Observational constraints on Hubble constant and deceleration parameter in power-law cosmology

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Note: This version of the paper matches the version published in Monthly Notices of the Royal Astronomical Society. The definitive version is available at www.blackwell-synergy.com.

ABSTRACT

In this paper, we show that the expansion history of the Universe in power-law cosmology essentially depends on two crucial parameters, namely the Hubble constant H_0 and deceleration parameter q. We find the constraints on these parameters from the latest H(z) and SNe Ia data. At 1σ level the constraints from H(z) data are obtained as $q=-0.18^{+0.12}_{-0.12}$ and $H_0=68.43^{+2.84}_{-2.80}$ km s⁻¹ Mpc⁻¹ while the constraints from the SNe Ia data read as $q=-0.38^{+0.53}_{-0.05}$ and $H_0=69.18^{+0.55}_{-0.54}$ km s⁻¹ Mpc⁻¹. We also perform the joint test using H(z) and SNe Ia data, which yields the constraints $q=-0.34^{+0.05}_{-0.05}$ and $H_0=68.93^{+0.53}_{-0.52}$ km s⁻¹ Mpc⁻¹. The estimates of H_0 are found to be in close agreement with some recent probes carried out in the literature. The analysis reveals that the observational data successfully describe the cosmic acceleration within the framework of power-law cosmology. We find that the power-law cosmology accommodates well the H(z) and SNe Ia data. We also test the power-law cosmology using the primordial nucleosynthesis, which yields the constraints $q\gtrsim 0.72$ and $H_0\lesssim 41.49$ km s⁻¹ Mpc⁻¹. These constraints are found to be inconsistent with the ones derived from the H(z) and SNe Ia data. We carry out the statefinder analysis, and find that the power-law cosmological models approach the standard Λ CDM model as $q\to -1$. Finally, we conclude that despite having several good features power-law cosmology is not a complete package for the cosmological purposes.

Key words: cosmological parameters - cosmology: observations - primordial nucleosynthesis.

1 INTRODUCTION

Power-law cosmology finds a reasonable place in the literature to address some common problems (e.g., age problem, flatness problem, horizon problem etc.) associated with the Standard Cold Dark Matter (SCDM) model based on Big Bang theory. In such a cosmology, the cosmological evolution is described by the scale factor $a(t) \propto t^{\alpha}$, where α is a constant. The viability of the model with $\alpha \geqslant 1$ has been explored in a series of articles in different contexts (Lohiya & Sethi 1999; Batra et al. 1999, 2000; Gehlaut et al. 2002, 2003; Dev et al. 2002, 2008; Sethi et al. 2005a, 2005b; Zhu et al. 2008). Observational constraints on phantom powerlaw cosmology are discussed by Kaeonikhom, Gumjudpai & Saridakis (2011). The motivation for such an endeavor is followed by a number of considerations. For instance, powerlaw cosmological models with $\alpha \geqslant 1$ do not encounter the horizon problem at all (Sethi, Dev & Jain 2005). These mod-

els do not witness the flatness problem since the matter density is not constrained by the scale factor. In these models, age of the Universe turns out at least fifty percent greater than the age predicted by the SCDM model. This bridges the gap between the age of the Universe and the age estimates of globular clusters and high-z redshift galaxies, and thus the age problem is alleviated. Sethi, Dev & Jain (2005) showed that an open linear coasting cosmological model constrained with type Ia supernovae (SNe Ia) gold sample and ages of old quasars accommodates a very old high-redshift quasar, which the SCDM model fails to do. The linear coasting cosmology is found to be consistent with the gravitational lensing statistics (Dev et al. 2002) and the primordial nucleosynthesis (Batra et al. 1999, 2000). Kaplinghat et al. (1999) found that the power-law cosmological models which succeed in primordial nucleosythesis are in conflict with the constraints from Hubble expansion rates and SNe Ia magnitude redshift relations.

In any cosmological model, the Hubble constant H_0 and deceleration parameter q play an important role is describ-

ing the nature of evolution of the Universe. The former one tells us the expansion rate of the Universe today while the latter one characterizes the accelerating (q < 0) or decelerating (q > 0) nature of the Universe. In the recent past, there have been numerous attempts to estimate the value of H_0 . Freedman et al. (2001) used the Hubble Space Telescope (HST) observations of Cepheid variable to estimate a value of $H_0 = 72 \pm 8 \text{ km s}^{-1} \text{ Mpc}^{-1}$. An observational determination of the Hubble constant obtained by Suyu et al. (2010) based upon measurements of gravitational lensing by using the HST yielded a value of $H_0 = 69.7^{+4.9}_{-5.0}$ km s⁻¹ Mpc⁻¹. WMAP seven-year results gave an estimate of $H_0 = 71.0 \pm 2.5 \text{ km s}^{-1} \text{ Mpc}^{-1}$ based on WMAP data alone, and an estimate of $H_0 = 70.4^{+1.3}_{-1.4} \text{ km s}^{-1} \text{ Mpc}^{-1}$ based on WMAP data with Gaussian priors corresponding to earlier estimates from other studies (Jarosik et al. 2011). A recent estimate of the Hubble constant, which used a new infrared camera on the HST to measure the distance and redshift for a collection of astronomical objects, gives a value of $H_0 = 73.8 \pm 2.4 \text{ km s}^{-1} \text{ Mpc}^{-1}$ (Riess et al. 2011). An alternative probe using data from galactic clusters gave a value of $H_0=67.0\pm3.2~{\rm km~s^{-1}~Mpc^{-1}}$ (Beutler et al. 2011).

In this paper, we show that the power-law cosmology essentially depends on the parameters q and H_0 . We intend to find the observational constraints on the power-law cosmology parameters using the recent observational data from H(z) and supernova observations. We also intend to test the power-law cosmology with primordial nucleosynthesis. The paper is organized as follows: The basic equations of powerlaw cosmology are introduced in Section 2. Section 3 deals with the constraints on the parameters q and H_0 from the latest H(z) data while Section 4 is devoted to find the constraints using Union2 compilation of 557 SNe Ia data points. In Section 5, we perform the joint test using H(z) and SNe Ia data. Section 6 deals with the constraints on power-law cosmology from primordial nucleosynthesis while Section 7 is devoted to study the statefinders in power-law cosmology. In the last Section, we summarize the main results of the paper.

BASIC EQUATIONS IN POWER-LAW COSMOLOGY

We study a general class of power-law cosmology described by the dimensionless scale factor

$$a(t) = a_0 \left(\frac{t}{t_0}\right)^{\alpha},\tag{1}$$

where t_0 is present age of the universe, a_0 is the value of a today and α is a dimensionless positive parameter. Hereafter, the subscript 0 denotes the present-day value of the parameter under consideration.

The deceleration parameter q, which characterizes accelerating (q < 0) or decelerating (q > 0) nature of the Universe, reads as

$$q = -\frac{a\ddot{a}}{\dot{a}^2} = \frac{1}{\alpha} - 1,\tag{2}$$

where an over dot denotes derivative with respect to cosmic time t. The positivity of α leads to q > -1.

The cosmic scale factor in terms of the deceleration parameter may be written as

$$a(t) = a_0 \left(\frac{t}{t_0}\right)^{1/(1+q)}. (3)$$

We observe that q > -1 is the condition for expanding Universe in the power-law cosmological model.

The expansion history of the Universe is described by the Hubble parameter,

$$H(t) = \frac{\dot{a}}{a} = \left(\frac{1}{1+q}\right)\frac{1}{t},\tag{4}$$

while the present expansion rate of the Universe is given by

 $H_0=\frac{1}{(1+q)t_0}.$ The scale factor a and the redshift z are connected through the relation $a = a_0(1+z)^{-1}$. Therefore, the Hubble parameter in terms of the redshift may be expressed as

$$H(z) = H_0(1+z)^{1+q}. (5)$$

This shows that the expansion history of the Universe in power-law cosmology depends on the parameters H_0 and

It may be noted that the above model is well motivated in the literature as mentioned in the previous section. However the focus has been on one parameter namely α (or q). But here we find the observational constraints on both parameters H_0 and q by subjecting the power-law cosmological model to the latest data from H(z) and SNe Ia observations. We also constrain H_0 and q using primordial nucleosynthesis scenario.

CONSTRAINTS FROM OBSERVATIONAL H(Z) **DATA**

Simon, Verde & Jimenez (2005) determined nine H(z) data points in the range $0 \le z \le 1.8$ by using the differential ages of passively evolving galaxies determined from the Gemini Deep Deep Survey and archival data. Recently, H(z) data at 11 different redshifts based on the differential ages of redenvelope galaxies were reported by Stern et al. (2010) while 3 more H(z) data points were obtained by Gaztanaga, Cabre & Hui (2009). The newly H(z) data points have been used to constrain parameters of various cosmological models (Yang & Zhang 2010; Cao, Zhu & Liang 2011; Chen & Ratra 2011; Paul, Thakur & Ghose 2010, 2011). Here, we use 13 observational H(z) data points given in Table 1 of the paper by Chen & Ratra (2011) and the one at z = 0 estimated in the work by Riess et al. (2011). For this sake, we define the χ^2

$$\chi_H^2(q, H_0) = \sum_{i=1}^{14} \left[\frac{H(z_i, q, H_0) - H_{obs}(z_i)}{\sigma_i} \right]^2.$$
 (6)

The model has two free parameters namely q and H_0 . We perform a grid search in the entire parametric space $(q > -1 \text{ and } H_0 \geqslant 0)$ to find the best fit model. We find that the best fit values of the parameters are q=-0.18 and $H_0=68.43$ together with $\chi^2_{\nu}=1.49$, where $\chi^2_{\nu}=$ $\chi^2_{min}/(\text{degree of freedom})$. Here and in what follows H_0 is in the units of km s⁻¹ Mpc⁻¹. The negative value of qsuggests that the power-law cosmological model fitted with the newly obtained H(z) data confirms the accelerating nature of the present-day Universe. The likelihood contours at 68.3% (inner contour), 95.4% (middle contour) and 99.73%

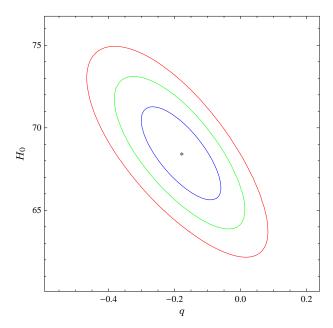


Figure 1. The likelihood contours at 68.3% (inner contour), 95.4% (middle contour) and 99.73% (outer contour) confidence levels around the best fit values point (-0.18, 68.43) (shown by star symbol) in the $q-H_0$ plane obtained by fitting power-law cosmological model with H(z) data.

(outer contour) confidence levels around the best fit values point (-0.18, 68.43) (represented by star symbol) in the $q-H_0$ plane are shown in Fig.1. The errors at 1σ level are obtained as $q=-0.18^{+0.12}_{-0.12}$ and $H_0=68.43^{+2.84}_{-2.80}$.

4 CONSTRAINTS FROM OBSERVATIONAL SNE IA DATA

The observations directly measure the apparent magnitude m of a supernova and its redshift z. The apparent magnitude m of the supernova is related to the luminosity distance d_L of the supernova through

$$m = M + 5\log_{10}\left(\frac{d_L}{1\ Mpc}\right) + 25,$$
 (7)

where M is the absolute magnitude, which is believed to be constant for all SNe Ia.

It is convenient to work with Hubble free luminosity distance given by

$$D_L(z) = \frac{H_0}{c} d_L(z). \tag{8}$$

Now, Eq.(7) can be written as

$$m = M + 5\log_{10} D_L(z) - 5\log_{10} H_0 + 52.38 . (9)$$

The distance modulus $\mu(z)$ is given by

$$\mu(z) = m - M = 5 \log_{10} D_L(z) - 5 \log_{10} H_0 + 52.38$$
 (10)

The Hubble free luminosity distance D_L , in the present case, for a geometrically flat Universe reads as

$$D_L(z) = (1+z) \int_0^z \frac{H_0}{H(z')} dz' = \frac{1}{q} [(1+z) - (1+z)^{1-q}].(11)$$

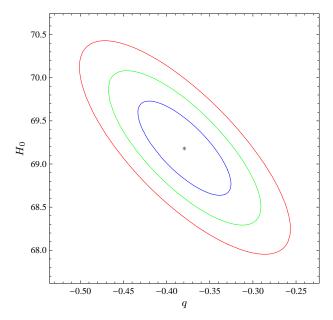


Figure 2. The likelihood contours at 68.3% (inner contour), 95.4% (middle contour) and 99.73% (outer contour) confidence levels around the best fit values point (-0.38, 69.18) (indicated by star symbol) in the $q-H_0$ plane obtained by fitting power-law cosmological model with SNe Ia data.

SNe Ia are always used as standard candles, and are believed to provide strongest constraints on the cosmological parameters. In the present analysis, we use recently released Union2 set of 557 SNe Ia from Supernova Cosmology Project (Amanullah et al. (2010). In this case, we define the χ^2 as

$$\chi_{SN}^2(q, H_0) = \sum_{i=1}^{557} \left[\frac{\mu(z_i, q, H_0) - \mu_{obs}(z_i)}{\sigma_i} \right]^2.$$
 (12)

After performing a grid search in the entire parametric space (q>-1) and $H_0\geqslant 0$, we find that the best fit values of the parameters are q=-0.38 and $H_0=69.18$ together with $\chi^2_{\nu}=0.99$. Again, the power-law cosmological model fitted with the 557 SNe Ia data confirms the cosmic acceleration with q=-0.38. The likelihood contours at 68.3% (inner contour), 95.4% (middle contour) and 99.73% (outer contour) confidence levels around the best fit values point (-0.38,69.18) (indicated by star symbol) in the $q-H_0$ plane are shown in Fig.2. The errors at 1σ level are derived as $q=-0.38^{+0.05}_{-0.05}$ and $H_0=69.18^{+0.55}_{-0.54}$.

5 BEST-FITTING MODEL FROM THE JOINT TEST: H(Z)+SNE IA DATA

In order to obtain tighter constraints on the model parameters and to avoid degeneracy in the observational data, we combine H(z) and SNe Ia data. Since H(z) and SNe Ia data are obtained from independent cosmological probes, the total likelihood is considered to be the product of separate likelihoods of the two probes. Therefore, we define

$$\chi_{total}^2 = \chi_H^2 + \chi_{SN}^2. \tag{13}$$

In the joint analysis, we find that the best fit values of the parameters are q=-0.34 and $H_0=68.93$ together with

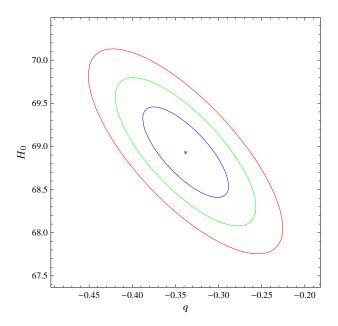


Figure 3. The likelihood contours at 68.3% (inner contour), 95.4% (middle contour) and 99.73% (outer contour) confidence levels around the best fit values point (-0.34, 68.93) (shown by star symbol) in the $q-H_0$ plane obtained by fitting power-law cosmological model with $H(z)+{\rm SNe}$ Ia data.

 $\chi^2_{\nu}=1.01$. The joint test also confirms the cosmic acceleration with q=-0.34. The likelihood contours at 68.3% (inner contour) and 95.4% (outer contour) confidence levels around the best fit values point (-0.34,68.93) (indicated by star symbol) in the $q-H_0$ plane are shown in Fig.3. The errors at 1σ level read as $q=-0.34^{+0.05}_{-0.05}$ and $H_0=68.93^{+0.53}_{-0.52}$.

Fig.4 demonstrates the comparison of the best fit cosmological model obtained from the joint test with the observational H(z) data in the 1σ region $68.41 \leqslant H_0 \leqslant 69.46, -0.39 \leqslant q \leqslant -0.29$. We observe that the model fits well to the observational 15 H(z) points shown with error bars, especially at redshifts z < 1.

In Fig.5, the comparison of the derived best fit model based on $H(z)+{\rm SNe}$ Ia with the observational 557 SNe Ia data points (shown with error bars) of Union2 compilation in the 1σ region $68.41 \leqslant H_0 \leqslant 69.46, -0.39 \leqslant q \leqslant -0.29$ is illustrated. We see that the model is in excellent agreement with the observational SNe Ia data.

6 CONSTRAINTS FROM PRIMORDIAL NUCLEOSYNTHESIS

Before we find constraints on power-law cosmology parameters from primordial big bang nucleosynthesis (BBN), it is helpful to reproduce the brief review of the BBN in standard model given by Kaplinghat et al. (1999). The neutron-proton ratio $n/p = \exp(-Q/T)$, where Q = 1.29 MeV is the neutron-proton mass difference, at high temperatures $T \gtrsim 1$ MeV is maintained by charged-current weak interactions among neutrons, protons, electrons, positrons and neutrinos. When the Universe is of order 1 s old, $T \lesssim 1$ MeV, the n/p ratio "freezes out" due to the inequilibrium of weak interactions and free neutron decay with a lifetime of 887 s. At this stage the deuterium (D) produced due to

collision of neutrons and protons is rapidly photodissociated by the cosmic background photons. This causes very low abundance of D and thus heavier nuclei are not formed at this epoch. Thus nucleosynthesis is delayed by this "photodissociation bottleneck". However, when the universe is \sim 3 minutes old, the temperature falls below \sim 80 keV, the deuterium bottleneck is broken. At this stage the nuclear reactions quickly burn out the remaining free neutrons into $^4{\rm He}$ and leave trace amounts of D, $^3{\rm He}$ and $^7{\rm Li}$ (Walker et al. 1991). A viable cosmological model must mimic the above scenario for proper synthesis of the light elements in the early Universe. In the following, we test the power-law cosmological model for primordial nucleosynthesis.

In power-law cosmology the scale factor a(t) and the cosmic microwave background temperature T(t) are related through the relation:

$$\frac{a}{a_0} = \frac{T_0}{\beta T} = \left(\frac{t}{t_0}\right)^{\frac{1}{1+q}},\tag{14}$$

where β stands for any non-adiabatic expansion due to entropy production. In standard cosmology, the instantaneous e^{\pm} annihilation is assumed at $T = m_e$. The heating due to this annihilation is accounted by β where $\beta = 1$ for $T < m_e$ while $\beta = (11/4)^{1/3}$ for $T > m_e$.

In order to find constraints from primordial nucleosythesis on power-law cosmology parameters, we utilize $t_0 \approx 13.7$ Gyr (age of the Universe) estimated by Komatsu et al. (2011) on the basis of 7 year data from WMAP and astrophysical data from other sources. Further, the model is assumed to have current temperature $T_0 = 2.728$ K. The primordial nucleosynthesis requires that $t \lesssim 887$ s when $T \approx 80$ keV. This puts the following constraints on q and H_0 :

We observe that primordial nucleosynthesis requires decelerating expansion (q > 0) of the Universe within the framework of power-law cosmology. This is contrary to outcome of accelerated expansion (q < 0) of the Universe obtained in earlier sections by using latest data sets of H(z)and SNe Ia observations. Also the primordial nucleosynthesis forces the Hubble constant $H_0 \lesssim 41.49$, which is much smaller than its values estimated in earlier sections by using the updated data sets of H(z) and SNe Ia observations. This shows that the power-law cosmological models which succeed in mimicking the nucleosynthesis scenario are in conflict with the constraints obtained on power-law cosmology parameters by using the latest observational data from H(z)and SNe Ia. A similar conclusion on power-law cosmologies was drawn by Kaplinghat et al. (1999). However, in the case at hand, it has been done with updated observational data sets and the constraints have been obtained on both the parameters q and H_0 .

7 CONSTRAINTS ON STATEFINDERS IN POWER-LAW COSMOLOGY

The Hubble parameter $H=\dot{a}/a$ and deceleration parameter $q=-\ddot{a}/aH^2$ are useful geometric parameters in cosmology, which describe the expansion history of the Universe. For instance, H>0 ($\dot{a}>0$) indicates an expanding Universe while q<0 ($\ddot{a}>0$) characterizes an accelerated expansion of the Universe. In order to explain accelerated expansion

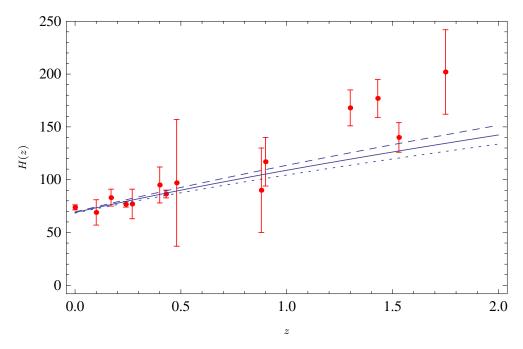


Figure 4. The observational 15 H(z) data points are shown with error bars (red color online). Variation of best fit model H(z) curve (solid) based on H(z)+SNe Ia data is shown vs z. The dashed curve corresponds to the maximum values of H(z) in the 1σ region $68.41 \le H_0 \le 69.46, -0.39 \le q \le -0.29$ while the dotted curve corresponds to the minimum values of H(z) in the same region. We observe that the best fit model fits well to the observational data points of H(z) especially at redshits z < 1.

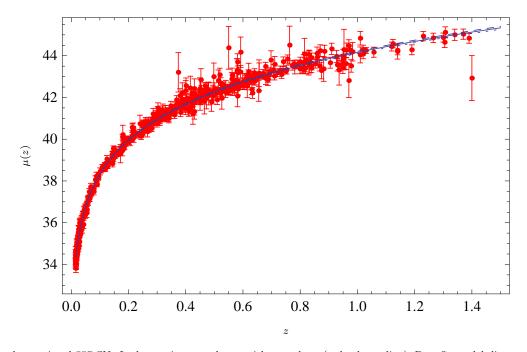
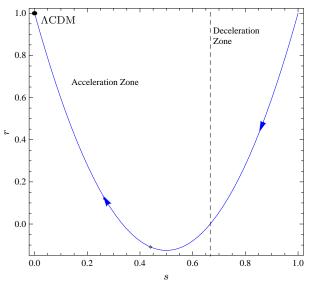


Figure 5. The observational 557 SNe Ia data points are shown with error bars (red color online). Best fit model distance modulus $\mu(z)$ curve (solid) based on H(z)+SNe Ia data is shown vs z. The dashed curve and the dotted curve respectively correspond to the maximum and minimum values of $\mu(z)$ in the 1σ region $68.41 \le H_0 \le 69.46$, $-0.39 \le q \le -0.29$. We observe that the best fit model is in excellent agreement with the observational data points of SNe Ia at all redshifts.

of the Universe, various dark energy models have been proposed in the literature. However, these models encounter degeneracy on the geometric parameters H (involving first time derivative of scale factor) and q (involving second time derivative of scale factor) at the present epoch (Malekjani &

Khadom-Mohamaddi 2012). Thus the geometric parameters H and q are not capable of discriminating between different dark energy models and a viable diagnostic tool is required for this purpose. Sahni et al. (2003) proposed a pair of parameters $\{r,s\}$ called statefinders as a means of distinguish-



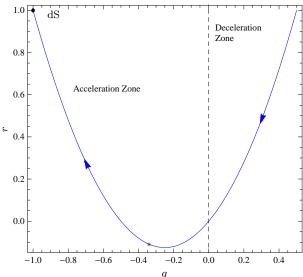


Figure 6. (a) Variation of r versus s. The black dot represents the statefinder pair (s,r)=(0,1) or equivalently location of flat Λ CDM model in the s-r plane, and star symbol on the s-r curve shows the position of statefinder parameters in the best fit model based on H(z)+SNe Ia data. (b) Variation of r versus q. The black dot represents the location of de Sitter (dS) point (q,r)=(-1,1) in the q-r plane, and star symbol on the q-r curve shows the position of q and r in the best fit model obtained from H(z)+SNe Ia data. In both panels, the vertical dashed line separates the acceleration and deceleration zones. The arrows show the direction of the evolution of trajectories as q varies from 0.5 to -1. We observe that Λ CDM point (0,1) or equivalently the dS point (-1,1) is an attractor in power-law cosmology.

ing between different dark energy models. The statefinders involve derivatives of scale factor upto third order and are defined as

$$r = \frac{\dot{a}}{aH^3}$$
 and $s = \frac{r-1}{3(q-1/2)}$.

The remarkable feature of statefinders is that these parameters depend on scale factor and its time derivatives, and hence are geometric in nature (Sahni 2002). Further, different dark energy models exhibit different evolutionary trajectories in the s-r plane. Moreover, the well known flat Λ CDM model corresponds to the point s=0 and r=1 in the s-r plane (Alam et al. 2003). These features of statefinders provide an opportunity to distinguish between different dark energy models. The statefinder diagnostic tool has been extensively used in the literature as a means to distinguish between different dark energy models (see Alam et al. 2003; Ali et al. 2010; Malekjani & Khadom-Mohamaddi 2012 and references therein). In what follows, we test the power-law cosmology by statefinder diagnostic tool.

In power-law cosmology, the statefinders read as

$$r = 2q^2 + q$$
 and $s = \frac{2}{3}(q+1)$, where $q \neq \frac{1}{2}$.

We immediately notice that r=1 and s=0 at q=-1. Thus the the power-law cosmology mimics the $\Lambda {\rm CDM}$ model at q=-1. We obtain the evolutionary s-r and q-r trajectories for the power-law cosmology as shown in Fig. 6 for the values of q in the range $-1 \leqslant q < 0.5$. The black dot in the left panel (a) at (s,r)=(0,1) represents the location of flat $\Lambda {\rm CDM}$ model while the the black dot in the right panel (b) shows the location of the de Sitter (dS) point (q,r)=(-1,1). The star symbol in both panels corresponds to the best fit model based on $H(z)+{\rm SNe}$ Ia. It is interesting to note that the $\Lambda {\rm CDM}$ statefinder pair (0,1) or equivalently the dS point (-1,1) is an attractor in power-law cosmology.

Now we find the constraints on the statefinders of power-law cosmology from H(z), SNe Ia and BBN observations. The H(z) data constrain the statefinders as $r=-0.09^{+0.04}_{-0.03}$ and $s=0.58^{+0.04}_{-0.12}$ while the SNe Ia data constraints on statefinders are $r=-0.09^{+0.03}_{-0.02}$ and $s=0.41^{+0.03}_{-0.03}$. The joint test of H(z) and SNe Ia data puts the following constraints on statefinders: $r=-0.11^{+0.02}_{-0.01}$ and $s=0.44^{+0.03}_{-0.03}$. The errors in the above values are at 1σ level. The primordial nucleosynthesis restricts $r\gtrsim 1.76$ and $s\gtrsim 1.15$. We observe that the best fit values of statefinders r and s predicted by observational H(z) and SNe Ia data are in conflict with the ones estimated by BBN, as expected.

8 SUMMARY

In this paper, we have found the bounds on the parameters H_0 and q of the power-law cosmology. The numerical results are summarized in Table 1.

Some key observations are as follows:

- (i) The constraints on the deceleration parameter q clearly indicate that the astronomical observations of H(z) and SNe Ia predict the cosmic acceleration within the framework of power-law cosmology. Thus, power-law cosmological models are viable for describing the observed accelerating nature of Universe.
- (ii) We see that the estimates of Hubble constant in power-law cosmology are in close agreement with independent investigations of H_0 carried out in literature (Freedman et al. 2001; Suyu et al. 2010; Jarosik et al. 2010; Riess et al. 2011; Beutler et al. 2011) as discussed in Section 1.
- (iii) The derived best-fitting model fits well to the observational data points from H(z) and SNe Ia observations (see Figs 4 and 5).

Data/Source	q	H_0	$\chi^2_{ u}$	r	s
H(z)	$-0.18^{+0.12}_{-0.12}$	$68.43^{+2.84}_{-2.80}$	1.49	$-0.09^{+0.04}_{-0.03}$	$0.58^{+0.04}_{-0.12}$
SNe Ia	$-0.38^{+0.05}_{-0.05}$	$69.18^{+0.55}_{-0.54}$	0.99	$-0.09^{+0.03}_{-0.02}$	$0.41^{+0.03}_{-0.03}$
H(z)+SNe Ia	$-0.34^{+0.05}_{-0.05}$	$68.93^{+0.53}_{-0.52}$	1.01	$-0.11^{+0.02}_{-0.01}$	$0.44^{+0.03}_{-0.03}$
BBN	$\gtrsim 0.72$	$\lesssim 41.49$		$\gtrsim 1.76$	$\gtrsim 1.15$

Table 1. Summary of the numerical results

- (iv) The primordial nucleosynthesis demands a decelerating expansion of the Universe with smaller values of Hubble constant.
- (v) The statefinder analysis shows that power-law cosmological models approach the standard Λ CDM model in future (see Fig. 6) with varying values of q.

We see that the power-law cosmology turns out viable in the description of the acceleration of present-day Universe when subjected to recent observations of H(z) and SNe Ia. Also the Hubble constant within the framework of power-law cosmology falls in the range of observations. However, the power-law cosmology fails to produce primordial nucleosytheis with the values of q and H_0 estimated from observational data of H(z) and SNe Ia as discussed in Section 6. Moreover, because of the constant value of deceleration parameter q in power-law cosmology, it fails to provide time or redshift based transition of the Universe from deceleration to acceleration. Thus, one has to use different values of q for the description of Universe at different epochs. Finally, despite having several useful features, the power-law cosmology is not a complete package for cosmological purposes.

ACKNOWLEDGEMENTS

The author is thankful to M. Sami, Deepak Jain and Sanjay Jhingan for fruitful discussions. Thanks are also due to Bharat Ratra and Özgür Akarsu for useful comments on the initial draft of the manuscript. The author would like to put forward his sincere thanks to the referee whose valuable comments have helped in improving the quality of this manuscript.

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