

PURE MATHS OBJECTIVES

#LEARN WITH WROK

ANSWERS: INTEGRATION MCQS

1. (D)
2. (A)
3. (C)
4. (B)
5. (D)

$$\begin{aligned} 1. \int \left(x^2 + \frac{2}{x^3} - 7 \right) dx &= \int (x^2 + 2x^{-3} - 7) dx \\ &= \frac{x^3}{3} + \frac{2x^{-2}}{-2} - 7x + c \\ &= \frac{x^3}{3} - \frac{1}{x^2} - 7x + c \end{aligned}$$

$$\begin{aligned} 2. \int \left(\sqrt{x} - \frac{1}{\sqrt{x}} + \sqrt[3]{x} \right) dx &= \int (x^{1/2} - x^{-1/2} + x^{1/3}) dx \\ &= \frac{x^{3/2}}{3/2} - \frac{x^{1/2}}{1/2} + \frac{x^{4/3}}{4/3} + c \\ &= \frac{2}{3}x^{3/2} - 2x^{1/2} + \frac{3}{4}x^{4/3} + c \end{aligned}$$

$$\begin{aligned} 3. \int \sec^2 5x dx &= \frac{\tan 5x}{5} + c & \because \int \sec^2 x = \tan x + c \\ & & \because \frac{d}{dx} 5x = 5 \end{aligned}$$

$$4. \int \cos \sqrt{x} dx = \frac{\sin \sqrt{x}}{\frac{1}{2\sqrt{x}}} \quad \because \int \cos x = \sin x + c$$

$$= 2\sqrt{x} \sin \sqrt{x} \quad \because \frac{d}{dx} \sqrt{x} = \frac{1}{2\sqrt{x}}$$

$$5. \int \sin^2 x \cos x dx$$

$$\text{Let } u = \sin x$$

$$\frac{du}{dx} = \cos x \quad \Rightarrow \quad du = \cos x dx$$

By Replacing $\sin x = u$ and $\cos x = du$, we have

$$\begin{aligned} \int \sin^2 x \cos x dx &= \int u^2 du \\ &= \frac{u^3}{3} + c \\ &= \frac{1}{3} \sin^3 x + c \end{aligned}$$