

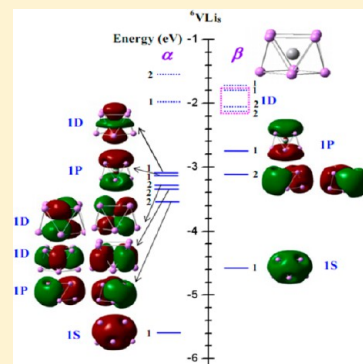
# Magnetic Superatoms in $\text{VLi}_n$ ( $n = 1-13$ ) Clusters: A First-Principles Prediction

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**ABSTRACT:** We demonstrated a first-principles investigation to search for magnetic superatoms in the vanadium-doped lithium clusters  $\text{VLi}_n$  ( $n = 1-13$ ). The stabilities of  $\text{VLi}_n$  clusters were determined through geometrical and electronic optimizations. It is found that the growth pattern of  $\text{VLi}_n$  in 3-space follows adding a Li atom capped on  $\text{VLi}_{n-1}$  clusters. All doped clusters show larger relative binding energies compared with pure  $\text{Li}_{n+1}$  partners and display tunable magnetic properties. When  $n = 8-13$ , the  $\text{VLi}_n$  clusters adopt a cage-like structure with an endohedral V atom and are identified as superatoms with their magnetic moments successively decreasing from 5 to 0  $\mu_B$ . The isolated  $\text{VLi}_8$  superatom is emphasized due to its robust magnetic moment as well as high structural and chemical stability analogue of a single  $\text{Mn}^{2+}$  ion. Molecular orbitals analysis shows that  $\text{VLi}_8$  has an electronic configuration of  $1\text{S}^2 1\text{P}^6 1\text{D}^5$ , exhibiting Hund's filling rule of maximizing the spin-like atoms. Electronic shell structures of  $1\text{S}^2$  and  $1\text{P}^6$  are virtually unchanged in  $\text{Li}_9$  cluster as the V atom substitutes for the embedded Li atom, indicating that the electron-shell-closing model is valid for explaining its structures and stabilities. The results show that the tailored magnetic building blocks for nanomaterials can be formed by seeding magnetic dopants into alkali metal cluster cages.



## 1. INTRODUCTION

Since the pioneering finding of the celebrated  $\text{C}_{60}$ ,<sup>1</sup> one of the major goals of cluster science has been dedicated to discovering highly stable clusters with unique properties for the purpose of building blocks in novel nanomaterials. Metal clusters often show different physical and chemical properties from their bulk counterparts yet drawing tremendous attention due to their unique optical properties, magnetic properties, as well as catalytic reactivities.<sup>2-4</sup> Particularly, newly developed cluster superatoms consisting of specific atoms that share electrons but mimicking chemical behaviors of other elements have been studied extensively in recent years.<sup>5-13</sup> Superatoms with unusual properties give a new perspective on the periodic table and provide an unprecedented ability to design novel materials. Bergeron et al. reported that  $\text{Al}_{13}$  and  $\text{Al}_{14}$  are halogen-like and alkaline-earth-like superatoms in the  $\text{Al}_{13}\text{I}_n^-$  ( $n = 1-12$ ) and  $\text{Al}_{14}\text{I}_n^-$  ( $n = 1-11$ ) complexes, respectively.<sup>14</sup> It was proposed later by Walter et al. that the superatom concept can also be extended to thiolate (RS)-coordinated gold clusters such as  $\text{Au}_{25}(\text{SR})_{18}^-$  and  $\text{Au}_{102}(\text{SR})_{44}^-$ .<sup>15</sup> The electronic shells in superatoms can be grouped into shells  $1\text{S}$ ,  $1\text{P}$ ,  $1\text{D}$ ,  $2\text{S}$ , ... by examining the nodal shapes of their molecular orbitals (MOs), much in the same way as that in atoms (s, p, d, f, ...), where the uppercase letters are used to distinguish them from atomic orbitals that are generally labeled by lowercase symbols.

Different from a single atom whose orbital fillings follow the Hund's rule, clusters can undergo atomic deformations to break degeneracy in electronic states through Jahn–Teller effects. Early studies of cluster superatoms were within the so-called

jellium sphere framework.<sup>16</sup> Collections of atoms in a compact spherical arrangement species consist of filled electronic shells, such as the cluster  $\text{Al}_{13}^-$  with the magic number of the 40 valence electrons.<sup>9</sup> All electrons in such stable electronic configurations are paired, resulting in nonmagnetism of the superatoms. In 2009, Khanna and co-workers reported that encapsulating a vanadium atom into a cage of eight cesium atoms could create a stable supershell of electrons and prevent the vanadium atom's unpaired electrons from reacting with other atoms and maintain its magnetism. The  $\text{VCs}_8$  cluster has a magnetic moment of 5  $\mu_B$ , the same as a manganese atom.<sup>17</sup> Khanna et al. pointed out that one way to stabilize magnetic superatoms is to introduce an additional transition metal (TM) atom, which can breed magnetism through its specific orbital configuration that hybridizes with the superatom and stabilizes the magnetic state. Later, they extended their investigations to other alkali metals and alkaline earth metal systems doped with 3d TM dopants. The bimetallic clusters  $\text{VNa}_8$ ,  $\text{FeCa}_8$ ,  $\text{CrSr}_9$ ,  $\text{MnCa}_9$ ,  $\text{ScNa}_{12}$ ,  $\text{ScK}_{12}$ , and  $\text{ScCs}_{12}$  are also considered magnetic superatoms with large spin.<sup>18-22</sup> This research opened a new path of infusing magnetic character in otherwise nonmagnetic elements through controlled association with a single magnetic atom.

Lithium is the first alkali metal that can be considered as an ideal prototype for simple metals and presents a good starting

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**Table 1.** Calculated Bond Distance  $d$  (Å), Vibrational Frequency  $\omega_e$  ( $\text{cm}^{-1}$ ), Average Binding Energies Per Atom  $E_b$  (eV), and Ionization Potential IP (eV) of the  $\text{Li}_2$ ,  $\text{Li}_2^-$ , and  $\text{Li}_3$  Clusters Optimized Using Different Density Functional Methods

methods	$\text{Li}_2$				$\text{Li}_2^-$		$\text{Li}_3$
	$d$	$\omega_e$	$E_b$	IP	$d$	$\omega_e$	IP
BP	2.74	432	0.40	4.93	3.12	276.9	4.05
BLYP	2.70	333.6	0.47	4.99	3.14	244.7	3.88
PBE	2.70	306.2	0.46	5.03	3.10	282.8	4.06
PW91	2.70	332	0.48	5.12	3.09	275.9	4.09
expt. <sup>23–26</sup>	2.67	351.4	0.52	5.14	$3.09 \pm 0.015$	$232 \pm 35$	4.08

point for theoretical understanding of metal clusters. Moreover, lithium has received intense research interest due to its high power and capacity for rechargeable lithium batteries and high capacity for hydrogen storage in lithium materials. Lithium and lithium-based clusters continue to attract attention because of their interesting physical and chemical properties. During the past 2 decades, pure lithium clusters in the small size range have been assigned through experimental<sup>23–27</sup> and theoretical studies<sup>28–39</sup> by various density functional theory (DFT) and ab initio methods. In 2013, using Li clusters as a test case, Cheng et al. proposed a new concept for bonding between superatoms and gave more generalized insight to the stability of nonspherical clusters. They found that  $\text{Li}_{14}$ ,  $\text{Li}_{10}$ , and  $\text{Li}_8$  clusters are analogues to  $\text{F}_2$ ,  $\text{N}_2$ , and  $\text{CH}_4$  molecules, respectively.<sup>40</sup> In addition, a considerable amount of work has been carried out on lithium clusters doped with an impurity atom, which can lead to fundamental changes in geometries, energy properties, and the bonding nature of lithium clusters. For example, the heterogeneous  $\text{XLi}_n$  clusters doped with group IA elements with  $\text{X} = \text{Na}$  and  $\text{K}$ ,<sup>41–43</sup> group IIA elements including beryllium  $\text{BeLi}_n$ <sup>44</sup> and magnesium  $\text{MgLi}_n$ ,<sup>45</sup> group IIIA elements such as  $\text{BLi}_n$ <sup>46–52</sup> and  $\text{AlLi}_n$ ,<sup>53–62</sup> and group IVA with  $\text{X} = \text{C}$ ,  $\text{Si}$ ,  $\text{Ge}$ , and  $\text{Sn}$ <sup>63–73</sup> have extensively been studied by many groups. These studies focused on the investigations of s-block and p-block element doped small lithium clusters; however, there have been few studies on lithium clusters doped with transition elements.

Beyond the above studies based on alkali metal matrixes, however, research of employing lithium clusters as superatom doping hosts has been carried out far less. Taking the above research progress and importance of TM-doped alkali metal clusters into account, we performed a first-principles study of the vanadium-doped lithium clusters  $\text{VLi}_n$  ( $n = 1–13$ ) to systematically explore their structural evolution and properties. Because the lithium has the  $s^1$  valence configuration, similar to cesium, it is expected that the aggregation of lithium clusters and TM elements with the partially filled d shells will probably result in magnetic superatoms. We started our explorations on the size-dependent growth behavior related to the stability of the bimetallic  $\text{VLi}_n$  clusters, and then, we investigate the electronic and magnetic properties of  $\text{VLi}_n$  in comparison to pure lithium clusters. Following the research focuses in the formation of superatoms in  $\text{VLi}_n$  clusters, we found the highly stable cluster  $\text{VLi}_8$  as a magnetic superatom candidate with  $5 \mu_B$ , meanwhile consisting of closed shells of eight paired electrons and five unpaired electrons occupying the  $1D_{xy}$ ,  $1D_{x^2-y^2}$ ,  $1D_{xz}$ ,  $1D_{yz}$ , and  $1D_{z^2}$  levels. Moreover, it demonstrates that the  $\text{VLi}_n$  clusters from the size of  $n = 8$  to 13 with cage-like structures all have the superatomic orbitals. The magnetic properties of the various 3d TM atom doped  $\text{Li}_8$  cages are also discussed in the context. We hope that our work will add new types of superatoms in alkali metal clusters.

## 2. COMPUTATIONAL METHODS

Calculations in this work were performed by using DFT implemented in the DMOL3 program.<sup>74</sup> Relativistic calculations were carried out with scalar relativistic corrections to valence orbitals relevant to atomic bonding properties via a local pseudopotential (VPSR). All-electron spin-unrestricted calculations with double-numerical basis sets including d polarization functions (DNP) were employed. The quality of the self-consistent field (SCF) convergence tolerance was set as “fine” with a convergence criterion of  $1 \times 10^{-5}$  Hartree on the total energy and electron density,  $2 \times 10^{-3}$  Hartree/Å on the gradient, and  $5 \times 10^{-3}$  Å on the displacement in our calculations. Harmonic vibrational frequencies were computed to confirm that the low-energy isomers are true minima. There is no imaginary frequency for structures presented here. In addition, for geometry optimization of each isomer, the spin multiplicities (SMs) were considered to be at least 1, 3, 5, 7, and 9 for even-electron clusters and 2, 4, 6, 8, and 10 for odd-electron clusters. If the total energy decreases with increasing SM, we will consider a higher spin state until the energy minimum with respect to the SM is reached. In the present work, we chose the initial structures of  $\text{VLi}_n$  clusters by two methods, as follows: First, the basin-hopping global optimization method was employed to produce a large number of isomers for further DFT optimization.<sup>75,76</sup> Second, the low-lying structures were obtained by placing the V atom on each possible site of the  $\text{Li}_n$  host clusters randomly as well as by substituting one Li by a V atom in the  $\text{Li}_{n+1}$  cluster.

To choose the most valid gradient-corrected exchange–correlation functionals for the lithium clusters system, we performed calculations on  $\text{Li}_2$ ,  $\text{Li}_2^-$ , and  $\text{Li}_3$  clusters with four popular functionals, namely, Becke’s 1988 exchange functional and the correlation functional of Perdew (BP86),<sup>77</sup> Becke’s 1988 exchange functional and the correlation functional of Lee, Yang, and Parr (BLYP),<sup>78</sup> the 1996 exchange functional of Perdew, Burke, and Ernzerhof (PBE),<sup>79</sup> and Perdew and Wang’s 1991 exchange and correlation functional (PW91).<sup>80</sup> The results are listed in Table 1. It can be seen from Table 1 that the calculated bond length, average binding energies, and ionization potential based on the PW91 method are in best agreement with the experimental values. This indicates that the functional PW91 is confirmed to yield the most reliable results. Therefore, we selected the functional PW91 for most calculations carried out in this study.

## 3. RESULTS AND DISCUSSION

Aiming for the discovery of stable superatoms in the present system, we dug thoroughly through the whole sequence of V-doped  $\text{Li}_n$  ( $n = 1–13$ ) clusters. The  $\text{VLi}_n$  cluster growth pattern was first investigated. Relative stabilities were justified afterward through their electronic structures. Magnetic properties of the

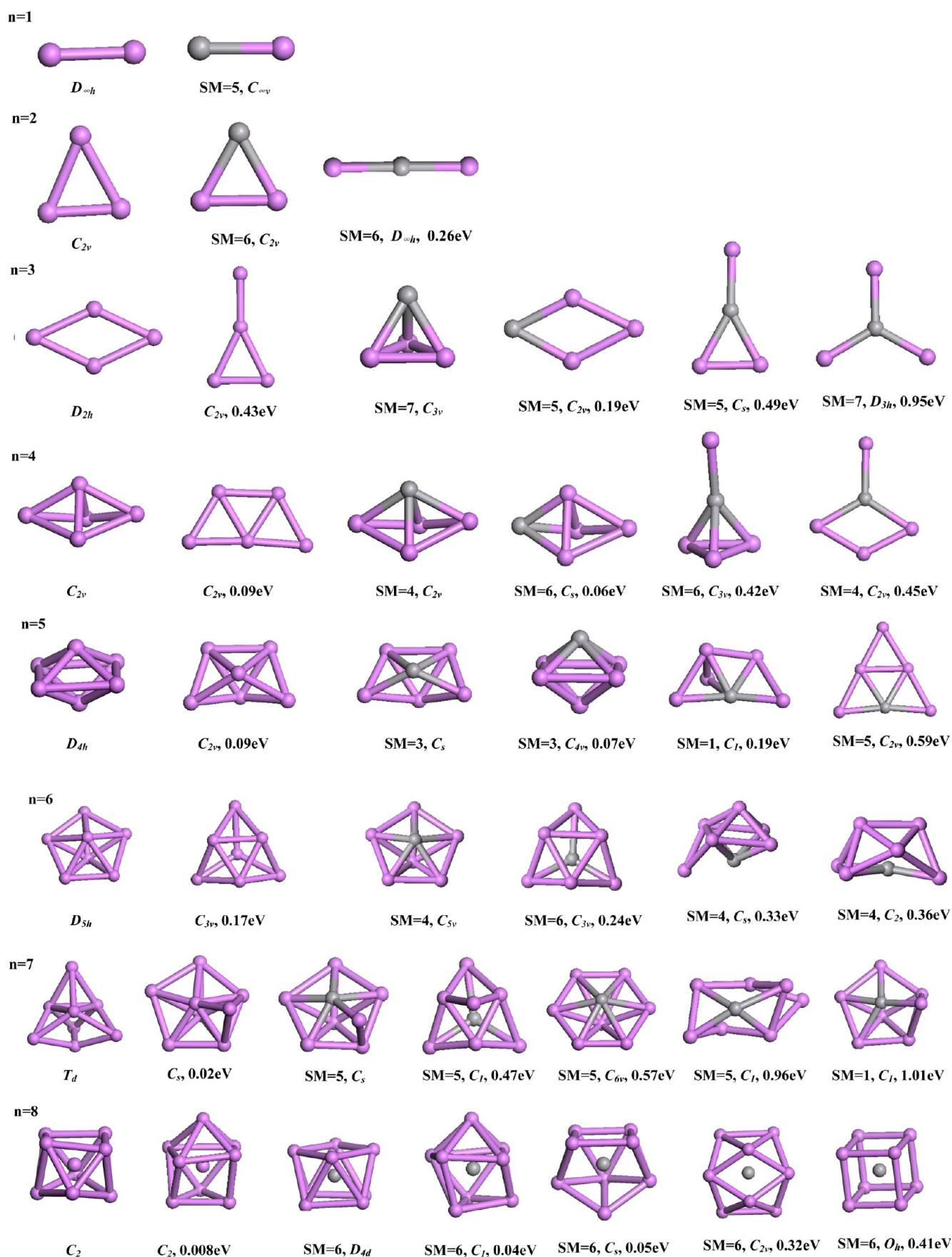
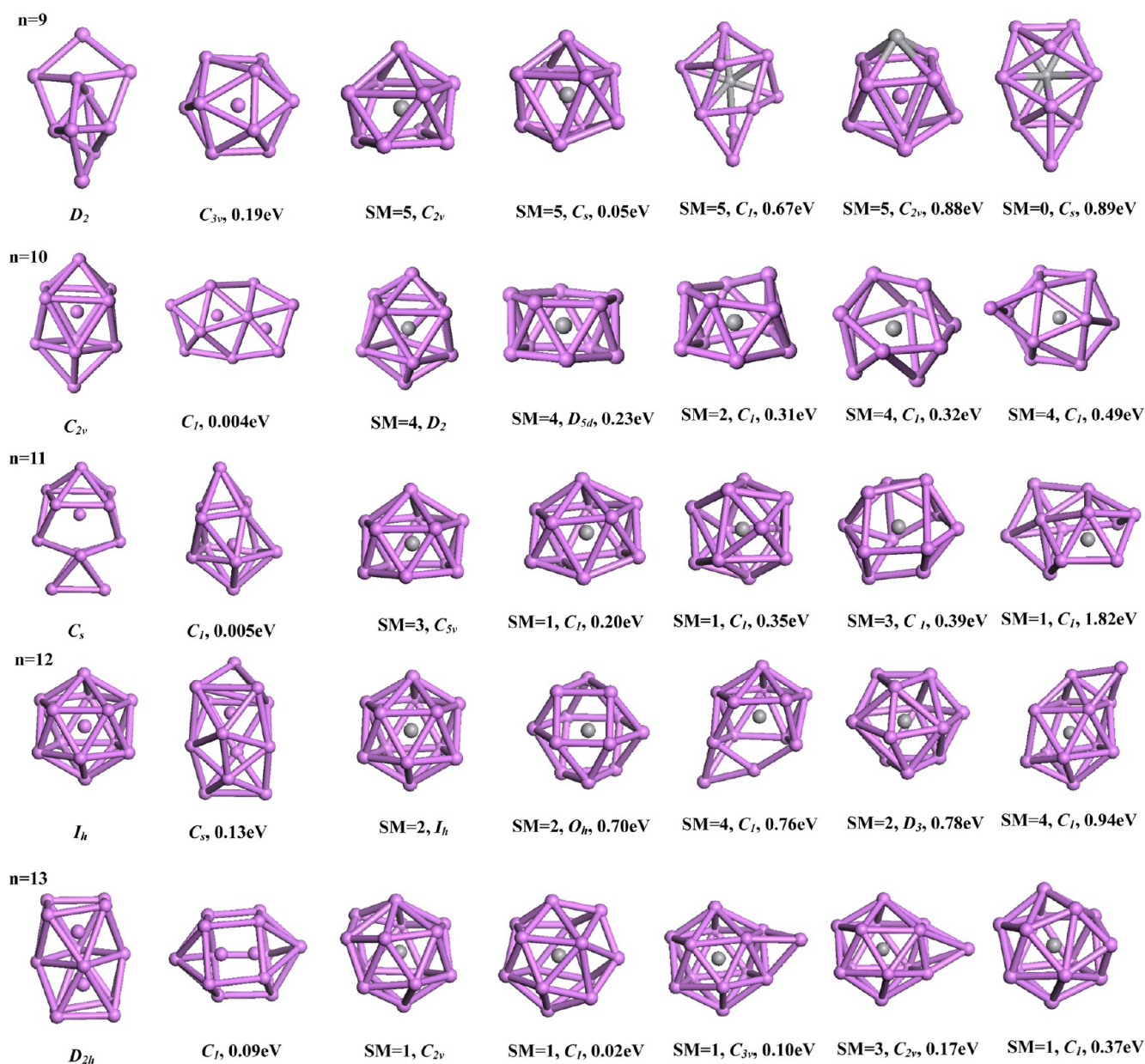


Figure 1. continued





**Figure 1.** The lowest-energy structures and low-lying isomers with the spin multiplicities (SMs) and relative energies (in eV) of  $VLi_n$  ( $n = 1-13$ ) clusters. The ground-state and metastable geometries of the corresponding bare  $Li_{n+1}$  clusters are also given on the left. See Table 2 for the corresponding energetic and structural information. The V atom is represented by the gray sphere.

stable binary clusters were discussed subsequently. Taking their magnetic and stable characteristics into considerations, a distinctive magnetic superatom was found with a potential extension to other similar TM-doped  $Li_n$  clusters. Thus, the present section is subdivided into four parts, with each part describing the above-mentioned steps.

**3.1. Geometric Structure.** We considered extensive two-dimensional (2D) and three-dimensional (3D) structures to determine the lowest-energy geometries for each bimetallic  $VLi_n$  cluster. Many stable isomers were obtained. The lowest-energy structures together with some low-lying isomers of  $VLi_n$  and corresponding bare  $Li_{n+1}$  ( $n = 1-13$ ) clusters are shown in Figure 1. The symmetries, SMs, and the differences of the total binding energies between an isomer and the lowest-energy structure optimized with PW91/VPSR are also listed below each isomer in Figure 1. The lowest-energy geometries of pure

$Li_{n+1}$  clusters from our optimized results are in agreement with the results reported in the literature.<sup>28-33,38-40</sup> The calculated ionization potential (IP) of the pure  $Li_3$  cluster with a planar triangle structure in the present work is in good agreement with the result of the experiment (see Table 1).<sup>23</sup> For pure lithium clusters, the 2D  $\rightarrow$  3D transition is found to occur in  $Li_5$  in our calculations, in accordance with the previous calculations of Tai et al. using the coupled-cluster theory CCSD(T)/complete basis set (CBS) methods based on DFT.<sup>51,52</sup> Moreover, the structural transition from the compact to hollow-cage structure is found at  $n = 8$ , which is in agreement with the results of Yepes et al.<sup>29</sup> The optimized geometries reveal that  $VLi_n$  clusters prefer 3D structures with the successive lithium atoms surrounding the central vanadium site. A single Li-atom-capped structure of the  $VLi_{n-1}$  cluster is a dominant growth pattern. The structure evolves toward a compact

**Table 2.** Geometrical Structures with the Symmetry Type, the SM, the Binding Energy ( $E_b$ ) Per Atom, the Fragmentation Energy ( $E_f$ ), and the HOMO–LUMO Energy Gap  $E_{\text{gap}}$  of  $\text{VLi}_n$  Clusters and the Corresponding Bare  $\text{Li}_{n+1}$  Clusters ( $n = 1–13$ ) for the Lowest-Energy Structures<sup>a</sup>

pure $\text{Li}_n$						$\text{VLi}_n$					
cluster	symmetry	$E_b$ (eV)	$E_b$ (expt.)	$E_f$ (eV)	$E_{\text{gap}}$ (eV)	cluster	symmetry	SM	$E_b$ (eV)	$E_f$ (eV)	$E_{\text{gap}}$ (eV)
$\text{Li}_2$	$D_{\infty h}$	0.48	0.53	0.95	1.491	$\text{VLi}$	$C_{\infty v}$	5	0.70	1.41	0.468
$\text{Li}_3$	$C_{2v}$	0.54	0.50	0.67	0.494	$\text{VLi}_2$	$D_{\infty h}$	6	0.81	1.02	0.308
$\text{Li}_4$	$D_{2h}$	0.72	0.63	1.26	0.976	$\text{VLi}_3$	$C_{3v}$	7	0.95	1.36	0.756
$\text{Li}_5$	$C_{2v}$	0.79	0.78	1.07	0.338	$\text{VLi}_4$	$C_{2v}$	4	1.02	1.31	0.510
$\text{Li}_6$	$D_{4h}$	0.89	0.88	1.42	0.738	$\text{VLi}_5$	$C_s$	3	1.08	1.39	0.604
$\text{Li}_7$	$D_{5h}$	0.98	0.91	1.51	0.562	$\text{VLi}_6$	$C_{5v}$	4	1.18	1.76	0.374
$\text{Li}_8$	$T_d$	1.01	0.95	1.22	0.976	$\text{VLi}_7$	$C_s$	5	1.21	1.40	0.514
$\text{Li}_9$	$C_2$	1.01		1.02	0.390	$\text{VLi}_8$	$D_{4d}$	6	1.28	1.80	0.779
$\text{Li}_{10}$	$D_2$	1.05		1.42	0.875	$\text{VLi}_9$	$C_{2v}$	5	1.30	1.51	0.328
$\text{Li}_{11}$	$C_{2v}$	1.06		1.16	0.416	$\text{VLi}_{10}$	$D_2$	4	1.32	1.55	0.309
$\text{Li}_{12}$	$C_i$	1.09		1.42	0.660	$\text{VLi}_{11}$	$C_{5v}$	3	1.34	1.53	0.196
$\text{Li}_{13}$	$I_h$	1.12		1.42	0.524	$\text{VLi}_{12}$	$I_h$	2	1.38	1.86	0.196
$\text{Li}_{14}$	$D_{2h}$	1.13		1.32	0.842	$\text{VLi}_{13}$	$C_{2v}$	1	1.36	1.16	0.519

<sup>a</sup>For the sake of comparison, the experimental values (ref 26) of  $E_b$  of the bare  $\text{Li}_{n+1}$  clusters ( $n = 1–7$ ) are given.

icosahedral shape with the increase of lithium atom number. It is found that the SMs for the low-lying isomers of the  $\text{VLi}_n$  clusters are not only size-dependent but also structure-dependent, as shown in Figure 1.

The ground state of diatomic  $\text{VLi}$  exhibits a  $C_{\infty v}$  symmetry. For the triatomic  $\text{VLi}_2$  cluster, the angular isomer with the  $C_{2v}$  symmetry, which relates to the lowest-energy structure of the  $\text{Li}_3$  cluster, is found to be the most stable structure. The linear configuration in which the Li atom occupies the central position with the  $D_{\infty h}$  symmetry is 0.26 eV higher in energy than the triangle isomer. Starting at the size of  $n = 3$ , the lowest-energy structures of  $\text{VLi}_n$  clusters begin to show the appearance of 3D geometries. A triangular pyramid with  $C_{3v}$  symmetry is the most stable structure for  $\text{VLi}_3$ . The 2D  $C_{2v}$  rhombic form and the Y-shaped planar geometry lie 0.19 and 0.49 eV higher in energy, respectively. The most stable isomer of the  $\text{VLi}_4$  cluster has a triangular bipyramidal structure with a  $C_{2v}$  point group. The second isomer of the  $\text{VLi}_4$  cluster in which the V atom lies at the corner of the bipyramid is 0.06 eV higher in energy. The lowest-energy structure of  $\text{VLi}_5$  is obtained by subsequent addition of one Li atom to the  $\text{VLi}_4$  structure. The squared pyramidal with  $C_{4v}$  is calculated to be only 0.07 eV less stable than the  $C_s$  structure. Similar to the configuration of the ground-state  $\text{Li}_7$  cluster, a pentagonal bipyramid ( $C_{5v}$ ) with the impurity V atom at one of the apexes is the lowest-energy structure for  $\text{VLi}_6$  clusters.  $\text{VLi}_7$  can be viewed as adding a Li atom to the pentagonal bipyramid of  $\text{VLi}_6$  by distortion.

The number of isomers for  $\text{VLi}_n$  is increasing as successive Li atoms are added to a V atom. From  $n = 8$  to 13, the lithium atoms adopt a cage-like structure, and the endohedral V atom occupies at the center site in the ground-state structures. The isomers with the V atom at a surface site are all found to be higher in energy. The  $\text{VLi}_8$  cluster in  $D_{4d}$  symmetry is derived from the lowest-energy structure of pure  $\text{Li}_9$  with a square antiprism where the dopant V atom is sitting in the center. This structure is similar to other superatoms such as  $\text{VCs}_8$ ,  $\text{VNa}_8$ , and  $\text{FeCa}_8$  clusters.<sup>17,20</sup> The second and third lowest-energy isomers are very close in energy and have a large structural distortion relative to the most stable structure. The higher-symmetry  $O_h$  cubic structure is 0.41 eV higher than the square antiprism isomer, and from this cluster onward, the V atom is seen to be encapsulated in a Li cage, as shown in Figure 1.  $\text{VLi}_9$

can be viewed as a capped square antiprism of a  $\text{VLi}_8$  cluster. This trend of capping continues up to  $n = 13$ . In addition, the tendency for the formation of a pentagonal ring is also clear. The lowest-energy structure of  $\text{VLi}_{12}$  is the icosahedron with perfect  $I_h$  symmetry, in which the V atom is located in the center of the  $\text{Li}_{12}$  cage. The octahedral isomer with  $O_h$  symmetry is 0.70 eV higher in energy than the icosahedral isomer.

It should be noted that the geometrical structures of TM impurity V-atom-doped  $\text{Au}_n$  ( $n = 1–14$ ) clusters were systematically investigated by Nhat et al. using BP86/cc-pVTZ-PP calculations.<sup>81</sup> Although Au and Li have similar outermost shell electronic structures, namely, one s electron, the structures of  $\text{VAu}_n$  clusters obtained by Nhat et al. are very different from the corresponding  $\text{VLi}_n$  clusters. This is because lithium is the lightest metal, while gold is an element whose unique properties are strongly influenced by relativistic effects. The strong relativistic effect in gold leads to a reduced 5d–6s energy gap and strong s–d hybridization. For TM impurities in a nonmagnetic host, the interaction of the impurity d states with the different host metal plays a crucial role in determining the structures and properties of the clusters.

**3.2. Relative Stabilities.** Table 2 gives various structural and energetic characteristics for the lowest-energy structures of  $\text{VLi}_n$  clusters and the corresponding bare  $\text{Li}_{n+1}$  clusters ( $n = 1–13$ ). To further analyze the stability of clusters, we calculated the average binding energy ( $E_b$ ) per atom of  $\text{VLi}_n$ , which is defined as the difference between the energy sum of all of the free atoms constituting the cluster and the total energy of the cluster using the following formula:

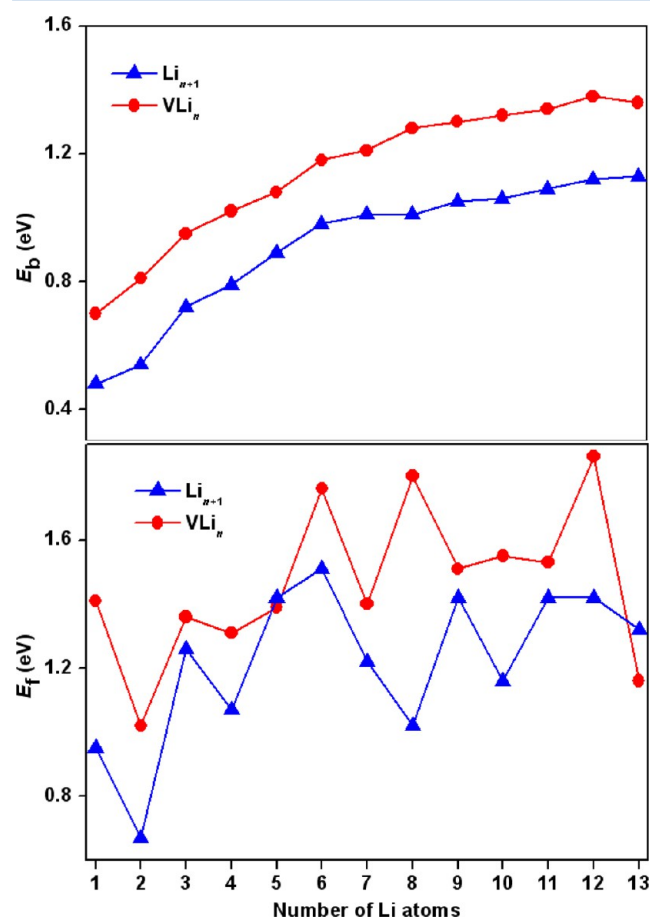
$$E_b(\text{VLi}_n) = \frac{[nE(\text{Li}) + E(\text{V}) - E(\text{VLi}_n)]}{(n + 1)} \quad (1)$$

The fragmentation energy ( $E_f$ ) of the lowest-energy structure is also discussed, which is defined as the energy that is released when a Li atom is separated from these clusters calculated using the equation

$$E_f(\text{VLi}_n) = [E(\text{VLi}_{n-1}) + E(\text{Li}) - E(\text{VLi}_n)] \quad (2)$$

In the above equation,  $E(\text{VLi}_n)$  and  $E(\text{VLi}_{n-1})$  represent the energy of the lowest-energy structures of  $\text{VLi}_n$  and  $\text{VLi}_{n-1}$

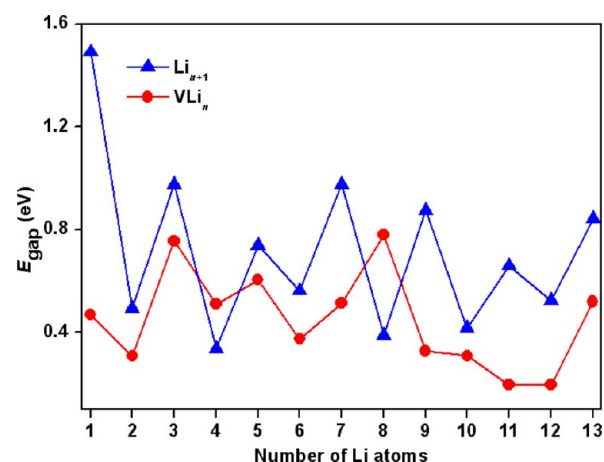
clusters, respectively. The average binding energies per atom of the pure  $\text{Li}_{n+1}$  clusters are in good agreement with the available experimental results, as Table 2 shows.<sup>26</sup> It can be seen from Table 2 that the  $E_b$  for the ground state of  $\text{VLi}_n$  ( $n = 1-13$ ) clusters is significantly higher than that of the corresponding pure  $\text{Li}_{n+1}$ . This indicates that doping with the V atom, which has the partially filled d shells, can enhance the stabilities of the  $\text{Li}_n$  clusters. Figure 2 shows the  $E_b$  and  $E_f$  of the  $\text{VLi}_n$  clusters



**Figure 2.** Comparison of the average binding energies per atom ( $E_b$ ) and fragmentation energies ( $E_f$ ) of the  $\text{VLi}_n$  and bare  $\text{Li}_{n+1}$  clusters ( $n = 1-13$ ) for the lowest-energy structures.

for the lowest-energy structures as a function of the number of Li atoms. As seen from the Figure 2, the binding energy of  $\text{VLi}_n$  clusters increases monotonically with cluster size. However, three conspicuous maxima of fragmentation energies for  $\text{VLi}_n$  clusters are found at  $n = 6, 8$ , and  $12$  in Figure 2, indicating that  $\text{VLi}_6$ ,  $\text{VLi}_8$ , and  $\text{VLi}_{12}$  clusters possess relatively higher stability than their respective neighbors.

The energy gap ( $E_{\text{gap}}$ ) between the highest occupied molecular orbital (HOMO) and the lowest unoccupied molecular orbital (LUMO) is another useful quantity for examining the kinetic stability of small clusters. A large energy gap corresponds to a high energy required for electron excitation. We plotted the energy gap of the most stable  $\text{VLi}_n$  and  $\text{Li}_{n+1}$  clusters in Figure 3. There are clear odd–even oscillations in the energy gap spectrum of the pure  $\text{Li}_{n+1}$  clusters. We found that the  $E_{\text{gap}}$  of  $\text{VLi}_n$  clusters varies significantly with size, and  $\text{VLi}_8$  exhibits a particularly large  $E_{\text{gap}}$  with 0.779 eV. Figure 3 shows a distinct maximum at  $\text{VLi}_8$



**Figure 3.** The HOMO–LUMO energy gap ( $E_{\text{gap}}$ ) of the  $\text{VLi}_n$  and bare  $\text{Li}_{n+1}$  clusters ( $n = 1-13$ ) for the lowest-energy structures.

clusters, larger than the values of other clusters, indicating that  $\text{VLi}_8$  is relatively more stable in the electronic structure.

Mulliken population analysis was performed for the lowest-energy structures, and the atomic charge on the V atom of  $\text{VLi}_n$  clusters is given in Table 3 and plotted in Figure 4. The charge on the impurity V atom, ranging from  $-0.167$  to  $0.217$  au, clearly shows that there are obvious charge transfers between V and Li atoms. In small clusters from  $\text{VLi}$  to  $\text{VLi}_5$ , charge transfers occur from the Li to V atom due to a larger electronegativity of the V. However, charge transfers reverse as successive Li atoms are added. The impurity V atom is likely to lose its valence electrons, and the host Li has a negative charge. The  $\text{VLi}_8$  cluster with a vanadium atom surrounded by a square antiprism of eight lithium atoms has the largest charge transfers among these clusters, which is responsible for the higher stability of the  $\text{VLi}_8$  cluster than its neighbors due to ionic-like bonding of the V–Li interaction through the charge transfers. To have a better view of the interactions between V and Li atoms, the deformation electron density (DED) of the bare  $\text{Li}_9$  and  $\text{VLi}_8$  clusters for the lowest-energy structures as the example is plotted in Figure 5a. The DED is defined as the total charge density of a cluster with the density of the isolated atoms subtracted. The blue area indicates electron accumulation when atoms form a cluster. From Figure 5a, we can see that the DED distributes not only surrounding the V and Li atoms but also surrounding the intervals between Li and V atoms in the  $\text{VLi}_8$  cluster, which shows some covalent character in the V–Li bonds. In comparison to the pure  $\text{Li}_9$  cluster (see Figure 5a), when the V atom substitutes one Li atom in the square antiprism structure, the electron accumulations of V–Li atoms and Li–Li atoms show a marked increase. This verifies that the strong interaction between the V and Li exists in  $\text{VLi}_8$  and results in the high stability of the structure.

**3.3. Magnetic Properties.** Different from a single atom, the filling of the electronic orbitals in clusters does not follow Hund's rule of maximizing the spin because the structural distortions in small clusters can remove the degeneracies in electronic shells and stabilize the clusters via the Jahn–Teller effect.<sup>82</sup> This results in superatoms with pairs of electrons favoring nonmagnetic character. In what follows, we will examine the variation in the magnetic moment of  $\text{VLi}_n$  clusters as successive Li atoms are added. The local magnetic moments on 3d, 4s, and 4p states of the V and Li atoms and the total magnetic moment of the ground-state  $\text{VLi}_n$  clusters are listed in



Table 3. Mulliken Charge (au) on the V Atom, Local Magnetic Moment ( $\mu_B$ ) of the Guest V and Host Li Atoms, and Total Magnetic Moment of  $\text{VLi}_n$  ( $n = 1-13$ ) Clusters for the Lowest-Energy Structures

		moment ( $\mu_B$ )					
			V				
system	charge (au)	Li <sub>n</sub>	3d	4s	4p	local	total
VLi	−0.106	−0.205	3.809	0.391	0.005	4.205	4
VLi <sub>2</sub>	−0.089	0.709	3.746	0.489	0.056	4.291	5
VLi <sub>3</sub>	−0.122	1.429	3.932	0.524	0.115	4.571	6
VLi <sub>4</sub>	−0.167	−0.662	3.759	−0.157	0.058	3.662	3
VLi <sub>5</sub>	−0.112	−1.636	3.728	−0.120	0.028	3.636	2
VLi <sub>6</sub>	0.027	0.607	3.534	−0.055	0.129	3.607	3
VLi <sub>7</sub>	0.101	−0.023	3.673	0.140	0.209	4.023	4
VLi <sub>8</sub>	0.217	0.568	3.965	0.218	0.250	4.432	5
VLi <sub>9</sub>	0.180	−0.091	3.622	0.227	0.242	4.091	4
VLi <sub>10</sub>	0.155	−0.876	3.469	0.173	0.233	3.876	3
VLi <sub>11</sub>	0.195	−1.646	3.187	0.226	0.233	3.646	2
VLi <sub>12</sub>	0.188	−2.302	2.887	0.199	0.217	3.302	1
VLi <sub>13</sub>	0.174	0	0	0	0	0	0

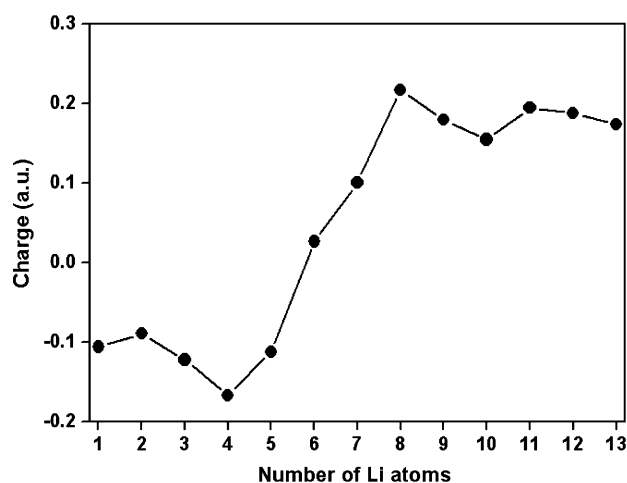


Figure 4. The atomic charge (au) on the V atom of the  $\text{VLi}_n$  clusters ( $n = 1-13$ ) for the lowest-energy structures.

Table 3 and plotted in Figure 6. The total magnetic moment of bare  $\text{Li}_{n+1}$  clusters shows a pronounced odd–even alternation (0 and  $1 \mu_B$ , respectively) with the number of Li atoms. A single V atom has three unpaired electrons with an atomic configuration of  $3d^3 4s^2$ . When a V atom with the partially filled 3d orbital is doped into  $\text{Li}_n$  clusters, the formed  $\text{VLi}_n$  clusters generate a diversiform magnetic moment, varying from 0 to  $6 \mu_B$  with the different cluster sizes. It is found that the  $\text{VLi}_8$  has the robust magnetic moment of  $5 \mu_B$ . Figure 6 displays that from the size of  $n = 5$  to 13, the magnetic moment of  $\text{VLi}_n$  clusters increases with Li number and reaches its maximum at  $\text{VLi}_8$  and then decreases gradually to  $0 \mu_B$  at the size of  $n = 13$ . Consequently, the various styles of magnetic moments in  $\text{VLi}_n$  clusters suggest that nonmagnetic  $\text{Li}_n$  clusters can serve as flexible hosts to enhance, protect, or reduce the spins of the dopant magnetic atom, which has potential applications in new nanomaterials with tunable magnetic properties.

Mulliken population analysis shows that the total magnetic moment of the clusters is mainly localized in the V atom. A small amount of magnetic moment is found in host Li atoms, which show that the 3d V atom plays a decisive role in the magnetic moment of Li nanoclusters. This phenomenon can also be reflected from Figure 5b and c that although the total

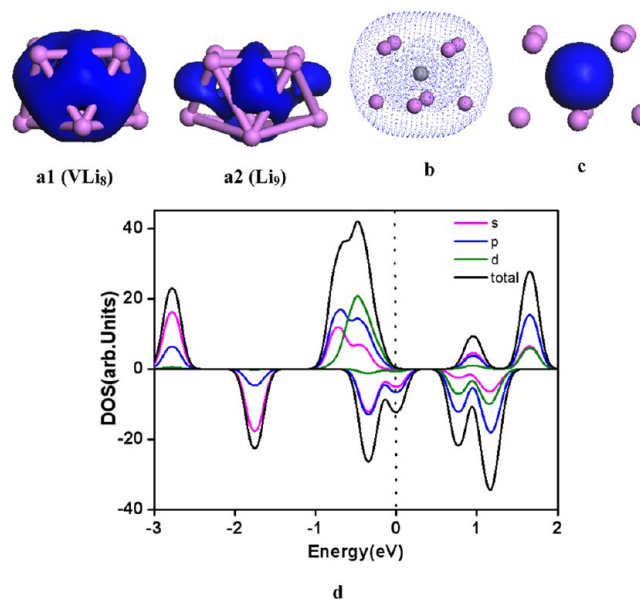
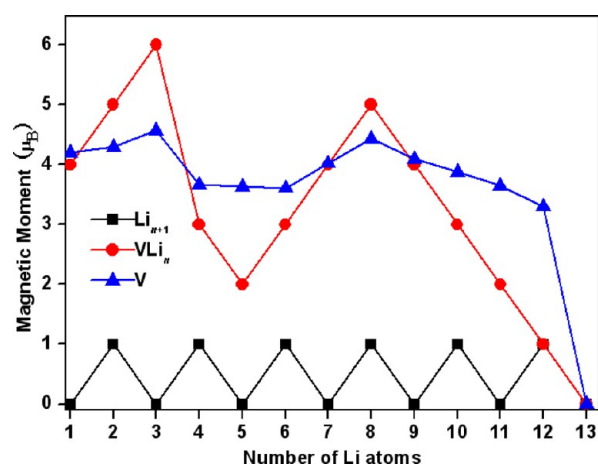


Figure 5. The DED (a), total electron density (b), net spin electron density (c), and electronic density of states (DOS) (d) of the  $\text{VLi}_8$  cluster for the lowest-energy structure. The surface isovalue for MO plotting is  $0.3 \text{ e}/\text{\AA}^3$ . The DOS is obtained by Gaussian extension applied to the eigenvalues, and the broadening width parameter is chosen to be  $0.1 \text{ eV}$ . Spin-up (positive) and spin-down (negative) densities are given, and the dashed lines indicate the location of the HOMO level.

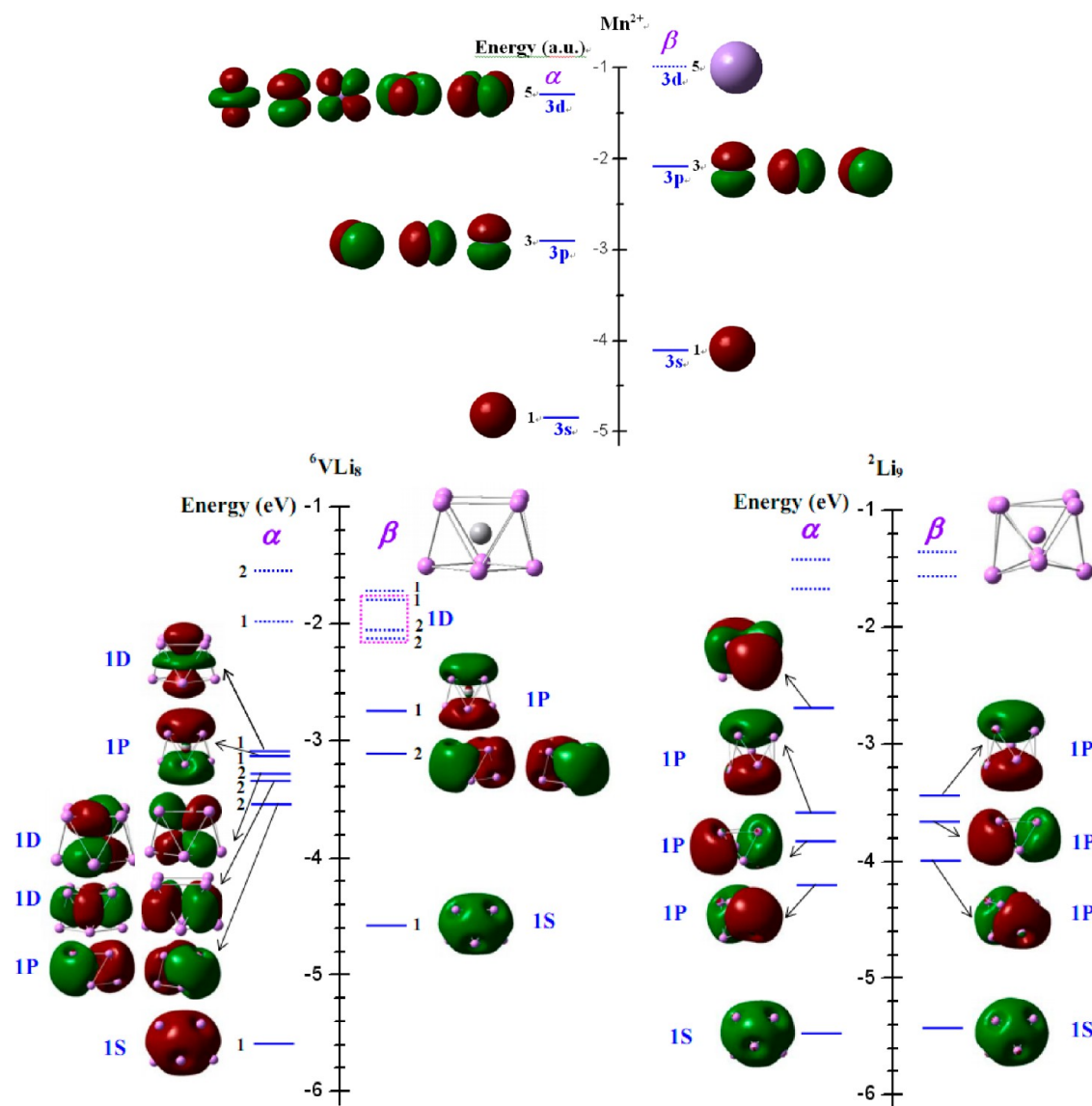
charge density of  $\text{VLi}_8$  is extended over the entire cluster, the spin density is almost entirely located on the vanadium site. The magnetic moment of the V atom in the  $\text{VLi}_{13}$  cluster is fully quenched because this cluster attains an 18-electron shell closing. Except for  $\text{VLi}_{13}$ , the local magnetic moments contributed to by the 3d state electrons of V are about  $2.887-3.965 \mu_B$  in  $\text{VLi}_n$  ( $n = 1-12$ ) clusters. The 4s and 4p subshells, which are nonmagnetic for a free V atom, provide a small contribution to the magnetic moments, as shown in Table 3. This may be ascribed to the internal charge transfer from the 4s and 4p orbitals to the 3d orbital and the hybridization between the d state and the s and p states. The partial density of states (PDOS) of the  $\text{VLi}_8$  cluster in Figure 5d clarifies the



**Figure 6.** The local magnetic moment on the V and Li atoms and the total magnetic moment of the  $\text{VLi}_n$  clusters ( $n = 1-13$ ) for the lowest-energy structures.

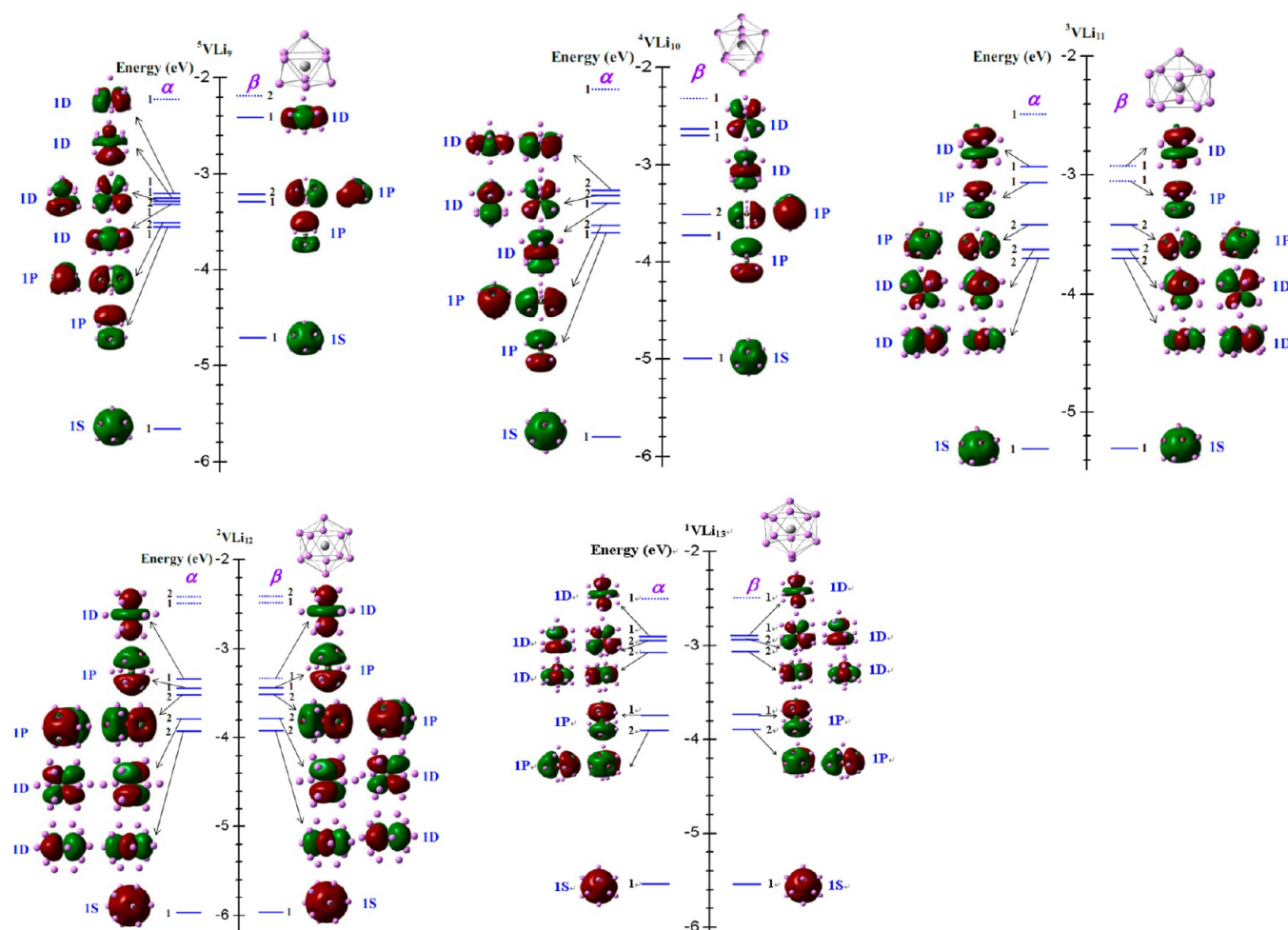
obvious hybridization between the atomic orbitals of the guest atom V (d orbital) and host atom Li (s orbital). Figure 5d shows that the shapes of the total density of states for the  $\alpha$  electron (spin-up) and  $\beta$  electron (spin-down) are quite different in forming the magnetism of  $\text{VLi}_8$  with  $5 \mu_B$ .

**3.4. Magnetic Superatoms.** On the basis of the above discussion, we note that  $\text{VLi}_8$  is an isolated cluster with a high fragmentation energy of 1.80 eV, a big energy gap of 0.78 eV, a large charge transfer of 0.217 au, and a robust magnetic moment of  $5 \mu_B$  among these clusters. This indicates that  $\text{VLi}_8$  has enhanced structural and chemical stability and large spin state, and it can be a candidate to magnetic superatoms. To identify the nature of orbitals, we present the MO and orbital energy level correlation diagram of the  $\text{VLi}_8$  in Figure 7. The MO results of the pure  $\text{Li}_9$  clusters are also depicted for comparison. The MO analysis was calculated with the PW91/LANL2DZ level in G09.<sup>83</sup> The  $\text{VLi}_8$  cluster contains 13 valence electrons and does not correspond to a magic species with an 18-electron shell closing. However, the electronic configuration



**Figure 7.** The MOs and MO energy level correlation diagrams of the  $\text{VLi}_8$ ,  $\text{Li}_9$ , and single  $\text{Mn}^{2+}$  cation for the lowest-energy structures calculated with the PW91/LANL2DZ level in G09. Continuous lines correspond to the filled levels, and the dotted lines correspond to the unfilled states. For each level, the degeneracy is marked. The surface isovalue for MO plotting is  $0.02 \text{ e}/\text{\AA}^3$ .





**Figure 8.** The MOs and MO energy level correlation diagrams of the  $\text{VLi}_n$  ( $n = 9-13$ ) for the lowest-energy structures calculated with the PW91/LANL2DZ level in G09. The illustration is the same as that in Figure 7.

of  $\text{VLi}_8$  can be considered as a jellium sphere. It consists of the five vanadium electrons in excess of the closed-shell eight-electron configuration, which contains the four orbitals in the 1S and 1P shells, each with an electron pair. The extra five electrons from the V atom are then placed singly into each of the five orbitals of the 1D shell so that they are all unpaired. Therefore, the  $\text{VLi}_8$  cluster has a half-filled D subshell with a magnetic moment of  $5 \mu_B$ , and the remaining electrons form a filled shell of  $1S^2 1P^6$  electrons, which leads to a stable species. Here, the  $\text{VLi}_8$  cluster exhibits Hund's filling rule of maximizing the spin-like atoms. Figure 7 shows that the first two electrons occupy the lowest state, which is spread out over the whole  $\text{VLi}_8$  cluster and has 1S superorbital character. The next majority states are two degenerate 1P states that have a  $1P_x$  and  $1P_y$  character, while the  $1P_z$  state is pushed around 0.43 eV higher in energy as the  $\text{VLi}_8$  cluster can be regarded as a compression of the spherical jellium in the  $z$  direction. The next higher energy orbitals above the 1P orbitals are 1D orbitals. The oblate shape of the cluster broke the degeneracy of the 1D orbitals into three groups of two ( $D_{xy}$  and  $D_{x^2-y^2}$ ), two ( $D_{xz}$  and  $D_{yz}$ ), and one ( $D_{z^2}$ ) orbitals due to a crystal field splitting. In the minority states, after the  $P_z$  state, we found five unfilled 1D orbitals with similar degeneracies of the majority states (see Figure 7). The filling of majority and minority orbitals leads to  $1S^2 1P^6 1D^5$  orbitals resulting in a  $5 \mu_B$  magnetic moment in the  $\text{VLi}_8$  cluster, which can mimic the situation in a manganese ion

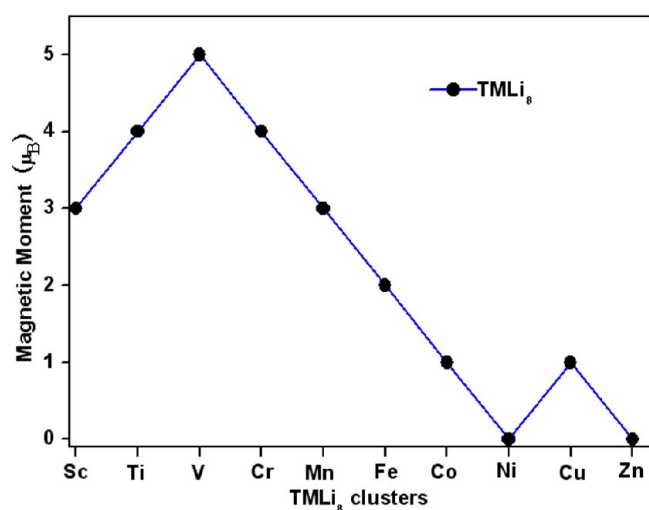
( $\text{Mn}^{2+}$ ) with a half-filled 3d shell. The  $\text{Mn}^{2+}$  ion has five electrons in excess of the closed-shell 18-electron argon configuration, as Figure 7 shows. Our finding of the  $\text{VLi}_8$  cluster as a magnetic superatom can be classified into the previous discovery of superatoms in alkali metal clusters ( $\text{VNa}_8$  and  $\text{VCs}_8$ ) by Khanna and collaborators.<sup>17</sup>

We also made a detailed comparison between the  $\text{VLi}_8$  and the corresponding pure  $\text{Li}_9$  cluster. The lowest-energy isomer of the pure  $\text{Li}_9$  cluster has a distorted squared-pyramidal structure similar to  $\text{VLi}_8$ . Figure 7 shows that the electronic shell structures of  $1S^2$  and  $1P^6$  are virtually unchanged as the V atom substitutes for the embedded Li atom, despite the slight loss of orbital degeneracy of the 1P state in the  $\text{Li}_9$  cluster due to a lower symmetry. The delocalized electrons from the s valence states of Li atoms occupy the superatom S and P states. On the other hand, the localized electrons from the 3d V atom stabilize the magnetic moments. The present work shows that magnetic superatoms can be designed by appropriate combinations of localized and delocalized electrons in the valence space of a cluster. This also demonstrates that the electron shell closing model can be regarded as a simple but valid tool for explaining the structures and stabilities of metal clusters.

It is noticed from  $n = 8$  that the geometries of the most stable  $\text{VLi}_n$  clusters are very similar, with an endohedral V atom in  $\text{Li}_n$  cages. We extended the orbital analysis to all of the  $\text{VLi}_n$

clusters from the size of  $n = 9$  to 13. The results are depicted in Figure 8. It is clear that all of the  $\text{VLi}_n$  ( $n = 9-13$ ) clusters have superatomic orbitals. For example, the icosahedral  $\text{VLi}_{12}$  with perfect  $I_h$  symmetry can be viewed as another superatom with the superatomic configuration of  $1\text{S}^21\text{P}^61\text{D}_{\alpha}^51\text{D}_{\beta}^8$  orbitals, as Figure 8 shows. Very recently, Cheng et al. reported that the pure lithium clusters can mimic the behavior of simple molecules in electronic shells, and they found that nonspherical clusters  $\text{Li}_{14}$ ,  $\text{Li}_{10}$ , and  $\text{Li}_8$  are analogues of  $\text{F}_2$ ,  $\text{N}_2$ , and  $\text{CH}_4$  molecules, respectively.<sup>40</sup> The geometries of  $\text{Li}_{14}$ ,  $\text{Li}_{10}$ , and  $\text{Li}_8$  clusters reported by Cheng et al. are consistent with the lowest-energy structures obtained in our work, as shown in Figure 1. This indicates that both pure lithium clusters and 3d TM impurity encapsulated lithium clusters hold strong tendency of forming superatoms.

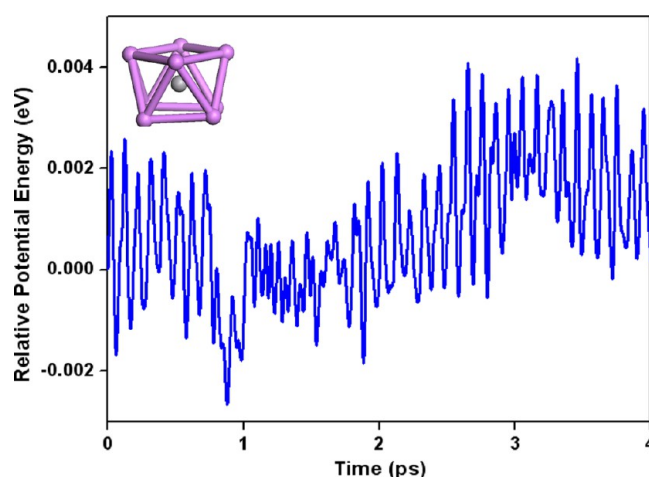
Inspired by the result of doping a V atom in a  $\text{Li}_8$  host to yield the most robust magnetic superatom among the above superatoms, we further extended studies to the situation of encapsulating other TM atoms (TM = Sc, Ti, V, Cr, Mn, Fe, Co, Ni, Cu, and Zn) in a  $\text{Li}_8$  cage to examine the universality of the stability and magnetic properties. Our optimizations show that the lowest-energy structures of all  $\text{TMLi}_8$  clusters are found to be a square antiprism of eight Li atoms with an endohedral TM atom, except for  $\text{ScLi}_8$ , which is a distorted square antiprism in  $\text{C}_{2v}$  symmetry with a Sc atom in the bottom of one square. Figure 9 gives the magnetic trends of  $\text{TMLi}_8$



**Figure 9.** Magnetic trends of  $\text{TMLi}_8$  (TM = Sc, Ti, V, Cr, Mn, Fe, Co, Ni, Cu, and Zn) clusters for the lowest-energy structures.

clusters as a function of the TM atom. It can be seen that there is a maximum value at  $\text{VLi}_8$  with  $5 \mu_B$ , and the magnetic moment decreases successively on both sides of the  $\text{VLi}_8$  cluster.

The thermodynamic stability of the ground-state structure of  $\text{VLi}_8$  is also confirmed by using the Born–Oppenheimer molecular dynamics simulation implemented in the DMOL3 code at room temperature ( $T = 300 \text{ K}$ ). Our molecular dynamics simulation lasted for 4 ps, and the structure was monitored during this time. Each step in the molecular dynamics simulation was 0.4 fs long. We show that the  $D_{4d}$  symmetry structure of  $\text{VLi}_8$  is stable. As shown in Figure 10, the relative potential energy remains unchanged within the time of the dynamic simulation.



**Figure 10.** Relative potential energy (eV) of the  $\text{VLi}_8$  structure during 4 ps of molecular dynamics simulation.

#### 4. CONCLUSIONS

To find possible magnetic superatoms, a systematic study of geometrical structures, growth-pattern behaviors, relative stabilities, and electronic and magnetic properties of vanadium impurity doped  $\text{Li}_n$  ( $n = 1-13$ ) clusters has been carried out via relativistic all-electron DFT with the generalized gradient approximation. Small  $\text{VLi}_n$  clusters exhibit extraordinary size-dependent properties. A single Li-atom-capped structure of the  $\text{VLi}_{n-1}$  cluster is a dominant growth pattern, while a cage-like structure happens when  $n \geq 8$  and evolves toward an icosahedral shape with successive lithium atoms.

$\text{VLi}_n$  clusters are found to be more stable in structural stability and tunable in magnetism than their corresponding pure  $\text{Li}_{n+1}$  clusters. Following the electronic and magnetic properties, the  $\text{VLi}_8$  cluster is identified as a magnetic superatom with a jellium sphere electronic structure and a robust magnetic moment of  $5 \mu_B$ . Moreover, we found that magnetic superatoms exist in  $\text{VLi}_n$  clusters with an endohedral V atom from the size of  $n = 8$  to 13. Taking the stability, tunable magnetic moment, and rich lithium environment of the  $\text{VLi}_n$  clusters into consideration, the  $\text{VLi}_n$  cluster superatoms show potential applications in spin-controllable energy storage electronics. The electronics will possess both magnetic properties as well as self-powering merits. We hope that the present work of a cluster superatom combining magnetism and stable features will serve as the starting point for further experimental synthesis and functionalization of such magnetic energy storage materials.

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##### Notes

The authors declare no competing financial interest.

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