

(a) (i) I use a iteration when y's value equals 1 I give the color "red", else give the color "green", and I set the x axis as 'x_1', set the y axis as 'x_2', because on the plot the x-axis is the value of parameter 'x1', the y-axis is the value of the second parameter 'x1', and the parameter of 'str' is the title of the plot. Since I have to plot many times using the same pattern, so I define a plot function in the "funcfile.py" :

```
def scattersth(x1, x2, y, str):  
    for i in range(len(x1)):  
        if y[i] == 1:  
            plt.scatter(x1[i], x2[i], color='red', s=5)  
        else:  
            plt.scatter(x1[i], x2[i], color='green', s=5)  
    plt.xlabel('x_1')  
    plt.ylabel('x_2')  
    plt.title(str)  
  
plt.subplot(331)  
scattersth(x1, x2, y, "original data")
```

And just call it to plot the original data, and the subplot means this is the first image of 3*3=9 (all images), because I have many plots, this helps to see clearly:

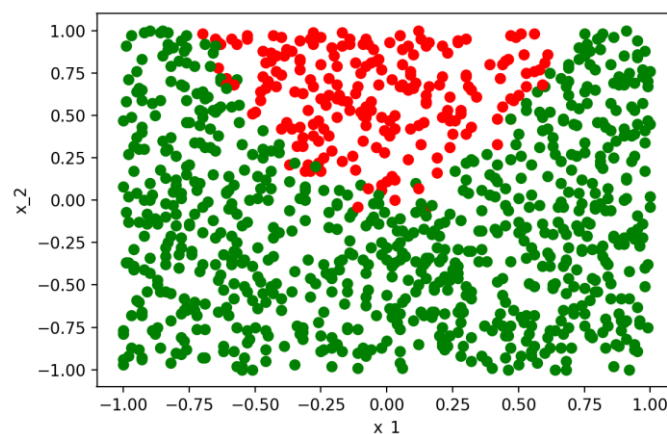


Figure 1: the original data, as we can see from the plot the red points mean the value of y is 1, green ones mean -1, we can see clearly there's a boundary of the two colors' points.

(ii)

```
#train the logistic regression classifier on the data
mul_lr = linear_model.LogisticRegression()
mul_lr.fit(x,y)
y_pre = mul_lr.predict(x)
print("linear_model.LogisticRegression :intercept {0}, slope {1} , cost {2}".format(mul_lr.intercept_, mul_lr.coef_,mul_lr.score
```

I use sklearn to train a logistic regression classifier on the data and the result is intercept : [-2.29502037], slope : [[-0.22934877 3.51212233]]

And the score of this model is 0.8268268268268268, which means this model's accuracy is 82.68% when predicts the data.

(iii)Because this requires different color with 2 datasets , so I define a function "scattersthoothercolor" to plot the two datasets and could clearly see the different y value of the original ones and the prediction ones . When y=1 plot red point , y=-1 plot the green point , y_pre=1 plot the yellow point , y_pre=-1 plot the black point , in case the overlap so I set the size of point of the prediction data 1 while the original data is 5 , then we can see clearly the yellow points with red circle are the data when y's value equals y_pre , the whole green points are the data when y's value is -1 while the y_pre is 1 ; the black points with red circle is when y=1 and y_pre=-1 , the black points with green circle is when y=-1 and y_pre=-1.

```
def scattersthothcolor(x1, x2, y, y_pre, str):
    for i in range(len(x1)):
        if y[i] == 1:
            plt.scatter(x1[i], x2[i], color='red', s=5)
        if y_pre[i] == 1:
            plt.scatter(x1[i], x2[i], color='yellow', s=1)
        if y[i] == -1:
            plt.scatter(x1[i], x2[i], color='green', s=5)
        if y_pre[i] == -1:
            plt.scatter(x1[i], x2[i], color='black', s=1)
    plt.xlabel('x_1')
    plt.ylabel('x_2')
    plt.title(str)
```

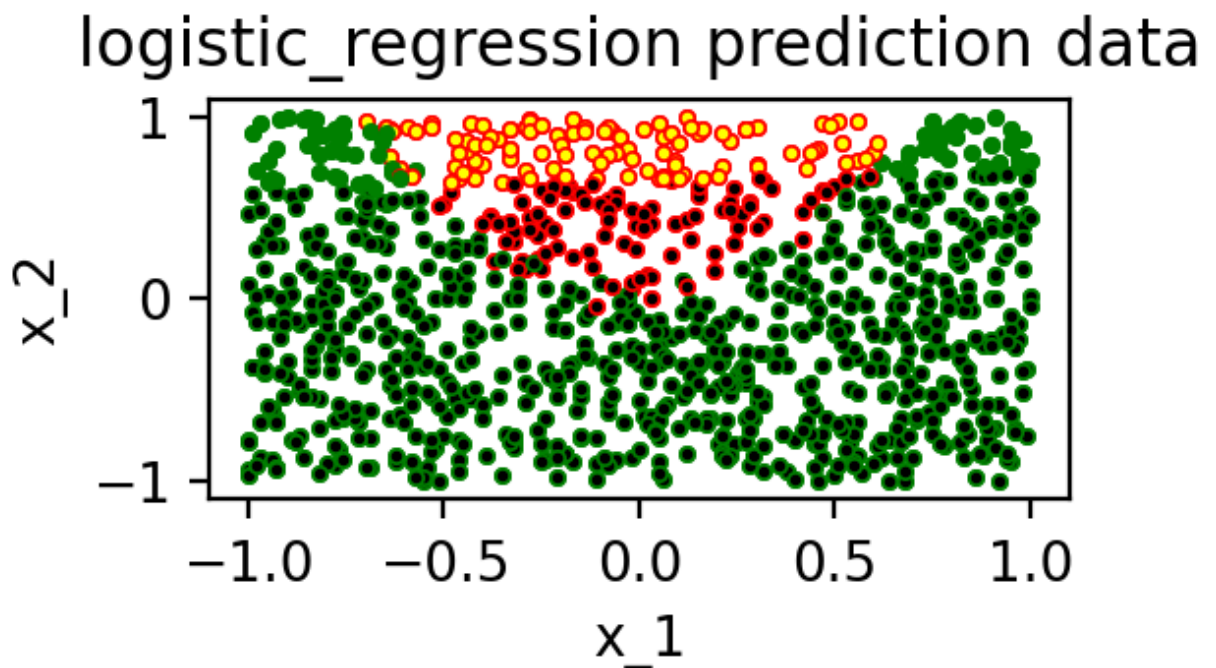


Figure 2 the prediction data with the original data

We usually use $w_1 x_1 + w_2 x_2 + b = 0$ to define

decision boundary, when $h_w(x) = w_1 x_1 + w_2 x_2 + b > 0$

we classify it to $y=1$, and the parameters b is the intercept and

$[w_1, w_2]$ =slop, so we can get the x_2 equals $-(w_1 x_1 + b)/w_2$, so I

define a function to draw the linear decision boundary in "funcfile.py", the parameter "intercept" is the b , the parameter "coef" is the array of $[w_1, w_2]$:

```
def plotsth(x, intercept, coef):  
    plt.plot(x, -(intercept+coef[0][0]*x)/coef[0][1], color='blue', label='decision boundary')  
    plt.legend()
```

So just recall it and the output image comes.

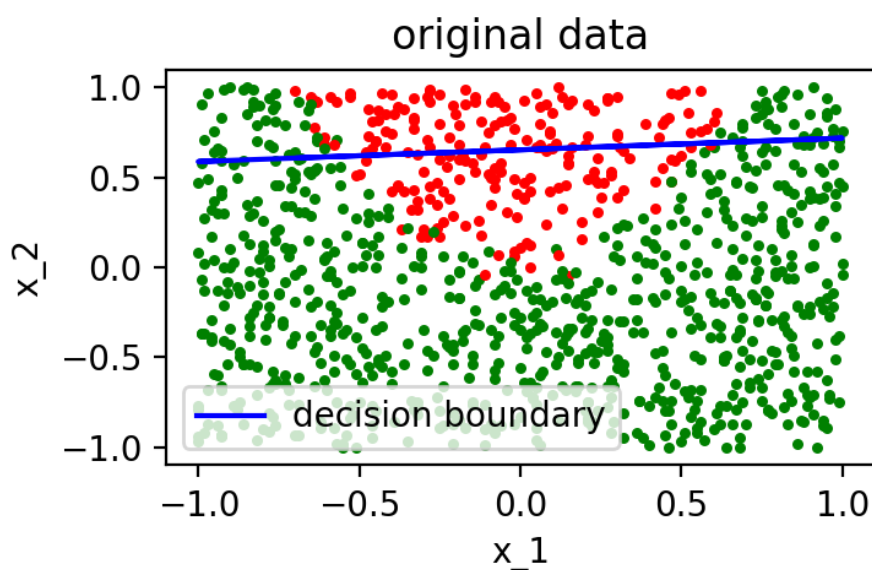


Figure 3: the decision boundary of the trained model in the original data

(iv) This prediction can't reflect the feature of all original data, I think it just return whichever class is the most likely, and the model can be improved to some extent, because the model is linear and through the plot of original data I think it's more like a curve using quadratic function to plot the decision boundary.

(b) (i) I pick 6 numbers of C to train the model, and print the parameters, after that predict the data then plot it, using the

"add_subplot" function.

```
fig2 = plt.figure()
svc_c = [0.001, 1, 10, 100, 500, 1000]
for i in range(6):
    linear_svc_model = LinearSVC(C=svc_c[i]).fit(x, y)
    print("linear_svc_model{0} :when C={1},intercept {2}, slope {3} ,score {4}".format(i+1,svc_c[i], linear_svc_model.intercept_,
                                                                                      linear_svc_model.coef_, linear_svc_model.score(x,y)))
    y_svc_pre = linear_svc_model.predict(x)
    linear_svc_model_subplot = fig2.add_subplot(2, 3, i+1)
    scattersth(x1, x2, y_svc_pre, "predictiondata when c is {0}".format(svc_c[i]))
    plotsth(x1, linear_svc_model.intercept_, linear_svc_model.coef_)
plt.show()
```

I found when C is too small or too large , the score of the model would decrease.

linear_svc_model1 :when C=0.001,intercept [-0.38304573], slope [[-0.02813036 0.31868212]] ,score 0.78778778778777878

linear_svc_model2 :when C=1,intercept [-0.78348024], slope [[-0.08562309 1.2261786]] ,score 0.8248248248248248

linear_svc_model3 :when C=10,intercept [-0.78858122], slope [[-0.08627484 1.23652484]] ,score 0.8268268268268268

linear_svc_model4 :when C=100,intercept [-0.80587576], slope [[-0.05154838 1.24861954]] ,score 0.8288288288288288

linear_svc_model5 :when C=500,intercept [-0.85731115], slope [[0.21140994 1.02179456]] ,score 0.7977977977977978

linear_svc_model6 :when C=1000,intercept [-1.17827911], slope [[0.03957859 1.56852242]] ,score 0.8118118118118118

(ii)

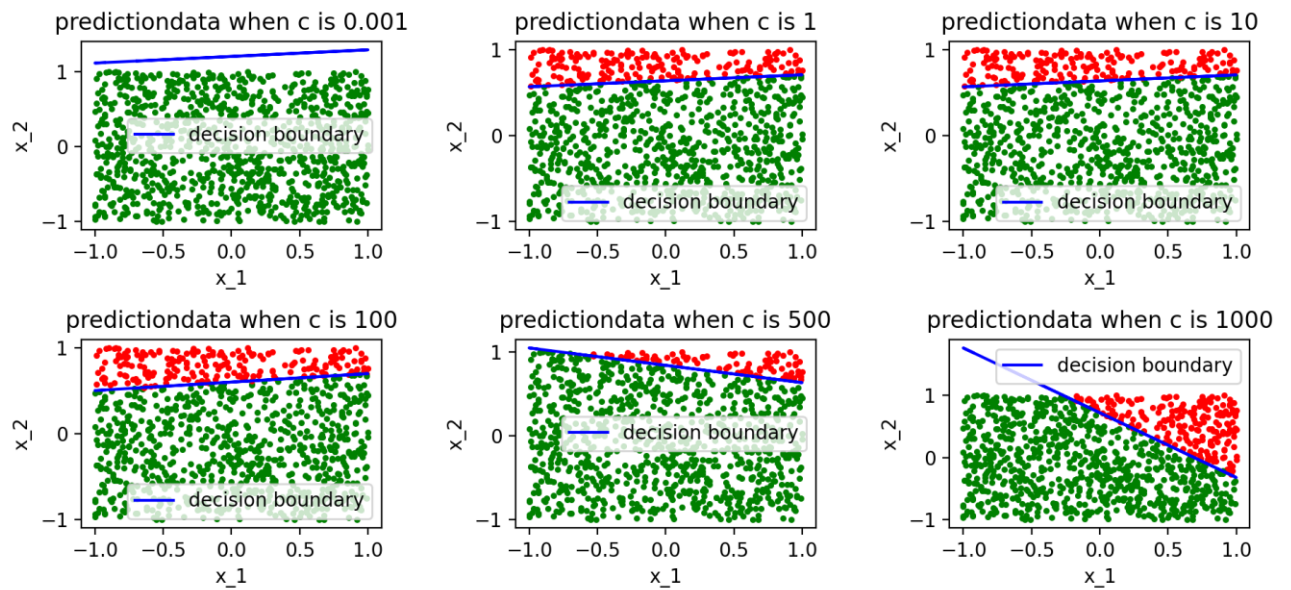


Figure 4 the prediction_data with different value of C

I find the if C is too small it's underfitting while too large is overfitting , and they are all linear prediction models. When the value of c limits to a range the prediction data doesn't vary so much , once out of that bound it varies much.

(iii) As we can see from the SVM cost function :

$$J(\theta) = \frac{1}{m} \sum_{i=1}^m \max(0, 1 - y^{(i)} \theta^T x^{(i)}) + \theta^T \theta / C$$

The less value of C , the model would be underfitting, the higher the value of C , the less the model is regularized , and the less important penalty is ,that means you can tolerate higher cost function values. If C is so big that the SVM predictions would be changing at each run time , because it is over-fitting which means it doesn't generalize well and doesn't predict well for data outside the training set.

(c)

(i) To get the parameter:

```
x_new = np.array(df.iloc[:, 0:4])
mul_lr1 = linear_model.LogisticRegression()
mul_lr1.fit(x_new, y)
print("new linear_model.LogisticRegression :intercept {0}, slope {1} ".format(mul_lr1.intercept_, mul_lr1.coef_))
```

(new linear_model.LogisticRegression)

intercept [-0.80227213]

slope [[-0.22141638 5.35919863 -8.05566943 -0.26219426]]

(ii) I use subplot function and recall the "scattersth" function to plot the two sets of data.

```
y_pre1 = mul_lr1.predict(x_new)
plt.subplot(121)
scattersth(x1, x2, y_pre1, "new linear_model.LogisticRegression")
plt.axhline(y=0, color='yellow', linestyle='--', label='baseline')
plt.legend()
plt.subplot(122)
scattersth(x1, x2, y, "original data")
plt.axhline(y=0, color='yellow', linestyle='--', label='baseline')
plt.legend()
```

When add two features the graph , as we can see from the baseline , the new model's prediction doesn't change much compared with the original data.

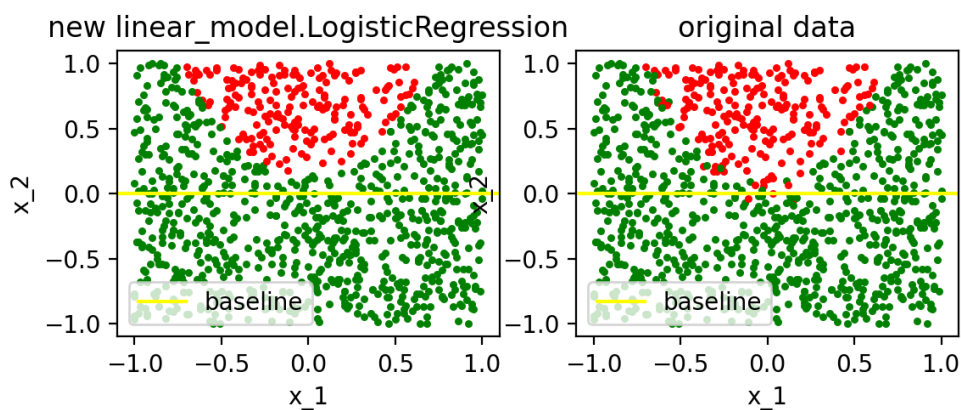


Figure 5 the new model and the original data with the y=0 baseline

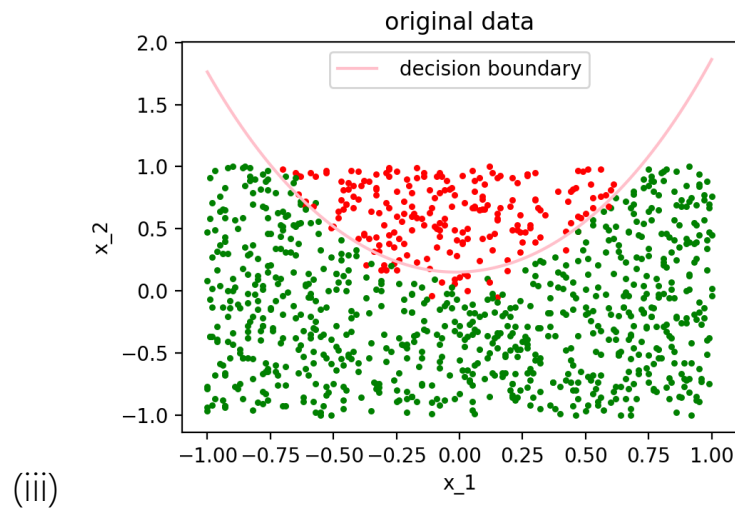


Figure 6 the decision boundary of the original data

I define each of the coefficient as a,b,c,d , and e is the intercept ,
then I apply the mathematic quadratic formula

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

,and in this case m is the c in the formula

because we can regard the x1 as constant to get the x2_new , and
then call the plot function.

```
a = mul_lr1.coef_[0][0]
b = mul_lr1.coef_[0][1]
c = mul_lr1.coef_[0][2]
d = mul_lr1.coef_[0][3]
e = mul_lr1.intercept_
m = e + a*x1_new + c*x1_new*x1_new
x2_new = (-b+(b*b-4*d*m)**0.5)/(2*d)
plt.plot(x1_new, x2_new, label=' decision boundary', color='pink')
scattersth(x1, x2, y, "original data")
plt.legend()
plt.show()
```

Appendix

week2.py

```
import numpy as np
import pandas as pd
from funcfile import *
from sklearn import linear_model
from sklearn.svm import LinearSVC
```



```

from sklearn.pipeline import Pipeline
from sklearn.preprocessing import PolynomialFeatures

#read data
df = pd.read_csv("week2.csv",comment="#")
print(df.head())

x = np.array(df.iloc[:, 0:2])#read the first two columns as array
y = np.array(df.iloc[:, 4])#read the y value

#train the logistic regression classifier on the data
mul_lr = linear_model.LogisticRegression()
mul_lr.fit(x,y)
y_pre = mul_lr.predict(x)
print("linear_model.LogisticRegression :intercept {0}, slope {1} ,
score {2}".format(mul_lr.intercept_, mul_lr.coef_,mul_lr.score(x,y)))

x1 = x[:, 0]
x2 = x[:, 1]

plt.subplot(331)
scattersth(x1, x2, y, "original data")
plotsth(x1, mul_lr.intercept_, mul_lr.coef_)

plt.subplot(332)
plt.plot()
scattersthothercolor(x1, x2, y,y_pre, "logistic_regression prediction
data")
plt.show()
#pick 6 numbers of C to train the model , and print the parameters,
#after that predict the data then plot it , using the "add_subplot"
function
fig2 = plt.figure()
svc_c = [0.001,1,10,100,500,1000]
for i in range(6):
    linear_svc_model = LinearSVC(C=svc_c[i]).fit(x, y)
    print("linear_svc_model{0} :when C={1},intercept {2}, slope
{3} ,score {4}".format(i+1,svc_c[i], linear_svc_model.intercept_,
linear_svc_model.coef_, linear_svc_model.score(x,y)))
    y_svc_pre = linear_svc_model.predict(x)
    linear_svc_model_subplot = fig2.add_subplot(2, 3, i+1)
    scattersth(x1, x2, y_svc_pre, "predictiondata when c is
{0}".format(svc_c[i]))

```

```

    plotsth(x1, linear_svc_model.intercept_, linear_svc_model.coef_)

plt.show()

# (c)
x_new = np.array(df.iloc[:, 0:4])
mul_lr1 = linear_model.LogisticRegression()
mul_lr1.fit(x_new, y)
print("new linear_model.LogisticRegression :intercept {0}, slope {1}
".format(mul_lr1.intercept_, mul_lr1.coef_))
y_pre1 = mul_lr1.predict(x_new)
plt.subplot(121)
scattersth(x1, x2, y_pre1, "new linear_model.LogisticRegression")
plt.axhline(y=0, color='yellow', linestyle='-' , label = 'baseline')
plt.legend()
plt.subplot(122)
scattersth(x1, x2, y, "original data")
plt.axhline(y=0, color='yellow', linestyle='-' , label = 'baseline')
plt.legend()
"""define each of the coefficient as a,b,c,d , and e is the
intercept , then I apply the mathematic quadratic formula """
x1_new = np.linspace(-1, 1, 9999)#to get the axis of x
a = mul_lr1.coef_[0][0]
b = mul_lr1.coef_[0][1]
c = mul_lr1.coef_[0][2]
d = mul_lr1.coef_[0][3]
e = mul_lr1.intercept_
m = e + a*x1_new + c*x1_new*x1_new
x2_new = (-b+(b*b-4*d*m)**0.5)/(2*d)
plt.plot(x1_new, x2_new, label=' decision boundary', color='pink')
scattersth(x1, x2, y, "original data")
plt.legend()
plt.show()

```

"funcfile.py"

```

import matplotlib.pyplot as plt
import sympy as sp

#plot the data
"""when y's value equals 1 color is "red" ,else "green", and set the
x axis as 'x_1' ,
set the y axis as 'x_2' , because on the plot the x-axis is the value
of parameter 'x1 ',

```

```

the y-axis is the value of the second parameter 'x1' , and the
parameter of 'str' is
the title of the plot"""
def scattersth(x1, x2, y, str):
    for i in range(len(x1)):
        if y[i] == 1:
            plt.scatter(x1[i], x2[i], color='red', s=5)
        else:
            plt.scatter(x1[i], x2[i], color='green', s=5)
    plt.xlabel('x_1')
    plt.ylabel('x_2')
    plt.title(str)

""" plot the two datasets and could clearly see the different y value
of the original ones and the prediction ones"""
def scattersthothecolor(x1, x2, y, y_pre , str):
    for i in range(len(x1)):
        if y[i] == 1 :
            plt.scatter(x1[i], x2[i], color='red', s=5)
        if y_pre[i] == 1:
            plt.scatter(x1[i], x2[i], color='yellow', s=1)
        if y[i] == -1:
            plt.scatter(x1[i], x2[i], color='green', s=5)
        if y_pre[i] == -1 :
            plt.scatter(x1[i], x2[i], color='black', s=1)
    plt.xlabel('x_1')
    plt.ylabel('x_2')
    plt.title(str)

"""plot the line with intercept and coef"""
def plotsth(x, intercept, coef):
    plt.plot(x, -(intercept+coef[0][0]*x)/coef[0][1], color='blue',
label='decision boundary')
    plt.legend()

```