

Appendix.R

kschy

2021-03-24

```
#Question 5
```

```
#Part A
```

```
#Setting Data Point
```

```
y <- matrix(c(27.3, 42.4 ,38.7, 4.5, 23, 166.3, 109.7, 80.1, 150.7, 20.3, 189.7,  
              131.3, 404.2, 149),14,1,byrow = TRUE)
```

```
y
```

```
##      [,1]  
## [1,] 27.3  
## [2,] 42.4  
## [3,] 38.7  
## [4,]  4.5  
## [5,] 23.0  
## [6,] 166.3  
## [7,] 109.7  
## [8,]  80.1  
## [9,] 150.7  
## [10,]  20.3  
## [11,] 189.7  
## [12,] 131.3  
## [13,] 404.2  
## [14,] 149.0
```

```
x <- matrix(c(rep(1,14),13.1, 15.3, 25.8, 1.8, 4.9, 55.4,  
              39.3, 26.7, 47.5, 6.6, 94.7, 61.1, 135.6, 47.6), 14, 2)
```

```
x
```

```
##      [,1] [,2]  
## [1,]    1 13.1  
## [2,]    1 15.3  
## [3,]    1 25.8  
## [4,]    1  1.8  
## [5,]    1  4.9  
## [6,]    1 55.4  
## [7,]    1 39.3  
## [8,]    1 26.7  
## [9,]    1 47.5  
## [10,]   1  6.6  
## [11,]   1 94.7  
## [12,]   1 61.1  
## [13,]   1 135.6  
## [14,]   1  47.6
```

```

#Part B
#Finding Least Square Estimator
b <- solve(t(x)%*%x,t(x)%*%y)
b

##           [,1]
## [1,] -1.233836
## [2,]  2.701553

#Inverse of diagonal  $X^T X$ 
xtx.inverse <- solve(t(x)%*%x)
xtx.inverse

##           [,1]           [,2]
## [1,]  0.163081936 -2.230009e-03
## [2,] -0.002230009  5.425812e-05

```

```

#Part C
#Calculating Sample Variance
e <- y-x%*%b
e

##           [,1]
## [1,] -6.8565106
## [2,]  2.3000724
## [3,] -29.7662361
## [4,]  0.8710405
## [5,] 10.9962256
## [6,] 17.8677893
## [7,]  4.7627957
## [8,]  9.2023660
## [9,] 23.6100596
## [10,]  3.7035852
## [11,] -64.9032511
## [12,] -32.5310639
## [13,] 39.1032233
## [14,] 21.6399042

```

```

#Calculating Sum-squared
SSRes <- sum(e^2)
SSRes

```

```
## [1] 9325.833
```

```

#Calculating sample variance
s2 <- SSRes/(14-2)
s2

```

```
## [1] 777.1528
```

```

#Calculating the variance of the least square estimator
b.var <- solve(t(x)%*%x)*s2
diag.b.var <- diag(solve(t(x)%*%x))*s2
diag.b.var

```

```
## [1] 126.73957949  0.04216685
```

```

#Part D
#Calculating ocean trout expected price in 1980

```

```
t <- matrix(c(1,28),2,1)
t
```

```
##      [,1]
## [1,]    1
## [2,]   28
```

```
y.bar <- t(t)%*%b
y.bar
```

```
##      [,1]
## [1,] 74.40965
```

#Part E

#Calculating the H(hat) matrix

```
hat <- x%*%solve(t(x)%*%x)%*%t(x)
hat
```

```
##      [,1]      [,2]      [,3]      [,4]      [,5]      [,6]
## [1,] 0.11396694 0.11062464 0.09467275 0.13113421 0.12642461 0.04970362
## [2,] 0.11062464 0.10754494 0.09284642 0.12644305 0.12210349 0.05141058
## [3,] 0.09467275 0.09284642 0.08412985 0.10405344 0.10147998 0.05955744
## [4,] 0.13113421 0.12644305 0.10405343 0.15522970 0.14861943 0.04093605
## [5,] 0.12642461 0.12210348 0.10147997 0.14861943 0.14253059 0.04334131
## [6,] 0.04970362 0.05141057 0.05955743 0.04093605 0.04334131 0.08252382
## [7,] 0.07416318 0.07394831 0.07292284 0.07526679 0.07496403 0.07003197
## [8,] 0.09330545 0.09158654 0.08338272 0.10213433 0.09971225 0.06025574
## [9,] 0.06170552 0.06246947 0.06611561 0.05778157 0.05885805 0.07639427
## [10,] 0.12384192 0.11972372 0.10006872 0.14499445 0.13919154 0.04466033
## [11,] -0.01000202 -0.00360390 0.02693257 -0.04286508 -0.03384955 0.11301634
## [12,] 0.04104402 0.04343138 0.05482558 0.02878169 0.03214569 0.08694639
## [13,] -0.07213842 -0.06085815 -0.00702053 -0.13007796 -0.11418304 0.14475029
## [14,] 0.06155359 0.06232948 0.06603260 0.05756833 0.05866164 0.07647186
##      [,7]      [,8]      [,9]      [,10]      [,11]      [,12]
## [1,] 0.07416318 0.09330544 0.06170552 0.12384192 -0.01000202 0.04104402
## [2,] 0.07394832 0.09158654 0.06246947 0.11972373 -0.00360390 0.04343138
## [3,] 0.07292284 0.08338272 0.06611562 0.10006872 0.02693257 0.05482559
## [4,] 0.07526679 0.10213432 0.05778157 0.14499445 -0.04286508 0.02878169
## [5,] 0.07496403 0.09971224 0.05885805 0.13919154 -0.03384955 0.03214569
## [6,] 0.07003197 0.06025573 0.07639427 0.04466033 0.11301633 0.08694639
## [7,] 0.07160437 0.07283494 0.07080352 0.07479800 0.06619374 0.06947528
## [8,] 0.07283494 0.08267953 0.06642814 0.09838401 0.02954998 0.05580223
## [9,] 0.07080352 0.06642814 0.07365098 0.05944838 0.09004127 0.07837361
## [10,] 0.07479800 0.09838400 0.05944838 0.13600930 -0.02890555 0.03399047
## [11,] 0.06619375 0.02954998 0.09004128 -0.02890555 0.22730998 0.12959328
## [12,] 0.06947528 0.05580223 0.07837361 0.03399047 0.12959328 0.09313182
## [13,] 0.06219926 -0.00240588 0.10424388 -0.10546647 0.34625681 0.17397642
## [14,] 0.07079375 0.06635001 0.07368571 0.05926119 0.09033210 0.07848213
##      [,13]      [,14]
## [1,] -0.07213842 0.06155359
## [2,] -0.06085815 0.06232948
## [3,] -0.00702053 0.06603260
## [4,] -0.13007796 0.05756833
## [5,] -0.11418304 0.05866164
## [6,] 0.14475028 0.07647186
## [7,] 0.06219926 0.07079375
```

```
## [8,] -0.002405883 0.06635001
## [9,] 0.104243884 0.07368571
## [10,] -0.105466475 0.05926119
## [11,] 0.346256817 0.09033210
## [12,] 0.173976424 0.07848213
## [13,] 0.555967177 0.10475662
## [14,] 0.104756624 0.07372098
```

```
#Sea scallops leverage
```

```
hat[13,13]
```

```
## [1] 0.5559672
```

```
#Calculating Residual variance
```

```
e.var <- s2*(diag(14)-hat)
```

```
e.var
```

```
##           [,1]      [,2]      [,3]      [,4]      [,5]      [,6]
## [1,] 688.583054 -85.972246 -73.575192 -101.91132 -98.25123 -38.62731
## [2,] -85.972246 693.573923 -72.155856 -98.26557 -94.89307 -39.95387
## [3,] -73.575192 -72.155856 711.771027 -80.86542 -78.86544 -46.28523
## [4,] -101.911316 -98.265570 -80.865419 656.51559 -115.50001 -31.81356
## [5,] -98.251233 -94.893065 -78.865445 -115.50001 666.38474 -33.68282
## [6,] -38.627305 -39.953875 -46.285227 -31.81356 -33.68282 713.01917
## [7,] -57.636122 -57.469141 -56.672188 -58.49380 -58.25850 -54.42554
## [8,] -72.512587 -71.176741 -64.801113 -79.37398 -77.49165 -46.82791
## [9,] -47.954613 -48.548322 -51.381935 -44.90511 -45.74170 -59.37002
## [10,] -96.244091 -93.043627 -77.768685 -112.68284 -108.17309 -34.70790
## [11,] 7.773098 2.800782 -20.930721 33.31272 26.30627 -87.83096
## [12,] -31.897476 -33.752817 -42.607856 -22.36777 -24.98211 -67.57063
## [13,] 56.062576 47.296087 5.456029 101.09045 88.73767 -112.49309
## [14,] -47.836546 -48.439532 -51.317419 -44.73939 -45.58905 -59.43032
##           [,7]      [,8]      [,9]      [,10]      [,11]      [,12]
## [1,] -57.63612 -72.512587 -47.95461 -96.24409 7.773098 -31.89748
## [2,] -57.46914 -71.176741 -48.54832 -93.04363 2.800782 -33.75282
## [3,] -56.67219 -64.801113 -51.38193 -77.76869 -20.930721 -42.60786
## [4,] -58.49380 -79.373977 -44.90511 -112.68284 33.312716 -22.36777
## [5,] -58.25850 -77.491649 -45.74170 -108.17309 26.306272 -24.98211
## [6,] -54.42554 -46.827915 -59.37002 -34.70790 -87.830961 -67.57063
## [7,] 721.50524 -56.603878 -55.02515 -58.12947 -51.442655 -53.99291
## [8,] -56.60388 712.898147 -51.62482 -76.45940 -22.964850 -43.36686
## [9,] -55.02515 -51.624816 719.91471 -46.20047 -69.975829 -60.90827
## [10,] -58.12947 -76.459404 -46.20047 671.45277 22.464029 -26.41579
## [11,] -51.44265 -22.964850 -69.97583 22.46403 600.498189 -100.71378
## [12,] -53.99291 -43.366860 -60.90827 -26.41579 -100.713777 704.77512
## [13,] -48.33833 1.869738 -81.01342 81.96356 -269.094448 -135.20626
## [14,] -55.01756 -51.564095 -57.26505 -46.05500 -70.201844 -60.99260
##           [,13]      [,14]
## [1,] 56.062576 -47.83655
## [2,] 47.296087 -48.43953
## [3,] 5.456029 -51.31742
## [4,] 101.090448 -44.73939
## [5,] 88.737669 -45.58905
## [6,] -112.493087 -59.43032
## [7,] -48.338331 -55.01756
## [8,] 1.869738 -51.56410
```

```
## [9,] -81.013424 -57.26505
## [10,] 81.963564 -46.05500
## [11,] -269.094448 -70.20184
## [12,] -135.206262 -60.99260
## [13,] 345.081342 -81.41190
## [14,] -81.411901 719.86032

#Standardised Residual calculation function
z <- function(i){
  e[i,1]/sqrt(s2*(1-hat[i,i]))
}

#Calculating Standardised Residual for sea scallops
z(13)
```

```
## [1] 2.104999
```

```
#Part F
#Cook's distance function
d <-function(i){
  (((z(i))^2)/2)*((hat[i,i])/(1-hat[i,i]))
}

#Cook's distance for sea scallops
d(13)
```

```
## [1] 2.774008
```

```
#Part G
#Cook's Distance matrix for all observation
cook.d <- matrix(c(0,14), 14, 1)
i <- 0
while (i < 15) {
  cook.d[i,1]=d(i)
  i = i+1
}
cook.d
```

```
##           [,1]
## [1,] 0.0043908534
## [2,] 0.0004595830
## [3,] 0.0571733691
## [4,] 0.0001061788
## [5,] 0.0150807062
## [6,] 0.0201370081
## [7,] 0.0012124417
## [8,] 0.0053532616
## [9,] 0.0307813052
## [10,] 0.0016078990
## [11,] 1.0318211614
## [12,] 0.0771027556
## [13,] 2.7740080577
## [14,] 0.0258869983
```

```
#Omitting Sea Scallop observation fitting
x.omit <- x[-13,]
x.omit
```

```
##      [,1] [,2]
## [1,]    1 13.1
## [2,]    1 15.3
## [3,]    1 25.8
## [4,]    1  1.8
## [5,]    1  4.9
## [6,]    1 55.4
## [7,]    1 39.3
## [8,]    1 26.7
## [9,]    1 47.5
## [10,]   1  6.6
## [11,]   1 94.7
## [12,]   1 61.1
## [13,]   1 47.6

y.omit <- y[-13,1]
y.omit

## [1] 27.3 42.4 38.7  4.5 23.0 166.3 109.7  80.1 150.7  20.3 189.7 131.3
## [13] 149.0

b.omit <- solve(t(x.omit)%*%x.omit,t(x.omit)%*%y.omit)
b.omit

##      [,1]
## [1,] 11.034093
## [2,]  2.250015

#Plotting Regression Graph with and without sea scallop
plot(x[,2],y)
abline(b[1,1],b[2,1], col = "blue")
abline(b.omit[1,1],b.omit[2,1], col = "red")
legend("topleft",
      c("With Sea Scallops","Without Sea Scallop"),
      fill=c("blue","red"))
```

