

```

1 # univariate normal
2 Normal(loc=0.0, scale=1.0)
3 # vector of 5 univariate normals
4 Normal(loc=tf.zeros(5), scale=tf.ones(5))
5 # 2 x 3 matrix of Exponentials
6 Exponential(rate=tf.ones([2, 3]))

```

Figure 1

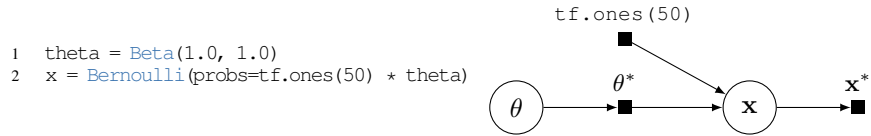


Figure 2

```

1 X = tf.placeholder(tf.float32, [N, D])
2 f = MultivariateNormalTriL(loc=tf.zeros(N),
3                             scale_tril=tf.cholesky(rbf(X)))
4 y = Bernoulli(logits=f)

```

Figure 3

```

1 X = Normal(loc=tf.zeros([N, Q]), scale=tf.ones([N, Q]))
2 f = MultivariateNormalTriL(loc=tf.zeros([N, D]),
3                             scale_tril=tf.cholesky(rbf(X)))
4 y = Bernoulli(logits=f)

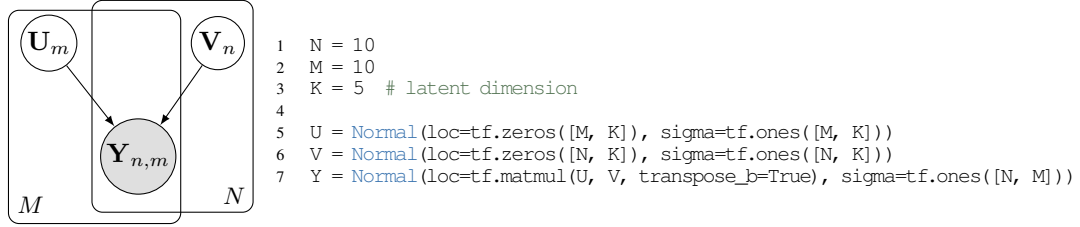
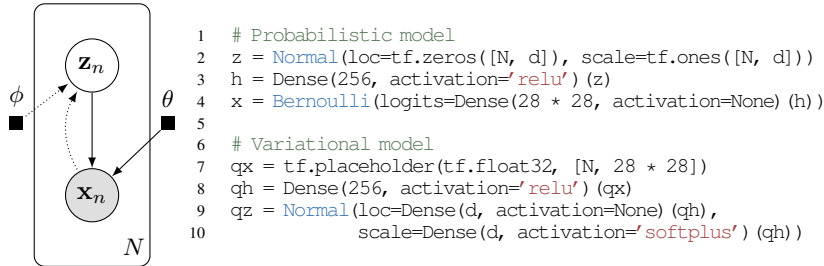
```

Figure 4

```

1 X = Normal(loc=tf.zeros([N, Q]), scale=tf.ones([N, Q]))
2 h1 = MultivariateNormalTriL(loc=tf.zeros([N, H1]),
3                              scale_tril=tf.cholesky(rbf(X)))
4 h2 = MultivariateNormalTriL(loc=tf.zeros([N, H2]),
5                              scale_tril=tf.cholesky(rbf(h1)))
6 f = MultivariateNormalTriL(loc=tf.zeros([N, D]),
7                              scale_tril=tf.cholesky(rbf(h2)))
8 y = Bernoulli(logits=f)

```

Figure 5**Figure 6****Figure 7**

Inference method	Neg. log-likelihood
VAE [Kingma & Welling 2014]	≤ 88.2
VAE without analytic KL	≤ 89.4
VAE with analytic entropy	≤ 88.1
VAE with score function gradient	≤ 87.9
Normalizing flows [Rezende & Mohamed 2015]	≤ 85.8
Hierarchical variational model [Ranganath+ 2016]	≤ 85.4
Importance-weighted auto-encoders ($K = 50$) [Burda+ 2016]	≤ 86.3
HVM with IWAE objective ($K = 5$)	≤ 85.2
Rényi divergence ($\alpha = -1$) [Li & Turner 2016]	≤ 140.5

Table 1

```

1 N = 1000 # number of data points
2 d = 10 # latent dimensionality
3
4 # DATA
5 x_data = np.loadtxt('mnist.txt', np.float32)
6
7 # MODEL
8 z = Normal(loc=tf.zeros([N, d]), scale=tf.ones([N, d]))
9 h = Dense(256, activation='relu')(z)
10 x = Bernoulli(logits=Dense(28 * 28, activation=None)(h))
11
12 # INFERENCE
13 qx = tf.placeholder(tf.float32, [N, 28 * 28])
14 qh = Dense(256, activation='relu')(qx)
15 qz = Normal(loc=Dense(d, activation=None)(qh),
16             scale=Dense(d, activation='softplus')(qh))
17
18 inference = ed.KLqp({z: qz}, data={x: x_data, qx: x_data})
19 inference.run()

```

```

1 N = 1000 # number of data points
2 d = 10 # latent dimensionality
3
4 # DATA
5 x_data = np.loadtxt('mnist.txt', np.float32)
6
7 # MODEL
8 z = Normal(loc=tf.zeros([N, d]), scale=tf.ones([N, d]))
9 h = Dense(256, activation='relu')(z)
10 x = Bernoulli(logits=Dense(28 * 28, activation=None)(h))
11
12 # INFERENCE
13 T = 10000 # number of samples
14 qz = Empirical(params=tf.Variable(tf.zeros([T, N, d])))
15
16 inference = ed.HMC({z: qz}, data={x: x_data})
17 inference.run()

```

Figure 8

```

1 inference = ed.Inference({beta: qbeta, z: qz}, data={x: x_train})

```

```

1 qbeta = Normal(loc=tf.Variable(tf.zeros([K, D])),
2               scale=tf.exp(tf.Variable(tf.zeros([K, D]))))
3 qz = Categorical(logits=tf.Variable(tf.zeros([N, K])))
4
5 inference = ed.VariationalInference({beta: qbeta, z: qz}, data={x: x_train})

```

```

1 T = 10000 # number of samples
2 qbeta = Empirical(params=tf.Variable(tf.zeros([T, K, D])))
3 qz = Empirical(params=tf.Variable(tf.zeros([T, N])))
4
5 inference = ed.MonteCarlo({beta: qbeta, z: qz}, data={x: x_train})

```

Figure 9

Probabilistic programming system	Runtime (s)
Handwritten NumPy (1 CPU)	534
Stan (1 CPU) [Carpenter+ 2016]	171
PyMC3 (12 CPU) [Salvatier+ 2015]	30.0
Edward (12 CPU)	8.2
Handwritten TensorFlow (GPU)	5.0
Edward (GPU)	4.9 (35x faster than Stan)

Table 2

```

1 def generative_network(eps):
2     h = Dense(256, activation='relu')(eps)
3     return Dense(28 * 28, activation=None)(h)
4
5 def discriminative_network(x):
6     h = Dense(28 * 28, activation='relu')(x)
7     return Dense(h, activation=None)(1)
8
9 # Probabilistic model
10 eps = Normal(loc=tf.zeros([N, d]), scale=tf.ones([N, d]))
11 x = generative_network(eps)
12
13 inference = ed.GANInference(data={x: x_train},
14                             discriminator=discriminative_network)
15 inference.run()

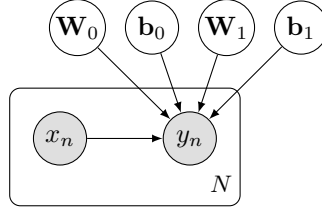
```

```

1 def generative_network(eps):
2     h = Dense(256, activation='relu')(eps)
3     return Dense(28 * 28, activation=None)(h)
4
5 def discriminative_network(x):
6     h = Dense(28 * 28, activation='relu')(x)
7     return Dense(h, activation=None)(1)
8
9 # Probabilistic model
10 eps = Normal(loc=tf.zeros([N, d]), scale=tf.ones([N, d]))
11 x = generative_network(eps)
12
13 inference = ed.WGANInference(data={x: x_train},
14                              discriminator=discriminative_network)
15 inference.run()

```

Figure 10

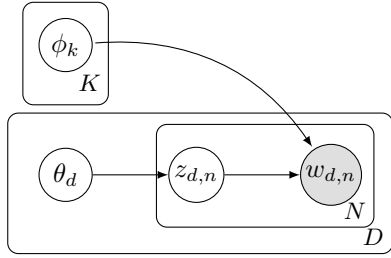


```

1 W_0 = Normal(loc=tf.zeros([D, H]), sigma=tf.ones([D, H]))
2 W_1 = Normal(loc=tf.zeros([H, 1]), sigma=tf.ones([H, 1]))
3 b_0 = Normal(loc=tf.zeros(H), sigma=tf.ones(H))
4 b_1 = Normal(loc=tf.zeros(1), sigma=tf.ones(1))
5
6 x = tf.placeholder(tf.float32, [N, D])
7 y = Bernoulli(logits=tf.matmul(tf.nn.tanh(tf.matmul(x, W_0) + b_0), W_1) + b_1)

```

Figure 11



```

1 D = 4 # number of documents
2 N = [11502, 213, 1523, 1351] # words per doc
3 K = 10 # number of topics
4 V = 100000 # vocabulary size
5
6 theta = Dirichlet(alpha=tf.zeros([D, K]) + 0.1)
7 phi = Dirichlet(alpha=tf.zeros([K, V]) + 0.05)
8 z = [[0] * N] * D
9 w = [[0] * N] * D
10 for d in range(D):
11     for n in range(N[d]):
12         z[d][n] = Categorical(pi=theta[d, :])
13         w[d][n] = Categorical(pi=phi[z[d][n], :])

```

Figure 12

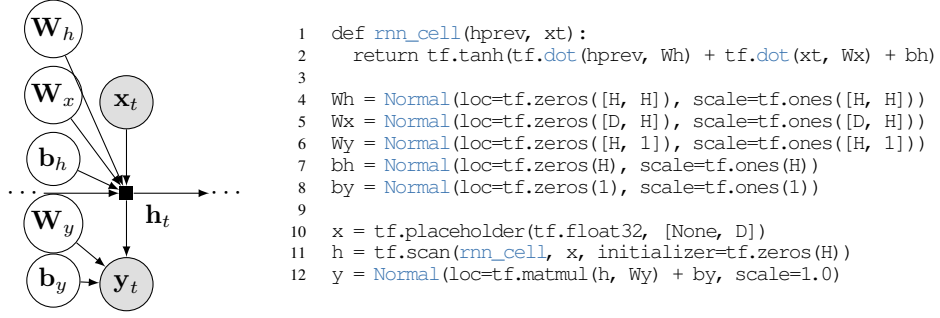


Figure 13

```

1 qbeta = PointMass(params=tf.Variable(tf.zeros([K, D])))
2 qz = Categorical(logits=tf.Variable(tf.zeros([N, K])))
3
4 inference_e = ed.VariationalInference({z: qz}, data={x: x_train, beta: qbeta})
5 inference_m = ed.MAP({beta: qbeta}, data={x: x_train, z: qz})
6 ...
7 for _ in range(10000):
8     inference_e.update()
9     inference_m.update()

```

Figure 14

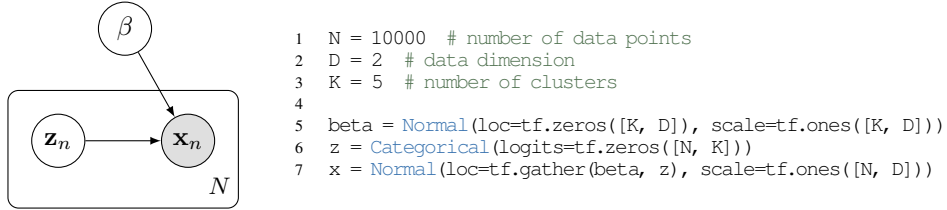


Figure 15

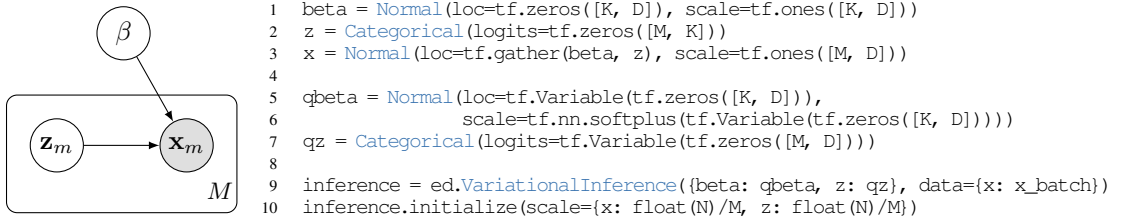


Figure 16

```
1 loc = DirichletProcess(0.1, Normal(tf.zeros(D), tf.ones(D)), sample_shape=N)
2 x = Normal(loc=loc, scale=tf.ones([N, D]))

1 def dirichlet_process(alpha):
2     def cond(k, beta_k):
3         flip = Bernoulli(p=beta_k)
4         return tf.equal(flip, tf.constant(1))
5
6     def body(k, beta_k):
7         beta_k = beta_k * Beta(a=1.0, b=alpha)
8         return k + 1, beta_k
9
10    k = tf.constant(0)
11    beta_k = Beta(a=1.0, b=alpha)
12    stick_num, stick_beta = tf.while_loop(cond, body, loop_vars=[k, beta_k])
13    return stick_num
```

Figure 17