

Homework #2:

Integrations

Set-up

As you learned in electrodynamics (well...and Physics 2) the electric potential of some charge distribution $\rho(\vec{r}')$ is a scalar quantity given by the integral

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \int \frac{\rho(\vec{r}')}{(|\vec{r} - \vec{r}'|)} d^3\vec{r}', \quad (1)$$

where \vec{r}' is the position of the charge distribution and \vec{r} is the position at which you are calculating the potential. The difficult part of this problem involved expressing the charge density $\rho(\vec{r}')$ correctly and evaluating that integral. Luckily, you now have a computer to do the hard part, leaving you another hard part - coding it. From this expression, you could then find the electric field at any point \vec{r} by taking the gradient of the potential,

$$\vec{E}(\vec{r}) = -\vec{\nabla}V(\vec{r}) \quad (2)$$

Consider 3 charge distributions: a 1D case and two 2D cases. First, a charged line,

$$\lambda(x) = 2x, \quad 0 < x < 1. \quad (3)$$

Second, a charged 'L' made from two charged lines - one parallel to the x axis and the other parallel to the y axis

$$\begin{aligned} \lambda(x, y) &= x^2, \quad 0 < x < 1 \\ &= y, \quad 1 < y < 2. \end{aligned} \quad (4)$$

Third, a charge disk in the x - y plane, centered at the origin plane with a radius of 2 and a charge distribution of

$$\sigma(r, \phi) = r \cos(\phi) \quad (5)$$

Goal

Write a program in Python and MATLAB to calculate the (i) electric potential and (ii) electric field in the vicinity of each charge distribution. Graph the electric potential and electric field (try a 3D plot for the field).