STIFFNESS NONLINEARITY OF THREE SANDS

By Satoshi Yamashita, Michele Jamiolkowski, and Diego C. F. Lo Presti³

Abstract: This paper presents the results of 254 drained triaxial compression tests. The results are analyzed with the aim of obtaining a phenomenological description of secant Young's modulus variation according to different test conditions. Using empirical fitting equations, the influences of different factors such as axial strain, vertical consolidation stress, consolidation stress ratio, and stress history on the secant Young's modulus under axisymmetric (triaxial) loading conditions at small and intermediate axial strains are singled out and presented. The main purpose of this paper is to identify the factors affecting the nonlinear secant stiffness of sand and to quantify their relevance at different levels of strain.

INTRODUCTION

Stiffness reduction with increasing strain and shear stress levels has been widely recognized in geotechnical engineering for the last half century. Moreover, more recently [e.g., Tatsuoka (1988)] the improvement achieved in the reliable measurement of soil behavior at small ($\varepsilon \approx 10^{-5}$) and intermediate strains $(10^{-5} < \varepsilon \le 5 \times 10^{-3})$ in the laboratory has highlighted the degree of nonlinearity exhibited by soil stiffness, emphasizing the paramount importance of this phenomenon for predicting the displacement of geotechnical constructions.

Based on the above, this paper is aimed at the purely phenomenological description of the secant Young's modulus $(E_{\rm sec})$ nonlinearity at small and intermediate strains, as inferred from a large number of drained triaxial compression tests performed on three sands.

All the triaxial tests were performed on specimens prepared by means of an air pluvial deposition subjected thereafter to both isotropic and anisotropic consolidation. Both the local axial strain and the local radial strain were measured in many tests. The results obtained have been analyzed with the aim of quantifying the relevance of the different factors that influence the $E_{\rm sec}$ nonlinearity at small and intermediate strains of the three test sands.

heading EXPERIMENTAL DATA

Test Sands

The soils used were Toyoura, Quiou, and Ticino sands. Toyoura sand has been widely used for laboratory stress-strain tests in Japan. Ticino sand has been used for Calibration Chamber and laboratory stress-strain tests in Italy since 1976. More recently, Quiou sand (a French sand) has also been used in Italian Calibration Chamber and stress-strain laboratory tests. Toyoura sand is a subangular, uniform, fine quartz sand that does not contain fines. Quiou sand is a subangular, wellgraded, coarse to medium carbonate sand containing about 2% of fines. Quiou sand is a crushable material containing 73% in weight of shell fragments (Fioravante et al. 1994b). Ticino sand is a medium to coarse, uniform, predominantly silica sand that does not contain fines (Bellotti et al. 1996). The main physical properties of these sands are shown in Table 1.

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Sample Preparation

Specimens with 70 mm in diameter and 140 mm in height were reconstituted by dry pluvial deposition method. Only for some tests on Ticino sand were smaller samples tested (i.e., 40 and 60 mm in diameter). The ratio of height to diameter H/D of all specimens is two.

Toyoura sand specimens were reconstituted to a void ratio after consolidation e_c ranging from 0.65 to 0.89 (i.e., $D_r = 25$ to 90%). For Quiou sand specimens, the e_c ranged between 0.79 and 1.04 (i.e., $D_r = 55$ to 105%), while for Ticino sand specimens the e_c ranged between 0.58 and 0.88 (i.e., $D_r = 15$ to 100%).

All the relevant information concerning the triaxial tests performed is given in Table 2.

Triaxial Tests

Apparatus

The triaxial testing systems used for the tests, developed at ISME\$ (Istituto Sperimentale Modelli e Strutture, Italy) and the Technical University of Turin, are computer-controlled triaxial cells with internal tie rods. A load cell to measure the axial load without any piston friction is located inside the pressure chamber. In the triaxial apparatus developed at the Technical University of Turin, the loading ram is virtually frictionless. The axial strain was measured locally using high resolution submergible LVDTs, and externally. The details of the test apparatuses were described by Fioravante et al. (1994b), Jamiolkowski et al. (1994b), and Lo Presti et al. (1994).

Twenty-six tests on Toyoura sand and eight tests on Quiou sand were performed at the Technical University of Turin, while all the tests on the Ticino sand (184) and other tests on the Quiou sand (36) were performed at ISMES (Table 2). The axial strain was only measured externally for the majority of the Ticino sand tests.

Test Procedures

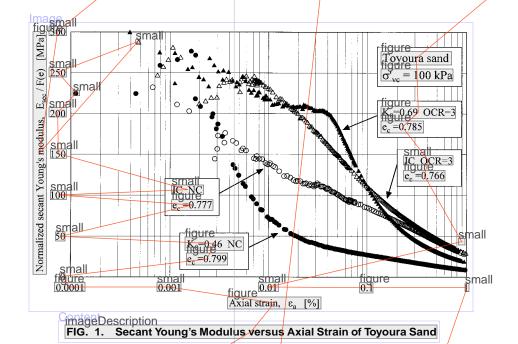
Two sets of drained triaxial compression tests were performed at constant axial strain rate and lateral pressure with confining stress ranging between 50 and 800 kPa. The first set

TABLE 1. Physical Properties of Tested Sands

	figure	Percentage		
figure Sand name		fines		
Sand name	$G_{\rm s}$ figure $G_{\rm s}$ (mm)	<u>S</u> Gna (≤75 μm)	€ i@ure	• figure
(1)	f(2) (3)	(4) (5)	(6)	(7)
figure ' Toyoura sand	2,650	1.3 Flaure	0,985	0.611
Quipe sand	2716e 071	4.5 Small	flo28rb	0.831
Ticino sand	2.690 0.55	1.6	0.934	0.582

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table TABLE 2. List of Test Conditions figure Number 땡 figure OCR figure Consplidation figure Laboratory figure Sand name figure (5) mm)re of tests (4) (1) (3) (7)(8)(Ž) (9) small Isma small 3 0.648-0.886 Zenali 70 50 s 149 II Toyoura sand Isotropic consolidation Mall **Email** 0.766-0.894 140 small 140 all Turin 100 mall K_0 consolidation small 100–180 sma 0.759-0.885 0.776-0.830 78 18 70 ... Turin Turin mal 100 140 mal figure Quiou sand figure Isotropic consolidation Tigure Tigure ISMES 05792=1.024 Shall Shall Shall floure 70 50_{S1}400 \$40all ²dmal \$mat sevall Senall headerOrFooter emal emal **\$**₩all s ma ema Turin, ISMES ISMES .865 <u>1.000</u> 1.001 Mall fig0re \$40 140 Small Smal s mal 0.810 - 0.896ISMES mal sma figure K_0 consolidation 3mall 100₅₁500 Small Zghall Zghall Zghall Zghall mall THAT ISMES Qn7941-1.036 \$49all **S**ma \$500 \$600 1150 3ma 3ma 3 mal 0.932 - 0.979I∰all ISMES Twin ISMES mal 0.839 11003 **\$40**all 140 small 39ma ma figure Isotropic consolidation small 60₅₁701 small 120m140 SMIS Ticino sand Q₀596<u>-0.816</u> 0518001 mall \$000 \$000 1330 re 100 0.600-0.708 30 30hall **figure LSMI**ES **§**ma mal' 0<u>ტ</u>02-0.783 **g**ma **ISMES fig**0re 0.654 -0.714 0.602 -0.758 sinall ISMES ISMES 70 70 gmal sma 150rd,450 05772-0.814 ASMES ASMES ASMES K₀ consolidation mall 4**G**m7911 80ml40 58mal 3hall 3hall 1gure 0615-0.782 small Small Raoma00 \$40all gmal small 100 220 0.608-0.77 140 all small small 100 1500 061rle-0.795 **ISMES Source 1**gure **figura5**0 **figura5**0 **50=200** Sure Small emall Heure 13 ISMES ISMES **figure** 0.60&-0.881 0,595-0.776 0.596-0.785 Smal 10 40 40 ISMES



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was performed on isotropic normally consolidated (NC) and overconsolidated (OC) specimens. The second set was performed on K_0 (the condition of zero radial strain) NC and OC specimens. The K_0 condition was obtained by adjusting the cell pressure as the axial stress increased in order to prevent radial displacement. The radial deformation was measured locally using two proximity transducers placed horizontally on the specimen. The adopted overconsolidation ratio (OCR = $\sigma'_{\text{max}}/\sigma'_{\nu}$) ranged between 1.2 and 8. After the consolidation stage, a rest period of 1 to 2 h was adopted before starting the shearing phase.

The shearing stage of triaxial tests was carried out in drained conditions, under a strain-controlled frame, at a constant rate headerOrFooter

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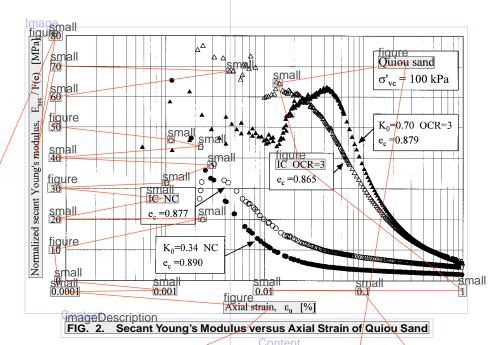
of axial strain (about 0.01%/min). The radial pressure was kept constant.

The consolidation stress ratio, OCR, and effective vertical stress at the end of consolidation are also shown in Table 2.

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Test Results

Typical results of the triaxial compression tests on Toyoura and Quiou sands are shown in Figs. 1 and 2. These figures show the secant Young's modulus $E_{\rm sec}$ versus the axial strain, plotted in logarithmic scale, for four compression loading tests with almost the same void ratio (Toyoura sand: 0.77-0.80; Quiou sand: 0.87-0.89) and the effective vertical consolida-



tion stress (100 kPa) but subject to different consolidation stress ratios ($K_c = 1$ and $K_c = K_0$) and histories ($1 \le OCR \le$ 3). In order to eliminate the effect of the difference of density on test results in these figures, the secant Young's modulus was normalized by dividing it by the following void ratio functions: Toyoura sand $F(e) = (2.17 - e)^2/(1 + e)$ (Iwasaki et al. 1978), while for Quiou sand $F(e) = (3.82 - e)^2/(1 + e)$ (Fioravante et al. 1994a).

Downloaded from the recomposition of the recomposi In spite of a certain scatter observed at very small strain ($\varepsilon_a \le 5 \times 10^{-5}$), it can be seen that the small strain secant Young's modulus E_0 of Toyoura sand is virtually the same for the four tests $[E_0/F(e) \approx 250 \text{ MPa}]$, that is, it does not depend on the K_c , the horizontal stress σ'_h , or the OCR, being only a function of the axial consolidation stress. On the other hand, in the case of Quiou sand, the small strain secant Young's modulus of the OC specimens $[E_0/F(e) \approx 60 \text{ to } 70 \text{ MPa}]$ is higher than that of the NC specimens $[E_0/F(e) \approx 40 \text{ to } 50]$ MPa]. In other words, for a clean sand, such as Toyoura sand, the E_0 value is a function of the effective axial stress and is quite independent of the radial effective stress and the stress history, as already shown by Flora et al. (1994), Kohata et al. (1994), and Lo Presti et al. (1995). In the case of sand containing crushable material, such as Quiou sand, although E_0 does not depend on the K_c or the σ'_h , it instead depends on the stress history (Lo Presti et al. 1995).

On the other hand, at intermediate strain, it can be seen that the reduction of E_{sec} in NC specimens occurs for ε_a larger than 0.001%. It can be also seen that the reduction of E_{sec} in NC Quiou sand is much more pronounced than that observed for NC Toyoura sand; for example, $E_{\rm sec}/E_0$ at $\varepsilon_a = 0.01\%$ is about 0.55 in the NC Toyoura specimen and is about 0.45 in the NC Quiou specimen. In the case of OC specimens, the sudden reduction of $E_{\rm sec}$ occurs for strain levels larger than about 0.05% for both sands. This experimental fact indicates that the amount of plastic deformation decreased for axial strain by as much as 0.05%, as a consequence of the mechanical overconsolidation. It is said that the linear threshold strain increases according to the overconsolidation history, as reported by Jardine et al. (1984) and Tatsuoka and Kohata (1994).

STIFFNESS NONLINEARITY

Empirical Fitting Equation

In order to evaluate the effects of the confining pressure, the stress ratio at consolidation, and the overconsolidation history on the secant Young's modulus E_{sec} under small and intermediate strain levels, an empirical study was performed on a large number of triaxial compression test results on Toyoura, Quiou, and Ticino sands.

It has generally been recognized that the shear modulus of sand can be expressed by means of an empirical equation as a function of the void ratio, the confining pressure, and strain levels (Hardin and Richart 1963; Iwasaki and Tatsuoka 1977; Jamiolkowski et al. 1994a). For example, Iwasaki and Tatsuoka indicated that the shear modulus of clean sands obtained from resonant column and cyclic torsional tests can be expressed by

$$G_{eq} = K(\gamma)F(e)p^{\prime n(\gamma)}$$
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where G_{eq} = equivalent shear modulus; $K(\gamma)$ = material constant that depends on shear strain level; F(e) = void ratio function; p' = mean effective stress; and $n(\gamma) = m$ empirical exponent that depends on shear strain level.

According to Hardin and Blandford (1989), it is also possible to express the dependence of the small strain shear modulus G_0 on the current state of a soil by means of the following relationship:

> $G_0 = S_{ij}F(e)(OCR)^k p_a^{(1-n_i-n_j)} \sigma_i^{\prime n_i} \sigma_j^{\prime n_j}$ (2)

where S_{ii} = nondimensional material constant of given soil that also reflects its fabric; k = empirical exponent that depends onplasticity index (PI) of soil; σ'_i and σ'_j = effective principal τ_{ext} stresses acting on plane in which G_0 is measured; n_i and n_i empirical exponents; and p_a = reference stress.

Moreover, Hardin and Blandford suggested that the Young's modulus for elastic compressive strain increments in a certain direction is a unique function of the normal stress in that direction. Lo Presti et al. (1995) and Hoque and Tatsuoka (1998) reported similar results for triaxial tests performed on clay and sand.

As mentioned before, it was indicated that the secant Young's modulus depends on the stress ratio and the stress history under consolidation. Moreover its effects were different from sand to sand. Thus, to clarify the effects of the confining pressure, the stress ratio at consolidation (i.e., isotropic and K_0 consolidation) and the overconsolidation history on the secant Young's modulus E_{sec} under wide strain levels (0.001) to 1%), an empirical study was performed on triaxial compression test results using the following equations:

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Mattentoside Text $E_{\text{sec(IC)}} = S_{\nu} F(\nu) \sigma_{\nu}^{\prime n} p_a^{(1-n)}$ (isotropic normally consolidated sand) $E_{\text{sec}(K_0)} = aS_v F(e) \sigma_{ve}^{\prime n} p_a^{(1-n)}$ (K_0 normally consolidated sand)

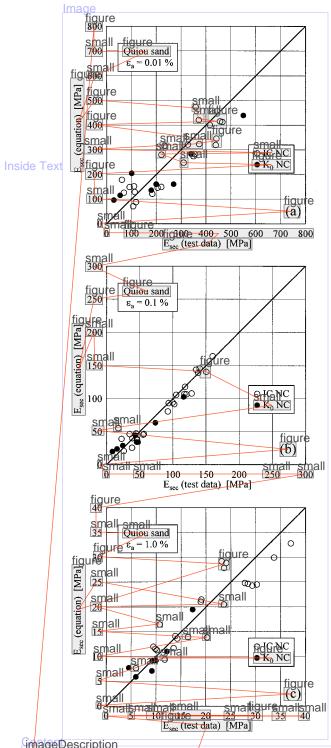
where $S_v =$ nondimensional material constant that depends on axial strain level of isotropic normally consolidated sands; F(e)= void ratio function $[F(e)] = (2.17 + e)^2/(1 + e)$ (Toyoura and Ticino sands) and $F(e) = (3.82 - e)^2/(1 + e)$ (Quiou sand)]; σ'_{vc} = effective axial stress at end of consolidation; n = empirical exponent that depends on axial stress and axial strain level of isotropic normally consolidated sands; $p_a =$ reference stress (98 KPa); and a = empirical constant that

small sma 250 Toyoura sand $\varepsilon_a = 0.01 \%$ figure 200 200 small (equation) mall small OLG NC figure (ă) small smal 50 150 200 E_{sec} (test data) [MPa] figure Toyoura sand $\varepsilon_a = 0.1 \%$ 100 Esec (equation) [MPa] 0 small smal small figure (b) mall small small small small small [100]

E_{sec} (test data) [MPa] Toyoura sand Esec (equation) [MPa]Esec (equation) [MPa]Esec Esec (equation) [MPa]Esec Esec (equation) [MPa]Esec (equation) [MP small 30 Small SMG INC (č) small 10 mall E_{sec} (test data) [MPa]

imageDescription FIG. 3. Comparison of Empirical Fitting Study and Test Data on Toyoura Sand: (a) $\varepsilon_a = 0.01\%$; (b) $\varepsilon_a = 0.1\%$; (c) $\varepsilon_a = 1.0\%$

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FIG. 4. Comparison of Empirical Fitting Study and Test Data on Quiou Sand: (a) $\varepsilon_a = 0.01\%$; (b) $\varepsilon_a = 0.1\%$; (c) $\varepsilon_a = 1.0\%$

depends on axial strain level of K_0 normally consolidated

Figs. 3–5 show the comparison of the secant modulus obtained from the test data and the empirical fitting equation for normally consolidated [isotropic consolidated (IC) and K_0 consolidated (K_0C)] Toyoura, Quiou, and Ticino sands for three kinds of strain levels, respectively. Although a certain scatter is recognized, it can be seen that the empirical fitting equation that uses (3) and (4) above agrees well with the test data at small and intermediate strain levels and stress ratios for normally consolidated sands. Table 3 lists the parameter values of the empirical fitting equation for the three sands.

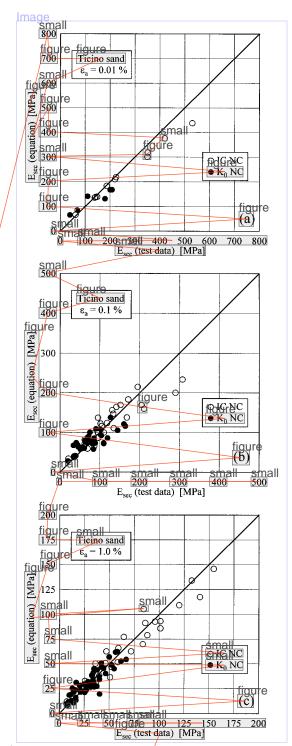


image Description FIG. 5. Comparison of Empirical Fitting Study and Test Data on Ticino Sand: (a) $\varepsilon_a = 0.01\%$; (b) $\varepsilon_a = 0.1\%$; (c) $\varepsilon_a = 1.0\%$

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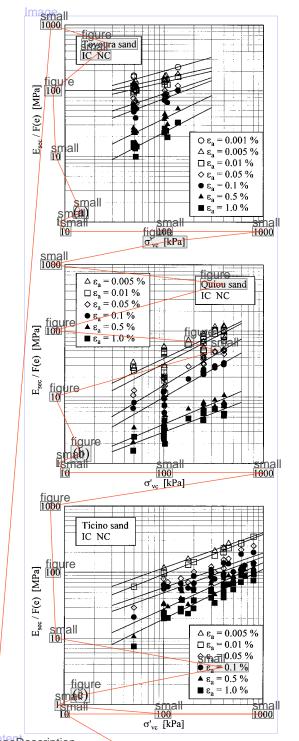
Influence Factors

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Consolidation Stress

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Fig. 6 shows the variations of $E_{\rm sec}/F(e)$ at several strain levels with respect to effective axial stress σ'_{vc} using double logarithmic scales for isotropic NC Toyoura, Quiou, and Ticino sand specimens. From this figure, it has been found that the relationships between $\log(E_{\rm sec}/F(e))$ and $\log(\sigma'_{vc})$ for each strain level and sand can be approximated as a straight line. Accordingly, the secant Young's modulus of isotropic NC sand specimens can be explained by an exponent function of the headerOrFooter



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FIG. 6. Normalized Secant Young's Modulus versus Effective Vertical Stress at Consolidation: (a) Toyoura Sand; (b) Quiou Sand; (c) Ticino Sand

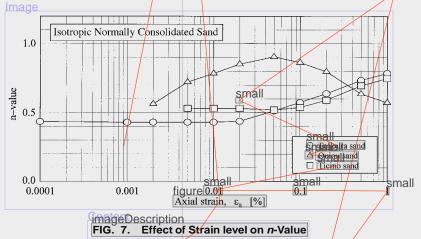
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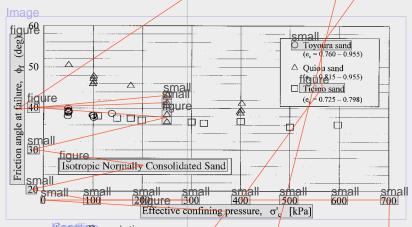
effective vertical stress at any strain level, as in the case of

Fig. 7 shows the relationships of n-value versus $\log(\varepsilon_a)$ for Toyoura, Quiou, and Ticino sand specimens. The strain level dependency of the n-value of Toyoura sand is similar to that of Ticino sand. The n-values at small strain levels of Toyoura and Ticino sands are almost equal to 0.5, and those increase gradually with the increase in the strain levels. On the other hand, in the case of Quiou sand, the n-value increases at lower strain levels than other sands, and for $\varepsilon_a > 0.05\%$ it decreases with an increase in the strain levels. It would seem that this is the effect of the high crushability of Quiou sand. Fig. 8

Image figure TABLE 3. Parameter Val						of Empirical F	itting Equatio	on	<i>(</i> :		
4Em ino	Toyoura Sand				Quiou Sand				Ticing Sand		
foure	small n	fiSrure	a (for <i>K</i> ₀)	n		S_{ν}	a (for <i>K</i> ₀)	figure	Sure	a (for K _e)	
figure	(2)	(3)	(4)	(5)		(6)	(7)	(8)	(9)	(10)	
$0.0001_{10}(E_0)$	0.434	70172	1.04	sma				_			
0.001	Q:430	3,028	1.01			_	_	_	/ —		
0.002	0.430	4766e	1.08	0.562		512	0.83	_	figure	small	
0 <u>3</u> 005	9.430	1,572	0.78	0.722		387	0.66	0.531	figure	small smail	
Q-94	9.430	1,367	0.56	0.785		321	0.76	0.530	l garoali	953	
9.021	9.437	1,122	0.46	0.852		246	0.70	0.530	342a11	9,52	
9,05	9,513	911	0.38	0.905		150	0.58	0.519	595all	9:49	
9 dall	9057241	763	0.35	0.864		99.6	0.50	ର୍ଜ୍ୟୁ ବ୍ୟୁ	497	9,44	
9 _R all	Qr638	599	0.34	0 <mark>.</mark> 799		64.2	0.47	10g59de /	\$13all	037 re	
0.5 mall	9.736	378	0.34	0.636		39.3	0.51	Qr696	282	0 <u>6</u> 2re 0.29	
fictionic	0.786	234	0.35	Ø .573		30.0	0.51	0.749	199	0.29	
Note: $E_{rest}(z) = \frac{8}{5}F(e)\sigma \frac{m}{m}\rho^{(1-n)}$ (isotropic normally consolidated): $E_{rest}(z) = aE_{rest}(z)$ (K_0 normally consolidated): $F(e) = (2\sqrt{1-e})^2/(1+e)$ (Toyour											

and Ticino sands); and $F(e) = (3.82 - e)^2/(1 + e)$ (Quiou sand)





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FIG. 8. Stress Dependency of Friction Angle at Failure

shows the stress dependency of the friction angle at failure for isotropic NC specimens. It has been found that the stress dependency of Quiou sand is larger than that of Toyoura and Ticino sands. In particular, the friction angle of Quiou sand decreases rapidly with an increase in the confining pressure. This is because the crushability of Quiou sand is higher than that of other sands. Therefore, the *n*-value of Quiou sand decreased for $\varepsilon_a > 0.05\%$.

Consolidation Stress Ratio

The secant modulus decrease with an increase in the strain level is more pronounced in K_0 consolidated (K_0 C) specimens than in isotropic consolidated (IC) specimens, as mentioned before.

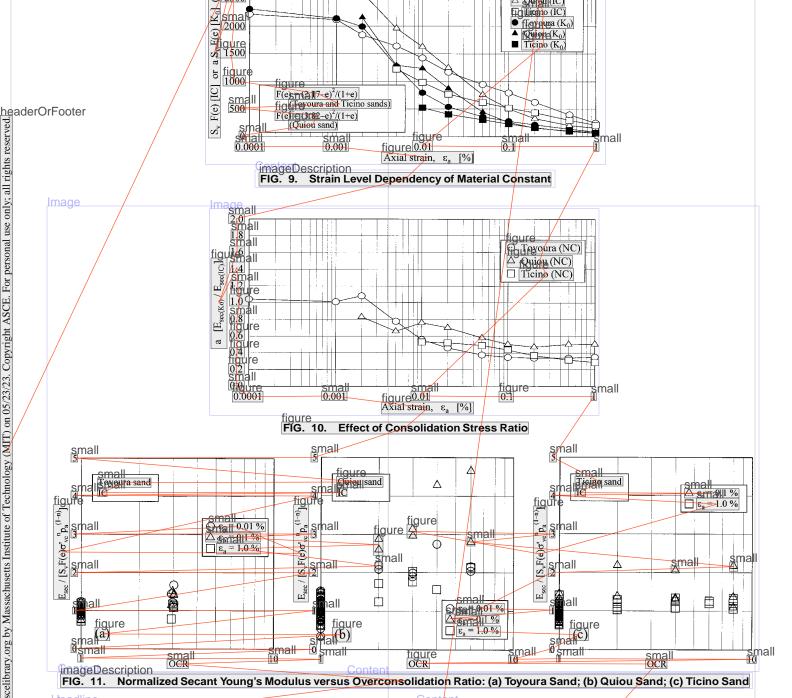
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Fig. 9 shows the relations of the material constant $S_v \times F(e)$ (for IC) or $a \times S_v \times F(e)$ (for K_0 C) versus $\log(\varepsilon_a)$ to better clarify the effect of the strain level on the secant modulus. It can be seen that the reductions of material constants predominantly occur for strain levels that are larger than about 0.001%. The reduction of material constant of IC Quiou sand is larger than those of Toyoura and Ticino sands. In addition, the reduction of the material constants of K_0 C specimens is larger than that of IC specimens.

Fig. 10 shows the relationships between the ratio of the secant Young's modulus $E_{\text{sec}(K_0)}/E_{\text{sec}(IC)}$ (i.e., a-value) and $\log(\varepsilon_{\bar{a}})$ for NC specimens. It has been found that the $E_{\text{sec}(K_0)}/E_{\text{sec}(IC)}$ at small strains are nearly equal to one. It has also been found that the $E_{\text{sec}(K_0)}/E_{\text{sec}(IC)}$ decreases with an in-

crease in the strain level.



small Smalloura (IC) Qvi vi(IC)

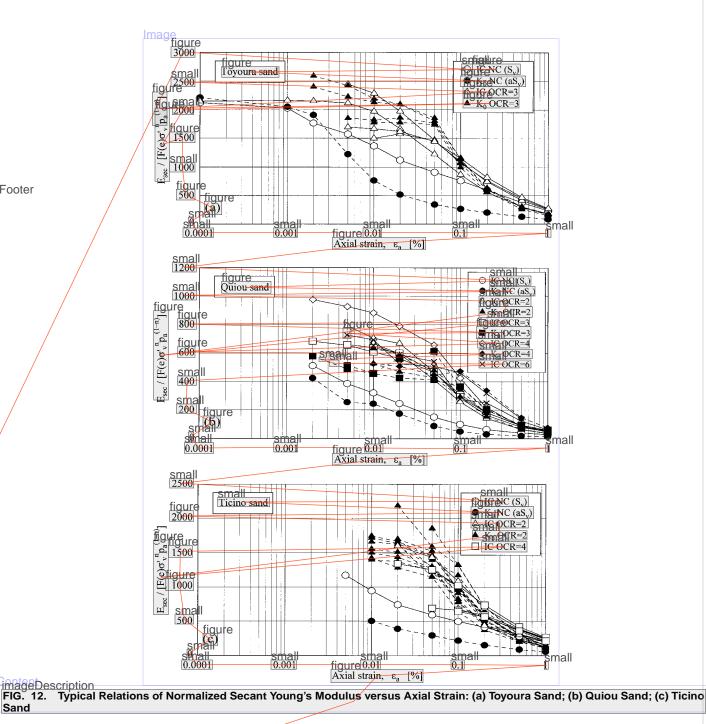
It has been shown that the secant Young's modulus was significantly dependent on overconsolidation history. Fig. 11 shows the variations of normalized secant Young's modulus $E_{\text{sec}}/[S_v F(e) \sigma_{vc}^{\prime n} p_a^{(1-n)}]$, with respect to OCR, as examined using a single logarithmic scale at several strain levels for IC Toyoura, Quiou and Ticino sand specimens. From this figure, it has been found that the effects of overconsolidation history on the secant Young's modulus for Quiou sand are larger than thase for Toyoura and Ticino sands.

Overconsolidation Ratio (OCR)

Figs. 12(a-c) show the typical relations of the secant modulus normalized by void ratio function and confining pressure versus $\log(\varepsilon_a)$ to better clarify the effect of the overconsolidation on the secant modulus for the three IC and K_0 C sand specimens, respectively. In these figures, the normalized secant modulus for isotropic and K_0 normally consolidated specimens were indicated by the S_v -value or $a \times S_v$ -value in (3) and (4), respectively. Fig. 13 shows the variation of the K_0 -value after consolidation, due to the difference in the overconsolidation ratio.

It can be seen that the strain level at which the reduction of $E_{\rm sec}$ in OC specimens occurs is larger than that in NC specimens. It can be also seen that the sudden reduction of $E_{\rm sec}$ in Φ C specimens that occurs for ε_a is larger than about 0.05% for all sands. In addition, it is found that the reduction tendency of E_{sec} is relatively similar for isotropic and K_0 OC specimens for the same OCR. This is because (1) the yield locus (the linear threshold strain) expanded because of the overconsolidation history; and (2) the K_0 -value of the OC specimen increases with an increase in the overconsolidation ratio, as shown in Fig. 13.

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Chargeura sand
A Agricu sand Ó Ticino sand small small small small 4 small small l small fig**u**re Overconsolidation ratio, figure FIG. 13. Effect of Overconsolidation History on Ko-Value 936 / JOURNAL OF GEOTECHNICAL AND GEOEN TRONMENTAL ENGINEERING / OCTOBER 2000

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figure

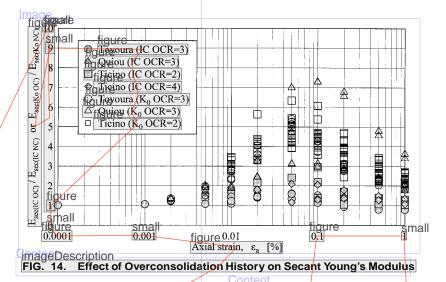


Fig. 14 shows the relationships of the secant modulus ratios $E_{\text{sec(OC)}}/E_{\text{sec(NC)}}$ versus log (ε_a) for isotropic and K_0 consolidated Toyoura (OCR = 3), Quiou (OCR = 3), and Ticino (OCR = 2, 4) sand specimens. It has been found that the effects of the overconsolidation history for Toyoura sand are negligibly small at small strain levels. The effects of the OC history on the secant modulus are greatest at ε_a , around 0.05 to 0.1%. The effects of the OC history are similar on Toyoura and Ticino sands. On the other hand, the effects of OC history on Quiou sand are much larger than for other sands. This can be seen because the soil particle crush of Quiou sand had significantly progressed because of the OC history and shearing.

It has also been found that the effects of OC history on K_0 C specimens are larger than those on IC specimens. This is because (1) the secant Young's modulus of K_0 specimens is smaller than that of the IC specimen, except that at small strain levels under the same vertical consolidation stress, as shown in Fig. 12, and (2) the K_0 -value increases with an increase in OCR, as shown in Fig. 13. Consequently, the effects of OC history on the secant Young's modulus of the K₀C specimen were larger than those of the IC specimens.

CONCLUSIONS

This paper presents the analysis of a large number of drained triaxial compression tests, many of which were carried out with local strain measurement. The tests were performed on both isotropically and anisotropically consolidated specimens of three sands prepared by pluvial deposition in air and allow the following conclusions, all of which refer to the value of sand moduli at $\sigma'_{vc} = 100 \text{ kPa}$:

- 1. For all three sands, the secant Young's modulus normalized with respect to the consolidation void ratio exhibits very pronounced degradation with increasing strain.
- 2. Nonlinearity starts to show when the axial strain exceeds $\approx 1 \times 10^{-3}$ and 5×10^{-2} % for NC and OC with OCR = 3 specimens, respectively.
- 3. Below such a strain level, which corresponds to the linear threshold strain, the secant Young's modulus coincides with the initial tangent stiffness (E_0) , which depends only on the magnitude of σ'_{ν} being independent of σ'_h .
- 4. For silica Ticino and Toyoura sands, the E_0 results were found to be independent of OCR, while in carbonatic Quiou sands it moderately influences the magnitude of the initial stiffness.
- 5. Beyond the linear threshold strain, the reduction of E_{sec} for normally consolidated specimens can be matched by the empirical fitting formulae.

- 6. For isotropically consolidated specimens, the stress exponent n of σ'_{w} increases gradually from a minimum value (0.43 to 0.56) at very small ε_a with the increase in the strain levels. In this respect, the irregular trend of n versus ε_a , observed for Quiou sand, cannot be explained. However, it could be due to the pronounced grains' crushability.
- 7. The effect of overconsolidation on the secant modulus was found to be highly axial strain level dependent. As has been shown by many researchers, it is insignificant for silica sands at very small strain ($\varepsilon_a = 1 \times 10^{-3}$ %), increasing thereafter with an increase of the strain and reaching the maximum values at ε_a around 0.05 to 0.1%. The influence of OCR on the $E_{\rm sec}$ results are more pronounced for the anisotropically K_0 -consolidated specimens than for those subjected to isotropical consolidation.

Overall, the phenomenological examination of the drained triaxial compression tests results gathered for three sands has shown that, in the strain range of 0.01 to 0.1%, the soil stiffness under axisymmetric loading conditions exhibits a highly pronounced nonlinearity and is strongly influenced by the test conditions, in particular, the consolidation stress ratio and **OCR**

The data presented here provide evidence of the inadequacy of some existing quasilinear fitting equations (e.g., conventional hyperbola) to reproduce the variation of E_{sec} in the strain range of practical interest. Moreover, data presented in this paper can guide practitioners in selecting the equivalent stiffness that can be used for simple calculations using the formula of the theory of elasticity.

appendix

APPENDIX. REFERENCES

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