

When used with the 'thin' option, `bwmorph` uses the following algorithm (References [3]):

1. Divide the image into two distinct subfields in a checkerboard pattern.
2. In the first subiteration, delete pixel  $p$  from the first subfield if and only if the conditions  $G_1$ ,  $G_2$ , and  $G_3$  are all satisfied.
3. In the second subiteration, delete pixel  $p$  from the second subfield if and only if the conditions  $G_1$ ,  $G_2$ , and  $G_3'$  are all satisfied.

### Condition G1:

$$X_H(p) = 1$$

where

$$X_H(p) = \sum_{i=1}^4 b_i$$

$$b_i = \begin{cases} 1, & \text{if } x_{2i-1} = 0 \text{ and } (x_{2i} = 1 \text{ or } x_{2i+1} = 1) \\ 0, & \text{otherwise} \end{cases}$$

$x_1, x_2, \dots, x_8$  are the values of the eight neighbors of  $p$ , starting with the east neighbor and numbered in counter-clockwise order.

### Condition G2:

$$2 \leq \min\{n_1(p), n_2(p)\} \leq 3$$

where

$$n_1(p) = \sum_{k=1}^4 x_{2k-1} \vee x_{2k}$$

$$n_2(p) = \sum_{k=1}^4 x_{2k} \vee x_{2k+1}$$

### Condition G3:

$$(x_2 \vee x_3 \vee \bar{x}_8) \wedge x_1 = 0$$

### Condition G3':

$$(x_6 \vee x_7 \vee \bar{x}_4) \wedge x_5 = 0$$

The two subiterations together make up one iteration of the thinning algorithm. When the user specifies an infinite number of iterations ( $n=\text{Inf}$ ), the iterations are repeated until the image stops changing. The conditions are all tested using `applylut` with precomputed lookup tables.