# **Kurt Gödel**

**Kurt Friedrich Gödel** (/ˈgɜːrdəl/;<sup>[2]</sup> German: [ˈkʊɐ̯t ˈgøɪdl] ( listen); April 28, 1906 – January 14, 1978) was an Austro-Hungarian-born Austrian logician, mathematician, and analytic philosopher. Considered along with Aristotle and Gottlob Frege to be one of the most significant logicians in history, Gödel had an immense effect upon scientific and philosophical thinking in the 20th century, a time when others such as Bertrand Russell, Alfred North Whitehead, and David Hilbert were analyzing the use of logic and set theory to understand the foundations of mathematics pioneered by Georg Cantor.

Gödel published his two <u>incompleteness theorems</u> in 1931 when he was 25 years old, one year after finishing his doctorate at the <u>University of Vienna</u>. The first incompleteness theorem states that for any self-consistent <u>recursive axiomatic system powerful</u> enough to describe the arithmetic of the <u>natural numbers</u> (for example <u>Peano arithmetic</u>), there are true propositions about the naturals that cannot be proved from the <u>axioms</u>. To prove this theorem, Gödel developed a technique now known as <u>Gödel numbering</u>, which codes formal expressions as natural numbers.

He also showed that neither the <u>axiom of choice</u> nor the <u>continuum hypothesis</u> can be disproved from the accepted <u>axioms of set theory</u>, assuming these axioms are <u>consistent</u>. The former result opened the door for mathematicians to assume the axiom of choice in their proofs. He also made important contributions to proof theory by clarifying the connections between classical logic, intuitionistic logic, and modal logic.

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# **Kurt Gödel Born** Kurt Friedrich Gödel April 28, 1906 Brünn, Austria-Hungary (now Brno, Czech Republic) January 14, 1978 Died (aged 71)

Princeton, New

Austrian, American

Jersey, U.S.

Citizenship Czechoslovak,

Mid-1930s: further work and U.S. visits Princeton, Einstein, U.S. citizenship

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# Early life and education

#### Childhood

Gödel was born April 28, 1906, in Brünn, <u>Austria-Hungary</u> (now <u>Brno</u>, <u>Czech Republic</u>) into the German family of Rudolf Gödel (1874–1929), the manager of a textile factory, and Marianne Gödel (<u>née</u> Handschuh, 1879–1966).<sup>[4]</sup> Throughout his life, Gödel would remain close to his mother; their correspondence was frequent and wide-ranging.<sup>[5]</sup> At the time of his birth the city had a <u>German-speaking</u> majority which included his parents.<sup>[6]</sup> His father was Catholic and his mother was Protestant and the children were raised Protestant. The ancestors of Kurt Gödel were often active in Brünn's cultural life. For example, his grandfather Joseph Gödel was a famous singer of that time and for some years a member of the *Brünner Männergesangverein* (Men's Choral Union of Brünn).<sup>[7]</sup>

### Alma mater University of Vienna Known for Gödel's incompleteness theorems Gödel's completeness theorem Gödel's constructible universe Gödel metric Gödel logic Gödel-Dummett logic Gödel's ß function Gödel numbering Gödel operation Gödel's speed-up theorem Gödel's ontological proof Gödel-Gentzen translation Von Neumann-Bernays-Gödel set theory ω-consistent theory the consistency of the continuum hypothesis with ZFC Axiom of constructibility Condensation lemma Dialectica

interpretation

Gödel automatically became a <u>Czechoslovak</u> citizen at age 12 when the Austro-Hungarian Empire collapsed, following its defeat in the <u>World War I</u>. (According to his classmate Klepetař, like many residents of the predominantly German <u>Sudetenländer</u>, "Gödel considered himself always Austrian and an exile in Czechoslovakia".)<sup>[8]</sup> In February 1929 he was granted release from his Czechoslovakian citizenship and then, in April, granted Austrian citizenship.<sup>[9]</sup> When <u>Germany annexed Austria</u> in 1938, Gödel automatically became a German citizen at age 32. After <u>World War II</u> (1948), at the age of 42, he became an American citizen.<sup>[10]</sup>

In his family, young Kurt was known as *Herr Warum* ("Mr. Why") because of his insatiable curiosity. According to his brother Rudolf, at the age of six or seven Kurt suffered from <u>rheumatic fever</u>; he completely recovered, but for the rest of his life he remained convinced that his heart had suffered permanent damage. Beginning at age four, Gödel suffered from "frequent episodes of poor health", which would continue for his entire life.<sup>[11]</sup>

Gödel attended the *Evangelische Volksschule*, a Lutheran school in Brünn from 1912 to 1916, and was enrolled in the *Deutsches Staats-Realgymnasium* from 1916 to 1924, excelling with honors in all his subjects, particularly in mathematics, languages and religion. Although Kurt had first excelled in languages, he later became more interested in history and mathematics. His interest in mathematics increased when in 1920 his older brother Rudolf (born 1902) left for <u>Vienna</u> to go to medical school at the <u>University of Vienna</u>. During his teens, Kurt studied <u>Gabelsberger shorthand</u>, <u>Goethe's *Theory of Colours* and criticisms of Isaac Newton, and the writings of Immanuel Kant.</u>

### Studying in Vienna

At the age of 18, Gödel joined his brother in Vienna and entered the University of Vienna. By that time, he had already mastered university-level mathematics. [12] Although initially intending to study theoretical physics, he also attended courses on mathematics and philosophy. During this time, he adopted ideas of mathematical realism. He read Kant's *Metaphysische Anfangsgründe der Naturwissenschaft*, and participated in the Vienna Circle with Moritz Schlick, Hans Hahn, and Rudolf Carnap. Gödel then studied number theory, but when he took part in a seminar run by Moritz Schlick which studied Bertrand Russell's

	Slingshot argument
Spouse(s)	Adele Nimbursky (married 1938)
Awards	Albert Einstein Award (1951)
	National Medal of Science (1974)
	ForMemRS (1968) <sup>[1]</sup>
Sci	entific career
Fields	Mathematics, mathematical logic, analytic philosophy, physics
Institutions	Institute for Advanced Study
Thesis	Über die Vollständigkeit des Logikkalküls (On the Completeness of the Calculus of Logic) (htt p://journals.cambridge. org/action/displayAbstr act?fromPage=online &aid=9079526&fileId= S0022481200026633)
Doctoral advisor	Hans Hahn
	Signature

book *Introduction to Mathematical Philosophy*, he became interested in <u>mathematical logic</u>. According to Gödel, mathematical logic was "a science prior to all others, which contains the ideas and principles underlying all sciences."<sup>[13]</sup>

Kuntgodel

Attending a lecture by <u>David Hilbert</u> in <u>Bologna</u> on completeness and consistency of mathematical systems may have set Gödel's life course. In 1928, Hilbert and <u>Wilhelm Ackermann</u> published *Grundzüge der theoretischen Logik* (<u>Principles of Mathematical Logic</u>), an introduction to <u>first-order logic</u> in which the problem of completeness was posed: *Are the axioms of a formal system sufficient to derive every statement that is true in all models of the system?* 

This problem became the topic that Gödel chose for his doctoral work. In 1929, at the age of 23, he completed his doctoral <u>dissertation</u> under Hans Hahn's supervision. In it, he established his eponymous <u>completeness theorem</u> regarding the <u>first-order predicate calculus</u>. He was awarded his doctorate in 1930, and his thesis (accompanied by some additional work) was published by the Vienna Academy of Science.

#### Career

### Incompleteness theorem

Kurt Gödel's achievement in modern logic is singular and monumental—indeed it is more than a monument, it is a landmark which will remain visible far in space and time. ... The subject of logic has certainly completely changed its nature and possibilities with Gödel's achievement.

- John von Neumann<sup>[14]</sup>

In 1930 Gödel attended the Second Conference on the Epistemology of the Exact Sciences, held in Königsberg, 5–7 September. Here he delivered his incompleteness theorems.<sup>[15]</sup>

Gödel published his incompleteness theorems in *Über formal unentscheidbare Sätze der Principia Mathematica und verwandter Systeme* (called in English "On Formally Undecidable Propositions of *Principia Mathematica* and Related Systems"). In that article, he proved for any computable axiomatic system that is powerful enough to describe the arithmetic of the <u>natural numbers</u> (e.g., the <u>Peano axioms</u> or <u>Zermelo-Fraenkel set theory with the axiom of choice</u>), that:

1. If a (logical or axiomatic formal) system is consistent, it cannot be complete.

2. The consistency of axioms cannot be proved within their own system.

These theorems ended a half-century of attempts, beginning with the work of <u>Frege</u> and culminating in <u>Principia Mathematica</u> and <u>Hilbert's</u> formalism, to find a set of axioms sufficient for all mathematics.

In hindsight, the basic idea at the heart of the incompleteness theorem is rather simple. Gödel essentially constructed a formula that claims that it is unprovable in a given formal system. If it were provable, it would be false. Thus there will always be at least one true but unprovable statement. That is, for any <u>computably enumerable</u> set of axioms for arithmetic (that is, a set that can in principle be printed out by an idealized computer with unlimited resources), there is a formula that is true of arithmetic, but which is not provable in that system. To make this precise, however, Gödel needed to produce a method to encode (as natural numbers) statements, proofs, and the concept of provability; he did this using a process known as Gödel numbering.

In his two-page paper *Zum intuitionistischen Aussagenkalkül* (1932) Gödel refuted the finite-valuedness of <u>intuitionistic logic</u>. In the proof, he implicitly used what has later become known as <u>Gödel-Dummett intermediate logic</u> (or <u>Gödel fuzzy logic</u>).

#### Mid-1930s: further work and U.S. visits

Gödel earned his <u>habilitation</u> at Vienna in 1932, and in 1933 he became a <u>Privatdozent</u> (unpaid lecturer) there. In 1933 <u>Adolf Hitler</u> came to power in Germany, and over the following years the Nazis rose in influence in Austria, and among Vienna's mathematicians. In June 1936, <u>Moritz Schlick</u>, whose seminar had aroused Gödel's interest in logic, was assassinated by one of his former students, <u>Johann Nelböck</u>. This triggered "a severe nervous crisis" in Gödel. He developed paranoid symptoms, including a fear of being poisoned, and spent several months in a sanitarium for nervous diseases. [17]

In 1933, Gödel first traveled to the U.S., where he met <u>Albert Einstein</u>, who became a good friend.<sup>[18]</sup> He delivered an address to the annual meeting of the <u>American Mathematical Society</u>. During this year, Gödel also developed the ideas of computability and <u>recursive functions</u> to the point where he was able to present a lecture on general recursive functions and the concept of truth. This work was developed in number theory, using Gödel numbering.

In 1934, Gödel gave a series of lectures at the <u>Institute for Advanced Study</u> (IAS) in <u>Princeton</u>, New Jersey, entitled *On undecidable propositions of formal mathematical systems*. <u>Stephen Kleene</u>, who had just completed his PhD at Princeton, took notes of these lectures that have been subsequently published.

Gödel visited the IAS again in the autumn of 1935. The travelling and the hard work had exhausted him and the next year he took a break to recover from a depressive episode. He returned to teaching in 1937. During this time, he worked on the proof of consistency of the <u>axiom of choice</u> and of the <u>continuum hypothesis</u>; he went on to show that these hypotheses cannot be disproved from the common system of axioms of set theory.

He married Adele Nimbursky (née Porkert, 1899–1981), whom he had known for over 10 years, on September 20, 1938. Their relationship had been opposed by his parents on the grounds that she was a divorced dancer, six years older than he was.

Subsequently, he left for another visit to the United States, spending the autumn of 1938 at the IAS and publishing Consistency of the axiom of choice and of the generalized continuum-hypothesis with the axioms of set theory, [19] a classic of modern mathematics. In that work he introduced the constructible universe, a model of set theory in which the only sets that exist are those that can be constructed from simpler sets. Gödel showed that both the axiom of choice (AC) and the generalized continuum hypothesis (GCH) are true in the constructible universe, and therefore must be consistent with the Zermelo-Fraenkel axioms for set theory (ZF). This result has had considerable consequences for working mathematicians, as it means they can assume the axiom of choice when proving the Hahn-Banach theorem. Paul Cohen later constructed a model of ZF in which AC and GCH are false; together these proofs mean that AC and GCH are independent of the ZF axioms for set theory.

Godel spent the spring of 1939 at the University of Notre Dame. [20]

### Princeton, Einstein, U.S. citizenship

After the <u>Anschluss</u> on 12 March 1938, Austria had become a part of <u>Nazi Germany</u>. Germany abolished the title <u>Privatdozent</u>, so Gödel had to apply for a different position under the new order. His former association with Jewish members of the Vienna Circle, especially with Hahn, weighed against him. The University of Vienna turned his application down.

His predicament intensified when the German army found him fit for conscription. World War II started in September 1939. Before the year was up, Gödel and his wife left Vienna for <u>Princeton</u>. To avoid the difficulty of an Atlantic crossing, the Gödels took the <u>Trans-Siberian Railway</u> to the Pacific, sailed from Japan to San Francisco (which they reached on March 4, 1940), then crossed the US by train to Princeton. There Gödel accepted a position at the <u>Institute for Advanced Study</u> (IAS), which he had previously visited during 1933–34. [21]

<u>Albert Einstein</u> was also living at Princeton during this time. Gödel and Einstein developed a strong friendship, and were known to take long walks together to and from the Institute for Advanced Study. The nature of their conversations was a mystery to the other Institute members. Economist <u>Oskar Morgenstern</u> recounts that toward the end of his life Einstein confided that his "own work no longer meant much, that he

came to the Institute merely ... to have the privilege of walking home with Gödel".[22]

Gödel and his wife, Adele, spent the summer of 1942 in <u>Blue Hill, Maine</u>, at the Blue Hill Inn at the top of the bay. Gödel was not merely vacationing but had a very productive summer of work. Using *Heft 15* [volume 15] of Gödel's still-unpublished *Arbeitshefte* [working notebooks], <u>John W. Dawson Jr.</u> conjectures that Gödel discovered a proof for the independence of the axiom of choice from finite type theory, a weakened form of set theory, while in Blue Hill in 1942. Gödel's close friend <u>Hao Wang</u> supports this conjecture, noting that Gödel's Blue Hill notebooks contain his most extensive treatment of the problem.

On December 5, 1947, Einstein and Morgenstern accompanied Gödel to his <u>U.S. citizenship</u> exam, where they acted as witnesses. Gödel had confided in them that he had discovered an inconsistency in the <u>U.S. Constitution</u> that could allow the U.S. to become a dictatorship. Einstein and Morgenstern were concerned that their friend's unpredictable behavior might jeopardize his application. The judge turned out to be <u>Phillip Forman</u>, who knew Einstein and had administered the oath at Einstein's own citizenship hearing. Everything went smoothly until Forman happened to ask Gödel if he thought a dictatorship like the <u>Nazi regime</u> could happen in the U.S. Gödel then started to explain his discovery to Forman. Forman understood what was going on, cut Gödel off, and moved the hearing on to other questions and a routine conclusion. [23][24]

Gödel became a permanent member of the Institute for Advanced Study at Princeton in 1946. Around this time he stopped publishing, though he continued to work. He became a full professor at the Institute in 1953 and an emeritus professor in 1976. [25]

During his many years at the Institute, Gödel's interests turned to philosophy and physics. In 1949, he demonstrated the existence of solutions involving closed timelike curves, to <u>Einstein's field equations</u> in general relativity. [26] He is said to have given this elaboration to Einstein as a present for his 70th birthday. [27] His "rotating universes" would allow <u>time travel</u> to the past and caused Einstein to have doubts about his own theory. His solutions are known as the <u>Gödel metric</u> (an exact solution of the <u>Einstein field equation</u>).

He studied and admired the works of <u>Gottfried Leibniz</u>, but came to believe that a hostile conspiracy had caused some of Leibniz's works to be suppressed. To a lesser extent he studied <u>Immanuel Kant</u> and <u>Edmund Husserl</u>. In the early 1970s, Gödel circulated among his friends an elaboration of Leibniz's version of Anselm of Canterbury's ontological proof of God's existence. This is now known as Gödel's ontological proof.

### Awards and honours

Gödel was awarded (with <u>Julian Schwinger</u>) the first <u>Albert Einstein Award</u> in 1951, and was also awarded the <u>National Medal of Science</u>, in 1974. Gödel was elected a <u>Foreign Member of the Royal Society (ForMemRS) in 1968</u>. He was a Plenary Speaker of the <u>ICM</u> in 1950 in Cambridge, Massachusetts. Gödel <u>Prize</u>, an annual prize for outstanding papers in the area of theoretical computer science, is named after him.

### Later life and death

Later in his life, Gödel suffered periods of mental instability and illness. He had an obsessive fear of being poisoned; he would eat only food that his wife, Adele, prepared for him. Late in 1977, she was hospitalized for six months and could subsequently no longer prepare her husband's food. In her absence, he refused to eat, eventually starving to death. He weighed 29 kilograms (65 lb) when he died. His death certificate reported that he died of "malnutrition and inanition caused by personality disturbance" in Princeton Hospital on January 14, 1978. He was buried in Princeton Cemetery. Adele's death followed in 1981.



Gravestone of Kurt and Adele Gödel in the Princeton, N.J., cemetery

### Personal life

### **Religious views**

Gödel was a convinced theist, in the Christian tradition.<sup>[33]</sup> He held the notion that God was personal.

He believed firmly in an afterlife, stating: "Of course this supposes that there are many relationships which today's science and received wisdom haven't any inkling of. But I am convinced of this [the afterlife], independently of any theology." It is "possible today to perceive, by pure reasoning" that it "is entirely consistent with known facts." "If the world is rationally constructed and has meaning, then there must be such a thing [as an afterlife]." [34]

In an unmailed answer to a questionnaire, Gödel described his religion as "baptized Lutheran (but not member of any religious congregation). My belief is <u>theistic</u>, not <u>pantheistic</u>, following <u>Leibniz</u> rather than <u>Spinoza</u>."<sup>[35]</sup> Describing religion(s) in general, Gödel said: "Religions are, for the most part, bad—but religion is not".<sup>[36]</sup> According to his wife Adele, "Gödel, although he did not go to church, was religious and read the Bible in bed every Sunday morning",<sup>[37]</sup> while of Islam, he said, "I like Islam: it is a consistent [or consequential] idea of religion and open-minded."<sup>[38]</sup>

### Legacy

The Kurt Gödel Society, founded in 1987, was named in his honor. It is an international organization for the promotion of research in the areas of logic, philosophy, and the history of mathematics. The University of Vienna hosts the Kurt Gödel Research Center for Mathematical Logic. The Association for Symbolic Logic has invited an annual Kurt Gödel lecturer each year since 1990. Gödel's Philosophical Notebooks (http://w

ww.bbaw.de/en/research/goedel) are edited at the Kurt Gödel Research Centre (http://www.bbaw.de/en/research/goedel) which is situated at the Berlin-Brandenburg Academy of Sciences and Humanities (http://www.bbaw.de/en/academy) in Germany.

Five volumes of Gödel's collected works have been published. The first two include Gödel's publications; the third includes unpublished manuscripts from Gödel's *Nachlass*, and the final two include correspondence.

A biography of Gödel was published by <u>John Dawson</u> in 2005: *Logical Dilemmas: The Life and Work of Kurt Gödel* (<u>A. K. Peters</u>, Wellesley, MA, <u>ISBN</u> <u>1-56881-256-6</u>). Gödel was also one of four mathematicians examined in the 2008 <u>BBC</u> documentary entitled *Dangerous Knowledge* by David Malone. [39]

Douglas Hofstadter wrote a popular book in 1979 called *Gödel, Escher, Bach* to celebrate the work and ideas of Gödel, along with those of artist M. C. Escher and composer Johann Sebastian Bach. The book partly explores the ramifications of the fact that Gödel's incompleteness theorem can be applied to any Turing-complete computational system, which may include the human brain.

# **Bibliography**

#### Important publications

In German:

- 1930, "Die Vollständigkeit der Axiome des logischen Funktionenkalküls." Monatshefte für Mathematik und Physik 37: 349–60.
- 1931, "Über formal unentscheidbare Sätze der <u>Principia Mathematica</u> und verwandter Systeme, I." <u>Monatshefte für Mathematik und Physik</u>
   38: 173–98.
- 1932, "Zum intuitionistischen Aussagenkalkül", Anzeiger Akademie der Wissenschaften Wien 69: 65–66.

#### In English:

- 1940. The Consistency of the Axiom of Choice and of the Generalized Continuum Hypothesis with the Axioms of Set Theory. Princeton University Press.
- 1947. "What is Cantor's continuum problem?" *The American Mathematical Monthly 54*: 515–25. Revised version in <u>Paul Benacerraf</u> and Hilary Putnam, eds., 1984 (1964). *Philosophy of Mathematics: Selected Readings*. Cambridge Univ. Press: 470–85.
- 1950, "Rotating Universes in General Relativity Theory." *Proceedings of the international Congress of Mathematicians in Cambridge*, 1: 175–81

#### In English translation:

- Kurt Gödel, 1992. On Formally Undecidable Propositions Of Principia Mathematica And Related Systems, tr. B. Meltzer, with a comprehensive introduction by Richard Braithwaite. Dover reprint of the 1962 Basic Books edition.
- Kurt Gödel, 2000. [40] On Formally Undecidable Propositions Of Principia Mathematica And Related Systems, tr. Martin Hirzel
- Jean van Heijenoort, 1967. A Source Book in Mathematical Logic, 1879–1931. Harvard Univ. Press.
  - 1930. "The completeness of the axioms of the functional calculus of logic," 582–91.
  - 1930. "Some metamathematical results on completeness and consistency," 595–96. Abstract to (1931).
  - 1931. "On formally undecidable propositions of *Principia Mathematica* and related systems," 596–616.
  - 1931a. "On completeness and consistency," 616–17.
- "My philosophical viewpoint" (https://web.archive.org/web/20160304074030/http://www.geocities.ws/kandathil/phil\_view.html), c. 1960, unpublished.
- "The modern development of the foundations of mathematics in the light of philosophy" (https://web.archive.org/web/20160304080342/http://www.geocities.ws/kandathil/foundations\_mathematics.html), 1961, unpublished.
- Collected Works: Oxford University Press: New York. Editor-in-chief: Solomon Feferman.
  - Volume I: Publications 1929–1936 ISBN 978-0-19-503964-1 / Paperback: ISBN 978-0-19-514720-9,
  - Volume II: Publications 1938–1974 ISBN 978-0-19-503972-6 / Paperback: ISBN 978-0-19-514721-6
  - Volume III: Unpublished Essays and Lectures ISBN 978-0-19-507255-6 / Paperback: ISBN 978-0-19-514722-3,
  - Volume IV: Correspondence, A–G ISBN 978-0-19-850073-5,
  - Volume V: Correspondence, H–Z ISBN 978-0-19-850075-9.
- Philosophische Notizbücher / Philosophical Notebooks: De Gruyter: Berlin/München/Boston. Editor: Eva-Maria Engelen.
  - Volume 1: Philosophie I Maximen 0 / Philosophy I Maxims 0 ISBN 978-3-11-058374-8.

### See also

- Gödel machine
- Gödel Prize
- List of Austrian scientists
- List of pioneers in computer science
- Mathematical Platonism
- Original proof of Gödel's completeness theorem

#### **Notes**

- 1. Kreisel, G. (1980). "Kurt Godel. 28 April 1906–14 January 1978". *Biographical Memoirs of Fellows of the Royal Society*. **26**: 148–224. doi:10.1098/rsbm.1980.0005 (https://doi.org/10.1098%2Frsbm.1980.0005).
- 2. "Gödel" (https://www.merriam-webster.com/dictionary/G%C3%B6del). *Merriam-Webster Dictionary*.
- 3. For instance, in their <u>Principia Mathematica (http://plato.stanford.edu/entries/principia-mathematica/)</u> (Stanford Encyclopedia of Philosophy edition).
- 4. Dawson 1997, pp. 3-4.
- 5. Kim, Alan (January 1, 2015). Zalta, Edward N. (ed.). *Johann Friedrich Herbart* (http://plato.stanford.edu/archives/win2015/entries/johann-he rbart/) (Winter 2015 ed.).
- 6. Dawson 1997, p. 12
- 7. Procházka 2008, pp. 30-34.
- 8. Dawson 1997, p. 15.
- 9. Gödel, Kurt (1986). *Collected works* (https://books.google.co.uk/books?id=5ya4A0w62skC&pg=PA37#v=onepage&q&f=false). Feferman, Solomon. Oxford. p. 37. ISBN 0195039645. OCLC 12371326 (https://www.worldcat.org/oclc/12371326).
- 10. Balaguer, Mark. "Kurt Godel" (https://school.eb.com/levels/high/article/Kurt-G%C3%B6del/37162). Britannica School High. Encyclopædia Britannica, Inc. Retrieved June 3, 2019.
- 11. Kim, Alan (January 1, 2015). Zalta, Edward N. (ed.). *Johann Friedrich Herbart* (http://plato.stanford.edu/archives/win2015/entries/johann-herbart/) (Winter 2015 ed.).
- 12. Dawson 1997, p. 24.
- 13. Gleick, J. (2011) The Information: A History, a Theory, a Flood, London, Fourth Estate, p. 181.
- 14. Halmos, P.R. (April 1973). "The Legend of von Neumann". *The American Mathematical Monthly.* **80** (4): 382–94. doi:10.1080/00029890.1973.11993293 (https://doi.org/10.1080%2F00029890.1973.11993293).
- 15. Stadler, Friedrich (2015). *The Vienna Circle: Studies in the Origins, Development, and Influence of Logical Empiricism* (https://books.google.com/?id=2rAlCQAAQBAJ&pg=PA161&lpg=PA161&dq=Erkenntnis+1930+Konigsberg#v=onepage&q=Erkenntnis%201930%20Konigsberg &f=false). Springer. ISBN 9783319165615.
- 16. Casti, John L.; Depauli, Werner; Koppe, Matthias; Weismantel, Robert (2001). *Gödel: a life of logic. Mathematics of Operations Research.*31. Cambridge, Mass.: Basic Books. p. 147. arXiv:math/0410111 (https://arxiv.org/abs/math/0410111). doi:10.1287/moor.1050.0169 (https://doi.org/10.1287%2Fmoor.1050.0169). ISBN 978-0-7382-0518-2.. From p. 80, which quotes Rudolf Gödel, Kurt's brother and a medical doctor. The words "a severe nervous crisis", and the judgement that the Schlick assassination was its trigger, are from the Rudolf Gödel quote. Rudolf knew Kurt well in those years.
- 17. Dawson 1997, pp. 110-12
- 18. Hutchinson Encyclopedia (1988), p. 518
- 19. Gödel, Kurt (November 9, 1938), "The Consistency of the Axiom of Choice and of the Generalized Continuum-Hypothesis" (https://www.nc

- bi.nlm.nih.gov/pmc/articles/PMC1077160). Proceedings of the National Academy of Sciences of the United States of America. 24 (12): 556–57. Bibcode:1938PNAS...24..556G (https://ui.adsabs.harvard.edu/abs/1938PNAS...24..556G). doi:10.1073/pnas.24.12.556 (https://doi.org/10.1073%2Fpnas.24.12.556). ISSN 0027-8424 (https://www.worldcat.org/issn/0027-8424). PMC 1077160 (https://www.ncbi.nlm.nih.gov/pmc/articles/PMC1077160). PMID 16577857 (https://pubmed.ncbi.nlm.nih.gov/16577857).
- 20. Dawson, John W. Jr. "Kurt Gödel at Notre Dame" (https://math.nd.edu/assets/13975/logicatndweb.pdf) (PDF). p. 4. "the Mathematics department at the University of Notre Dame was host ... for a single semester in the spring of 1939 [to] Kurt Gödel"
- 21. "Kurt Gödel" (https://www.ias.edu/scholars/godel). Institute for Advanced Study.
- 22. Goldstein (2005), p. 33.
- 23. Dawson 1997, pp. 179–80. The story of Gödel's citizenship hearing is repeated in many versions. Dawson's account is the most carefully researched, but was written before the rediscovery of Morgenstern's written account. Most other accounts appear to be based on Dawson, hearsay or speculation.
- 24. Oskar Morgenstern (September 13, 1971). "History of the Naturalization of Kurt Gödel" (https://robert.accettura.com/wp-content/uploads/20 10/10/Morgenstern\_onGoedelcitizenship.pdf) (PDF). Retrieved April 16, 2019.
- 25. "Kurt Gödel Institute for Advanced Study" (https://www.ias.edu/people/godel). Retrieved December 1, 2015.
- 26. Gödel, Kurt (July 1, 1949). "An Example of a New Type of Cosmological Solutions of Einstein's Field Equations of Gravitation". *Rev. Mod. Phys.* 21 (447): 447–450. doi:10.1103/RevModPhys.21.447 (https://doi.org/10.1103%2FRevModPhys.21.447).
- 27. "Das Genie & der Wahnsinn" (http://www.tagesspiegel.de/magazin/wissen/Albert-Einstein-Kurt-Goedel;art304,2454513). *Der Tagesspiegel* (in German). January 13, 2008.
- 28. Dawson, John W., Jr. (2005). Logical Dilemmas: The Life and Work of Kurt Gödel (https://books.google.com/?id=gA8SucCU1AYC&pg=PA1 66&dq=godel+leibniz). A K Peters. p. 166. ISBN 9781568812564.
- 29. "The President's National Medal of Science: Recipient Details I NSF National Science Foundation" (https://www.nsf.gov/od/nms/recip\_details.jsp?recip\_id=138). www.nsf.gov. Retrieved September 17, 2016.
- 30. Gödel, Kurt (1950). "Rotating universes in general relativity theory" (http://www.mathunion.org/ICM/ICM1950.1/Main/icm1950.1.0175.0181. ocr.pdf) (PDF). In: Proceedings of the International Congress of Mathematicians, Cambridge, Massachusetts, August 30–September 6, 1950. vol. 1. pp. 175–81.
- 31. Davis, Martin (May 4, 2005). "Gödel's universe". *Nature*. **435** (7038): 19–20. <u>Bibcode</u>:2005Natur.435...19D (https://ui.adsabs.harvard.edu/abs/2005Natur.435...19D). doi:10.1038/435019a (https://doi.org/10.1038%2F435019a).
- 32. Toates, Frederick; Olga Coschug Toates (2002). Obsessive Compulsive Disorder: Practical Tried-and-Tested Strategies to Overcome OCD. Class Publishing. p. 221. ISBN 978-1-85959-069-0.
- 33. Tucker McElroy (2005). *A to Z of Mathematicians* (https://archive.org/details/tozofmathematici0000mcel/page/118). Infobase Publishing. p. 118 (https://archive.org/details/tozofmathematici0000mcel/page/118). ISBN 978-0-8160-5338-4. "Gödel had a happy childhood, and was called "Mr. Why" by his family, due to his numerous questions. He was baptized as a Lutheran, and re-mained a theist (a believer in a personal God) throughout his life."
- 34. Hao Wang, "A Logical Journey: From Gödel to Philosophy", 1996, pp. 104-05.

- 35. Goder's answer to a special questionnaire sent nim by the sociologist burke Grandjean. This answer is quoted directly in wang 1987, p. 18, and indirectly in Wang 1996, p. 112. It's also quoted directly in Dawson 1997, p. 6, who cites Wang 1987. The Grandjean questionnaire is perhaps the most extended autobiographical item in Gödel's papers. Gödel filled it out in pencil and wrote a cover letter, but he never returned it. "Theistic" is italicized in both Wang 1987 and Wang 1996. It is possible that this italicization is Wang's and not Gödel's. The quote follows Wang 1987, with two corrections taken from Wang 1996. Wang 1987 reads "Baptist Lutheran" where Wang 1996 has "baptized Lutheran". Wang 1987 has "rel. cong.", which in Wang 1996 is expanded to "religious congregation".
- 36. Wang 1996 p. 316
- 37. Wang 1996, p. 51.
- 38. Wang 1996, p. 148, 4.4.3. It is one of Gödel's observations, made between 16 November and 7 December 1975, which Wang found hard to classify under the main topics considered elsewhere in the book.
- 39. "Dangerous Knowledge" (https://www.bbc.co.uk/bbcfour/documentaries/features/dangerous-knowledge.shtml). BBC. June 11, 2008. Retrieved October 6, 2009.
- 40. Kurt Godel (1931). "Über formal unentscheidbare Sätze der Principia Mathematica und verwandter Systeme, I" (http://www.research.ibm.com/people/h/hirzel/papers/canon00-goedel.pdf) [On formally undecidable propositions of Principia Mathematica and related systems I] (PDF). Monatshefte für Mathematik und Physik. 38: 173–98. doi:10.1007/BF01700692 (https://doi.org/10.1007%2FBF01700692).

### References

- Dawson, John W (1997), Logical dilemmas: The life and work of Kurt Gödel, Wellesley, MA: AK Peters.
- Goldstein, Rebecca (2005), *Incompleteness: The Proof and Paradox of Kurt Gödel*, New York: W.W. Norton & Co, <u>ISBN</u> <u>978-0-393-32760-1</u>.

## **Further reading**

- Casti, John L; DePauli, Werner (2000), Gödel: A Life of Logic, Cambridge, MA: Basic Books (Perseus Books Group), ISBN 978-0-7382-0518-2.
- Dawson, Jr, John W (1996), Logical Dilemmas: The Life and Work of Kurt Gödel, AK Peters.
- Dawson, Jr, John W (1999), "Gödel and the Limits of Logic", Scientific American, 280 (6): 76–81, Bibcode:1999SciAm.280f..76D (https://ui.adsabs.harvard.edu/abs/1999SciAm.280f..76D), doi:10.1038/scientificamerican0699-76 (https://doi.org/10.1038%2Fscientificamerican0699-76), PMID 10048234 (https://pubmed.ncbi.nlm.nih.gov/10048234).
- Franzén, Torkel (2005), Gödel's Theorem: An Incomplete Guide to Its Use and Abuse, Wellesley, MA: AK Peters.
- Ivor Grattan-Guinness, 2000. The Search for Mathematical Roots 1870–1940. Princeton Univ. Press.
- Jaakko Hintikka, 2000. On Gödel. Wadsworth.
- Douglas Hofstadter, 1980. Gödel, Escher, Bach. Vintage.

- Stephen Kleene, 1967. Mathematical Logic. Dover paperback reprint c. 2001.
- Stephen Kleene, 1980. *Introduction to Metamathematics*. North Holland <u>ISBN</u> <u>0-7204-2103-9</u> (Ishi Press paperback. 2009. <u>ISBN</u> <u>978-0-923891-57-2</u>)
- J.R. Lucas, 1970. The Freedom of the Will. Clarendon Press, Oxford.
- Ernest Nagel and Newman, James R., 1958. Gödel's Proof. New York Univ. Press.
- Procházka, Jiří, 2006, 2006, 2008, 2008, 2010. Kurt Gödel: 1906–1978: Genealogie. ITEM, Brno. Volume I. Brno 2006, ISBN 80-902297-9-4. In German, English. Volume II. Brno 2006, ISBN 80-903476-0-6. In German, English. Volume III. Brno 2008, ISBN 80-903476-4-9. In German, English. Volume IV. Brno, Princeton 2008, ISBN 978-80-903476-5-6. In German, English Volume V, Brno, Princeton 2010, ISBN 80-903476-9-X. In German, English.
- Procházka, Jiří, 2012. "Kurt Gödel: 1906–1978: Historie". ITEM, Brno, Wien, Princeton. Volume I. ISBN 978-80-903476-2-5. In German, English.
- Ed Regis, 1987. Who Got Einstein's Office? Addison-Wesley Publishing Company, Inc.
- Raymond Smullyan, 1992. *Godel's Incompleteness Theorems*. Oxford University Press.
- Olga Taussky-Todd, 1983. Remembrances of Kurt Gödel (http://calteches.library.caltech.edu/605/02/Todd.pdf). Engineering & Science, Winter 1988.
- Gödel, Alois, 2006. Brünn 1679–1684. ITEM, Brno 2006, edited by Jiří Procházka, ISBN 80-902297-8-6
- Procházka, Jiří 2017. "Kurt Gödel: 1906–1978: Curriculum vitae". ITEM, Brno, Wien, Princeton 2017. Volume I. (ISBN 978-80-903476-9-4).
   In German, English.
- Procházka, Jiří 2019. "Kurt Gödel 1906-1978: Curriculum vitae". ITEM, Brno, Wien, Princeton 2019. Volume II. (ISBN 978-80-903476-1-8). In German, English.
- Hao Wang, 1987. Reflections on Kurt Gödel. MIT Press.
- Hao Wang, 1996. A Logical Journey: From Godel to Philosophy. MIT Press.
- Yourgrau, Palle, 1999. Gödel Meets Einstein: Time Travel in the Gödel Universe. Chicago: Open Court.
- Yourgrau, Palle, 2004. A World Without Time: The Forgotten Legacy of Gödel and Einstein. Basic Books. Book review by John Stachel in the Notices of the American Mathematical Society (54 (7), pp. 861–68):

### **External links**

- Weisstein, Eric Wolfgang (ed.). "Gödel, Kurt (1906–1978)" (http://scienceworld.wolfram.com/biography/Goedel.html). ScienceWorld.
- Kennedy, Juliette. "Kurt Gödel" (https://plato.stanford.edu/entries/goedel/). In Zalta, Edward N. (ed.). Stanford Encyclopedia of Philosophy.
- Time Bandits (http://www.newyorker.com/archive/2005/02/28/050228crat\_atlarge): an article about the relationship between Gödel and Einstein by Jim Holt
- Notices of the AMS, April 2006, Volume 53, Number 4 (http://www.ams.org/notices/200604/200604-toc.html) Kurt Gödel Centenary Issue

- Paul Davies and Freeman Dyson discuss Kurt Godel (http://www.abc.net.au/rn/scienceshow/stories/2006/1807626.htm)
- "Gödel and the Nature of Mathematical Truth" (http://www.edge.org/3rd\_culture/goldstein05/goldstein05\_index.html) Edge: A Talk with Rebecca Goldstein on Kurt Gödel.
- It's Not All In The Numbers: Gregory Chaitin Explains Gödel's Mathematical Complexities. (https://web.archive.org/web/20091106003330/http://simplycharly.com/godel/gregory\_chaitin\_interview.htm)
- Gödel photo gallery. (https://web.archive.org/web/20090301015757/http://www.univie.ac.at/bvi/photo-gallery/photo\_gallery.htm)
- Kurt Gödel (http://www-history.mcs.st-andrews.ac.uk/Biographies/Godel.html)
- National Academy of Sciences Biographical Memoir (http://www.nasonline.org/publications/biographical-memoirs/memoir-pdfs/gdel-kurt.pdf
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