse a)
(determinant a)
(chol-decomp a)
(qr-decomp a)
(sv-decomp a)
```

ASA, August 1992 Tierney

#### Some Statistical Functions

#### Some Basic Functions

```
> (difference '(1 3 6 10))
(2 3 4)
> (pmax '(1 2 3) 2)
(2 2 3)
> (split-list '(1 2 3 4 5 6) 3)
((1 2 3) (4 5 6))
> (cumsum '(1 2 3 4))
(1 3 6 10)
> (accumulate #'* '(1 2 3 4))
(1 2 6 24)
```

### Sorting Functions

```
> (sort-data '(14 10 12 11))
(10 11 12 14)
> (rank '(14 10 12 11))
(3 0 2 1)
> (order '(14 10 12 11))
(1 3 2 0)
```

Other useful format directives are "a and "s:

```
> (format t "Examples: ~a ~s~%" '(1 2) '(3 4))
Examples: (1 2) (3 4)
NIL
> (format t "Examples: ~a ~s~%" "ab" "cd")
Examples: ab "cd"
```

These two directives differ in their handling of escape characters.

There are many other format directives.

#### **Format**

format is a very flexible output function.

It prints to *output streams* or to strings.

The default output stream is \*standard-output\*; it can be abbreviated to t:

```
> (format *standard-output* "Hello~%")
Hello
NIL
> (format t "Hello~%")
Hello
NIL
> (format nil "Hello")
"Hello"
```

<sup>&</sup>quot;% is the format directive for a new line.

#### Arrays

The matrix function constructs a two-dimensional array:

```
> (matrix '(2 3) '(1 2 3 4 5 6))
#2A((1 2 3) (4 5 6))
```

Again you can type the printed representation

```
> (setf m '#2A((1 2 3) (4 5 6)))
#2A((1 2 3) (4 5 6))
```

and select extracts and modifies elements:

```
> (select m 1 1)
5
> (select m 1 '(0 1))
#2A((4 5))
> (select m '(0 1) '(0 1))
#2A((1 2) (4 5))
> (setf (select m 1 1) 'a)
A
> m
#2A((1 2 3) (4 A 6))
```

#### Sequences

Lists, vectors, and strings are sequences. Several functions operate on any sequence:

```
> (length '(1 2 3))
3
> (length '#(1 2 3))
3
> (length "abc")
3
> (select '(1 2 3) 0)
1
> (select '#(1 2 3) 0)
1
> (select "abc" 0)
#\a
```

Sequences can be coerced to different types with coerce:

```
> (coerce '(1 2 3) 'vector)
#(1 2 3)
> (coerce "abc" 'list)
(#\a #\b #\c)
```

Vectors can be copied with copy-vector.

Vectors are usually stored more efficiently than lists, and their elements can be accessed more rapidly.

But there are fewer functions for operating on vectors than on lists:

```
> (first x)
error: bad argument type - #(1 5 3)
> (rest x)
error: bad argument type - #(1 5 3)
```

#### <u>Vectors</u>

Vectors are a second form of compound data.

A vector is constructed with the vector function

```
> (vector 1 2 3)
#(1 2 3)
```

or by typing its printed representation:

```
> (setf x '#(1 2 3))
#(1 2 3)
> x
#(1 2 3)
```

Elements of vectors can be extracted and changed with select:

```
> (select x 1)
2
> (setf (select x 1) 5)
5
> x
#(1 5 3)
```

In addition to using select, you can get pieces of a list with

```
> (first '(1 2 3))
1
> (second '(1 2 3))
2
> (rest '(1 2 3))
(2 3)
```

Two other useful functions are remove-duplicates

```
> (remove-duplicates '(1 1 2 3 3))
(1 2 3)
```

and count:

```
> (count 2 '(1 2 3 4) :test #'=)
1
> (count 2 '(1 2 3 4) :test #'<=)
3</pre>
```

remove-duplicates also accepts a :test argument.

# More on Compound Data

#### <u>Lists</u>

Lists are the most important compound data type.

Lists can be empty:

```
> (list)
NIL
> '()
NIL
> ()
NIL
```

They can be used to represent sets:

```
> (union '(1 2 3) '(3 4 5))
(5 4 1 2 3)
> (intersection '(1 2 3) '(3 4 5))
(3)
> (set-difference '(1 2 3) '(3 4 5))
(2 1)
```

# Mapping

Mapping is the process of applying a function elementwise to a list.

The primary mapping function is mapcar:

```
> (setf x (normal-rand '(2 3 2)))
((0.27397 3.5358) (-0.11065 1.2178 1.050)
  (0.78268 0.95955))
> (mapcar #'mean x)
(1.904895 0.71913 0.8711149)
```

Mapcar can take several lists as arguments:

```
> (mapcar #'+ '(1 2 3) '(4 5 6))
(5 7 9)
```

Using mapcar, we can define a simple numerical integrator for functions on [0, 1]:

A function with a variable number of arguments is defined as

```
(defun f (x &rest y) ...)
```

All arguments beyond the first are made into a list and bound to y.

For example:

```
> (defun my-plus (&rest x) (apply #'+ x))
MY-PLUS
> (my-plus 1 2 3)
6
```

If more than one of these modifications is used, they must appear in the order &optional, &rest, &key.

There is an upper limit on the number of arguments a function can receive.

Keyword arguments are defined similarly to optional arguments:

```
(defun f (x &key y) ...)
(defun f (x &key (y 1)) ...)
(defun f (x &key (y 1 z)) ...)
```

The function is then called as

```
(f 1 : y 2)
```

Using a keyword argument in num-deriv:

With a keyword argument, num-deriv is called as

```
(num-deriv #'f 1 :h 0.001)
```

## Optional, Keyword and Rest Arguments

A number of functions used so far take optional arguments, keyword arguments, or variable numbers of arguments.

A function taking an optional argument is defined one of three ways:

```
(defun f (x &optional y) ...)
(defun f (x &optional (y 1)) ...)
(defun f (x &optional (y 1 z)) ...)
```

In the second and third forms, the default value is 1; in the first form it is nil

In the third form, z is t if the optional argument is supplied; otherwise z is nil.

We can add an optional argument for the step size to num-deriv:

#### **Local Functions**

It is also possible to set up local functions using flet:

flet sets up bindings in parallel, like let flet cannot be used to define local recursive functions.

labels is like flet but allows mutually recursive function definitions.

Another example: making a normal log likelihood:

The log likelihood of a sample from a normal distribution is

$$-\frac{n}{2}\left[\log\sigma^2 + \frac{(\overline{x} - \mu)^2}{\sigma^2} + \frac{s^2}{\sigma^2}\right]$$

A function for evaluating this expression as a function of  $\mu$  and  $\sigma^2$  is returned by

The result returned by this function can be maximized, or it can be plotted with spin-function or contour-function.

An example: making a derivative function:

We need a convention for determining the bindings of free variables.

This is the reason we need to use function on lambda expressions:

Free variables in a function are bound to their values in the environment where the function is created

This is called the *lexical* or *static* scoping rule. Other scoping rules are possible. Consider the lambda expression

(lambda (x) (+ x a))

The meaning of x in the body is clear – it is bound to the calling argument.

The meaning of **a** is not so clear – it is a *free* variable.

### Local Variables and Environments

## Variables and Scoping

A pairing of a variable symbol with a value is called a *binding* 

Collections of bindings are called an environment.

Bindings can be global or they can be local to a group of expressions.

let and let\* expressions and function definitions set up local bindings.

Lambda expressions are not yet Lisp functions.

To make them into functions, you need to use function or #':

To take our derivative:

To plot  $2x + x^2$  over the range [-2, 4],

Functions can also use lambda expressions to make new functions and return them as the value of the function.

We will see a few examples of this a bit later.

ASA, August 1992 Tierney

# Anonymous Functions

Defining and naming throw-away functions like f is awkward.

The same problem exists in mathematics.

Logicians developed the lambda calculus:

$$\lambda(x)(x+x^2)$$

is "the function that returns  $x + x^2$  for the argument x."

Lisp uses this idea:

is a lambda expression for our function.

We need a function that calls the value of fun with an argument:

```
> (funcall #'+ 1 2)
3
```

A correct definition of num-deriv is

Another useful function is apply:

```
> (apply #'+ '(1 2 3))
6
> (apply #'+ 1 2 '(3 4))
10
> (apply #'+ 1 '(2 3))
6
```

#### More on Functions

### Function as Data

Suppose we want a function num-deriv to compute a numerical derivative.

If we define

```
(defun f (x) (+ x (^ x 2)))
```

then we want to get

```
> (num-deriv #'f 1)
3
```

Defining num-deriv as

will not work – our function is the *value* of fun, not its *function definition*:

```
> (num-deriv #'f 1)
error: unbound function - FUN
```

Logical expressions can be combined using and, or, and not.

```
> (defun in-range (x) (and (< 3 x) (< x 5)))
IN-RANGE
> (in-range 2)
NIL
> (in-range 4)
Τ
> (defun not-in-range (x)
    (or (>= 3 x) (>= x 5)))
NOT-IN-RANGE
> (not-in-range 2)
Τ
> (defun in-range (x) (< 3 x 5))
IN-RANGE
> (in-range 2)
NIL
> (in-range 4)
Τ
> (defun not-in-range (x) (not (in-range x)))
NOT-IN-RANGE
```

### Conditional Evaluation and Predicates

The basic Lisp conditional evaluation construct is cond.

Several simplified versions exist, including if, unless and when

```
(defun my-abs (x) (if (>= x 0) x (-x)))
```

Another simplified version of cond is case:

# Some Lisp Programming

#### Weighted Least Squares Estimates:

```
Constant 2.80316 (0.148162)
Variable 0 -0.0837691 (0.0167996)
```

Scale taken as: 1
Deviance: 24.5704
Number of cases: 18
Degrees of freedom: 16

:residuals and other methods are inherited:

```
> (send m :residuals)
(-0.0439191 -0.790305 ...)
> (send m :plot-residuals)
```

#### Generalized Linear Models

The generalized linear model system includes functions for fitting models with gamma, binomial, and poisson errors and various links.

New error structures and link functions can be added.

## An Example:

bayes-model finds the posterior mode and prints a summary of first approximations to posterior means and standard deviations:

More accurate approximations are available:

```
> (send lk :moments)
((65.3085 0.485295) (17.158 0.186587))
```

Moments of functions of the parameters can also be approximated with :moments.

Marginal densities can be approximated using the :margin1 message.

## Approximate Bayesian Computations

Suppose times-pos are survival times and wbc-pos white blood cell counts for AG-positive leukemia patients (Feigl & Zelen, 1965).

The log posterior density for an exponential regression model with a flat prior density is

$$\sum_{i=1}^{n} \theta_{1} x_{i} - n \log(\theta_{0}) - \frac{1}{\theta_{0}} \sum_{i=1}^{n} y_{i} e^{\theta_{1} x_{i}}$$

It is computed by

Using these starting values, we can maximize the log likelihood function:

```
> (newtonmax #'gllik (list 83.5 1.4))
maximizing...
Iteration 0.
Criterion value = -155.603
Iteration 1.
Criterion value = -155.354
Iteration 2.
Criterion value = -155.347
Iteration 3.
Criterion value = -155.347
Reason for termination: gradient size is less than gradient tolerance.
(83.5173 1.67099)
```

You can use numgrad to check that the gradient is close to zero, and numhess to compute an approximate covariance matrix.

newtonmax will return the derivative information if it is given the keyword argument :return-derivs with value t.

If newtonmax does not converge, nelmeadmax may be able to locate the maximum.

A function to evaluate the log likelihood is

This definition uses the function log-gamma to evaluate  $log(\Gamma(\beta))$ .

Initial estimates for  $\mu$  and  $\beta$  are

```
> (mean x)
83.5172
> (^ (/ (mean x) (standard-deviation x)) 2)
1.39128
```

#### Maximization and ML Estimation

The function newtonmax maximizes a function using Newton's method with backtracking.

As an example, times between failures on aircraft air-conditioning units are

A simple model for these data assumes that the times are independent gamma variables with density

$$\frac{(\beta/\mu)(\beta x/\mu)^{\beta-1}e^{-\beta x/\mu}}{\Gamma(\beta)}$$

where  $\mu$  is the mean time between failures and  $\beta$  is the gamma exponent.

The function nreg-model fits a nonlinear regression model:

```
> (setf m (nreg-model #'f y (list 200 .1)))
```

Residual sum of squares: 7964.185 Residual sum of squares: 1593.158

. . .

Residual sum of squares: 1195.449

Least Squares Estimates:

```
Parameter 0 212.6837 (6.947153)
Parameter 1 0.06412127 (0.0082809)
```

R Squared: 0.9612608 Sigma hat: 10.93366 Number of cases: 12 Degrees of freedom: 10

Several methods are available for examining the model:

```
> (send m :residuals)
(25.434 -3.56598 -5.81094 4.1891 ...)
> (send m :leverages)
(0.124852 0.124852 0.193059 0.193059 ...)
> (send m :cooks-distances)
(0.44106 0.0086702 0.041873 0.021761 ...)
```

## More Models and Techniques

# Nonlinear Regression

Suppose we record reaction rates y of a chemical reaction at various concentrations x:

```
(def x (list 0.02 0.02 0.06 0.06 0.11 0.11 0.22 0.22 0.56 0.56 1.10 1.10))
(def y (list 76 47 97 107 123 139 159 152 191 201 207 200))
```

A model often used for the mean reaction rate is the Michaelis-Menten model:

$$\eta(\theta) = \frac{\theta_0 x}{\theta_1 + x}$$

A lisp function to compute the mean response:

Initial estimates can be obtained from a plot

```
> (plot-points x y)
#<Object: ...>
```

For example, suppose h is a histogram created by

```
(setf h (histogram (normal-rand 20)))
```

We can define a method for changing the sample by

```
(defmeth h :new-sample ()
  (send self :clear :draw nil)
  (pause 10)
  (send self :add-points (normal-rand 20)))
```

The variable self refers to the object receiving the message.

This special variable is needed because methods can be inherited.

The loop we used earlier can now be written as

```
(dotimes (i 50) (send h :new-sample))
```

Later on we will see how to override and augment standard methods.

# Defining Methods

Objects are arranged in a hierarchy.

When an object receives a message, it will use its own method to respond, if it has one.

If it does not have its own method, it asks its parents, and so on.

New methods are defined using defmeth.

A probability plot of the untransformed data is constructed by

```
(setf p (plot-points nq (bc x 1)))
```

Since the power is 1, bc just rescales the data.

To change the power used in the graph, define

```
(defun change-power (r)
  (send p :clear :draw nil)
  (send p :add-points nq (bc x r)))
```

Evaluating

```
(change-power .5)
```

redraws the plot for a square root transformation.

We could use a loop to run through some powers, but it is nicer to use a slider dialog:

The action function change-power is called every time the slider is adjusted.

A function to compute the transformation and normalize the result:

let\* is like let, but it establishes its bindings
sequentially.

Next, sort the observations and compute the approximate expected normal order statistics:

```
(def x (sort-data precipitation))
(def nq (normal-quant (/ (iseq 1 30) 31)))
```

# Graphical Animation Control

We have already seen how to construct some simple animations.

Using functions, we can provide graphical controls for animations.

As an example, let's look at the effect of the Box-Cox power transformation

$$h(x) = \begin{cases} \frac{x^{\lambda} - 1}{\lambda} & \text{if } \lambda \neq 0\\ \log(x) & \text{otherwise} \end{cases}$$

on a normal probability plot of our precipitation variable.

## Functions as Arguments

Earlier we used the function definition of sin as an argument to plot-function.

We can use functions defined with defun as well:

```
> (defun f (x) (+ (* 2 x) (^ x 2)))
F
> (plot-function #'f -2 3)
```

Recall that #'f is short for (function f), and is used for obtaining the function associated with the symbol f.

spin-function lets you construct a rotating plot of a function of two variables:

```
> (defun f (x y) (+ (^ x 2) (^ y 2)))
F
> (spin-function #'f -1 1 -1 1)
```

contour-function takes the same required arguments and produces a contour plot.

Functions can send messages to objects:

Suppose m1 is a submodel of m2.

A function to compute the F statistic is

The let construct is used to create local variables that simplify the expression.

The documentation string is used by help:

## Defining Functions

Functions are defined with the special form defun.

The simplest form of the defun syntax is

```
(defun < name > < parameters > < body >)
```

For example, a function to delete an observation can be defined as

```
> (defun delete-case (i x)
          (select x (remove i (iseq (length x)))))
DELETE-CASE
> (delete-case 2 (list 3 7 5 9 12 3 14 2))
(3 7 9 12 3 14 2)
```

None of the arguments to defun are quoted: defun is a special form that does not evaluate its arguments.

# **Defining Functions and Methods**

No system can provide all tools any user might want.

Being able to define your own functions lets you

- provide short names for functions you use often
- provide simple commands to execute a long series of operations on different data sets
- develop new methods not provided in the system

### Some examples:

```
> (send m :coef-estimates)
(885.537 -1.37537 -6.573)
> (send m :coef-standard-errors)
(61.801 0.194465 0.583655)
> (send m :residuals)
(5.05705 2.43809 9.50074 19.9904 ...)
> (send m :fit-values)
(366.943 203.562 165.499 ...)
> (send m :plot-residuals)
#<Object: 1568394, prototype = SCATTER...>
> (send m :cooks-distances)
(0.00247693 0.000255889 0.00300101 ...)
> (plot-lines (iseq 1 30) *)
```

The regression-model function accepts a number of keyword arguments, including

:print - print summary or not

:intercept - include intercept term or not

:weights - optional weight vector

A range of messages are available for examining and modifying the model:

> (send m :help)
REGRESSION-MODEL-PROTO
Normal Linear Regression Model
Help is available on the following:

:ADD-METHOD :ADD-SLOT :BASIS :CASE-LABELS :COEF-ESTIMATES :COEF-STANDARD-ERRORS ...

# Regression

Regression models are implemented using objects and message-sending.

We can fit abrasion-loss to tensile-strength and hardness:

Least Squares Estimates:

Constant	885.537	(61.801)
Variable 0	-1.37537	(0.194465)
Variable 1	-6.573	(0.583655)

```
R Squared: 0.840129
Sigma hat: 36.5186
Number of cases: 30
Degrees of freedom: 27
```

#<Object: 303170820, prototype = REGRESS...>

dotimes is one of several simple looping constructs available in Lisp; another is dolist.

If you have a very fast workstation or micro, this animation may move by too quickly.

One solution is to insert a pause of 10/60 of a second using

```
(pause 10)
```

So an alternate version of the loop is

```
(dolist (i (iseq 50))
  (send h :clear :draw nil)
  (pause 10)
  (send h :add-points (normal-rand 20)))
```

## Dynamic Simulations

We can also use plot modification to make a simple animation.

As an example, let's look at the variability in a histogram of 20 normal random variables.

Start by setting up a histogram:

```
> (setf h (histogram (normal-rand 20)))
#<Object: 303107988, prototype = HISTOGRAM...>
```

Then use a simple loop to replace the data:

```
(dotimes (i 50)
  (send h :clear :draw nil)
  (send h :add-points (normal-rand 20)))
```

The :draw nil insures that each histogram remains on the screen until it is replaced by the next one.

A quadratic regression of abrasion-loss on tensile-strength produces the fit equation

$$Y = -280.1 + 5.986X + -0.01845X^2 + \epsilon$$

To put this curve on our plot we can use

The :clear message clears the plot.

> (send p :help :clear)
:CLEAR
Message args: (&key (draw t))
Clears the plot data. If DRAW is true the plot
is redrawn; otherwise its current screen image
remains unchanged.

:add-lines and :add-points add new data:

> (send p :help :add-points)
:ADD-POINTS

Method args:

(points &key point-labels (draw t))
or: (x y &key point-labels (draw t))
Adds points to plot. POINTS is a list of
sequences, POINT-LABELS a list of strings. If
DRAW is true the new points are added to the
screen. For a 2D plot POINTS can be replaced
by two sequences X and Y.

The term *sequence* means a list or a vector.

. . .

Plot objects understand a number of other messages.

The help message provides a (partial) listing:

```
> (send p :help)
SCATTERPLOT-PROTO
Scatterplot.
Help is available on the following:
:ABLINE :ACTIVATE :ADD-FUNCTION :ADD-LINES
```

The list of topics is the same for all scatterplots, but is somewhat different for rotating plots, scatterplot matrices, and histograms.

#### Modifying a Scatterplot

After producing a plot, you can add more points or lines to it.

To do this, you need to save the *plot object* returned by plotting functions in a variable:

To use this object, you can send it messages.

This is done with expressions like

```
(	ext{send } < object> \\ < message \ selector> \\ < argument \ 1> \ \ldots)
```

For example,

```
(send p :abline -2.18 0.66)
```

adds a regression line to the plot.

#### Linked Plots

A scatterplot matrix links points in separate scatterplots.

You can link any plots by choosing **Link View** from the menus of the plots you want to link.

For example, you can link a histogram of hardness to a scatterplot of abrasion-loss against tensile-strength.

If you want to be able to select points with a particular label, you can use name-list.

(name-list 30)

You can also give name-list a list of strings.

Linking is based on the point index, so you have to use the same observation order in each plot.

### Interacting with Individual Plots

Plot menus contain several items that can be used together with selecting and brushing:

- If the **Labels** item is selected, point labels are shown next to selected or highlighted points.
- The selected points can be removed by choosing **Remove Selection**
- Unselected points can be removed by choosing Focus on Selection
- The plot can be rescaled after adding or removing points.
- You can change the color or the symbol used to draw a point.
- You can specify a set of indices to select or save the currently selected indices to a variable with the **Selection** item.

Depth cuing in spinning plots works by changing symbols, so it has to be turned off if you want to use different symbols.

To change the mouse mode, choose **Mouse Mode** from the plot menu, and then select the mode you want from the dialog that is presented.

You can change the shape of the brush by selecting **Resize Brush** from the plot menu.

Brushing and selecting are available in all plots.

These operations can be useful in spinning plots to highlight features, for example by looking at the shape of a slice of the data.

It is possible to change the way these two standard modes behave and to define new mouse modes; we will see examples of this later on.

#### Two mouse modes are available:

Selecting. A plot is in selecting mode when the cursor is an arrow; this is the default.

In this mode you can

- select a point by clicking on it
- select a group of points by dragging a selection rectangle
- add to a selection by clicking or dragging with the extend modifier

Brushing. In this mode the cursor looks like a paint brush, and a dashed rectangle, the brush, is attached to it.

#### In this mode

- as you move the brush, points in it are highlighted
- this highlighting is transient; it is turned off when points move out of the brush
- you can select points by clicking and dragging

# Scatterplot Matrices

Another way to look at three (or more) variables is to use a scatterplot matrix of all pairwise scatterplots:

One way to use this plot is to approximately condition on one or more variables using selecting and brushing.

The center of rotation is the midrange of the data.

There are three scaling options:

```
variable (the default) – each variable is scaled by a different amount to make their ranges equal to [-1, 1].
```

fixed – a common scale factor is applied to make the largest range equal to [-1,1]

nil - no scaling is used; the variables are assumed to have been scaled to [-1, 1].

You can center the variables at their means and scale them by a common factor with

```
For example,
(spin-plot (list hardness
                 tensile-strength
                 abrasion-loss)
           :title "Abrasion Loss Data"
           :variable-labels
           (list "Hardness"
                 "Tensile Strength"
                  "Abrasion Loss"))
and
(spin-plot (list hardness
                 tensile-strength
                 abrasion-loss)
           :variable-labels
           (list "Hardness"
                 "Tensile Strength"
                 "Abrasion Loss")
           :title "Abrasion Loss Data")
are equivalent.
```

spin-plot accepts several keyword arguments, including

:title - a title string for the plot

:variable-labels - a list of strings to use as axis labels

:point-labels - a list of strings to use as point labels

:scale - one of the symbols variable, fixed, or nil. (nil evaluates to itself, but the others need to be quoted).

A keyword symbol is a symbol starting with a colon.

Keyword symbols evaluate to themselves, so they do not need to be quoted.

Keyword arguments to a function must be given after all required (and optional) arguments.

Keyword arguments can be given in any order.

Every plot window provides a menu for communicating with the plot.

The menu on a rotating plot allows you to change the speed of rotation, or to choose whether to use depth cuing or whether to show the coordinate axes.

By default, the plot uses depth cuing: points closer to the viewer are drawn larger than points farther away.

The **Options** item in the menu lets you switch the background color from black to white; it also lets you change the type of scaling used.

# Spinning Plots

Three variables can be displayed in a three-dimensional rotating scatterplot.

Rotation, together with depth cuing, allow your mind to form a three-dimensional image of the data.

A rotating plot of the abrasion loss data is constructed by

You can rotate the plot by placing the mouse cursor in one of the Pitch, Roll, or Yaw squares and pressing the mouse button.

If you press the mouse button using the *extend* modifier, then the plot continues to rotate after you release the mouse; it stops the next time you click in the button bar.

## Dynamic Graphs

The abrasion loss data set used earlier includes a second covariate, the hardness values of the rubber samples.

Two-dimensional static graphs alone are not adequate for examining the relationship among three variables.

Instead, we can use some dynamic graphs.

Dynamic graphs use motion and interaction to allow us to explore higher-dimensional aspects of a data set.

We will look at

- spinning plots
- scatterplot matrices
- brushing and selecting
- linking plots

These functions should be adequate for most purposes.

If you need to read a file that is not of this form, you can use low-level file handling functions available in Lisp.

You can also use the load function or the Load menu command to load a file of Lisp expressions.

load requires the file name to have a .lsp extension.

You can use these functions together with select:

Suppose you have a file abrasion.dat of the form

```
      372
      162
      45

      206
      233
      55

      175
      232
      61
```

#### Then

```
> (read-data-columns "abrasion.dat" 3)
((372 206 175 ...)
  (162 233 232 ...)
  (45 55 61 ...))
> (read-data-file "abrasion.dat")
(372 162 45 206 233 55 ...)
```

The items in the file can be any items you would type into the interpreter (numbers, strings, symbols, etc.).

### Reading Data Files

Two functions let you read data from a standard text file:

```
(read-data-columns [<file> [<columns>]]) (read-data-file [<file>])
```

The items in the file must be separated by white space (any number or combination of spaces, tabs or returns), not commas or other delimiters.

The arguments are optional:

- If < file > is omitted, a dialog is presented to let you select the file to read from.
- If columns is omitted, the number is determined from the first line of the file.

read-data-columns returns a list of lists representing the columns in the file.

read-data-file returns a list of the items in the file read in a row at a time. The general form of a setf call is

```
(setf < form > < value >)
```

setf can be used to modify other compound data, such as vectors and arrays.

Like def, setf can also be used to assign a value to a symbol:

```
> (setf z 3)
3
> z
3
```

There are three differences between def and setf:

- def returns the symbol, setf returns the value.
- def keeps track of the variables it creates; variables returns a list of them.
- def can only change global variable values, not local ones.

To protect a list, you can copy it before making modifications:

```
> (def y (copy-list x))
Y
> (setf (select y 1) 'b)
B
> y
(A B 3 4)
> x
(A 2 3 4)
```

setf destructively modifies a list, it does not copy it:

```
> (def x (list 1 2 3 4))
X
> (def y x)
Y
> (setf (select y 0) 'a)
A
> y
(A 2 3 4)
> x
(A 2 3 4)
```

The symbols x and y are two different names for the same list, and setf has changed that list.

# Modifying Data

setf can be used to modify individual elements or sets of elements:

```
(def x (list 3 7 5 9 12 3 14 2))
X
> x
(3 7 5 9 12 3 14 2)
> (setf (select x 4) 11)
11
> x
(3 7 5 9 11 3 14 2)
> (setf (select x (list 0 2)) (list 15 16))
(15 16)
> x
(15 7 16 9 11 3 14 2)
```

### Combining Several Lists

append and combine allow you to merge several lists:

append requires its arguments to be lists and only appends at one level.

combine allows simple data arguments, and works recursively through nested lists:

```
> (combine 1 2 (list 3 4))
(1 2 3 4)
> (append (list (list 1 2) 3) (list 4 5))
((1 2) 3 4 5)
> (combine (list (list 1 2) 3) (list 4 5))
(1 2 3 4 5)
```

To select all elements of x except the element with index 2, you can use

or

The /= function produces

and which turns this into indices of the t elements:

#### Forming Subsets and Deleting Cases

The select function lets you to select one or more elements from a list:

```
(def x (list 3 7 5 9 12 3 14 2))
> (select x 0)
3
> (select x 2)
5
```

Lisp, like C but in contrast to FORTRAN, numbers elements of lists starting at zero.

To get a group of elements at once, use a list of indices:

```
> (select x (list 0 2))
(3 5)
```

The sample size arguments may also be lists of integers.

The result will then be a list of samples.

The function sample selects a random sample without replacement from a list:

```
> (sample (iseq 1 20) 5)
(20 11 3 14 10)
```

If t is given as an optional third argument, the sample is drawn with replacement:

```
> (sample (iseq 1 20) 5 t)
(2 14 14 11 18)
```

Any value other than nil can be given as the third argument.

[Logical operations usually interpret any value other than nil as true.]

Giving nil as the third argument is equivalent to omitting the argument.

ASA, August 1992 Tierney

## Generating Random Data

50 uniform variates are generated by

(uniform-rand 50)

normal-rand and cauchy-rand are similar.

50 gamma variates with unit scale and exponent 4 are generated by

(gamma-rand 50 4)

t-rand and chisq-rand are similar.

50 beta variates with  $\alpha = 3.5$  and  $\beta = 7.2$  are generated by

(beta-rand 50 3.5 7.2)

f-rand is similar.

Binomial and Poisson variates are generated by

(binomial-rand 50 5 .3) (poisson-rand 50 4.3)

#### For example, if the data in the table

	Variety		
Density	1	2	3
1	9.2 12.4 5.0	8.9 9.2 6.0	16.3 15.2 9.4
2	12.4 14.5 8.6	12.7 14.0 12.3	18.2 18.0 16.9
3	12.9 16.4 12.1	14.6 16.0 14.7	20.8 20.6 18.7
4	10.9 14.3 9.2	12.6 13.0 13.0	18.3 16.0 13.0

are entered by rows

then the density and variety levels are generated by

and

repeat is useful for generating sequences with a particular pattern:

```
> (repeat 2 3)
(2 2 2)

> (repeat (list 1 2 3) 2)
(1 2 3 1 2 3)

> (repeat (list 1 2 3) (list 3 2 1))
(1 1 1 2 2 3)
```

## Some Data-Handling Functions

# Generating Systematic Data

We have already seen two functions,

- iseq for generating a sequence of consecutive integers
- rseq for generating equally spaced real values.

iseq can also be used with a single integer argument n; this produces a list of integers  $0, 1, \ldots, n-1$ :

```
> (iseq 10)
(0 1 2 3 4 5 6 7 8 9)
```

# Interrupting a Calculation

Occasionally you may need to interrupt a calculation.

Each system has its own method for doing this:

- On the Macintosh, hold down the Command key and the Period key.
- In MS Windows, hold down CONTROL-C
- On UNIX systems, use the standard interrupt, usually CONTROL-C.

# Listing and Undefining Variables

variables gives a listing of variables created with def:

```
> (variables)
(PRECIPITATION RURAL URBAN ...)
```

To free up space, you may want to get rid of some variables:

```
> (undef 'rural)
RURAL
> (variables)
(PRECIPITATION URBAN ...)
```

The function apropos gives a listing of the symbols that contain its argument:

> (apropos 'norm)
NORMAL-QUANT
NORMAL-RAND
NORMAL-CDF
NORMAL-DENS
NORMAL
BIVNORM-CDF
NORM

help\* gives help information about all functions with names containing its argument:

<pre>&gt; (help* 'norm)</pre>	
BIVNORM-CDF	[function-doc]
Args: (x y r) Returns the value of the standard normal distribution function with at (X, Y). Vectorized.	
NORMAL-CDF Args: (x)	[function-doc]
Returns the value of the standard	normal
distribution function at X. Vecto	rized.

# Getting Help

The help function provides a brief description of a function:

> (help 'median)

MEDIAN

[function-doc]

Args: (x)

Returns the median of the elements of X.

help is an ordinary function – the quote in front of median is essential.

# A Command History Mechanism

There is a simple command history mechanism:

- the current input expression
- + the last expression read
- ++ the previous value of +
- +++ the previous value of ++
  - \* the result of the last evaluation
  - \*\* the previous value of \*
- \*\*\* the previous value of \*\*

The variables \*, \*\*, and \*\*\* are the most useful ones.

# More on the Interpreter

# Saving Your Work

#### It is possible to

- save a transcript of your session with the dribble function (available in one of the menus on a Macintosh or the MS Windows version)
- save one or more defined variables to a file using the savevar function.
- save a copy of a plot
  - to the clipboard on a Macintosh or in Windows
  - to a postscript file in X11

To get the function definition of sin we can use (function sin)

or the shorthand form

#'sin

A plot of  $\sin(x)$  between  $-\pi$  and  $\pi$  is then produced by

(plot-function (function sin) (- pi) pi)

or

(plot-function #'sin (- pi) pi)

## Plotting Functions

A simpler way to plot a function like sin(x) is to use plot-function.

It expects a function, a lower limit, and an upper limit as arguments.

Unfortunately, just using

(plot-function sin (- pi) pi)

will not work:

> (plot-function sin (- pi) pi)
error: unbound variable - SIN

The reason is that symbols have separate values and function definitions.

This can be a bit of a nuisance.

But it means that you can't accidentally destroy the list function by defining a variable called list.

Scatterplots are of course particularly useful for bivariate data.

As an example, abrasion-loss contains the amount of rubber lost in an abrasion test for each of 30 specimens; tensile-strength contains the tensile strengths of the specimens.

A scatterplot of abrasion-loss against tensile-strength is produced by

(plot-points tensile-strength abrasion-loss)

A connected lines plot is also useful for plotting functions.

As an example, let's plot the sine curve over the range  $[-\pi, \pi]$ .

A sequence of 50 equally spaced points between  $-\pi$  and  $\pi$  is constructed by

An expression for plotting sin(x) is

You can simplify this expression by first defining a variable x as

and then constructing the plot with

#### Two-Dimensional Plots

The precipitation data were collected over time.

It may be useful to look at a plot against time to see if there is any trend.

To construct a list of integers from 1 to 30 we use

```
> (iseq 1 30)
(1 2 ... 30)
```

A scatterplot of precipitation against time is produced by

```
(plot-points (iseq 1 30) precipitation)
```

Sometimes it is easier to see temporal patterns in a plot if the points are connected by lines:

(plot-lines (iseq 1 30) precipitation)

In Lisp-Stat, arithmetic operations are applied elementwise to compound data:

```
> (+ 1 precipitation)
(1.77 2.74 1.81 2.2 2.95 ...)
> (log precipitation)
(-0.2613648 0.5538851 -0.210721 ...)
> (sqrt precipitation)
(0.877496 1.31909 0.9 1.09545 ...)
```

The results can be passed to summary or plotting functions using compound expressions like

```
(mean (sqrt precipitation))
```

and

```
(histogram (sqrt precipitation))
```

The boxplot function produces a parallel boxplot when given a list of datasets:

```
(boxplot (list urban rural))
```

```
Some summaries:
```

```
> (mean precipitation)
1.675
> (median precipitation)
1.47
> (standard-deviation precipitation)
1.0157
> (interquartile-range precipitation)
1.145
And some plots:
> (histogram precipitation)
#<0bject: ...>
> (boxplot precipitation)
#<0bject: ...>
```

The results returned by these functions will be used later.

ASA, August 1992 Tierney

## Elementary Computations and Graphs

#### One-Dimensional Summaries and Plots

A small data set:

Precipitation levels in inches recorded during the month of March in the Minneapolis-St. Paul area over a 30-year period:

```
    0.77
    1.74
    0.81
    1.20
    1.95
    1.20

    0.47
    1.43
    3.37
    2.20
    3.00
    3.09

    1.51
    2.10
    0.52
    1.62
    1.31
    0.32

    0.59
    0.81
    2.81
    1.87
    1.18
    1.35

    4.75
    2.48
    0.96
    1.89
    0.90
    2.05
```

Use def and list to enter the data:

```
(def precipitation (list .77 1.74 .81 ...))
```

or

```
(def precipitation '(.77 1.74 .81 ...))
```

We will see later how to read the data from a file.

Complicated expressions are easier to read when they are properly indented:

The interpreter should help you with indentation, and with matching parentheses.

Exiting from Lisp-Stat:

- Choose Quit from the File menu
- Type (exit)

Since quote is needed very frequently, there is a shorthand form:

Compound expressions are just lists.

Quoting an expression tells the interpreter *not* to evaluate it.

```
> (quote (+ 1 2))
(+ 1 2)
```

Lisp quotation is similar to English quotation:

Think about

Say your name!

and

Say "your name"!

quote is a special form.

Data sets can be named (symbols given values) using def:

```
> (def x (list 1 2 3))
X
> x
(1 2 3)
```

def is a special form.

Numbers, strings, and symbols are *simple data*. Several forms of *compound data* are available. The most basic form of compound data is the list:

```
> (list 1 2 3)
(1 2 3)
> (list 1 "a string" (list 2 3))
(1 "a string" (2 3))
```

Other forms of compound data:

- vectors
- multi-dimensional arrays

Compound expressions like (+ 1 2) are evaluated by

- looking up the function definition of the symbol +
- evaluating the argument expressions
- applying the function to the arguments

[Exception: If the function definition is a  $special\ form$ ]

Compound expressions are evaluated recursively:

```
> (+ (* 2 3) 4)
10
```

Operators like +, \*, etc., are functions, like exp and sqrt

```
> (exp 1)
2.718282
> (sqrt 2)
1.414214
> (sqrt -1)
#C(0 1)
```

Logical values and strings also evaluate to themselves:

```
> t ; true
T
> nil ; false
NIL
> "This is a string 1 2 3 4"
"This is a string 1 2 3 4"
```

The semicolon ";" is the Lisp comment character.

Symbols are evaluated by looking up their values, if they have one:

```
> pi
3.141593
> PI
3.141593
> x
error: unbound variable - X
```

Symbol names are *not* case-sensitive.

Operations on numbers are performed with compound expressions:

```
> (+ 1 2)
3
> (+ 1 2 3)
6
> (* (+ 2 3.7) 8.2)
46.74
```

The basic rule: everything is evaluated.

Numbers evaluate to themselves:

```
> 416
416
> 3.14
3.14
> -1
-1
```

## The Interpreter

Your interaction with Lisp-Stat is a conversation between you and the interpreter.

When the interpreter is ready to start the conversation, it gives you a prompt like

>

When you type in an expression and hit *return*, the interpreter evaluates the expression, prints the result, and gives a new prompt:

> 1

1

>

We'll start with an introduction to using Lisp-Stat as a statistical calculator and plotter.

We will see how to

- interact with the interpreter
- perform numerical operations
- modify data
- construct systematic and random data
- use built-in dynamic plots
- construct linear regression models
- define simple functions
- use these functions for
  - a simple animation
  - fitting nonlinear regression models
  - maximum likelihood estimation
  - approximate posterior computations

# A Tutorial Introduction

You can define functions of your own to implement new numerical methods or dynamic graphical ideas of your own.

We will look at several examples:

- estimating a survival curve
- Weibull regression
- dynamic power transformation
- variability in density estimation
- a regression sensitivity demonstration
- the Grand Tour

In most versions of XLISP-STAT it is also possible to incorporate and access routines written in C or FORTRAN.

#### You can also

- fit generalized linear models
- numerically maximize likelihood functions
- compute approximate posterior moments and marginal densities.

#### and nonlinear regression models:

#### Least Squares Estimates:

Parameter 0 212.6837 (6.947153) Parameter 1 0.06412127 (0.0082809)

R Squared: 0.9612608 Sigma hat: 10.93366 Number of cases: 12 Degrees of freedom: 10

М

# You can fit linear regression models:

#### Least Squares Estimates:

Constant 885.5374 (61.80104)
Variable 0: -6.573002 (0.5836548)
Variable 1: -1.375367 (0.1944645)

R Squared: 0.840129
Sigma hat: 36.51856
Number of cases: 30
Degrees of freedom: 27

#<Object: ...>

You can construct a variety of interactive and dynamic graphs:

# Overview of Lisp-Stat

Lisp-Stat allows you to enter data, transform data, and compute summary statistics:

```
> (def abrasion-loss
       (list 372 206 175 154 136 112
                                       55
              45 221 166 164 113
                                   82
                                       32
             228 196 128 97 64 249 219
             186 155 114 341 340 284 267
             215 148))
ABRASION-LOSS
> abrasion-loss
(372 206 175 154 136 112 55 45 ...)
> (log abrasion-loss)
(5.918894 5.327876 5.164786 ...)
> (mean abrasion-loss)
175.4667
> (standard-deviation abrasion-loss)
88.12755
```

## Course Objectives

After completing the course, you should be able to

- use Lisp-Stat with your own data for basic statistical calculations and graphics.
- develop some simple numerical and graphical tools for your own applications
- understand the basics of Lisp programming and object-oriented programming

You should also be well prepared to learn more about Lisp-Stat by working through the book.

## Course outline

- 1. Overview of Lisp-Stat
- 2. A Tutorial Introduction
- 3. Some Lisp Programming
- 4. Objects
- 5. Outline of the Graphics System
- 6. Some Dynamic Graphics Examples

## Some Historical Notes

- Several extensible statistical environments have been based on high level languages:
  - The New S language
  - APL-based systems (Anscombe)
  - Tools for the Gauss system
- Several researchers have based systems on the Lisp language:
  - McDonald and Pedersen
  - Stuetzle
  - Oldford and Peters
  - Buja and Hurley
- A strong argument in favor of Lisp is that Lisp provides excellent support for experimental programming.

#### **Documentation**

A tutorial introduction is available as a technical report:

Tierney, L., (1989), "XLISP-STAT: A statistical environment based on the XLISP language," U of M Tech. Rep. 528.

The LATEX source for this report is available for ftp from umnstat.stat.umn.edu or by email from statlib.

More complete documentation is available as a book:

Tierney, L., (1990), Lisp-Stat: An
Object-Oriented Environment for Statistical
Computing and Dynamic Graphics, New
York, NY: Wiley.

The technical report corresponds to Chapter 2 of the book.

If you do not have access to ftp, you can get a copy of the Macintosh or MS Windows executables by sending disks and a self-addressed, stamped mailer to

Luke Tierney School of Statistics University of Minnesota Minneapolis, MN 55455

The number of disks required is

Two 800K disks for the Macintosh version One  $3\frac{1}{4}$ " high-density disk for the MS Windows version

## Obtaining XLISP-STAT

XLISP-STAT source code and executables are available free of charge.

Source code for the UNIX, Macintosh, and MS Windows versions is available by anonymous ftp from umnstat.stat.umn.edu and by email from statlib.

If you have access to the *internet* but have never used ftp, there is probably someone at your site who can help you.

Executables for Macintosh and MS Windows are also available for anonymous ftp from umnstat.stat.umn.edu and some other sites.

#### Implementation and Portability:

- Lisp-Stat is a general specification
- XLISP-STAT is a first implementation
- XLISP-STAT runs on
  - Apple Macintosh
  - MS Windows
  - Commodore Amiga (J. Lindsey)
  - -Sun workstations using SunView
  - BSD UNIX workstations running X11
- A Kyoto Common Lisp-based implementation may be available soon

## Some things Lisp-Stat does not do:

• incorporate a large collection of tools for specialized analyses

> Such tools can be implemented within the system or, if C or Fortran implementations are already available, they can be accessed through dynamic or static loading.

• provide extensive support for presentation graphics

Other systems on workstations and PC's already provide a wide range of tools for preparing presentation graphics.

## What is Lisp-Stat

Lisp-Stat is an extensible environment for statistical computing and dynamic graphics.

Some of its features are

- a variety of numerical statistical operations
- a variety of interactive and dynamic graphical methods
- a very high level programming language (Lisp) that can be used to
  - simplify combinations of calculations
  - adapt methods to specific problems
  - add new capabilities to the system
- an extensible graphics system through
  - access to graphical interface tools (Menus and Dialogs)
  - standard graphs as building blocks
  - use of object-oriented programming

#### Abstract

Lisp-Stat is an environment for general statistical computing and for using and developing dynamic graphical methods. The Lisp-Stat system contains a set of functions for performing basic statistical calculations and constructing dynamic statistical graphs such as linked scatterplots and rotatable three-dimensional plots. In addition, new numerical and graphical tools can be added to the system using the Lisp programming language and a simple object-oriented programming system.

The course will begin with an overview of the capabilities of the system and then introduce basic elements of Lisp programming and concepts of object-oriented programming. These ideas will then be used on several examples to illustrate how to add new graphical and numerical methods to the system. The examples will include some simple tools for examining survival data and an implementation of the Grand Tour for viewing data sets in four or more dimensions.

If possible, several extended breaks will be scheduled and a small number of microcomputers or workstations will be made available during these breaks to allow participants to experiment with the ideas presented.

# Statistical Computing and Dynamic Graphics Using Lisp-Stat

Luke Tierney School of Statistics University of Minnesota

June 24, 1992