# Grigori Perelman

Grigori Yakovlevich Perelman (Russian: Григорий Яковлевич Перельман, IPA: [gr<sup>j</sup>ɪˈgor<sup>j</sup>ɪj ˈjakəvl<sup>j</sup>ɪv<sup>j</sup>ɪtç p<sup>j</sup>ɪr<sup>j</sup>ɪl<sup>j</sup>man] (♠ listen); born 13 June 1966) is a Russian mathematician. He has made contributions to Riemannian geometry and geometric topology. In 1994, Perelman proved the soul conjecture. In 2003, he proved Thurston's geometrization conjecture. The proof was confirmed in 2006. This consequently solved in the affirmative the Poincaré conjecture.

In August 2006, Perelman was offered the <u>Fields Medal</u><sup>[1]</sup> for "his contributions to geometry and his revolutionary insights into the analytical and geometric structure of the <u>Ricci flow</u>", but he declined the award, stating: "I'm not interested in money or fame; I don't want to be on display like an animal in a zoo."<sup>[2]</sup> On 22 December 2006, the scientific journal <u>Science</u> recognized Perelman's proof of the <u>Poincaré conjecture</u> as the scientific "<u>Breakthrough of the Year</u>", the first such recognition in the area of mathematics.<sup>[3]</sup>

On 18 March 2010, it was announced that he had met the criteria to receive the first Clay <u>Millennium Prize</u><sup>[4]</sup> for resolution of the Poincaré conjecture. On 1 July 2010, he rejected the prize of one million dollars, saying that he considered the decision of the board of CMI and the award very unfair and that his contribution to solving the Poincaré conjecture was no greater than that of <u>Richard S. Hamilton</u>, the mathematician who pioneered the <u>Ricci flow</u> with the aim of attacking the conjecture. [5][6] He had previously rejected the prestigious prize of the European Mathematical Society, in 1996. [7]

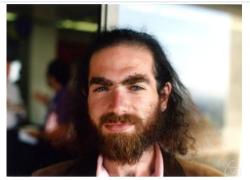
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### **Grigori Perelman**



Grigori Perelman in 1993

Born	13 June 1966
	Leningrad, Soviet
	Union

Nationality	Russian

Ci	itiz	ens	hip	Russia

Alma mater	Leningrad State
	University (PhD 100

	University (PhD 1990)
Known for	Riemannian geometry
	Geometric topology
	Proof of the soul
	conjecture
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conjecture

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Awards	Saint Petersburg

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	declined
	Millennium Prize
	(2010), declined
Sc	cientific career
So Fields	cientific career  Mathematics
Fields	Mathematics
Fields	Mathematics Saddle Surfaces in
Fields	Mathematics Saddle Surfaces in Euclidean
Fields Thesis	Mathematics  Saddle Surfaces in  Euclidean  Spaces (1990)

# Early life and education

Grigori Yakovlevich Perelman was born in Leningrad, Soviet Union (now Saint Petersburg, Russia) on 13 June 1966, to Russian-Jewish parents [8][9][10] Yakov (who now lives in Israel)[8] and Lyubov (who still lives in Saint Petersburg with Grigori). [8] Grigori's mother Lyubov gave up graduate work in mathematics to raise him. Grigori's mathematical talent became apparent at the age of ten, and his mother enrolled him in Sergei Rukshin's after-school mathematics training program. [11]

His mathematical education continued at the <u>Leningrad Secondary School #239</u>, a <u>specialized school</u> with advanced mathematics and physics programs. Grigori excelled in all subjects except <u>physical education</u>. In 1982, as a member of the <u>Soviet Union</u> team competing in the <u>International Mathematical Olympiad</u>, an international competition for high school students, he won a gold medal, achieving a perfect score. He continued as a student of The School of Mathematics and Mechanics at the <u>Leningrad State University</u>, without admission examinations and enrolled to the university.

After his PhD in 1990, Perelman began work at the Leningrad Department of Steklov Institute of Mathematics of the USSR Academy of Sciences, where his advisors were Aleksandrov and Yuri Burago. In the late 1980s and early 1990s, with a strong recommendation from the geometer Mikhail Gromov, [14] Perelman obtained research positions at several universities in the United States.

In 1991 Perelman won the Young Mathematician Prize of the St. Petersburg Mathematical Society for his work on Aleksandrov's spaces of curvature bounded from below. In 1992, he was invited to spend a semester each at the Courant Institute in New York University and Stony Brook University where he began work on manifolds with lower bounds on Ricci curvature. From there, he accepted a two-year Miller Research Fellowship at the University of California, Berkeley in 1993. After having proved the soul conjecture in 1994, he was offered jobs at several top universities in the US, including Princeton and Stanford, but he rejected them all and returned to the Steklov Institute in Saint Petersburg in the summer of 1995 for a research-only position.

# Soul conjecture

Cheeger and Gromoll's **soul conjecture** states:

Suppose (M, g) is complete, connected and non-compact with sectional curvature  $K \ge 0$ , and there exists a point in M where the sectional curvature (in all sectional directions) is strictly positive. Then the soul of M is a point; equivalently M is diffeomorphic to  $\mathbf{R}^n$ .

Perelman proved the conjecture by establishing that in the general case  $K \ge 0$ , Sharafutdinov's retraction  $P: M \to S$  is a submersion.

# Geometrization and Poincaré conjectures

Until late 2002, Perelman was best known for his work in <u>comparison theorems</u> in <u>Riemannian geometry</u>. Among his notable achievements was a short and elegant proof of the soul conjecture.

#### **Problem**

The Poincaré conjecture, proposed by French mathematician Henri Poincaré in 1904, was one of the key problems in topology. Any loop on a 3-sphere—as exemplified by the set of points at a distance of 1 from the origin in four-dimensional Euclidean space—can be contracted into a point. The Poincaré conjecture asserts that any closed three-dimensional manifold, such that any loop can be contracted into a point, is topologically a 3-sphere. The analogous result has been known to be true in dimensions greater than or equal to five since 1960 as in the work of Stephen Smale. The four-dimensional case resisted longer, finally being solved in 1982 by Michael Freedman. But the case of three-manifolds turned out to be the hardest of them all. Roughly speaking, this is because in topologically manipulating a three-manifold there are too few dimensions to move "problematic regions" out of the way without interfering with something else. The most fundamental contribution to the three-dimensional case had been produced by Richard S. Hamilton. The role of Perelman was to complete the Hamilton program.

### Perelman's proof

In November 2002, Perelman posted the first of a series of <u>eprints</u> to the <u>arXiv</u>, in which he claimed to have outlined a <u>proof</u> of the geometrization conjecture, of which the Poincaré conjecture is a particular case. [16][17][18]

Perelman modified Richard S. Hamilton's program for a proof of the conjecture. The central idea is the notion of the Ricci flow. Hamilton's fundamental idea is to formulate a "dynamical process" in which a given three-manifold is geometrically distorted such that this distortion process is governed by a differential equation analogous to the heat equation. The heat equation (which much earlier motivated Riemann to state his Riemann hypothesis on the zeros of the zeta function) describes the behavior of scalar quantities such as temperature. It ensures that concentrations of elevated temperature will spread out until a uniform temperature is achieved throughout an object. Similarly, the Ricci flow describes the behavior of a tensorial quantity, the Ricci curvature tensor. Hamilton's hope was that under the Ricci flow concentrations of large curvature will spread out until a uniform curvature is achieved over the entire three-manifold. If so, if one starts with any three-manifold and lets the Ricci flow occur, then one should, in principle, eventually obtain a kind of "normal form". According to William Thurston this normal form must take one of a small number of possibilities, each having a different kind of geometry, called Thurston model geometries.

This is similar to formulating a dynamical process that gradually "perturbs" a given square matrix and that is guaranteed to result after a finite time in its rational canonical form.

Hamilton's idea attracted a great deal of attention, but no one could prove that the process would not be impeded by developing "singularities", until Perelman's eprints sketched a procedure for overcoming these obstacles. According to Perelman, a modification of the standard Ricci flow, called *Ricci flow with surgery*, can systematically excise singular regions as they develop, in a controlled way.

It was known that singularities (including those that, roughly speaking, occur after the flow has continued for an infinite amount of time) must occur in many cases. However, any singularity that develops in a finite time is essentially a "pinching" along certain spheres corresponding to the <u>prime decomposition</u> of the 3-manifold. Furthermore, any "infinite time" singularities result from certain collapsing pieces of the JSJ decomposition. Perelman's work proves this claim and thus proves the geometrization conjecture.

#### **Verification**

Perelman's work was checked relatively quickly. In April 2003, Perelman visited the <u>Massachusetts Institute of Technology</u>, <u>Princeton University</u>, Stony Brook University, Columbia University and New York University to give a short series of lectures on his work.

On 25 May 2006, <u>Bruce Kleiner</u> and <u>John Lott</u>, both of the <u>University of Michigan</u>, posted a paper on <u>arXiv</u> that fills in the details of Perelman's proof of the Geometrization conjecture. [19] John Lott said in ICM2006, "It has taken us some time to examine Perelman's work. This is partly due to the originality of Perelman's work and partly to the technical sophistication of his arguments. All indications are that his arguments are correct."

In June 2006, the *Asian Journal of Mathematics* published a paper by Zhu Xiping of Sun Yat-sen University in China and Huai-Dong Cao of Lehigh University in Pennsylvania, giving a complete description of Perelman's proof of the Poincaré and the geometrization conjectures. The June 2006 paper claimed: "This proof should be considered as the crowning achievement of the Hamilton–Perelman theory of Ricci flow." [20] Even more boldly, in the introduction of the paper the authors state that they "give the first written account of a complete proof of the Poincaré conjecture and the geometrization conjecture of Thurston." Asked about the paper, Perelman said the pair had not contributed anything original, and had simply reworked his proof because they "did not quite understand the argument". [21]

In November 2006, Cao and Zhu published an erratum disclosing that they had failed to cite properly the previous work of Kleiner and Lott published in 2003. In the same issue, the *AJM* editorial board issued an apology for what it called "incautions" in the Cao–Zhu paper. [22]

On December 3, 2006, Cao and Zhu retracted the original version of their paper, which was titled "A Complete Proof of the Poincaré and Geometrization Conjectures — Application of the Hamilton—Perelman Theory of the Ricci Flow"<sup>[23]</sup> and posted a revised version, renamed, more modestly, "Hamilton—Perelman's Proof of the Poincaré Conjecture and the Geometrization Conjecture".<sup>[24]</sup> Rather than the grand claim of the original abstract, "we give a complete proof", suggesting the proof is by the authors, the revised abstract states: "we give a detailed exposition of a complete proof". The authors also removed the phrase "crowning achievement" from the abstract.

In July 2006, <u>John Morgan</u> of Columbia University and <u>Gang Tian</u> of the Massachusetts Institute of Technology posted a paper on arXiv titled, "Ricci Flow and the Poincaré Conjecture". In this paper, they provide a detailed version of Perelman's proof of the Poincaré conjecture. On 24 August 2006, Morgan delivered a lecture at the <u>ICM</u> in Madrid on the Poincaré conjecture. This was followed up with the paper on arXiv, "Completion of the Proof of the Geometrization Conjecture" on 24 September 2008.

### Fields Medal and Millennium Prize

In May 2006, a committee of nine mathematicians voted to award Perelman a <u>Fields Medal</u> for his work on the Poincaré conjecture. [21] However, Perelman declined to accept the prize. <u>Sir John Ball</u>, president of the <u>International Mathematical Union</u>, approached Perelman in <u>Saint Petersburg</u> in June 2006 to persuade him to accept the prize. After 10 hours of attempted persuasion over two days, Ball gave up. Two weeks later, Perelman summed up the conversation as follows: "He proposed to me three alternatives: accept and come; accept and don't

come, and we will send you the medal later; third, I don't accept the prize. From the very beginning, I told him I have chosen the third one ... [the prize] was completely irrelevant for me. Everybody understood that if the proof is correct, then no other recognition is needed."<sup>[21]</sup> "'I'm not interested in money or fame,' he is quoted to have said at the time. 'I don't want to be on display like an animal in a zoo. I'm not a hero of mathematics. I'm not even that successful; that is why I don't want to have everybody looking at me.'"<sup>[28]</sup> Nevertheless, on 22 August 2006, Perelman was publicly offered the medal at the <u>International Congress of Mathematicians in Madrid</u> "for his contributions to geometry and his revolutionary insights into the analytical and geometric structure of the Ricci flow".<sup>[29]</sup> He did not attend the ceremony, and declined to accept the medal, making him the only person to decline this prestigious prize.<sup>[7][30]</sup>

He had previously rejected a prestigious prize from the European Mathematical Society.<sup>[7]</sup>

On 18 March 2010, Perelman was awarded a Millennium Prize for solving the problem. On June 8, 2010, he did not attend a ceremony in his honor at the Institut Océanographique, Paris to accept his \$1 million prize. According to Interfax, Perelman refused to accept the Millennium prize in July 2010. He considered the decision of the Clay Institute unfair for not sharing the prize with Richard S. Hamilton, and stated that "the main reason is my disagreement with the organized mathematical community. I don't like their decisions, I consider them unjust."

The Clay Institute subsequently used Perelman's prize money to fund the "Poincaré Chair", a temporary position for young promising mathematicians at the Paris Institut Henri Poincaré. [33]

### Possible withdrawal from mathematics

Perelman quit his job at the Steklov Institute in December 2005.<sup>[34]</sup> His friends are said to have stated that he currently finds mathematics a painful topic to discuss; some even say that he has abandoned mathematics entirely.<sup>[35]</sup>

Perelman is quoted in an article in <u>The New Yorker</u> saying that he is disappointed with the ethical standards of the field of mathematics. The article implies that Perelman refers particularly to the efforts of Fields medalist <u>Shing-Tung Yau</u> to downplay Perelman's role in the proof and play up the work of <u>Cao</u> and <u>Zhu</u>. Perelman added, "I can't say I'm outraged. Other people do worse. Of course, there are many mathematicians who are more or less honest. But almost all of them are conformists. They are more or less honest, but they tolerate those who are not honest." He has also said that "It is not people who break ethical standards who are regarded as aliens. It is people like me who are isolated." [21]

This, combined with the possibility of being awarded a Fields medal, led him to quit professional mathematics. He has said that "As long as I was not conspicuous, I had a choice. Either to make some ugly thing or, if I didn't do this kind of thing, to be treated as a pet. Now, when I become a very conspicuous person, I cannot stay a pet and say nothing. That is why I had to quit." (*The New Yorker* authors explained Perelman's reference to "some ugly thing" as "a fuss" on Perelman's part about the ethical breaches he perceived.)<sup>[36]</sup>

It is uncertain whether his resignation from Steklov and subsequent seclusion mean that he has ceased to practice mathematics. Fellow countryman and mathematician Yakov Eliashberg said that, in 2007, Perelman confided to him that he was working on other things but it was too premature to talk about it. He is said to have been interested in the past in the Navier–Stokes equations and the problem of their existence and smoothness.<sup>[37]</sup>

In 2014, Russian media reported that Perelman was working in the field of <u>nanotechnology</u> in Sweden.<sup>[38]</sup> However, shortly afterwards, he was spotted again in his native hometown, Saint Petersburg.<sup>[38]</sup>

### Perelman and the media

Perelman has avoided journalists and other members of the media. <u>Masha Gessen</u>, the author of *Perfect Rigour: A Genius and the Mathematical Breakthrough of the Century*, a book about him, was unable to meet him.<sup>[39]</sup>

A Russian documentary about Perelman in which his work is discussed by several leading mathematicians including Mikhail Gromov was released in 2011 under the title "Иноходец. Урок Перельмана," "Maverick: Perelman's Lesson."

In April 2011, Aleksandr Zabrovsky, producer of "President-Film" studio, claimed to have held an interview with Perelman and agreed to shoot a film about him, under the tentative title *The Formula of the Universe*. [40] Zabrovsky says that in the interview, [41] Perelman explained why he rejected the one million dollar prize. [40] A number of journalists [42][43][44] believe that Zabrovky's interview is most likely a fake, pointing to contradictions in statements supposedly made by Perelman.

The writer Brett Forrest briefly interacted with Perelman in 2012. [45][46] Perelman refuses to talk to journalists. One who managed to reach him on his mobile was told: "You are disturbing me. I am picking mushrooms." [47]

# **Bibliography**

#### **Dissertation**

■ Перельман, Григорий Яковлевич (1990). *Седловые поверхности в евклидовых пространствах* [Saddle surfaces in Euclidean spaces] (in Russian). Ленинградский государственный университет. Автореф. дис. на соиск. учен. степ. канд. физ.-мат. наук.

#### **Research papers**

- Burago, Yu. D.; Gromov, M. L.; Perelman, G. Ya. (1992). "A. D. Aleksandrov spaces with curvatures bounded below" (https://semanticsc holar.org/paper/9ec7dadeebb8a3a9f269e43783ea0908e7a35e61). Russian Mathematical Surveys. 47 (2): 1–58.
   Bibcode:1992RuMaS..47....1B (https://ui.adsabs.harvard.edu/abs/1992RuMaS..47....1B). doi:10.1070/RM1992v047n02ABEH000877 (https://doi.org/10.1070%2FRM1992v047n02ABEH000877).
- Perelman, G. (1993). "Construction of manifolds of positive Ricci curvature with big volume and large Betti numbers" (http://www.msri.org/publications/books/Book30/files/perricci.pdf) (PDF). *Comparison Geometry.* **30**: 157–163. Retrieved August 23, 2006.
- Perelman, G. (1994). "Proof of the soul conjecture of Cheeger and Gromoll" (https://web.archive.org/web/20120301165338/http://intlpress.com/JDG/archive/pdf/1994/40-1-209.pdf) (PDF). *Journal of Differential Geometry.* **40** (1): 209–212. doi:10.4310/jdg/1214455292 (https://doi.org/10.4310%2Fjdg%2F1214455292). MR 1285534 (https://www.ams.org/mathscinet-getitem?mr=1285534). Archived from the original (http://intlpress.com/JDG/archive/pdf/1994/40-1-209.pdf) (PDF) on March 1, 2012.
- Perelman, G. (1993). "Collapsing with No Proper Extremal Subsets" (http://www.msri.org/publications/books/Book30). *Comparison Geometry.* **30**: 157–163.
- Perelman, G. (1994). "Elements of Morse theory on Aleksandrov spaces" (http://mi.mathnet.ru/eng/aa374). Saint Petersburg Mathematical Journal. 5 (1): 205–213.
- Perelman, G. Ya.; Petrunin, A. M. (1994). "Extremal subsets in Alexandrov spaces and the generalized Liberman theorem" (http://mi.ma thnet.ru/eng/aa375). Saint Petersburg Mathematical Journal. 5 (1): 215–227.

#### **Proof of the geometrization conjecture**

- Perelman, Grisha (November 11, 2002). "The entropy formula for the Ricci flow and its geometric applications". <a href="mailto:arXiv:math.DG/0211159"><u>arXiv:math.DG/0211159</u></a>). (https://arxiv.org/abs/math.DG/0211159).
- Perelman, Grisha (March 10, 2003). "Ricci flow with surgery on three-manifolds". <u>arXiv</u>:math.DG/0303109 (https://arxiv.org/abs/math.DG/0303109).
- Perelman, Grisha (July 17, 2003). "Finite extinction time for the solutions to the Ricci flow on certain three-manifolds". arXiv:math.DG/0307245 (https://arxiv.org/abs/math.DG/0307245).

### See also

- Homology sphere
- "Manifold Destiny" (On The New Yorker article)

- Uniformization theorem
- Asteroid 50033 Perelman

### **Notes**

- 1. "Fields Medals 2006" (https://web.archive.org/web/20130617222042/http://www.mathunion.org/General/Prizes/2006/). International Mathematical Union (IMU) Prizes. Archived from the original (http://www.mathunion.org/general/prizes/2006/) on June 17, 2013. Retrieved April 30, 2006.
- 2. "Russian maths genius Perelman urged to take \$1m prize" (http://news.bbc.co.uk/1/hi/8585407.stm). BBC News. March 24, 2010.
- 3. Dana Mackenzie (2006). "Breakthrough of the year. The Poincaré Conjecture—Proved". <u>Science</u>. **314** (5807): 1848–1849. doi:10.1126/science.314.5807.1848 (https://doi.org/10.1126%2Fscience.314.5807.1848). PMID 17185565 (https://pubmed.ncbi.nlm.nih. gov/17185565).
- 4. "The Poincaré Conjecture" (https://web.archive.org/web/20140705132527/http://www.claymath.org/millenium-problems/poincar%C3%A 9-conjecture). Archived from the original (http://www.claymath.org/millenium-problems/poincar%C3%A9-conjecture) on July 5, 2014. Retrieved May 1, 2014.
- 5. "Последнее "нет" доктора Перельмана" (http://www.interfax.ru/society/txt.asp?id=143603). Interfax. July 1, 2010. Archived (https://web/archive.org/web/20100702155304/http://www.interfax.ru/society/txt.asp?id=143603) from the original on July 2, 2010. Retrieved July 1, 2010.
- 6. Malcolm Ritter (July 1, 2010). "Russian mathematician rejects \$1 million prize" (http://www.physorg.com/news197209671.html). AP on PhysOrg. Archived (https://web.archive.org/web/20120117202129/http://www.physorg.com/news197209671.html) from the original on January 17, 2012. Retrieved May 15, 2011.
- 7. "Maths genius declines top prize" (http://news.bbc.co.uk/2/hi/science/nature/5274040.stm). BBC News. August 22, 2006. Archived (https://web.archive.org/web/20100815015937/http://news.bbc.co.uk/2/hi/science/nature/5274040.stm) from the original on August 15, 2010.
- 8. Osborn, Andrew (March 27, 2010). "Russian maths genius may turn down \$1m prize" (https://www.telegraph.co.uk/news/worldnews/eur ope/russia/7530771/Russian-maths-genius-may-turn-down-1m-prize.html). The Daily Telegraph. Archived (https://web.archive.org/web/20100330073600/http://www.telegraph.co.uk/news/worldnews/europe/russia/7530771/Russian-maths-genius-may-turn-down-1m-prize. <a href="https://www.telegraph.co.uk/news/worldnews/europe/russia/7530771/Russian-maths-genius-may-turn-down-1m-prize.html">https://www.telegraph.co.uk/news/worldnews/europe/russia/7530771/Russian-maths-genius-may-turn-down-1m-prize.html</a> from the original on March 30, 2010. Retrieved July 2, 2010. "He has suffered anti-Semitism (he is Jewish)....Grigory is pure Jewish and I never minded that but my bosses did"
- 9. McKie, Robin (2011-03-27). "Perfect Rigour: A Genius and the Mathematical Breakthrough of the Century by Masha Gessen review" (https://www.theguardian.com/books/2011/mar/27/perfect-rigour-grigori-perelman-review). The Guardian. Archived (https://web.archive.org/web/20131004063146/http://www.theguardian.com/books/2011/mar/27/perfect-rigour-grigori-perelman-review) from the original on October 4, 2013. Retrieved 2013-08-23. "Given that his parents were Jewish, Perelman, who was born in 1966, was fortunate in those who took up his cause."
- 10. Masha Gessen (2009, p. 48)

- 11. John Allen Paulos (April 29, 2010). "He Conquered the Conjecture" (http://www.nybooks.com/articles/23863). The New York Review of Books.
- 12. "Eccentric 'Mathsputin' Rejects Million Dollar Prize" (http://www.foxnews.com/scitech/2010/03/30/eccentric-mathsputin-solves-ancient-problem-rejects-million-dollar-prize/). Fox News. Archived (https://web.archive.org/web/20140715221607/http://www.foxnews.com/scitech/2010/03/30/eccentric-mathsputin-solves-ancient-problem-rejects-million-dollar-prize/) from the original on July 15, 2014. Retrieved July 8, 2014.
- 13. "International Mathematical Olympiad" (http://www.imo-official.org/participant\_r.aspx?id=10481). Imo-official.org. Archived (https://web.a rchive.org/web/20121102120643/http://www.imo-official.org/participant\_r.aspx?id=10481) from the original on November 2, 2012.

  Retrieved December 25, 2012.
- 14. Masha Gessen (2009, p. 45)
- 15. "Young mathematician prize of the St. Petersburg Mathematical Society" (http://www.mathsoc.spb.ru/mol\_mat.html).
- 16. Perelman, Grisha (November 11, 2002). "The entropy formula for the Ricci flow and its geometric applications". <a href="mailto:arXiv:math.DG/0211159">arXiv:math.DG/0211159</a>). (https://arxiv.org/abs/math.DG/0211159).
- 17. Perelman, Grisha (10 March 2003). "Ricci flow with surgery on three-manifolds". <a href="mailto:arXiv">arXiv</a>: <a href="mailto:math.DG/0303109">math.DG/0303109</a> (https://arxiv.org/abs/math.DG/0303109).
- 18. Perelman, Grisha (July 17, 2003). "Finite extinction time for the solutions to the Ricci flow on certain three-manifolds". arXiv:math.DG/0307245 (https://arxiv.org/abs/math.DG/0307245).
- 19. Kleiner, Bruce; Lott, John (2008). "Notes on Perelman's papers". *Geometry & Topology*. **12** (5): 2587–2855. arXiv:math/0605667 (https://arxiv.org/abs/math/0605667). doi:10.2140/gt.2008.12.2587 (https://doi.org/10.2140%2Fgt.2008.12.2587).
- 20. Asian Journal of Mathematics (http://www.ims.cuhk.edu.hk/~ajm/vol10/10\_2.pdf) Volume 10, Number 2 Cao and Zhu.
- 21. Nasar, Sylvia; Gruber, David (August 21, 2006). "Manifold Destiny: A legendary problem and the battle over who solved it" (http://www.newyorker.com/archive/2006/08/28/060828fa\_fact2?currentPage=all). *The New Yorker*. Archived (https://web.archive.org/web/20110319 235149/http://www.newyorker.com/archive/2006/08/28/060828fa\_fact2?currentPage=all) from the original on March 19, 2011. Retrieved January 21, 2011.
- 22. Cao, Huai-Dong; Zhu, Xi-Ping (2006). "Erratum to "A complete proof of the Poincaré and geometrization conjectures application of the Hamilton—Perelman theory of the Ricci flow", Asian J. Math., Vol. 10, No. 2, 165-492, 2006" (https://web.archive.org/web/201003280 85053/http://www.intlpress.com/AJM/AJM-v10.php#AJM-10-4). Asian Journal of Mathematics. 10 (4): 663–664.

  doi:10.4310/ajm.2006.v10.n2.a2 (https://doi.org/10.4310%2Fajm.2006.v10.n2.a2). MR 2282358 (https://www.ams.org/mathscinet-getite m?mr=2282358). Archived from the original (http://www.intlpress.com/AJM/AJM-v10.php#AJM-10-4) on 2010-03-28.
- 23. Cao, Huai-Dong; Zhu, Xi-Ping (2006). "A complete proof of the Poincaré and geometrization conjectures application of the Hamilton—Perelman theory of the Ricci flow" (https://web.archive.org/web/20100328085053/http://www.intlpress.com/AJM/AJM-v10.php#AJM-10-2). Asian Journal of Mathematics. 10 (2): 165–492. doi:10.4310/ajm.2006.v10.n2.a2 (https://doi.org/10.4310%2Fajm.2006.v10.n2.a2). MR 2233789 (https://www.ams.org/mathscinet-getitem?mr=2233789). Archived from the original (http://www.intlpress.com/AJM/AJM-v10.php#AJM-10-2) on 2010-03-28.

- 24. Cao, Huai-Dong; Znu, Xi-Ping (December 3, 2006). "Hamilton-Pereiman's Proof of the Poincare Conjecture and the Geometrization Conjecture". arXiv:math.DG/0612069 (https://arxiv.org/abs/math.DG/0612069).
- 25. John W. Morgan, Gang Tian Ricci Flow and the Poincaré Conjecture arXiv:math/0607607 (https://arxiv.org/abs/math/0607607)
- 26. "Schedule of the scientific program of the ICM 2006" (https://web.archive.org/web/20100211112009/http://icm2006.org/v\_f/web\_fr.php). Icm2006.org. Archived from the original (http://icm2006.org/v\_f/web\_fr.php) on February 11, 2010. Retrieved March 21, 2010.
- 27. John W. Morgan, Gang Tian Completion of the Proof of the Geometrization Conjecture arXiv: 0809.4040 (https://arxiv.org/abs/0809.4040)
- 28. "Maths genius urged to take prize" (http://news.bbc.co.uk/2/hi/europe/8585407.stm). BBC News. March 24, 2010. Archived (https://web.archive.org/web/20100419061533/http://news.bbc.co.uk/2/hi/europe/8585407.stm) from the original on April 19, 2010. Retrieved March 25, 2010.
- 29. "Fields Medal Grigory Perelman" (http://www.icm2006.org/dailynews/fields\_perelman\_info\_en.pdf) (PDF). International Congress of Mathematicians 2006. August 22, 2006.
- 30. Mullins.
- 31. "Prize for Resolution of the Poincaré Conjecture Awarded to Dr. Grigoriy Perelman" (http://www.claymath.org/sites/default/files/millenniumprizefull.pdf) (PDF) (Press release). Clay Mathematics Institute. March 18, 2010. Retrieved May 1, 2014. "The Clay Mathematics Institute (CMI) announces today that Dr. Grigoriy Perelman of St. Petersburg, Russia, is the recipient of the Millennium Prize for resolution of the Poincaré conjecture."
- 32. "Russian math genius ignores \$1 million Millennium Prize" (http://en.rian.ru/strange/20100608/159350481.html). RIA Novosti. July 8, 2010. Archived (https://web.archive.org/web/20100611164530/http://en.rian.ru/strange/20100608/159350481.html) from the original on June 11, 2010. Retrieved July 8, 2010.
- 33. "Poincaré Chair" (http://www.claymath.org/events/news/poincar%C3%A9-chair). Clay Institute. March 4, 2014.
- 34. Masha Gessen (2009, p. 185)
- 35. Главные новости (http://top.rbc.ru/society/22/08/2006/94703.shtml) (in Russian). RBC Information Systems. August 22, 2006.

  Archived (https://web.archive.org/web/20110716055141/http://top.rbc.ru/society/22/08/2006/94703.shtml) from the original on July 16, 2011. Retrieved March 21, 2010.
- 36. Nasar, Sylvia; Gruber, David (August 21, 2006). "Manifold Destiny: A legendary problem and the battle over who solved it" (http://www.newyorker.com/archive/2006/08/28/060828fa\_fact2?currentPage=11). *The New Yorker*. p. 11. Archived (https://web.archive.org/web/20121018065507/http://www.newyorker.com/archive/2006/08/28/060828fa\_fact2?currentPage=11) from the original on October 18, 2012. Retrieved January 21, 2011.
- 37. "Le génie qui s'est retiré du monde" (http://www.lepoint.fr/monde/le-genie-qui-s-est-retire-du-monde-30-09-2010-1246189\_24.php) [The genius who has withdrawn from the world]. *Le Point* (in French). September 30, 2010. pp. 74–77. Archived (https://web.archive.org/web/20120721073747/http://www.lepoint.fr/monde/le-genie-qui-s-est-retire-du-monde-30-09-2010-1246189\_24.php) from the original on July 21, 2012. Retrieved October 15, 2010.
- 38. "Komsomolskaya Pravda" found out where Perelman disappears (https://www.kp.ru/daily/26260.3/3138310) ANNA VELIGZHANINA

- 39. Nikolai Gerasimov (March 27, 2011). Чтобы купить русского хлеба, Перельман пешком ходил через весь Нью-Иорк (http://kp.ru/daily/25658/821159/) [To buy Russian bread, Perelman walked through the whole New York]. Komsomolskaya Pravda (in Russian).

  Archived (https://web.archive.org/web/20120917112720/http://kp.ru/daily/25658/821159/) from the original on September 17, 2012.

  Retrieved December 25, 2012.
- 40. Anna Veligzhanina (April 28, 2011). Интервью с математиком Григорием Перельманом: Зачем мне миллион долларов? Я могу управлять Вселенной (http://kp.ru/daily/25677.3/836229/) [Interview with mathematician Grigori Perelman: Why do I need million dollars? I can control the world]. Komsomolskaya Pravda (in Russian). Archived (https://web.archive.org/web/20121227090706/http://kp.ru/daily/25677.3/836229/) from the original on December 27, 2012. Retrieved December 25, 2012.
- 41. "Russian math genius answers \$1 million question" (http://en.rian.ru/russia/20110429/163769206.html). RIA Novosti. April 29, 2011. Retrieved December 25, 2012.
- 42. Masha Gessen (April 29, 2011). "6 странных ошибок в "интервью Перельмана" " (http://www.snob.ru/selected/entry/34911). Snob.ru. Archived (https://web.archive.org/web/20121017224115/http://www.snob.ru/selected/entry/34911) from the original on October 17, 2012. Retrieved May 8, 2012.
- 43. "Интервью Перельмана подделка?" (http://www.versii.com/news/231050/) [Interview with Perelman fake?]. Versii. May 5, 2011. Archived (https://web.archive.org/web/20121226235256/http://www.versii.com/news/231050/) from the original on December 26, 2012. Retrieved December 25, 2012.
- 44. "Grigori Perelman's interview full of mismatches" (http://english.pravda.ru/society/stories/06-05-2011/117816-grigori\_perelman-0/). English Pravda.ru. June 5, 2011. Archived (https://web.archive.org/web/20130122115715/http://english.pravda.ru/society/stories/06-05-2011/117816-grigori\_perelman-0/) from the original on January 22, 2013. Retrieved December 25, 2012.
- 45. "Articles » Shattered Genius" (http://brettforrest.com/shattered-genius/). Brett Forrest. Retrieved December 25, 2012.
- 46. "Seven of the week's best reads" (https://www.bbc.co.uk/news/magazine-19439860). BBC News. September 1, 2012. Archived (https://web.archive.org/web/20130308151452/http://www.bbc.co.uk/news/magazine-19439860) from the original on March 8, 2013. Retrieved December 25, 2012.
- 47. Luke Harding (23 March 2010). "Grigory Perelman, the maths genius who said no to \$1m" (https://www.theguardian.com/world/2010/ma r/23/grigory-perelman-rejects-1m-dollars). *The Guardian*.

### References

- Gessen, Masha (2009). Perfect Rigor: A Genius and the Mathematical Breakthrough of the Century (https://archive.org/details/perfectrig orgeni00gess). Boston, Massachusetts: Houghton Mifflin Harcourt. ISBN 978-0151014064.
- Anderson, M.T. 2005. Singularities of the Ricci flow (http://www.math.sunysb.edu/%7Eanderson/papers.html). Encyclopedia of Mathematical Physics, Elsevier. (Comprehensive exposition of Perelman's insights that lead to complete classification of 3-manifolds)
- The Associated Press, "Russian may have solved great math mystery" (http://www.cnn.com/2004/US/West/01/07/math.mystery.ap/index.html). CNN. July 1, 2004. Archived (https://web.archive.org/web/20060813185225/http://www.cnn.com/2004/US/West/01/07/math.mystery.ap/index.html) from the original on August 13, 2006. Retrieved August 15, 2006.

tory.ap/inaon.numij nom the original on August 10, 2000. Hethered August 10, 2000.

- Cao, Huai-Dong; Zhu, Xi-Ping (June 2006). "A Complete Proof of the Poincaré and Geometrization Conjectures application of the Hamilton-Perelman theory of the Ricci flow" (https://web.archive.org/web/20120514194949/http://www.intlpress.com/AJM/p/2006/10\_2/AJM-10-2-165-492.pdf) (PDF). Asian Journal of Mathematics. 10 (2). Archived from the original (http://www.intlpress.com/AJM/p/2006/10\_2/AJM-10-2-165-492.pdf) (PDF) on May 14, 2012. Erratum (https://web.archive.org/web/20120514194801/http://www.intlpress.com/AJM/p/2006/10\_2/AJM-10-2-Erratum.pdf). Revised version (December 2006): Hamilton-Perelman's Proof of the Poincaré Conjecture and the Geometrization Conjecture (https://arxiv.org/abs/math.DG/0612069)
- Collins, Graham P. (2004). "The Shapes of Space". <u>Scientific American</u>. **291** (July): 94–103. <u>Bibcode</u>: <u>2004SciAm.291a..94C</u> (https://ui.a dsabs.harvard.edu/abs/2004SciAm.291a..94C). doi: 10.1038/scientificamerican0704-94 (https://doi.org/10.1038%2Fscientificamerican0704-94). PMID 15255593 (https://pubmed.ncbi.nlm.nih.gov/15255593).
- Jackson, Allyn (September 2006). "Conjectures No More? Consensus Forming on the Proof of the Poincaré and Geometrization Conjectures" (http://www.ams.org/notices/200608/comm-perelman.pdf) (PDF). Notices of the AMS.
- Kleiner, Bruce; Lott, John (2008). "Notes on Perelman's papers". Geometry & Topology. 12 (5): 2587–2855. arXiv:math.DG/0605667 (https://arxiv.org/abs/math.DG/0605667). doi:10.2140/gt.2008.12.2587 (https://doi.org/10.2140%2Fgt.2008.12.2587).
- Kusner, Rob. "Witnesses to Mathematical History Ricci Flow and Geometry" (http://www.gang.umass.edu/~kusner/other/new-perelman. pdf) (PDF). Retrieved August 22, 2006. (an account of Perelman's talk on his proof at MIT; pdf file; also see Sugaku Seminar 2003-10 pp 4–7 for an extended version in Japanese)
- Lobastova, Nadejda; Hirst, Michael (August 20, 2006). "World's top maths genius jobless and living with mother" (https://www.telegraph.co.uk/news/1526782/Worlds-top-maths-genius-jobless-and-living-with-mother.html). The Daily Telegraph. Archived (https://web.archive.org/web/20140608030622/http://www.telegraph.co.uk/news/1526782/Worlds-top-maths-genius-jobless-and-living-with-mother.html) from the original on June 8, 2014. Retrieved May 10, 2014.
- Morgan, John W.; Gang Tian (July 25, 2006). "Ricci Flow and the Poincaré Conjecture". arXiv:math.DG/0607607 (https://arxiv.org/abs/math.DG/0607607).
- Mullins, Justin (22 August 2006). "Prestigious Fields Medals for mathematics awarded" (https://www.newscientist.com/article/dn9813.ht ml). New Scientist.
- Overbye, Dennis (August 15, 2006). "An Elusive Proof and Its Elusive Prover" (https://www.nytimes.com/2006/08/15/science/15math.html). The New York Times. Retrieved August 15, 2006.
- Randerson, James (August 16, 2006). "Meet the cleverest man in the world (who's going to say no to a \$1m prize)" (https://www.theguardian.com/frontpage/story/0,,1851095,00.html). The Guardian. London.
- Robinson, Sara (April 15, 2003). "Russian Reports He Has Solved a Celebrated Math Problem" (http://www.msri.org/people/members/s ara/articles/perlman.html). The New York Times. Retrieved August 20, 2006.
- Schecter, Bruce (July 17, 2004). "Taming the fourth dimension". *New Scientist*. **183** (2456).
- Weeks, Jeffrey R. (2002). <u>The Shape of Space</u> (https://archive.org/details/shapeofspace0000week). New York: Marcel Dekker. <u>ISBN 0-8247-0709-5</u>. (The author is a former PhD student of Bill Thurston.)
- Weisstein Fric (Anril 15, 2004) "Poincaré Conjecture Proved--This Time for Real" (http://mathworld.wolfram.com/news/2003-04-15/noi

ncare/). *Mathworld*. Retrieved August 22, 2006.

## **Further reading**

Gessen, Masha (2009). Perfect Rigor: A Genius and the Mathematical Breakthrough of the Century (https://archive.org/details/perfectrig orgeni00gess). Houghton Mifflin Harcourt. ISBN 978-0-15-101406-4. Retrieved December 12, 2012. (Story of Grigory Perelman based on information from people who interacted with him.)

### **External links**

- O'Connor, John J.; Robertson, Edmund F., "Grigori Perelman" (http://www-history.mcs.st-andrews.ac.uk/Biographies/Perelman.html),
   MacTutor History of Mathematics archive, University of St Andrews.
- Grigori Perelman (https://www.genealogy.math.ndsu.nodak.edu/id.php?id=84354) at the Mathematics Genealogy Project
- Grigori Perelman's results (https://www.imo-official.org/participant\_r.aspx?id=10481) at International Mathematical Olympiad

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